

Directed Evolution of Protoglobin Optimizes the Enzyme Electric Field

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Abstract. To unravel why computational design fails in creating viable enzymes, while directed evolution (DE) succeeds, our research delves into the laboratory evolution of Protoglobin. DE has adapted this protein to efficiently catalyze carbene transfer reactions. We show that the previously proposed enhanced substrate access and binding alone cannot account for increased yields during DE. The 3D electric field in the entire active site is tracked through protein dynamics, clustered using the affinity propagation algorithm, and subjected to principal component analysis. This analysis reveals notable changes in the electric field with DE, where distinct field topologies influence transition state energetics and mechanism. A chemically meaningful field component emerges and takes the lead during DE and facilitates crossing the barrier to carbene transfer. Our findings underscore intrinsic electric field dynamic's influence on enzyme function, the ability of the field to switch mechanisms within the same protein, and the crucial role of the field in enzyme design.

Introduction

Nature has evolved enzymes as remarkably proficient biocatalysts to facilitate a vast array of chemical transformations.¹ Through billions of years of evolutionary fine-tuning, natural enzymes have unlocked extraordinary catalytic power, selectivity, and efficiency.²⁻⁴ The drive to push beyond nature's set of catalyzed reactions, and achieve similarly efficient catalysis for other transformations has led to innovative approaches in modifying enzymes,⁵⁻⁸ and designing them *de novo*.⁹ Indeed, enzyme design has become a frontier of innovation, with the goal of customizing enzymes for the sustainable production of a variety of chemicals, pharmaceuticals, and materials.

Creating highly active enzymes from scratch remains an unsolved task, despite the potential.¹⁰ The initially designed enzymes often need more catalytic vigor, and are subjected to subsequent rounds of directed evolution (DE) to reach appreciable activity levels.¹¹ DE serves as an optimization step that provides designed enzymes with properties absent from initial designs, from improving enantioselectivity in rhodium-catalyzed artificial metalloenzymes,¹² to dramatic boosts in the activity of computationally designed retro-aldolases,^{13,14} and Kemp eliminases,^{15,16} to name just a few examples. DE produces stunning enhancements of k_{cat}/K_M of over 4400-fold.¹²⁻¹⁷ The need to evolve designed enzymes to attain catalytic viability underscores significant gaps in *de novo* design protocols. Understanding what DE contributes to enzyme design is crucial, as DE appears to provide essential elements that are missing in initial designs, potentially unlocking key strategies for efficient enzyme design in the future.

We study the directed evolution of *Aeropyrum pernix* Protoglobin, a Fe-heme protein, which was evolved to perform a new-to-nature selective carbene transfer to catalyze cyclopropanation of benzyl acrylate (Figure 1).^{18,19} Mutations introduced by DE are dispersed throughout the protein structure, located both close to the Fe-center (F145Q, I149L, Y60A, W59L),

and as far as >15 Å away from it (F175L, C102S, V63R), and include both hydrophobic and hydrophilic residues. We use this rich evolutionary journey to gain an understanding of how DE can imbue new catalytic functions into an enzyme. We perform and analyze replica molecular dynamics (MD) simulations of the wild-type (WT) Protoglobin and four evolved variants (LVRQ, LVRQL, GLVRSQL, GLAVRSQLL) that showed a progressive increase in activity, initially focusing on substrate access and binding improvements at the active site. Upon indications of changes in electrostatic preorganization at the active site along the evolutionary pathway, we develop and utilize a novel framework to study the dynamics of the heterogeneous electric field in the active site, combining electric field topological analysis, high-throughput computation, and graph compression algorithms for a comprehensive picture. Finally, we correlate changes in electrostatic preorganization with experimental yield through QM/MM reaction mechanism calculations. This workflow illuminates the critical factors DE exploits to enhance enzyme catalysis—insights crucial for refining enzyme design protocols.

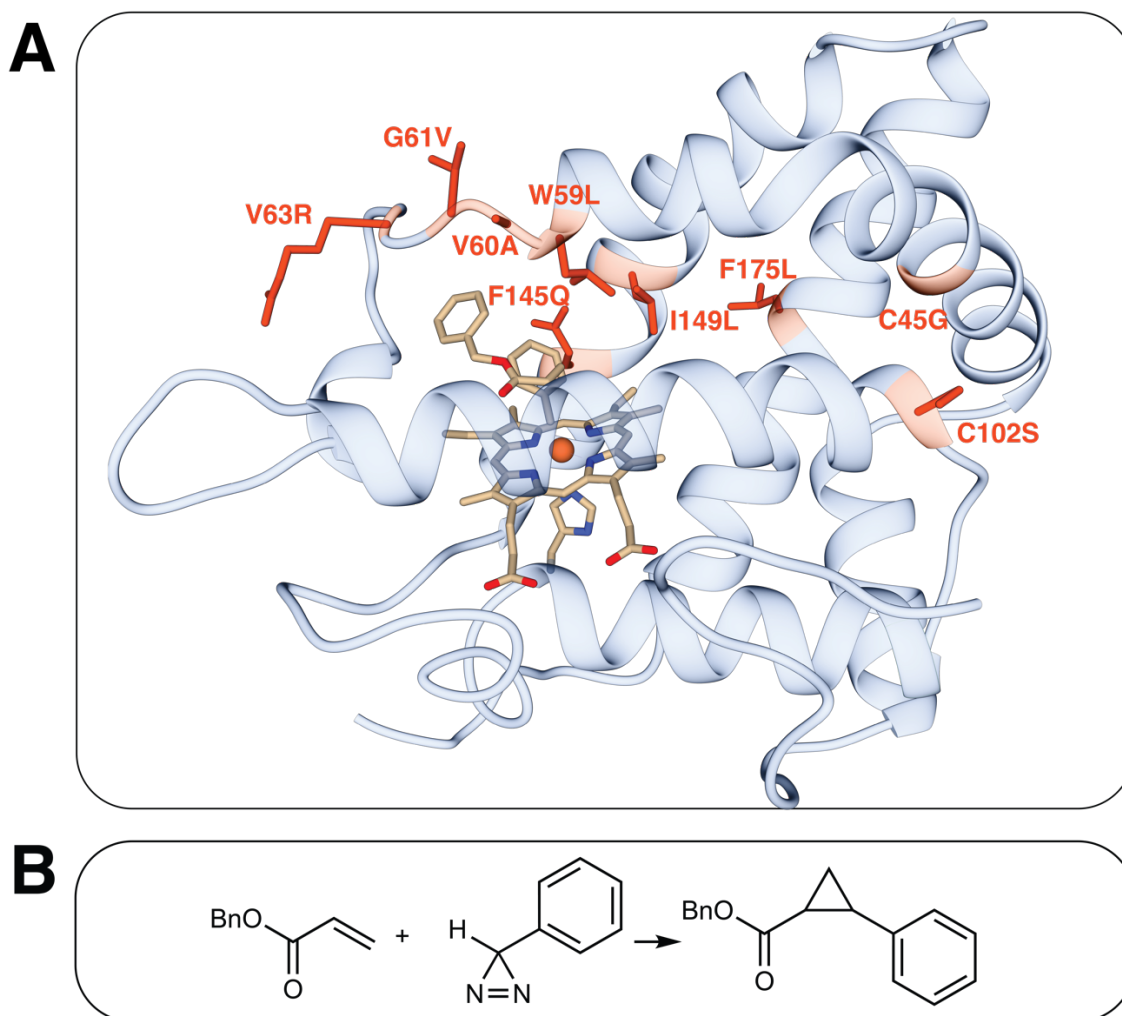


Figure 1. (A) Protoglobin with directed evolution mutation sites highlighted in red and labeled with the bound substrate (PDB ID: 7UTE). (B) the carbene transfer reaction being optimized along the directed evolution path.

Methods

Our developed methodology has six primary components, visualized in **Figure 2**. We use MD simulations to sample configurations of the protein. We use methods in field analysis to calculate the point electric field and electric field topology at the active site throughout the molecular dynamics trajectories. These topologies are compared using statistical distance metrics to obtain a distance matrix for each trajectory. To analyze how these field topologies change, we then use clustering on the distance matrices to obtain representative “snapshots” of the electric field at the active site. These snapshots are subjected to quantum mechanical/classical mechanical (QM/MM) reaction path calculations and principal component analysis (PCA).

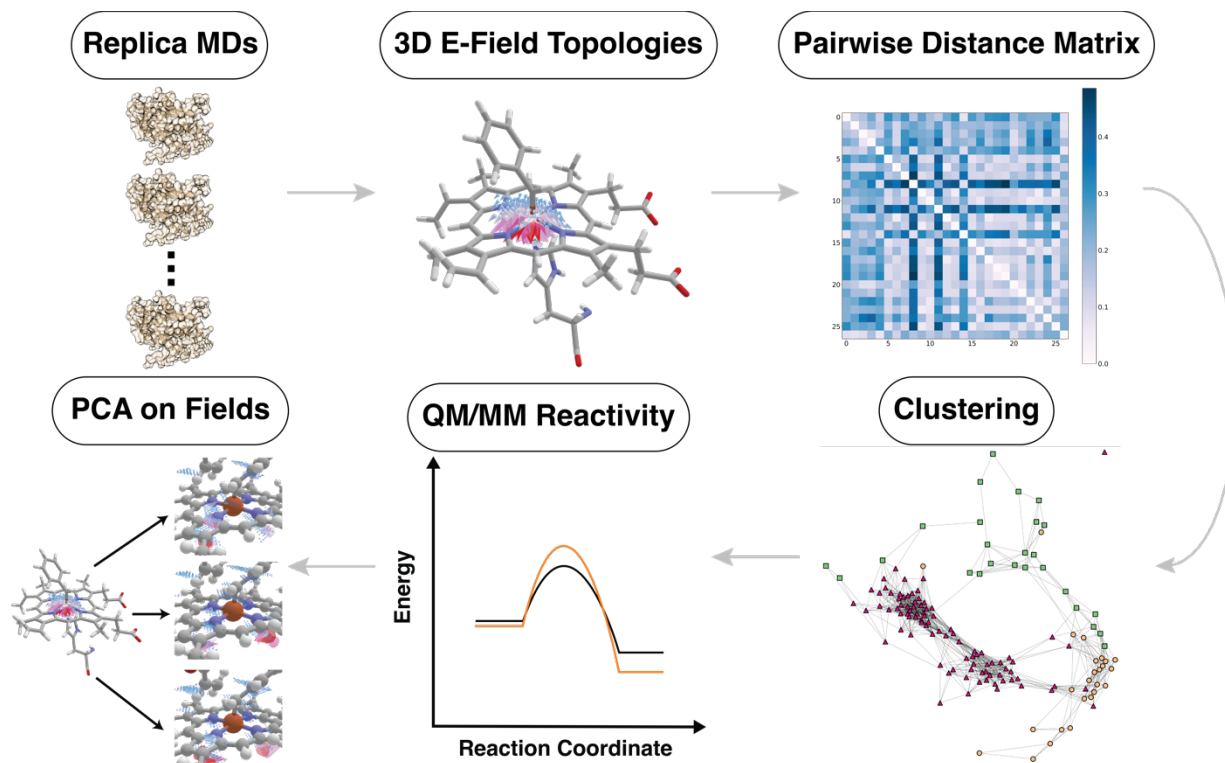


Figure 2. This study's approach measures electrostatic preorganization by analyzing the heterogeneous electric field topology across replica MD simulations. It further involves comparing these topologies using a pairwise distance matrix, clustering based on similarity, and then quantifying reactivity through QM/MM methods. The reactivity difference is chemically elucidated using Principal Component Analysis.

System Preparation and Molecular Dynamics: We performed MD simulations on the carbene-substrate intermediate of the WT Protoglobin and the four directed evolved variants—LVRQ, LVRQL, GLVRSQL, and GLAVRSQLL. When compared to the WT, the LVRQ evolved variant presents mutations W59L, G60V, F145Q, and V63R. The LVRQL variant includes an additional I149L mutation. The GLVRSQL variant incorporates further C45G and C102S mutations. Lastly, the GLAVRSQLL evolved variant introduces additional mutations V60A, G61V, and F175L. We used the crystal structure of the Protoglobin GLVRSQL variant as the template to model the carbene-substrate intermediate of the other evolved variants. In the absence of an experimentally

determined crystal structure for WT Protoglobin ApPgb, we employed the AlphaFold2 model as a vital alternative.²⁰ Notably, the AlphaFold-predicted structure for WT Protoglobin ApPgb demonstrated a high average pLDDT confidence score of 96.8, indicating a robust prediction. This high level of confidence was uniformly maintained across the core structural regions, crucial for our analysis, with only a few terminal residues displaying confidence scores below 95. Furthermore, the experimentally structure of the GLAVRSQL mutant of Protoglobin^{18,19} aligns closely with an RMSD of 0.5 Å in respect to the AlphaFold2 model, reinforcing the validity of using this approach for our simulations. AlphaFold2, and its subsequent successors, have been revolutionary in yielding rapid, largely reliable structure predictions for a large swath of protein space. It excels in predicting structures of single protein chains, protein-protein complexes, and even complex hetero-multimers.^{21,22} However, AlphaFold2 is not without limitations.^{21,23} It can struggle with accurately predicting structural alterations resulting from point mutations and may misplace functionally relevant residues,²⁴ particularly in lower-confidence structures. Additionally, its performance can be limited when dealing with orphan proteins or proteins from less-studied families. However, these limitations did not significantly impact our study. The structure of Protoglobin used in this study has high confidence scores, ensuring the reliability of the functionally relevant residues in our analysis. Furthermore, since our study employed the crystallized GLAVRSQL structure for initial MD simulations of point mutations, the issue of predicting structural changes due to mutations was not a concern. Lastly, Protoglobin is a well-characterized protein, mitigating concerns related to lesser-known protein families.²⁵

The carbene was modeled taking the Micro-ED crystal structure as a reference to simulate the carbene-substrate intermediate in WT Protoglobin. The substrate benzyl acrylate was docked into the active site using AutoDock Vina.^{26,27} The setup for the MD simulation was done via Amber 22 and AmberTools 22 modules.^{28,29} The active site parameters for the carbene-substrate intermediates encompassing the heme, Fe, carbene, and an axial histidine were derived using AmberTool's Metal Center Parameter Builder (MCPB) v3.0.³⁰ This protocol has been successfully utilized to model several metal containing systems especially hemes and non-heme iron complexes.³¹⁻³⁴ The GAFF tool in Antechamber generated the topology for the substrate benzyl acrylate. The protonation states of the protein in the carbene-substrate intermediate were determined using Chimera routines, and the parameters for the rest of the protein were generated using the AmberFF19SB³⁵ force field. The LEaP module of Amber 22 neutralized the system by adding counterions. The system was then immersed into an OPC water box of at least 10 Å from the surface of the protein. Periodic boundary conditions were applied to the system, and long-range electrostatic interactions were calculated using the particle mesh Ewald method with a cut-off distance of 8 Å. The SHAKE algorithm³⁶ was used to constrain bonds involving a hydrogen atom. The systems were minimized in two steps: using the steepest descent (10,000 steps), and (2) the conjugate gradient (10,000 steps) methods. During this phase, the protein's heavy atoms were restrained using a harmonic potential of 100 kcal mol⁻¹ Å², and the protein's hydrogen atoms, along with solvent molecules, were minimized. Subsequently, the entire system underwent a comprehensive minimization process without any restraints via steepest descent (10,000 steps) and conjugate gradient (10,000 steps) methods. The system was then heated from 0 to 300 K in 50 ps using an NVT ensemble and then remained at 300K for another 50 ps. Next, A weakly constrained

MD with constant pressure was performed to achieve uniform density in the systems, followed by equilibration MD in an NPT ensemble for 10 ns with restraints on the benzyl acrylate substrate to equilibrate it in the active site and then without any restraints for 2 ns. Finally, all production runs were performed using the GPU version of the AMBER 22 package. To enhance the credibility and precision of MD analysis, five replica MD simulations, each with a 100 ns duration, were performed.³⁷ RMSD was performed with CPPTRAJ to validate equilibration of all runs and is provided in **Figure S1**. Distance analysis was also done using CPPTRAJ.³⁸ The binding free energies were calculated with the MMPBSA/MMGBSA module implemented in AMBER 22.³⁹

Topological Electric Field Measurements and Comparison by Distance Metric

Many previous studies incorporating electric fields as an analytical tool for protein activity use the protein structure in the context of a single structural snapshot - either crystalized variants or at a single frame within a larger MD trajectory are common.⁴⁰⁻⁴³ These miss the effects of dynamics. Few studies, however, do incorporate dynamical information, including a study by Head-Gordon and coworkers where projections of electric field components were measured and correlated along an MD trajectory.⁴⁴ These projections amount to a low-dimensional embedding of the entire heterogeneous electric field and here we aim to increase the bandwidth to 3-D heterogeneous electric fields within a sampling box with our topological distance metric. We used a distance metric to construct a matrix of pairwise distances of electric fields along an entire MD trajectory. Every 5th frame of a 100 ns trajectory was used for the description of electric fields in the active site. The atomic charges were computed for the protein in each frame using ChargeFW2.⁴⁵ The field was calculated in a 3 Å box defined that is centered by the heme Fe – carbene carbon bond. We zero the charges on the heme, iron, and carbene moiety in all systems. This approach was taken to isolate and examine the charge effects originating from the protein scaffold alone. The pairwise distances between each electric field's topology (see eq (1) and (2)), were computed, and subsequently fed into a graph clustering algorithm.

Our group has previously developed a distance metric to measure differences between 3-D electric fields.⁴⁰ This formulation enjoys important mathematical properties such as rotational, scalar, and translational invariance - essential properties when describing dynamical structures. The method samples points within a rectangular prism where linearizations of the electric field are computed and followed to calculate curvature. These lines are known as *streamlines*, $r(t)$, and provide a highly parallelizable compute unit, as each streamline can be calculated independently. We compute the curvature (κ) at the beginning and end of these streamlines with:

$$\kappa = \frac{||r'(t) \times r''(t)||}{||r'(t)||^3} \quad eq (1)$$

Mean curvature values of the start and end points are compiled across each individual streamline along with the Euclidian distance between the start and end points to yield a histogram distribution of curvatures and mean distances for each electric field, a form of topology. This method computes the pairwise distance between two such normalized distributions (f, g) via the χ^2 distance across N bins:

$$\chi^2: D(f, g) = \frac{1}{2} \sum_{i=1}^N \frac{(f[i] - g[i])^2}{f[i] + g[i]} \quad eq (2)$$

With a defined distance comparing electric fields we can then create a graph where the edge lengths are the distances between two electric fields. This method requires the user to specify several parameters, including box size (Å), number of streamlines, and the step size (Å) for each linearization step along a streamline. The number of streamlines used for all calculations is 10000 with a step size of 0.001 - information on testing of box size can be found in the SI **Table S1**. Raw fields were preprocessed prior to input in visualization and clustering schemes. For clustering, we determined an upper boundary CPET distance above which edges were removed (**Figure S8**). This cutoff was the 10%ile distance from the collective distance matrix of all 5 WT runs. For affinity propagation, we also standardized the remaining distances. We used max_it = 10000 and 0.5 dampening. For PCA analysis, raw fields were used.

Affinity Propagation

Affinity Propagation intakes the “affinity” or similitude between different data points in a distance matrix, this can include non-connected graph nodes. We refer the audience to the original implementation of Affinity propagation⁴⁶ but will provide a brief outline of the method as follows. Affinity propagation is built on the iterative message passing of responsibility and availability between nodes in a graph. If $\mathbf{X} = \{x_1 \dots x_z\}$ represents a set of data points and $s(i, j)$ represents a similarity metric between points i and j . Responsibility $r(i, k)$ describes how representative point k is for point i and availability $a(i, k)$ measures how reasonable it is for k to pick i as a representative for itself. These values are updated using the following equations:

$$r(i, j) \leftarrow s(i, k) - \max_{k' \neq k} \{a(i, k') + s(i, k')\} \quad (\text{Update Responsibility matrix } r)$$

$$a(i, k) \leftarrow \min \left(0, r(k, k) + \sum_{i' \notin \{i, k\}} \max(0, r(i', k)) \right) \quad (\text{Update availability matrix } a)$$

Message-passing updates are repeated until convergence of representative structures/boundaries or a maximum number of iterations are reached.

PCA

Principal Component Analysis (PCA) is a widely-used dimensionality reduction algorithm that intakes descriptors on a dataset and performs a basis change to orthogonal components by order of descending variance – these new components are referred to as principal components.⁴⁷ PCA yields a few important statistical objects, namely the eigenvalues of the new principal components (PCs) and principal components themselves. Eigenvalues elucidate the variability in the dataset along the new basis and can be used to diagnose dataset dimensionality. The principal components themselves can be analyzed, along with the eigenvalues, to determine the directions of greatest variability in the dataset. We constructed PCA components from the compiled dataset of electric fields at every frame considered in the graph compression (all 5 mutants). This amounted to 25,000 electric fields where each field was centered at the heme-Fe. From here, we constructed a sampling mesh of 10 equidistant points in the six axial directions up to the boundary of 1.5 Å. This results in a 21 x 21 x 21 mesh of points spanning a 3 Å box – and thus, an input dimensionality of > 27,000 points to the PCA algorithm. Remarkably, 5 components accounted for > 77% of the explained variation, 10 for > 95%, and 25 for > 98%. This shows that a small number of

components likely can be used to understand the variability in the electric fields – though we note that variability does not signify importance and therefore we extend our analysis to include several lower-variance PCs. We selected the 10 most important components and projected the cluster centers' electric fields on those components – these 10 components account for 95% of the variance in the dataset and consist of components with >1% of the total variance each. This allows us to decompose the complex electric fields into simpler motifs for analysis and interpretation. Electric fields for the entire population of a mutant were analyzed along principal components to understand how the dynamic electric field evolves with mutations.

QM/MM Reaction Mechanism

For cluster centers obtained from affinity propagation, the reaction mechanism of carbene transfer and its energetics was elucidated with hybrid QM/MM reaction path optimizations and thermodynamics calculations. ChemShell^{48,49} was used for QM/MM calculations in combination with DL_POLY⁵⁰ for the energy of the molecular mechanics region and TURBOMOLE⁵¹ for the energy of the quantum mechanical region. The QM region included the Fe, carbene, reduced heme, and substrate, while the rest of the protein was in the MM region (SI **Figure S7**). The AmberFF19SB force field generated the protein MM region parametrization. To have a well-refined reaction path, only cluster centers with the benzyl acrylate within 5 Å of the heme Fe were included in the reaction profile calculation. To determine the reaction profile, we used a collective variable that optimally combined three factors: decreasing the distance between CC and C1, increasing the distance between Fe and CC, and reducing the distance between CC and C2. For the QM reaction path optimization, the TPSS DFT functional^{52,53} was employed, with def2-TZVP and def2-SVP basis sets for the Fe atom and the remaining atoms in the QM region, respectively. The transition states and products were freely optimized. Vibrational frequency calculations were used to verify the validity of product and transition states and to compute free energies within the harmonic approximation. Single point calculations were done at the reactant, product, and transition states using the TPSSh functional, with the def2-TZVP basis set for all atoms in the QM region to provide more precise electronic energies. To ensure the robustness of our findings, the QM/MM calculations were repeated using the B3LYP functional.⁵⁴ Finally, we performed single-point QM/MM calculations at the near-gold standard DLPNO-CCSD(T)⁵⁵ level using the def2-TZVP basis set to obtain accurate energy estimates for the reaction mechanism. ORCA was employed for the QM region calculations along with DL_POLY in ChemShell for these QM/MM calculations. All reported QM/MM free energies are derived from these single-point energies at the DLPNO-CCSD(T) level, incorporating thermodynamic corrections.

Results and Discussions

Can substrate binding explain the yield increase?

Based on the microcrystal electron diffraction structure of the GLVRSQ Protoglobin variant, it was proposed that DE facilitates the new-to-nature catalysis by enhancing substrate access to the active site.^{18,19} We analyzed the substrate access to the active site of Protoglobin, by measuring the distance between the terminal C1 atom of the benzyl acrylate substrate and the reactive CC atom of the carbene across the five replica molecular dynamics (MD) simulations of 100 ns each, for all variants (**Figure 3A**). In agreement with experiments, the mean distance of the

substrate to the active site was high in the WT enzyme, measuring 17.10 ± 9.25 Å, suggesting the benzyl acrylate substrate stays away from the active site and has a very low chance of undergoing catalysis. However, during DE, the mean distance reduced in LVRQ (7.78 ± 3.53 Å) and LVRQL (8.87 ± 8.72 Å), signifying an improvement in substrate accessibility to the active site. The large standard deviation observed for LVRQ indicates instances where the substrate approaches close to the active site but on average remains further away. (see SI **Figure S2**). The reduction in substrate distance from the active site was further pronounced in the GLVRSQL variant (4.44 ± 0.90 Å), suggesting a significant enhancement in substrate entry and stabilization within the active site. However, in the GLAVRSQLL variant, the distance of the substrate to the active site remained comparable to GLVRSQL (4.53 ± 1.09 Å), while the experimental yield dramatically increased. This observation challenges the notion that solely substrate access to the active site dictates yield enhancements. While enhanced substrate access might be a major contributor to yield improvement from WT to GLVRSQL (0-6%), it could not explain the drastic increase in yield going from GLVRSQL to GLAVRSQLL (6-28%).¹⁸

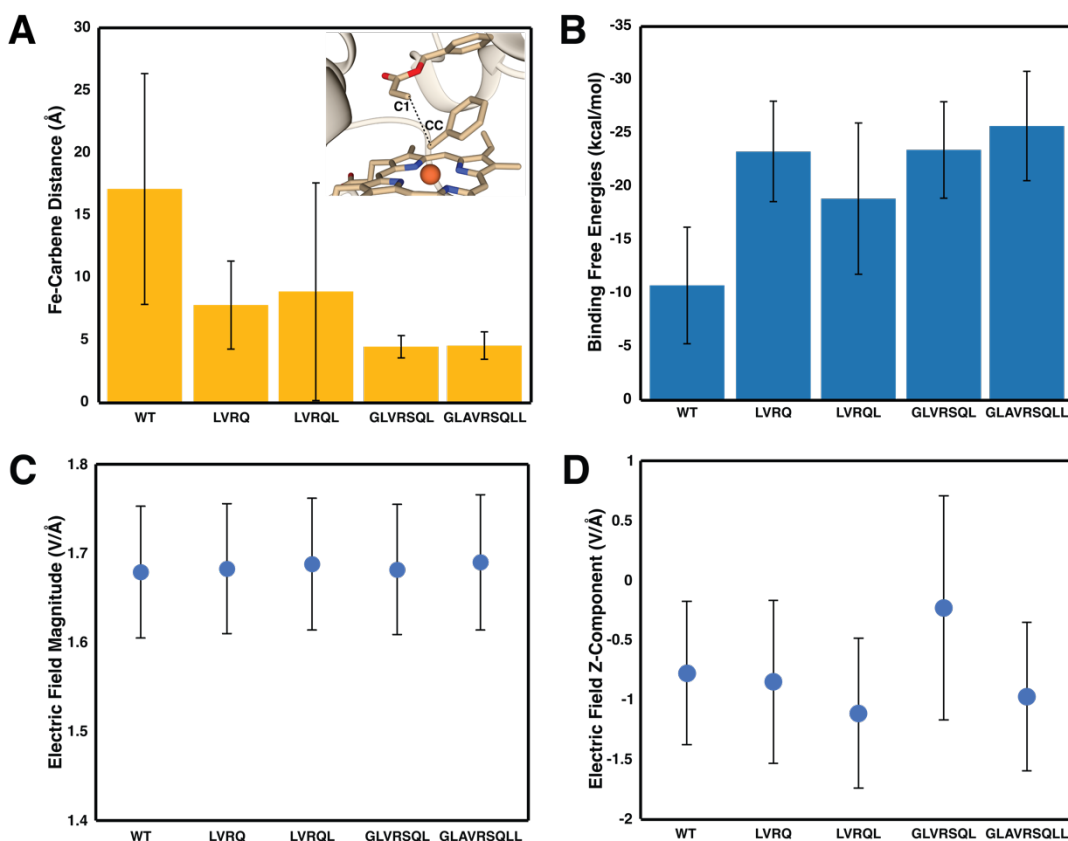


Figure 3. Initial parameters investigated as the cause of higher reactivity along DE path. (A) The mean and standard deviation of Fe-Carbene distance for all MD trajectories across all variants. (B) The mean and standard deviation of substrate-protein binding free energies (G_{binding}). (C) The total electric field magnitude computed on the Fe-Carbene bond of IPC for all systems across replica molecular dynamics. (D) The z-component of the electric field computed at the center of the Fe-Carbene bond of IPC for all systems across replica molecular dynamics.

Further, we sought to explore if enhanced benzyl acrylate substrate binding is the reason for the observed yield increase (**Figure 2B**). MMGBSA binding free energy calculations were performed, across the five replica MDs for each variant. The MMGBSA method has demonstrated efficacy in reproducing and rationalizing experimental outcomes, accurately reflecting the trends in experimental binding free energies across a variety of ligands and protein systems.^{56,57} Notably, the substrate binding in the evolved variants (LVRQ: -23 ± 4 , LVRQL: -18 ± 7 , GLVRSQL: -23 ± 4 , GLAVRSQLL: -25 ± 5 kcal/mol) was consistently stronger than in the WT (-10 ± 5 kcal/mol). However, the free energy of substrate binding did not reveal a discernible trend across the DE path. Specifically, LVRQ exhibited a higher binding energy, albeit at a larger distance from the active site, indicating strong substrate binding at non-active site regions and potentially contributing to the lower yield of carbene transfer (**Figure S3**). The mean binding free energies for GLVRSQL (-23 ± 4 kcal/mol) and GLAVRSQLL (-25 ± 5 kcal/mol) were within their respective standard deviations, and thus again, failing to provide a definitive explanation for the substantial yield increase from GLVRSQL to GLAVRSQLL. These findings suggest that while substrate binding energy is an important factor, it also does not adequately justify the enhancement in yield during DE of Protoglobin.

Electric field evolution during directed evolution

Now, we pivot towards analyzing if the electric fields generated by the studied enzyme changes, and its link to Protoglobin reactivity. Enzyme catalysis is often attributed to electrostatic preorganization and dynamics,^{44,58–61} occasionally put in contradiction with each other.⁶² We have previously observed that the reactivity of Fe-heme oxidoreductases is strongly regulated by the electric field from the protein scaffold, in addition to the regulation by the axial ligand to Fe.⁴¹ Electrostatic preorganization has also been cited previously as a compass of directed evolution of Kemp eliminases.⁶³ To comprehensively address both electric fields and dynamics, we performed an electric field analysis over several replica MD trajectories to sample and compare the electrostatic behavior of the enzyme in a dynamic fashion.

We performed point electric fields calculations at the center of the Fe-carbene bond, for the carbene-substrate intermediate replica MDs of all systems. The mean electric field magnitude is evidently seen to not change meaningfully along DE, with only a very small decrease in the GLVRSQL variant (**Figure 3C**). A more noteworthy observation emerged when examining the z-component of the electric field measured at the Fe-carbene bond center (the z-component being normal to the heme plane). The projection shows larger variation across the mutants, especially in the field directionality (**Figure 3D**). This suggests that a point electric field-based analysis is not enough to capture the changes in the heterogeneous 3-dimensional (3D) electric field of the enzyme, therefore requiring a more comprehensive approach (introduced in **Figure 2**).

We previously developed a method to quantify the heterogeneous 3D electric field topology in volumes within an enzyme active site, and map it to a single metric.⁴⁰ Using this method, we correlated 3D electric fields in ketosteroid isomerases to their reactivity. This is notable as electric field magnitudes at a point or along a particular bond showed no relationship between these two variables.⁴⁰ This approach involves defining a volume of interest for electric field topology calculations, which, in this study, is a cubic box centered on the Fe-carbene bond (**Figure 4A**). The heterogeneous electric field (**Figure 4B**) was calculated for a total of 5,000

frames derived from 5 x 100 ns replica MD runs for each variant. To analyze this vast dataset, we employed an affinity propagation algorithm to cluster similar electric field topologies within a dynamical trajectory. Affinity propagation provides a distinct advantage by eliminating *a priori* knowledge of the number of clusters. This flexibility allows us to track the changes in the distribution and the number of clusters along the DE of Protoglobin - signaling how diverse or, inversely, tightly controlled the electric field is within the protein's active site. Additionally, this clustering algorithm yields a single best representative frame for each cluster, aiding visualization and further analysis of the 3D electric field that the active site samples. The predominant clusters (those representing >5% of the MDs) from each system were considered and subsequently compared using a distance matrix (**Figure 4D**). A distance closer to 0 indicates high similarity in the 3D heterogeneous electric field topologies, while a score of 1 indicates high dissimilarity, for example, between WT and evolved variants.

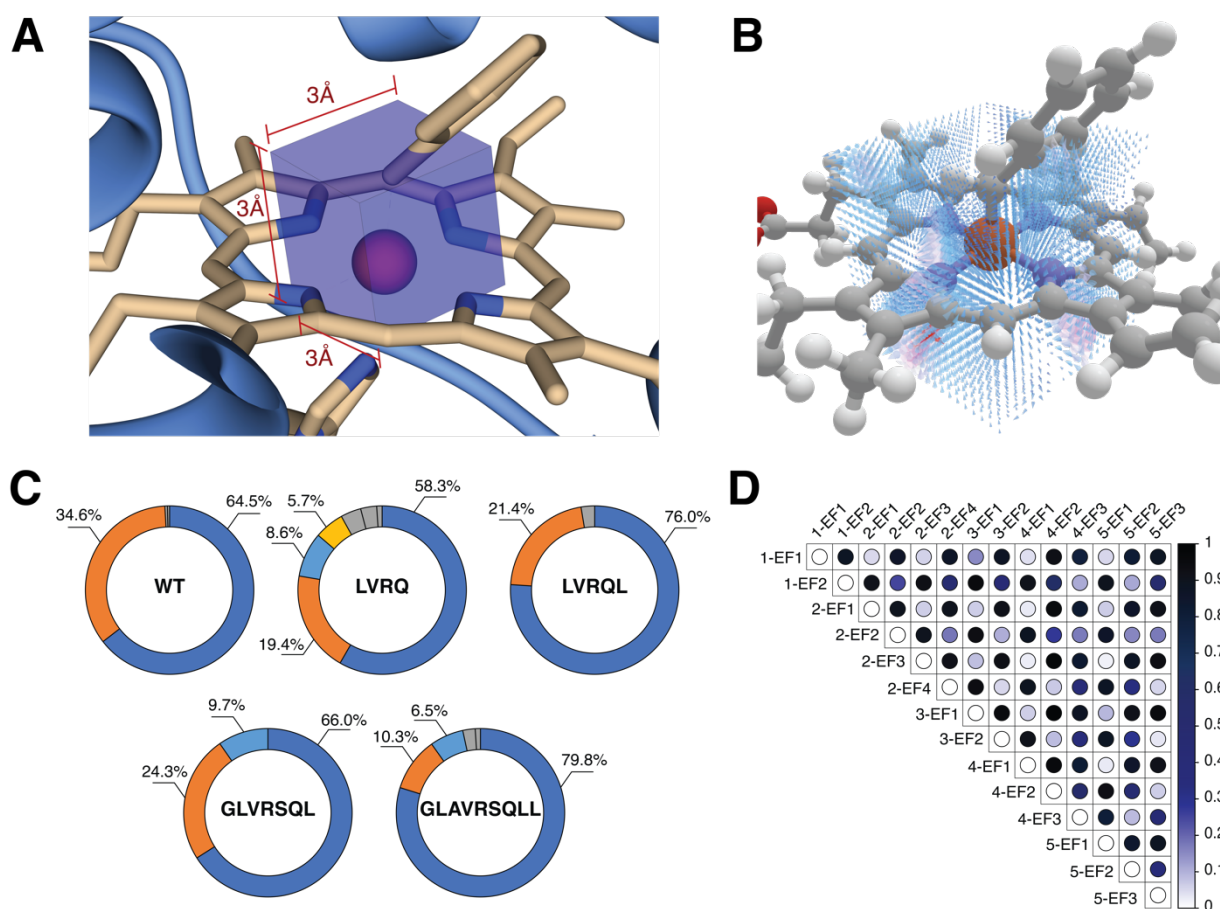


Figure 4. (A) Illustration of a 3Å box centered on the Fe-carbene bond for calculating the 3D heterogeneous electric field topology. (B) Example of a 3D heterogeneous electric field topology calculation. (C) Affinity Propagation clustering of electric field topologies for each variant, with blue indicating the most prevalent, orange the second, and green the third; clusters under 5% are in grey. (D) A pairwise distance matrix comparing the similarity (0) or difference (1) of electric field topology clusters across all systems. The first number in the labels indicate the stage of

directed evolution (1=WT, 5=GLAVRSQLL), and the second number indicates how often the field topology is visited along the trajectory (1=the most frequently visited).

WT Protoglobin features two highly distinct 3D electric fields, with clusters WT-EF1 (visited by the system 64.53% of the time) and WT-EF2 (34.58%). The LVRQ variant introduces four electric field clusters, LVRQ-EF1 to LVRQ-EF4, with visitations of 58.32%, 19.36%, 8.60%, and 5.68%, respectively. LVRQ-EF1 and LVRQ-EF3 closely resemble each other and WT-EF1, while LVRQ-EF2 and LVRQ-EF4 diverge significantly, marking the introduction of two novel electric fields. LVRQL further evolves this pattern, showing two main fields: LVRQL-EF1 (76.04%) and LVRQL-EF2 (21.36%), which are derivatives of LVRQ's clusters, illustrating an ongoing modification from WT through DE. GLVRSQ presents three clusters: GLVRSQ-EF1 (65.98%), GLVRSQ-EF2 (24.34%), and GLVRSQ-EF3 (9.68%), with EF1 and EF3 showing regressive similarity to WT-EF1 and EF2, respectively, while GLVRSQ-EF2 (0.92 and 0.62 from WT-EFs) remains distinct, reflecting influences from LVRQ-EF4 and LVRQL-EF2. The final GLAVRSQLL variant has three clusters: GLAVRSQLL-EF1 (79.82%), GLAVRSQLL-EF2 (10.34%), and GLAVRSQLL-EF3 (6.46%). GLAVRSQLL-EF1 demonstrate nuanced similarities to WT-EF1 (0.05) and GLAVRSQLL-EF2 is closest related to GLVRSQ-EF3 and WT-EF2 (0.08 and 0.11, respectively), indicating evolutionary modifications. In contrast, GLAVRSQLL-EF3 introduces a distinct electric field, diverging from WT, which evolved throughout the directed evolution process. It now remains to be seen how these field variations impact the reactivity.

Link between evolving electric fields and reactivity changes

The carbene transfer reaction in the engineered Protoglobin proceeds through the iron porphyrin carbene (IPC) intermediate with the substrate bound nearby.¹⁹ The IPC intermediate contains a highly reactive carbene carbon, which reacts with the double bond in the benzyl acrylate substrate, leading to the formation of two new carbon-carbon bonds and culminating in the formation of a cyclopropane ring embedded within the substrate. The IPC intermediate is capable of adopting three spin states, each potentially influencing the cyclopropanation pathway differently. However, most experimental evidence points to the existence of a closed-shell singlet spin state.^{64,65} Unpaired electron states (triplet or open shell singlet) may lead to a stepwise process, while a closed shell singlet state favors a direct, concerted mechanism either synchronous or asynchronous, without intermediates.⁶⁶ To explore the cyclopropanation reactivity, we performed hybrid quantum mechanics/molecular mechanics (QM/MM) calculations on the cluster centers for WT Protoglobin and the evolved variants. The calculations indicate the preferred spin state for the IPC complex is the closed shell singlet, favored over the triplet by 14.7 kcal/mol, with several attempts to converge the open shell singlet IPC leading to the closed shell singlet structure. The spin preference for closed shell singlet IPC is also supported by similarities in Fe-CC bond lengths between the QM/MM optimized closed-shell singlet state (1.79 Å) and the crystallized Protoglobin IPC intermediate (1.74 Å), contrasting with the longer bond length (1.93 Å) in the triplet state.¹⁹ Additional calculations across the complete reaction profile further confirm that the triplet spin state is energetically higher than the closed-shell singlet spin state. Moreover, the only successfully optimized open-shell singlet structure also exhibits an energy level comparable to that of the corresponding triplet state (**Figure S4**). Therefore, all further calculations were performed at the open-shell singlet spin state.

The reactivity calculations using a hybrid QM/MM method were conducted on all electric field clusters for variants containing the substrate within a reactive proximity (<5 Å) to the CC. The results showed that for the WT-RCs and EF1, EF2, and EF4 clusters for the LVRQ variant, the substrate was positioned at distances greater than the reactive range from the CC atom, classifying these states as unreactive (see SI **Table S2**). Consistent with other carbene transfer studies, all reactive clusters for the LVRQ, LVRQL, GLVRSQL, and GLAVRSQLL variants, with closed shell singlet spin state, demonstrated a concerted reaction mechanism, lacking stable intermediates and characterized by the asynchronous formation and breaking of bonds.^{66–68} Initially, the CC and substrate C1 atom bond formation and elongation of the Fe-CC bond is favored, followed by complete breaking of the Fe-CC bond, culminating in the bond formation between CC and C2. For the LVRQ variant with EF3, the Gibbs free energy barrier was identified as 28.8 kcal/mol, coupled with a product stabilization energy of -36.2 kcal/mol. The LVRQL variant exhibited a free energy barrier ranging between 23.8 and 32.0 kcal/mol and product stabilization energies between -38.7 and -41.9 kcal/mol. The GLVRSQL variant showed a barrier range of 27.0 to 35.9 kcal/mol and product stabilization energies between -30.8 and -33.4 kcal/mol. Lastly, the GLAVRSQLL variant displayed a barrier range from 13.4 to 34.6 kcal/mol with product stabilization energies between -34.6 and -53.5 kcal/mol.

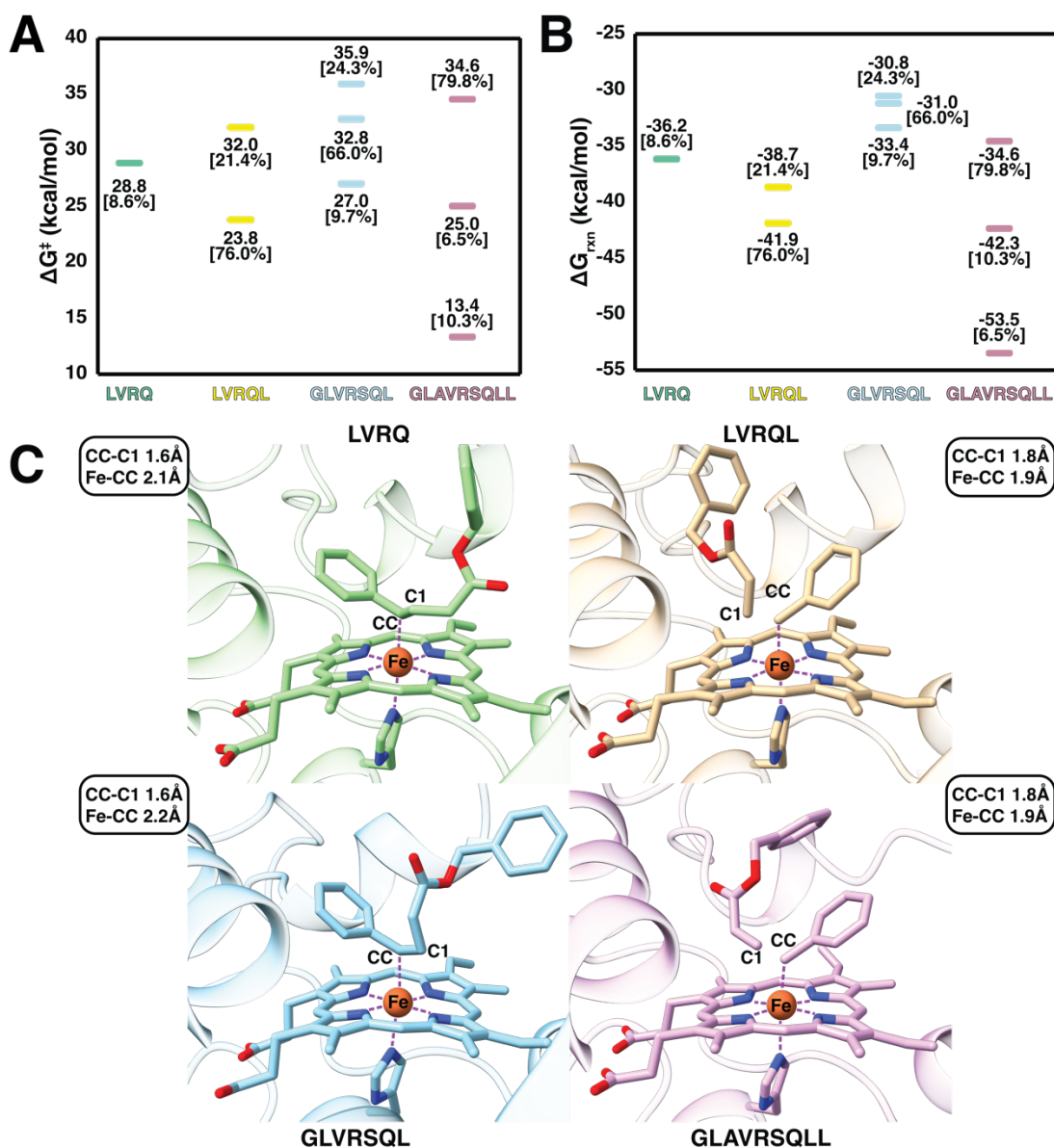


Figure 5. (A) Transition state free energy barriers for reactive clusters from each variant; (B) Product stabilization energies for reactive clusters from each variant. (C) Observed transition states from the best performing cluster centers of each variant. Transition state and product stabilization energies/structures were obtained from reaction path scans.

The results indicate that LVRQ do not produce very high free energy barriers and in LVRQL the barriers are even lower with a significant reaction exothermicity, aligning with some experimental activities observed.¹⁸ This suggests the observed low experimental reactivity in the LVRQ and LVRQL variants likely not due to a complete lack of intrinsic reactivity but rather from rare visiting of reactive configurations, as suggested by the mean distances from molecular dynamics (MD) simulations (7.78 ± 3.53 Å for LVRQ and 8.87 ± 8.72 Å for LVRQL). Conversely, the primary reason for the low experimental yields in GLVRSQL, despite the close proximity of the benzyl acrylate substrate (MD mean distance of 4.44 ± 0.90 Å), appears to be the absence of effective electric fields necessary for effectively lowering the barrier of the cyclopropanation

reaction and improving the overall reaction energy. This underscores the principle that mere access of the substrate to the active site is insufficient for high yield; the presence of a conducive electric field is critical for enhancing reactivity. The GLAVRSQLL variant, alongside the close binding of the benzyl acrylate substrate (MD mean distances of 4.53 ± 1.09 Å), has an effective electric field leading to both low energy barriers and favorable reaction energy, indicating its proficiency in catalyzing the cyclopropanation reaction. This agrees with and rationalizes the yield increase from approximately 8% in GLVRSQLL to about 28% in GLAVRSQLL. These trends in reactivity are also in line with additional QM/MM calculations with TPSSh and B3LYP functionals (**Table S3**).

Intriguingly, QM/MM calculations also reveal that the nature of the reaction TS within different enzyme variants is significantly influenced by the electric fields present. We identified two distinct types of TSs. The first type, observed in the most efficient EF clusters of the variants LVRQL and GLAVRSQLL, is characterized by the formation of the CC-C1 bond accompanied by a slight elongation of the Fe-CC bond. In contrast, the second type of TS, found in LVRQ and GLVRSQLL variants for the same cyclopropanation reaction, showcases a fully formed CC-C1 bond and a complete dissociation of the Fe-CC bond. Thus, the distinct 3D electric fields can facilitate a mechanism change of the cyclopropanation reaction. Moreover, within the GLVRSQLL variant, EF3 and EF1 both exhibit TS of the second type, whereas EF2 presents a TS of the first type. Hence, enzyme's dynamically visiting diverse electric fields has the potential for diverse mechanistic pathways to be active within the same enzyme.

Principal Component Analysis of the Fields

To link the 3D heterogeneous electric fields to reactivity in a chemically meaningful manner, we employed Principal Component Analysis (PCA).⁴⁷ We mapped cluster centers to PCA components constructed from the compiled set of electric fields across all trajectories for each variant. This yields a single basis for electric field variability within the protein active site. The population density of each mutant, as illustrated in **Figure S5**, is mapped across PC0-9 components. This mapping reveals that every mutant, including GLVRSQLL and GLAVRSQLL, exhibits significant variance from the WT Protoglobin along several PC components, confirming that DE influences the electric field and its dynamics within the active site considerably. The most dramatic shift between variants GLVRSQLL and GLAVRSQLL, the mutations that incur the greatest change in activity, is observed along component PC9 (**Figure 6A**). The population density of GLAVRSQLL shifts positively along PC9, suggesting a robust alignment of its electric field with this PC. The findings that the most pronounced changes occur in higher-order components point to a multifaceted impact of mutations on the electric field's characteristics, re-emphasizing that the full spectrum of electric field components, rather solely the dominant one, must be analyzed to elucidate the role of fields in the catalytic process.

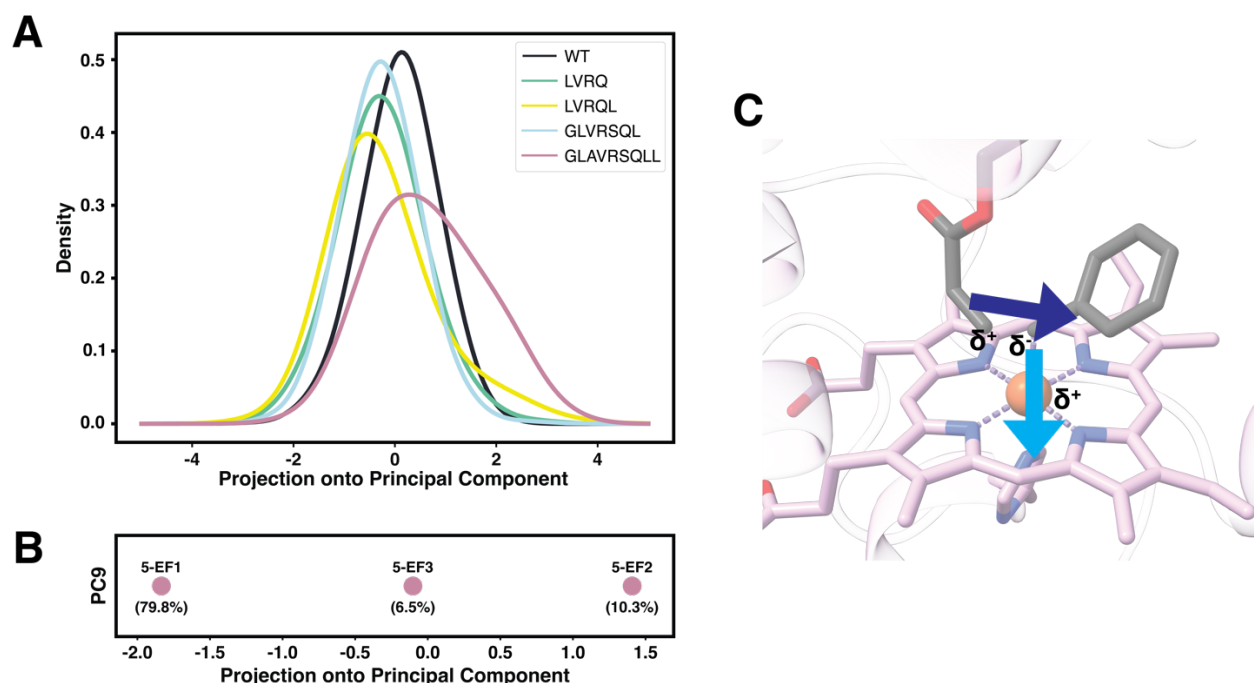


Figure 6. (A) Distribution of structures from replica molecular dynamics of all systems across the Principal Component 9. (B) Projections of GLAVRSQL electric field cluster centers on PC9. (C) Schematic of the PC9 direction plotted on **TS-GLAVRSQL-EF2** with the relative partial charges polarization marked on the atoms involved in bond rearrangements.

The isolated PC9 can be analyzed visually. It is curvy, and defined by two main directions: one tracing the path from the CC atom to the Fe and the other – from the C1 atom of the benzyl acrylate to the CC (**Figure 6C**, **Figure S6**). This field is straightforwardly linked to chemistry: in the TSs, the C1-CC bond is formed, and the electron density shifts from CC to C1 – a shift aided by the field of opposing direction. Similarly, the field pointing from CC to Fe aids the Fe-CC bond breaking in the TS. This implies that the intrinsic electric field alignment with PC9 in GLAVRSQL facilitates the barrier crossing. This relationship becomes even clearer when we plot the electric field clusters along PC9. We observe that the degree of alignment with PC9 in GLAVRSQL directly corresponds with the free energy barrier (**Figure 5A**, **Figure 6B**). Hence, the efficient catalysis observed in GLAVRSQL is largely driven by a shift in its intrinsic electric field toward the positive direction of PC9, which plays a key role in stabilizing its TS. The development of a PC9-type electric field appears to be a key achievement of DE of Protoglobin.

Conclusions

While computational design often struggles to enable enzymes to catalyze new chemical reactions, DE has emerged as a potent method for imparting novel catalytic abilities to enzymes. This contrast poses a crucial dichotomy: despite being effective, DE is a black box method where mechanisms for improved activity are obfuscated by the enzyme complexity. We shed new light on one possible mechanism by studying Protoglobin, a protein that, through DE, has developed the ability to catalyze carbene transfer reactions, leading to the cyclopropanation of benzyl acrylate. Initial analysis of multiple MD simulations of wild-type Protoglobin and its four evolved variants indicated that merely enhancing substrate access and binding to the active site does not fully

explain the improved cyclopropanation yield. Therefore, we turned our attention to the enzyme's electrostatic preorganization. We have developed a detailed and broadly applicable protocol to measure the 3D electric field topology and dynamics, and analyzed and compared these dynamic fields along the DE path using an affinity propagation clustering algorithm. We discovered significant alterations in the active site electric field as Protoglobin evolved. Through PCA, we identified a chemically meaningful field component that emerges and takes the lead during DE and facilitates crossing the barrier to carbene transfer. The catalytic role of the evolved electric field was confirmed by QM/MM mechanistic calculations. These calculations revealed that the nature of the reaction TS (concerted Fe-CC bond breaking and C1-CC bond formation, or asynchronous and led by the Fe-CC bond breaking) can be altered by the field geometry. In summary, fine-tuning the global electric field in the active site appears to be the key achievement of DE and is, therefore, an aspirational goal for *de novo* enzyme design.

Supporting Information. Additional molecular dynamics and QM/MM reaction mechanics analysis with optimized geometries, MCPB parameters, and PC9 html visualization files.

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