

Single-molecule spectroscopy and super-resolution mapping of physicochemical parameters in the living cell

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ABSTRACT

By super-localizing the positions of millions of single molecules over many camera frames, a class of super-resolution fluorescence microscopy methods known as single-molecule localization microscopy (SMLM) has revolutionized how we understand subcellular structures over the past decade. In this review, we highlight emerging studies that transcend the outstanding structural (shape) information offered by SMLM to extract and map physicochemical parameters in the living mammalian cell at single-molecule and super-resolution levels. By encoding-decoding high-dimensional information such as emission and excitation spectra, motion, polarization, fluorescence lifetime, and beyond, for every molecule, and mass-accumulating these measurements for millions of molecules, such multidimensional and multifunctional super-resolution approaches open new windows to intracellular architectures and dynamics, as well as their underlying biophysical rules, far beyond the diffraction limit.

1. Introduction

Recent advances in super-resolution fluorescence microscopy (SRM) based on the massive accumulation of the super-localized positions of single molecules that stochastically switch between emitting and dark states over different camera frames, *i.e.*, single-molecule localization microscopy (SMLM), have led to exciting scientific discoveries and technical developments (1-6). Many existing reviews on SMLM and SRM focus on the ever-increasing spatiotemporal resolutions, aiming to elucidate subcellular structural (shape) information to the best possible extent.

In this review, we focus on emerging work that transcends the outstanding structural information offered by SMLM to extract and map functional (7) physicochemical parameters in the living mammalian cell at single-molecule and super-resolution levels. While such experiments are often enabled by encoding-decoding new dimensions of single-molecule signal, they are also distinct from earlier single-

molecule studies in which isolated events are recorded (8-11). Instead, to achieve mapping at the nanoscale, single-molecule spectroscopies of various forms are mass-accumulated, often for millions of individual molecules, to be integrated with the super-localized positions of the same molecules. Below we categorize our discussion by the different single-molecule signal spaces being probed, including fluorescence intensity, spectra, motion, polarization, lifetime, and non-fluorescence methods. Together, these rising multidimensional SRM approaches afford rich spatial and functional information and hence exciting new insights into the dynamic processes and behaviors of the living cell.

2. Single-molecule fluorescence intensity

Fluorescence intensity remains the most straightforward parameter to analyze in single-molecule data. However, owing to the inherently large molecule-to-molecule variation in emission intensity in SMLM, small changes in intensity are difficult to discriminate. Fluorescence turn-on of initially dark probes offers a strategy to map physical parameters or chemical activities by counting the locally activated molecules. Still, such approaches leave ambiguities between the local level of activation and concentration of probes, hence a blurred boundary between functional and structural readouts. This issue may be overcome with fluorescence spectrum and lifetime detections, which are discussed later in Sections 3 and 6.

2.1. Fluorescence turn-on owing to specific local environments and protein conformations

A class of fluorogenic probes turn on when entering specific physical environments (12). For example, the solvatochromic dye Nile Red is non-fluorescent in aqueous solutions but becomes highly emitting in hydrophobic environments. This effect provides a mechanism in which dynamic single-molecule fluorescence on-off switching is maintained over long periods as probe molecules stochastically enter and exit the hydrophobic phase (**Figure 1a**), hence enabling SMLM for *in vitro* and cellular lipid membranes (**Figure 1b**) (13-16) and *in vitro* protein aggregates (15; 17-19). The fluorescence quantum yield of rotatable molecules can be strongly enhanced by conformation locking. For functional SMLM, such effects have enabled the detection and SRM imaging of specific protein conformations, *e.g.*, β -sheet aggregates in amyloid fibrils (19-24). Beyond the passive binding of fluorogenic probes, Liu *et al.* devised biosensors in which, upon protein conformation changes, a concealed small tag is exposed to bind with a fluorescent reporter. They thus detected single active proteins and tracked their motion in the live-cell plasma membrane (25).

2.2. Reaction-triggered fluorescence turn-on

Initially caged or quenched fluorophores may be turned on by chemical or enzymatic reactions (26), thus opening a window into local activities. For SMLM, Halabi *et al.* devised a fluorogenic probe that was activated by carboxylesterases (**Figure 1c**), and thus reconstructed SRM images of esterase activity in live cells (**Figure 1d**) (27). Chai *et al.* developed a β -galactosidase (β -Gal)-responsive photochromic fluorescent probe, enabling SMLM mapping of the subcellular distribution of β -Gal activity (28).

Fluorophore intensity may also be modulated by ion binding-unbinding. Fluorescent indicators have thus been employed to visualize local bursts of pH and Ca^{2+} signals in live cells. Treating individual

bursts, presumably owing to the collective responses of indicator molecules to individual sub-diffraction-limit events, *e.g.*, synaptic vesicle activities, analogous to single-molecule images in SMLM, thus allowed the super-resolution visualization of activity hotspots (29-31).

2.3. Fluorescence turn-on and fluctuation *via* interactions between biomolecules

Fluorescence turn-on and fluctuation may also be engineered *via* interactions between biomolecules. Based on the tension-induced unzipping of DNA structures, two recent studies employed fluorescent probes that were activated by the piconewton traction forces between single integrin proteins at the cell surface and the substrate, and so achieved SMLM force mapping (*e.g.*, **Figure 1ef**) (32; 33). With split fluorescent proteins (FPs), bimolecular fluorescence complementation (BiFC) has been successfully integrated with SMLM to map protein-protein interactions in live cells (34; 35). Meanwhile, fluorescence fluctuation increase by contact (FLINC) capitalizes on the elevated fluctuations in fluorescence intensity when two FPs are brought into proximity, thus achieving SRM of enzyme activities in live cells (36; 37).

3. Single-molecule spectral responses

Spectral responses provide a robust way to encode functional information that is decoupled from the fluorescence intensity and count of single molecules. Although it has been technically demanding to extract the spectral characteristics of single molecules, recent years have seen the emergence of new approaches that well suit the unique operational schemes of SMLM.

3.1. Wavelength-split detection

A facile method to detect single-molecule spectral responses is wavelength-split detection, in which a dichroic mirror splits (wide-field) fluorescence into two views for the separate, parallel recording of long- and short-wavelength components (**Figure 2a**). For SMLM, this approach enables the identification of single molecules based on the ratio of the detected photon counts in the two views (**Figure 2b**). With a single excitation laser, multicolor SMLM is thus concurrently performed for 2-4 fluorophores of overlapping spectra (*e.g.*, **Figure 2c**) (38-40). For imaging functional parameters, local pH has been examined in gel and silica systems through the two-wavelength ratiometric single-molecule detection of SNARF-1, a fluorescent pH indicator that exhibits substantially different emission spectra in its protonated and deprotonated states, so far limited to sparse molecules (41; 42).

Wavelength-split detection schemes have also been vital to Förster resonance energy transfer (FRET) experiments, in which the relative emission intensities of donor and acceptor fluorophores serve as a molecular ruler for quantifying interactions and conformational dynamics at sub-10 nm length scales (43; 44). Chemically synthesized and genetically encoded FRET-based biosensors have elucidated vital functional parameters inside the living cell, including ion and small-molecule concentrations, cellular microenvironments, and enzymatic activities (45; 46).

Single-molecule FRET (smFRET) offers powerful insights into parameters obscured in ensemble averaging, *e.g.*, multiple states and their interconversions, and so has become an indispensable tool for studying biomolecular conformations and dynamics *in vitro* (44; 47; 48). However, smFRET has seen

limited applications in live cells (44; 49). The relatively low brightness and large size of fluorescent proteins make them unfavorable for smFRET; various approaches have thus been devised to introduce organic dye-based smFRET probes into mammalian and bacterial cells, including microinjection (50-52), heat shock (53), and electroporation (54), or combining FPs with self-labeling tags and fluorogenic membrane-permeable dyes (55). Separately, dye tagging can be more readily achieved for targets at the cell surface (56-58).

With the labeling issues addressed, live-cell smFRET is so far still limited in spatial mapping capabilities. For example, the formation of SNARE protein complexes in the live cell has been examined with wide-field smFRET, but only for \sim 100 sparsely distributed molecules (51). With confocal smFRET, Konig *et al.* monitored the compaction of the intrinsically disorder protein ProTa in live cells, but only discussed limited spatial information by distinguishing molecules located in the nucleus, cytosol, and outside the cell (52). For studying the dimerization of G protein-coupled receptors (GPCRs) at the cell surface, Asher *et al.* recorded long time traces to monitor dimer conformations and intra-membrane diffusion, but under either low expression levels or after photobleaching to ensure sparse single molecules (58). Utilizing the dynamic binding-unbinding of epidermal growth factor (EGF) labeled by donor or acceptor dyes to EGF receptors (EGFRs) at the cell surface, Winckler *et al.* recorded high-density smFRET in the wide field over \sim 10⁴ frames, and so obtained SMLM maps of EGFR dimers, showing preferential localization to the cell edge (**Figure 2d**) (57). However, quantification of such smFRET data is difficult, as the stochastic labeling leads to only a small proportion of the dimers containing both the donor and acceptor dyes.

3.2. Spectrally resolved SMLM

Although wavelength-split detection is simple in implementation, it achieves limited spectral sensitivity. The ratiometric readouts calculated from the two split views depend on the spectral characteristics of the dichroic mirror used, and so are difficult to compare between studies and vulnerable to operational conditions, including backgrounds.

To resolve the actual emission spectra of single molecules, typical approaches spatially confine the illumination and/or detection (*e.g.*, to a single spot in a confocal setting) to ensure fluorescence is spectrally dispersed from only one single molecule at a time (9; 59). Scanning across the sample then maps out the spectra of different molecules. Although good spectra are recorded, such single-spot detection schemes afford low throughput and limit samples to sparse molecules that are resolvable with diffraction-limited optics.

These limitations are overcome by a new detection scheme in which single-molecule fluorescence is dispersed in the wide field (60; 61). For molecules sparsely distributed in each frame, as encountered in SMLM, it is noted that their images are self-confined into individual emission spots. Concurrent spectral dispersion of these point sources in the wide field thus enables the parallel recording of tens of single-molecule spectra with a \sim 10 ms camera snapshot (**Figure 3ab**). Next, utilizing single-molecule fluorescence on-off switching to visit different molecules over consecutive camera frames, a key strategy

of SMLM, the spectra of millions of single molecules are thus acquired in minutes, hence affording ultrahigh-throughput single-molecule spectroscopy.

The massively accumulated single-molecule spectra, alongside the concurrently super-localized positions of the same molecules, are synthesized into spectrally resolved SMLM (SR-SMLM) data affording local emission spectra at nanoscale spatial resolution (15; 60-63). When applied to multiplexed imaging (60; 62-64), such approaches achieved crosstalk-free three-dimensional (3D) SRM for four fluorophores with heavily overlapping spectra (60) and the simultaneous tracking of different single molecules and quantum dots (64; 65).

Integration with fluorescent probes that exhibit spectral changes in response to local physicochemical parameters next enabled super-resolution functional mapping. With the solvatochromic dye Nile Red, SR-SMLM thus resolved nanoscale heterogeneities in the membranes of live mammalian cells, showing the intracellular organelle membranes as chemically more polar than the plasm membrane owing to less ordered lipid packing (**Figure 3cd**), and noting the formation of low-polarity, raft-like nanodomains in the plasma membrane upon cholesterol addition or cholera-toxin treatment (16). For *in vitro* systems, Nile Red-based SR-SMLM has similarly resolved chemical polarities for model lipid bilayer membranes and vesicles (15; 16; 66), protein aggregates (**Figure 3ef**) (15; 17; 19), surface adlayers (67), and polymeric nanoparticles (68). A tailor-made Nile Red derivative further enabled the specific probing of the live-cell plasma membrane, unveiling nanoscopic protrusions and invaginations of reduced lipid order (**Figure 3g**) (69). Future SR-SMLM developments may harness the genetic targeting of Nile Red (70; 71) to probe specific subcellular targets.

3.3. Excitation-based spectral imaging

Although spectral fluorescence microscopy methods (72; 73), including SR-SMLM, provide powerful paths toward multiplexed and functional imaging, typical approaches of dispersing the local emission are difficult to implement and limit the time resolution.

Recent work highlights the power of excitation-based spectral microscopy (74-76). By collecting fluorescence with a fixed emission band but scanning the excitation wavelength for the entire imaging field, such schemes remove the need to disperse the emission signal over many detector pixels, as required in typical emission-based spectral microscopy, yet achieve comparable spectral unmixing capabilities. Thus, with camera frame-synchronized fast scanning of the excitation wavelength (**Figure 4a**), six subcellular targets, labeled by fluorophores substantially overlapping in spectrum, were simultaneously imaged in the wide field using a single filter cube at low crosstalk and high speeds (76). Combining different filter cubes enabled multiplexing with more fluorophores (77). The ability to quantify the abundances of different species via the excitation spectra (**Figure 4b**) further enabled the fast, quantitative imaging of intracellular physicochemical parameters, such as pH (**Figure 4c**) and macromolecular crowding, with bi-state and FRET-based biosensors (76).

The application of excitation-based spectral microscopy to SMLM, however, is non-trivial. As the excitation spectrum is collected by monitoring the emission intensity when the excitation wavelength is

scanned, the frequent on-off switching of single-molecule emission in SMLM makes it unreliable, if not impossible, to determine how the emission intensity responses to excitation wavelengths scanned over consecutive camera frames. Wu *et al.* provided an elegant solution in which a resonant mirror rapidly switched the wide-field image back and forth between three recording positions for many rounds within each camera frame (**Figure 4d**) (78). With three synchronized excitation lasers, they thus well discriminated four spectrally overlapped fluorophores for the tetra-color SMLM of fixed cells (**Figure 4e-g**). The potential application of related approaches to living cells and to the functional readouts of fluorescent biosensors presents exciting perspectives.

4. Single-molecule motions

Motions provide yet another great window into molecular behaviors and interactions. Resolving the intracellular movement of biomolecules may enable the spatial mapping of biophysical parameters including diffusion modes and constants, viscosity, binding kinetics, and conformational states (79-86).

4.1. Fluorescence correlation spectroscopy

Fluorescence correlation spectroscopy (FCS) measures fluorescence fluctuations as single molecules transiently enter and leave the detection spot, *e.g.*, in a confocal setting. Through time-correlating the detected fluctuations, FCS provides valuable insights into intracellular diffusions, concentrations, and intermolecular interactions (80; 87; 88). Recent integration with STED (stimulated emission depletion) SMLM has further pushed FCS beyond the diffraction limit (89). However, single-molecule events are not isolated, and FCS generally achieves limited spatial mapping capabilities (88; 90).

4.2. Single-particle tracking

To access motions at the true single-molecule level, single-particle tracking (SPT) has found wide use in living cells and been the subject of many reviews (79; 81; 82; 91). Super-localizing single molecules enables motion quantification at the nanoscale. Recent advances in MINFLUX, a method that modulates the illumination pattern to achieve photon-efficient localization of single molecules with exceptional spatiotemporal resolutions (92), have permitted the direct observation of a dye-tagged motor protein stepping on intracellular microtubules with <5 nm spatial resolution at few-millisecond temporal resolutions (93). Monitoring the motion of a single molecule over long trajectories further allows the observation of asynchronous dynamics, *e.g.*, transient intermolecular interactions, and the extraction of diverse biophysical parameters such as binding kinetics, non-Brownian diffusion modes, and directional transport (81; 84).

While SPT is traditionally applied to sparse molecules to avoid trajectory overlapping, recent developments integrating SMLM-inspired photoactivation and fluorophore-exchange schemes have permitted the high-density tracking of single-molecule trajectories (57; 91; 94-97). However, the focus is often on obtaining long trajectories to assign a diffusion coefficient value to each molecule, thus yielding limited spatial mapping and restricting applications to slow diffusion in membranes, where the bound molecules stay in focus over many frames.

4.3. Single-molecule displacement/diffusivity mapping

To overcome SPT's limited spatial mapping capabilities and access the fast diffusion of unbound molecules, an emerging approach, single-molecule displacement/diffusivity mapping (SMdM) (98; 99), forgoes trajectories but focuses on transient displacements. Thus, rather than following how each molecule behaves as it randomly visits different, potentially heterogeneous locations, SMdM flips the question to survey, for each fixed location, how different (yet identical) single molecules move locally. This location-centered strategy is naturally powerful for spatial mapping. Moreover, by focusing on transient displacements, each molecule only needs to be localized twice within a short time window. For fast-diffusing molecules, a tandem excitation scheme is thus devised to apply a pair of closely timed stroboscopic pulses across two camera frames to capture single-molecule images over time separations substantially shorter than the camera frame time, from which single-molecule displacements are extracted (**Figure 5ab**) (98). This tandem excitation scheme further leaves ample time between the anti-paired pulses (**Figure 5ab**) to allow efficient probe exchanges through diffusion, thus enabling SMdM for non-photoswitchable fluorophores (98; 100). Repeating the above scheme $\sim 10^4$ times next accumulates millions of single-molecule displacements to be spatially binned for individual fitting to extract local diffusion coefficient D (**Figure 5cd**) and generate its super-resolved map (**Figure 5e**) (98). Local displacement direction analysis is further developed to elucidate diffusion anisotropy (**Figure 5f**) (99; 101).

With ~ 30 kDa FPs, SMdM thus uncovered nanoscale diffusion heterogeneities in the mammalian cytoplasm (**Figure 5e**), nucleus (**Figure 5g**), and organelles, and identified the protein net charge as a key determinant of intracellular diffusion (**Figure 5h**) (98; 101). By squeezing the tandem-pulse time separation to 400 μ s and incorporating graphene-based electroporation for probe delivery (102), SMdM further quantified the very fast diffusion of small (<1 kDa) solutes, unveiling their unhindered diffusion in the mammalian cell (**Figure 5i**) (100). For cellular membranes, integration of SMdM with Nile Red-based SR-SMLM resolved diffusion heterogeneities of different origins (99). For *in vitro* FUS condensates formed through liquid-liquid phase separation, SMdM unveiled substantial diffusion slowdowns at surface nanoaggregates (19).

The massively accumulated single-molecule displacements in SMdM further enable D -value determination to $\pm 1\%$ precisions (103), which has been utilized to establish a universal dependency of D on molecular weight for proteins and small molecules (102; 103), show no changes in D in enzyme reactions (103), and determine how D scales with meshwork sizes in expandable hydrogels (104).

While SMdM of FPs in mammalian cells has so far focused on elucidating nonspecific charge interactions, tagging FPs to specific intracellular proteins could employ SMdM to map intracellular protein conformation, oligomerization, and interactions; recent SMdM work on bacteria has pointed to such directions (105; 106). The compatibility of SMdM with non-photoswitchable fluorophores (98; 100) and the demonstrated successful intracellular probe delivery for SMdM (100) further imply the possible integration of SMdM with the above-discussed dye-based smFRET for functional readouts. Meanwhile,

while SMdM has unveiled rich diffusion heterogeneity by just analyzing single-step displacements between tandem frames, future developments may expand on this concept to enable the detection of few-step short tracks, from which one may garner information on nonlinear diffusion and dynamic transition between states.

5. Single-molecule fluorescence polarization and anisotropy

Fluorescence polarization and anisotropy offer valuable information about molecular orientations and dynamics (107; 108). Splitting the fluorescence emission into orthogonal polarizations and/or modulating the polarization orientation of the excitation laser enable the encoding-decoding of single-molecule polarization and anisotropy in SMLM (109-112).

Biological filaments are often assembled from oriented subunits. For *in vitro* samples, the fixed binding orientations of fluorogenic probes to filaments have thus yielded clear molecular orientations for DNA strands (111-113) and amyloid fibrils (18; 21) in polarization-resolved SMLM data. For imaging in the mammalian cell, early studies examined fluorescence anisotropy in the SMLM data of FP-tagged actin to detect local heterogeneity in rotational mobility (109; 110). Valades Cruz *et al.* compared polarization-resolved SMLM data for differently labeled microtubule and actin cytoskeletons in fixed cells, and identified Alexa Fluor 488-phalloidin as a good probe to resolve the orientation of the latter (112). By delivering the same probe into live mammalian cells at low concentrations, Mehta *et al.* resolved actin filament orientations in SPT to compare with the retrograde flow direction at the leading edge (114). Rimoli *et al.* recently developed strategies to determine single molecules' orientation in 2D and infer their 3D orientations, which they applied to the SMLM of Alexa Fluor 488-phalloidin-labeled dense actin structures in fixed cells (**Figure 6a-d**) (115).

Polarization-based functional SMLM has also shed new light on the structure of lipid membranes. Integrating polarized beam-splitting and a spatial light modulator, Lu *et al.* encoded 3D orientation and wobbling into the single-molecule point spread function, and thus analyzed the ordering and packing effects of cholesterol in supported lipid bilayers and resolved nanoscale domains with different ordering parameters (116). A recent study constructed a radially and azimuthally polarized multi-view reflector to image single-molecule fluorescence across eight polarization channels to simultaneously determine molecular location and orientation in three dimensions each, and the resultant 6D SMLM resolved dye orientations in fixed-cell membranes (**Figure 6e-f**) (117).

6. Single-molecule fluorescence lifetime

By detecting the exponential decay rate of emission at the nanosecond time scale, fluorescence lifetime imaging microscopy (FLIM) provides a powerful, probe concentration-insensitive handle for the functional imaging of biological samples (118-120), with diverse probes developed for chemical polarity, viscosity, temperature, and different analytes.

Fluorescence lifetime-resolved SMLM (FL-SMLM) has been achieved with both confocal and wide-field experimental setups (**Figure 7a-d**), utilizing a single-element single-photon avalanche diode

detector or an array detector based on a microchannel-plate photomultiplier tube, respectively (121; 122). Whereas confocal setups can only image a relatively small field of view with reasonable imaging speeds, the currently available array detectors suffer from low (~5%) quantum efficiencies. Lifetime estimations can also be made for the wide field with conventional high-sensitivity cameras by time-gating the signal electro-optically with a Pockels cell (**Figure 7ef**) (123), but with limitations on sensitivity.

Thus far, the application of FL-SMLM has been limited to *in vitro* samples and fixed cells, with an initial focus on separating labels for multiplexed imaging (**Figure 7bcf**) (121; 122; 124). Recent work detected FRET (125) and metal/graphene-induced energy transfer (122; 126; 127), the latter further enabling 3D-SMLM by providing an interesting way to determine the fluorophore's distance to the substrate (**Figure 7d**). Possible future FL-SMLM applications to live cells and to the super-resolution mapping of local environments and intermolecular interactions hold great potential.

7. Non-fluorescence methods

The above success of SMLM for functional SRM imaging raises the question of whether related approaches could be applied to non-fluorescence methods, which may overcome the limited number of photons that can be extracted from individual fluorophores, enable label-free imaging, or access new spectroscopy insights for decoding physicochemical parameters (128-130).

Microspheres and nanoparticles have long served as unbleachable probes for live-cell SPT (91; 131). Recent advances in photothermal microscopy (91; 128; 132) and interferometric scattering microscopy (133-136) have further enabled the SPT of small gold nanoparticles in live cells, as well as the room-temperature detection and analysis of single molecules *in vitro*. It, however, remains a challenge to resolve single molecules in the crowded cell, or to detect many molecules within the diffraction limit.

Nonlinear optical methods such as nonlinear Raman, harmonic generation, multiphoton fluorescence, and transient absorption offer intriguing prospects for functional SRM for their outstanding chemical and structural contrasts (130; 137-139). Super-resolution nonlinear optical microscopy has been achieved with expansion microscopy (140; 141), STED-based imaging (142), and interferometric excitation (143), among other approaches (129; 130). Application to SMLM is limited by the relatively low probability of nonlinear optical processes and the need for a scalable approach to signal modulation for the isolation of single molecules. Plasmonic amplification of light-matter interactions (144) provides a viable path; surface-enhanced Raman spectroscopy (SERS) has achieved single-molecule sensitivity (145; 146), and its local blinking has enabled SMLM-type imaging of dried samples (147; 148). However, the patterned plasmonic substrates distort the resultant image, and their required proximity to the sample limits applicability.

8. Conclusion

In conclusion, while the outstanding spatial resolution of SMLM has attracted wide attention, in this review we have showcased how, by extending mass-accumulated single-molecule measurements to higher dimensions, including emission and excitation spectra, motion, polarization, and fluorescence lifetime,

the resultant multidimensional SRM approaches provide fascinating new insights into physicochemical parameters in the living cell.

Future developments call for a synergy of continued innovations in optics on both the excitation and detection fronts, fluorescent probe design, synthesis, and delivery methods, as well as algorithm and analysis tools. The need to detect single molecules and invoke fluorescence on-off switching poses significant challenges: optimal results thus demand bright probes with high fluorescence quantum yields, while on-off mechanisms such as photoswitching or reversible binding often need to be built in. Yet, the uniqueness of sparse molecules across the camera frame, as often achieved in SMLM, offers new possibilities, so that single-molecule images may be directly stretched/dispersed in the wide field for high-throughput recording, and the recorded signal from each molecule is guaranteed a single identity, removing the need of unmixing. New illumination sequences further enable SMLM/SMdM for constantly bright fluorophores *via* diffusion-based probe exchange. Integrations between different SMLM modules, as well as correlative approaches with other microscopy and spectroscopy techniques (149), provide additional opportunities.

DISCLOSURE STATEMENT

The authors are not aware of any affiliations, memberships, funding, or financial holdings that might be perceived as affecting the objectivity of this review.

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Figure Captions

Figure 1. SMLM *via* fluorescence turn-on from specific local environments, reactions, and engineered biomolecular interactions. (a) Fluorescence intensity time trace for a lipid vesicle, showing bursts due to the stochastic entering of single Nile Red molecules into the lipid phase from the aqueous medium. (b) SMLM image of a supported lipid bilayer obtained by localizing 2,778 single Nile Red molecules over 4,095 frames due to the above fluorescence turn-on process. Panels *a-b* adapted from Reference (13); copyright 2006 National Academy of Sciences. (c) Schematic: A caged (initially dark) probe (**1**) that can be photoactivated into a fluorescent state after removal of the acetyl group by carboxylesterases (**2**). (d) SMLM image of esterase activity based on **1** in a live mammalian cell. Panels *c-d* adapted with permission from Reference (27); copyright 2017 American Chemical Society. (e) Schematic: Cellular force SMLM

based on force-activatable emitters in which the unzipping of a DNA/PNA (peptide nucleic acid) hybrid leads to fluorescence dequenching and single-molecule emission. (f) Resultant integrin molecular tension SMLM of a migrating keratocyte from 20 frames of recording. Panels *e-f* adapted with permission from Reference (32); copyright 2020 American Chemical Society.

Figure 2. Split-wavelength detection for multicolor SMLM and smFRET in living cells. (a) Schematic: A dichroic mirror (DCM) separates long- and short-wavelength components of single-molecule emission for simultaneous imaging on two areas of a CCD. (b) Distribution of photon counts in the long- and short-wavelength channels for single molecules detected in SMLM, for four dyes with overlapping emission spectra (inset) (c) Simultaneous four-color SMLM of a fixed cell by separating the single-molecule emission of four dyes based on *b*. Panels *b-c* adapted with permission from Reference (39); copyright 2010 Elsevier. (d) SMLM images due to the binding-unbinding of a mixture of donor- and acceptor-labeled EGF molecules to EGFR in the plasma membrane of a live mammalian cell, for the donor (top) and acceptor (bottom) channels when exciting the donor. Insets: Zoom-ins of the boxed regions. Single-molecule emission in the acceptor channel is attributed to smFRET between single donor- and acceptor-labeled EGFs bound to an EGFR dimer. Panel *d* adapted from Reference (57) (CC BY-NC-ND).

Figure 3. SR-SMLM and super-resolution mapping of chemical polarity for live-cell membranes and *in vitro* protein aggregates. (a) Schematic: Fluorescence is dispersed in the wide field, so the emission spectra of many single molecules are concurrently captured in a camera frame. Single-molecule fluorescence on-off switching next enables the sampling of different molecules over consecutive frames. (b) Example spectra of single Alexa Fluor 647 molecules recorded in a 9-ms camera frame. Panel *b* adapted from Reference (60). (c) SR-SMLM image of Nile Red-highlighted lipid-membrane system in a live mammalian cell. Color presents the single-molecule spectral mean; longer emission wavelengths correspond to higher local chemical polarities. (d) Averaged single-molecule spectra at the plasma membrane versus the internal nanoscale organelle membranes, compared to that at supported lipid bilayers with and without the packing-order promoter cholesterol (Chol). Panels *c-d* adapted with permission from Reference (16); copyright 2017 American Chemical Society. (e) SR-SMLM images of Nile Red at the surfaces of *in vitro* amyloid- β oligomers (left) and fibrils (right). (f) Frequency histogram of fluorescence emission peaks for individual Nile Red molecules at the amyloid- β oligomers and fibrils. Panels *e-f* adapted from Reference (15) (CC BY). (g) SR-SMLM image for the plasma membrane of a live mammalian cell labeled by NR4A, a Nile Red derivative. Arrows point to higher local chemical polarities at endocytic sites due to reduced lipid order. Panel *g* adapted with permission from Reference (69).

Figure 4. Excitation-based spectral microscopy and application to SMLM. (a) Schematic: the excitation wavelength is varied in consecutive frames through the frame-synchronized modulation of the acousto-optic tunable filter (AOTF). P polarizer, L lens, F bandpass filter, DM dichroic mirror. (b) 8-wavelength excitation spectrum recorded with the setup in *a*, for pHRed FP expressed in a mammalian cell that was

equilibrated to $\text{pH} = 8.0$ (black solid line), and its linear unmixing into the deprotonated (A^-) and protonated (HA) components (dash lines). (c) Color-coded absolute pH map series for pHRed expressed in the mitochondrial matrix in a living mammalian cell, as obtained through the linear unmixing of the excitation spectrum as in *b*, showing concurrent fast changes in both the mitochondrial shape and matrix pH at 0.8 s time resolution. Panels *a-c* adapted from Reference (76) (CC BY 4.0). (d) Schematic for excitation-resolved SMLM: A resonant mirror fast-switches the wide-field image back and forth between three recording positions with synchronized excitation of three lasers of different wavelengths. (e) Scatter plot of the photon counts for individual Alexa Fluor 647 molecules when excited by the three lasers. (f) Tetra-color SMLM by separating the excitation characteristics of four dyes based on their three-excitation-wavelength single-molecule photon counts as shown in *e*. (g) Separated channels for the box in *f*, showing minimal crosstalk. Panels *d-g* adapted from Reference (78) (CC BY 4.0).

Figure 5. SMdM: Super-resolution mapping of fast intracellular diffusion. (a) Schematic: A pair of closely timed stroboscopic excitation pulses are applied across two tandem camera frames, so that the two recorded images correspond to the short time separation Δt between the paired pulses. This paired excitation scheme is repeated $\sim 10^4$ times to enable statistics. (b) Example single-molecule images of sulforhodamine-101 molecules diffusing in a living rat astrocyte, recorded in four consecutive frames with the above tandem excitation scheme. Here, each pulse lasted 200 μs , the center-to-center separation between paired pulses was $\Delta t = 500 \mu\text{s}$, and the camera frame time was 9.15 ms. Insets: comparison of the localized single-molecule positions across the tandem frames, from which single-molecule displacements are extracted. Panel *b* adapted with permission from Reference (100); copyright 2023 American Chemical Society. (c,d) Distributions of displacements in $\Delta t = 1 \text{ ms}$ for single mEos3.2 FP molecules in a living mammalian cell, for two adjacent $300 \times 300 \text{ nm}^2$ areas marked with orange and red boxes in *e*. Blue curves: fits to a diffusion model, with resultant D values labeled. (e) Color-coded SMdM D map for the intracellular diffusion of mEos3.2, obtained by spatially binning the accumulated single-molecule displacements onto $100 \times 100 \text{ nm}^2$ grids for local fitting as in *c,d*. Panels *c-e* adapted from Reference (98). (f) Color map presenting the SMdM-determined local principal direction of diffusion for BDP-TMR-alkyne in cellular membranes, showing anisotropic diffusion along the endoplasmic-reticulum tubules. Panel *f* adapted with permission from Reference (99) ; copyright 2020 American Chemical Society. (g) SMdM D map for mEos3.2 FP in the nuclear region of a living mammalian cell (left) versus SMLM of the same region with a DNA stain (right), showing reduced D in the nucleolus (asterisk) and fast and slow diffusion regions correlating to low and high local DNA densities (red and orange arrows). (h) SMdM-determined mean D values for mEos3.2 FPs of different net charges in different subcellular environments. Panels *g-h* adapted from Reference (98). (i) SMdM D map of Cy3B dye in a living mammalian cell, obtained with $\Delta t = 400 \mu\text{s}$. Panel *i* adapted with permission from Reference (100); copyright 2023 American Chemical Society.

Figure 6. Polarization-resolved SMLM and its applications to cytoskeleton and membrane in fixed cells. (a) Schematic: fluorescence polarization behavior of Alexa Fluor 488-phalloidin labeling an actin filament.

(b) Schematic: extracting single-molecule fluorescence polarization orientation and wobbling by combining a half-wave plate (HWP) and two polarizing beamsplitters (PBS) and applying diaphragms (D) to reduce the detection numerical aperture. (c-d) Resultant SMLM images resolving the mean orientation (c) and wobbling angle (d) of Alexa Fluor 488-phalloidin labeling the actin cytoskeleton in a fixed cell. Panels *a-d* adapted from Reference (115) (CC BY). (e,f) 6D (3D spatial and 3D orientational) SMLM imaging of merocyanine 540 molecules bound to the membrane of a fixed cell: (e) In plane (*x*-*y*) view, colored by the single-molecule azimuthal angle ϕ . (f) Vertical (*y*-*z*) view of the boxed region, colored by the single-molecule polar angle θ . Panels *e-f* adapted with permission from Reference (117).

Figure 7. Fluorescence lifetime-resolved SMLM. (a) Comparison of the fluorescence lifetime of single molecules of five dyes measured with confocal and wide-field SMLM setups. (b) Top: Wide-field lifetime-resolved SMLM image of a fixed cell double labeled with Cy3B against peroxisomes and Atto 550 against mitochondria, with color presenting the measured lifetime. Bottom: Zoom-in of the boxed region and separation of the two dyes based on lifetime. (c) Lifetime histograms corresponding to *b*. Panels *a-c* adapted from Reference (122) (CC-BY-NC-ND 4.0). (d) Fluorescence lifetime curves for AF647-DNA molecules on glass and on gold substrates with 10-50 nm thick SiO₂ spacers measured with confocal lifetime imaging, demonstrating distance-dependence decreases in fluorescence lifetime owing to metal-induced energy transfer. Panel *d* adapted from Reference (126) (CC BY-NC). (e) Schematic: Time-gated electro-optic imaging for wide-field lifetime-resolved SMLM using a resonantly driven Pockels cell and a polarizing beamsplitter. (f) Resultant lifetime-resolved SMLM image of DNA origamis labeled with Cy3B and Atto 565. Panels *e,f* adapted with permission from Reference (123); copyright 2021 American Chemical Society.

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