

The proto-galaxy of Milky Way-mass haloes in the FIRE simulations

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ABSTRACT

Observational studies are finding stars believed to be relics of the earliest stages of hierarchical mass assembly of the Milky Way (i.e. proto-galaxy). In this work, we contextualize these findings by studying the masses, ages, spatial distributions, morphology, kinematics, and chemical compositions of proto-galaxy populations from the 13 Milky Way (MW)-mass galaxies from the FIRE-2 cosmological zoom-in simulations. Our findings indicate that proto-Milky Way populations: (i) can have a stellar mass range between $1 \times 10^8 < M_\star < 2 \times 10^{10} [M_\odot]$, a virial mass range between $3 \times 10^{10} < M_\star < 6 \times 10^{11} [M_\odot]$, and be as young as $8 \lesssim \text{Age} \lesssim 12.8 [\text{Gyr}]$ ($1 \lesssim z \lesssim 6$); (ii) are pre-dominantly centrally concentrated, with ~ 50 per cent of the stars contained within 5–10 kpc; (iii) on average show weak but systematic net rotation in the plane of the host’s disc at $z = 0$ (i.e. $0.25 \lesssim \langle \kappa / \kappa_{\text{disc}} \rangle \lesssim 0.8$); (iv) present $[\alpha/\text{Fe}]-[\text{Fe}/\text{H}]$ compositions that overlap with the metal-poor tail of the host’s old disc; and (v) tend to assemble slightly earlier in Local Group-like environments than in systems in isolation. Interestingly, we find that ~ 60 per cent of the proto-Milky Way galaxies are comprised by 1 dominant system ($1/5 \lesssim M_\star / M_{\text{proto-MilkyWay}} \lesssim 4/5$) and 4–5 lower mass systems ($M_\star / M_{\text{proto-MilkyWay}} \lesssim 1/10$); the other ~ 40 per cent are comprised by 2 dominant systems and 3–4 lower mass systems. These massive/dominant proto-Milky Way fragments can be distinguished from the lower mass ones in chemical-kinematic samples, but appear (qualitatively) indistinguishable from one another. Our results could help observational studies disentangle if the Milky Way formed from one or two dominant systems.

Key words: Galaxy: general – Galaxy: formation – Galaxy: evolution – Galaxy: halo – Galaxy: abundances – Galaxy: kinematics and dynamics.

1 INTRODUCTION

In the current accepted model for cosmology (Λ CDM), haloes grow by accumulating lower mass building blocks through a process commonly referred to as hierarchical mass assembly (e.g. White & Rees 1978; White & Frenk 1991). During this process, the baryonic components (i.e. gas and stars that constitute observable galaxies) of haloes also undergo this mechanism of mass accumulation. This procedure is ubiquitous across the universe and affects all galaxies. Thus, the accretion history of a galaxy is a pivotal dictating factor for its evolution and assembly of mass over time, and the clues for

disentangling such intricate process are all contained in the stellar halo.

Our current picture for the formation of stellar haloes suggests that they form via a dual process. On the one hand, gas accretion from cosmic filaments drives secular evolution and *in situ* star formation. On the other hand, the accretion of different mass building blocks¹, each of which donate their gas and stars to the resulting larger mass host, contribute in mass to a given galaxy after becoming consumed. For the case of the Milky Way, early observational evidence has suggested that the former process dominates within the inner regions (i.e. $r \lesssim 20$ –30 kpc), whereas the latter dominates the outer regime

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¹A definition of building block and main branch systems is provided in Table 1.

(e.g. Chiba & Beers 2000; Carollo et al. 2007; Deason, Belokurov & Evans 2011). However, more recent observational results suggest that the *in situ* component may be a heated primordial disc (e.g. Bonaca et al. 2017; Di Matteo et al. 2019; Belokurov et al. 2020). This dual formation channel has also been somewhat shown to be the case in Andromeda (M31; e.g. Ferguson et al. 2002; Brown et al. 2006; Escala et al. 2019, 2020). The advent of detailed semi-analytic cosmological models and more recent detailed cosmological simulations have supported this hypothesis on a theoretical basis (Bullock & Johnston 2005; Abadi, Navarro & Steinmetz 2006; Bell et al. 2008; Font et al. 2008; Johnston et al. 2008; Cooper et al. 2010; Font et al. 2011; McCarthy et al. 2012; Amorisco 2017; Khoperskov et al. 2022a, b). However, whilst this picture may appear clear at current time, detailed spectroscopic, photometric, and astrometric observations of halo stars with *Gaia* (Gaia Collaboration et al. 2022) and large stellar surveys are starting to poke holes in this framework.

Recent observational results have shown that the inner ~ 30 kpc of the Milky Way's stellar halo is awash with debris from engulfed satellite systems. More specifically, it has been shown that in the Milky Way: (i) the local stellar halo is dominated by the debris of a massive and (likely) ancient merged galaxy (*Gaia*-Sausage/Enceladus; Belokurov et al. 2018; Haywood et al. 2018; Helmi et al. 2018; Mackereth et al. 2019), although see a counter-argument by Donlon Thomas et al. (2022); ii) the innermost regions of the galaxy ($r < 5$ kpc) likely host the debris from an ancient and massive building block (Heracles; Horta et al. 2021a)²; this system could be related to another population recently identified, referred to as the ‘proto-Milky Way’ or Aurora (Conroy et al. 2021; Belokurov & Kravtsov 2022; Rix et al. 2022); (iii) there are numerous smaller-mass halo substructures/streams postulated to be the debris from smaller mass accreted systems (see Helmi 2020 for a review). Along those lines, further out in the stellar halo, there are also streams from currently/recently disrupted satellites (e.g. Sagittarius dSph, Ibata, Gilmore & Irwin 1994; Cetus, Newberg, Yanny & Willett 2009; Orphan-Chenab, Grillmair & Dionatos 2006; Belokurov et al. 2007)³. All these different systems suggest that many components contribute to the formation of the Milky Way's stellar halo at all radii, in agreement with recent findings using cosmological simulations (e.g. Khoperskov et al. 2022b; Orkney et al. 2023; Horta et al. 2023b).

The recent plethora of observational findings hint towards the epoch of formation for the Milky Way being early ($\gtrsim 8$ Gyr). This implies that the major building blocks of the galaxy are many gigayears old. While lower-mass/unmixed accretions are interesting for unveiling the recent mass assembly history of the galaxy, or are useful in terms of potential measuring and dynamical studies, it is the early building blocks and accretion events that: (i) constitute the bulk of the inner regions of the present day stellar halo (i.e. $r \lesssim 30$ kpc); (ii) supply the gas and baryonic material to fuel the formation of the disc; (iii) dictate key episodes in the formation of the Milky Way. For this reason, observational studies have set out to investigate the properties of the oldest stellar populations in the Milky Way, and have reported chemical-kinematic evidence for the presence of stellar populations in the innermost regions of the galaxy – where one would expect the oldest stars formed *in situ* to inhabit (El-Badry et al. 2018; Frakoudi et al. 2020) – that are distinguishable from the dominant bar/disc, and are likely to constitute the entirety, or part of, the ‘proto-Milky Way’. This stellar population has been postulated to arise from the main

progenitor system of the Milky Way, a major building block, or both simultaneously. Whilst the nature of this population is yet to be fully established, these findings have instigated the search for answers to additional pivotal questions when it comes to understanding the formation of the galaxy:

- (i) When did the proto-Milky Way form?
- (ii) What constitutes the proto-Milky Way?
- (iii) Is it possible to distinguish the different systems that formed the proto-Milky Way from one another?

Santistevan et al. (2020) set out to investigate the formation times and building blocks of Milky Way-mass galaxies in the FIRE-2 simulations, which is directly related to the formation of proto-Milky Way populations. In their work, the authors traced the origin of star particles formed at all times in different regions of the Milky Way-mass galaxies, and found that: (i) Milky Way-mass galaxies typically assemble at $z \sim 3-4$ (i.e. 11.6–12.2 Gyr ago); (ii) Milky Way-mass galaxies at $z = 0$ are formed typically from ~ 100 building blocks with $M_* \gtrsim 10^5 M_\odot$; Milky Way-mass galaxies in Local Group environments typically assemble earlier than those in isolation, highlighting the importance of environment.

In this article, we set out to answer when and how proto-Milky Way systems may have assembled, and what are the (present day) observable properties of stellar populations that comprise a proto-Milky Way. To do so, we employ the 13 Milky Way-mass galaxies from the *Latte* and *ELVIS* suites (Wetzel et al. 2016) of high-resolution cosmological simulations from the Feedback In Realistic Environments (FIREs: Hopkins et al. 2018b) project (Section 2). We take these simulations and track the star particles belonging to all the resolvable luminous subhaloes, in order to identify the star particles belonging to all the galactic systems that coalesce to form a proto-Milky Way (Section 3). Upon selecting these populations, in Section 4 we go on to examine the present day observable properties of their stellar debris (namely, mass, age, spatial distribution, morphology, kinematics, and $[\alpha/\text{Fe}]$ and $[\text{Fe}/\text{H}]$ chemical compositions), in order to test if different systems constituting proto-Milky Way populations are distinguishable, and to provide clues on how to identify proto-Milky Way populations. We then discuss our results in the context of the current/future work in Section 5, provide the limitations and improvements to our work in Section 6, and list our concluding statements in Section 7.

2 SIMULATIONS

We make use of 13 Milky Way-mass galaxies from the *Latte* (Wetzel et al. 2016) and *ELVIS* (Garrison-Kimmel et al. 2019b) suites of FIRE-2.⁴ cosmological zoom-in simulations. In detail, *Latte* is a suite of seven isolated Milky Way-mass galaxies, and *ELVIS* is a suite of three Local Group-like pairs of Milky Way-mass galaxies. Both these suites of simulations were run with the FIRE-2 physics model (Hopkins et al. 2018b), utilizing the Lagrangian meshless finite-mass N -body gravitational plus hydrodynamics code *GIZMO*⁵ (Hopkins 2015). FIRE-2 simulations model many radiative cooling and heating processes for gas, including free-free emission, photoionization/recombination, Compton scattering, photoelectric, metal-line, molecular, fine-structure, dust-collisional, and cosmic ray heating across a temperature range of $10-10^{10}$ K. These simulations also include the spatially uniform, redshift-dependent, cosmic UV

²It has been postulated that GCs in the inner galaxy could be linked to this system (Forbes 2020; Kruijssen et al. 2020).

³And of course the Magellanic Clouds.

⁴FIRE project website: <http://fire.northwestern.edu>

⁵<http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html>.

background from Faucher-Giguère et al. (2009), for which H I reionization occurs at $z_{\text{reion}} \sim 10$. Moreover, FIRE-2 self-consistently generates and tracks 11 chemical abundance species (namely, H, He, C, N, O, Ne, Mg, Si, S, Ca, and Fe), including sub-grid diffusion of these abundances in gas via turbulence (Hopkins 2016; Su et al. 2017; Escala et al. 2018), as well as enrichment from core-collapse supernovae (CCSNe), Type Ia supernova, and stellar winds.

The *Latte* suite has an initial baryonic mass resolution of 7100 M_\odot for gas particles, whereas the *ELVIS* suite has an initial baryonic mass resolution of $3500\text{--}4000 \text{ M}_\odot$. *Latte* uses a fixed resolution of $35\,000 \text{ M}_\odot$ for dark matter particles, whereas *ELVIS* uses a fixed resolution of $19\,000 \text{ M}_\odot$. In both *Latte*/*ELVIS* star formation occurs in gas that is self-gravitating, Jeans-unstable, cold ($T < 10^4 \text{ K}$), dense ($n > 1000 \text{ cm}^{-3}$), and molecular (following Krumholz & Gnedin 2011). Each star particle inherits the mass and chemical abundance composition of its progenitor gas particle, and represents a single-stellar population with a Kroupa (2001) initial mass function. This population evolves according to the STARBURST v7.0 models (Leitherer et al. 1999), so the star particle decreases in mass with time as the most massive stars die. By the present day most star particles have a mass of $4000\text{--}5000 \text{ M}_\odot$. Stellar evolution gives rise to localized feedback at the location of each star particle, including core collapse and Ia supernovae, mass-loss from stellar winds, and radiation, including radiation pressure, photoionization, and photoelectric heating. Implementation of these processes follows the descriptions in Hopkins et al. (2018b) and Hopkins et al. (2018a).

The *Latte*/*ELVIS* suites were generated within periodic cosmological boxes of lengths $70.4\text{--}172 \text{ Mpc}$ using the code MUSIC (Hahn & Abel 2011), and constructing cosmological zoom-in initial conditions for each simulation at $z \simeq 99$. Each simulation has 600 snapshots saved down to $z = 0$, spaced every $\simeq 25 \text{ Myr}$. All simulations assume flat Λ -CDM cosmology with parameters consistent with Planck Collaboration et al. (2020). More specifically, the *Latte* suite (excluding m12r and m12w) used $\Omega_m = 0.272$, $\Omega_b = 0.0455$, $\sigma_8 = 0.807$, $n_s = 0.961$, $h = 0.702$. The m12r and m12w haloes were selected specifically because they host an LMC-mass satellite galaxy, and they adopted more up-to-date initial conditions from Planck Collaboration et al. (2020) compared to the rest of the *Latte* suite: $h = 0.68$, $\Omega_\Lambda = 0.31$, $\Omega_m = 0.31$, $\Omega_b = 0.048$, $\sigma_8 = 0.82$, $n_s = 0.961$. For the *ELVIS* suite, Thelma & Louise and Romulus & Remus both used the same cosmology as in the original *ELVIS* dark matter only suite: $\Omega_m = 0.266$, $\Omega_b = 0.0449$, $\sigma_8 = 0.801$, $n_s = 0.963$, $h = 0.71$. Conversely, Romeo & Juliet used the same cosmology as m12r/m12w. The post-processing is done using `gizmo` analysis (Wetzel & Garrison-Kimmel 2020b) and `halo` analysis (Wetzel & Garrison-Kimmel 2020a). Furthermore, dark matter particles in each snapshot are processed with `Rockstar` (Behroozi, Wechsler & Wu 2013) to produce halo catalogues. For further details of how the *Latte* and *ELVIS* suites were generated, we refer the reader to Wetzel et al. (2016) and Garrison-Kimmel et al. (2019b) and references therein, respectively.

The resolution of this suite of simulations enables luminous subhaloes to be well resolved even near each Milky Way-like galaxy. It also resolves the formation of tidal streams from satellite galaxies down to approximately 10^8 M_\odot in total mass or 10^6 M_\odot in stellar mass (at $z = 0$), similar to that of the Milky Way's 'classical' dwarf spheroidals (e.g. Panithanpaisal et al. 2021; Cunningham et al. 2022; Shipp et al. 2022; Horta et al. 2023b).

The properties of the host galaxies in *Latte* show broad agreement with the Milky Way, including the stellar-to-halo mass relation (Hopkins et al. 2018b), stellar haloes (Bonaca et al. 2017; Sanderson et al. 2018, 2020), and the radial and vertical structure of their

discs (Ma et al. 2017; Bellardini et al. 2021). Moreover, the satellite populations of these simulation suites have also been demonstrated to agree with several observed properties, such as: the mass and velocity dispersions (Wetzel et al. 2016; Garrison-Kimmel et al. 2019a); star formation histories (Garrison-Kimmel et al. 2019b); and radial distributions (Samuel et al. 2020). Despite great similarities in the properties of the satellite galaxies in *Latte* and that of the observed satellites around the Milky Way, it has been shown that the former are generally too metal-poor when compared to the latter (Escala et al. 2018; Wheeler et al. 2019; Panithanpaisal et al. 2021). This could be in part because of the assumed delay-time distributions assumed for Type Ia supernova (Gandhi et al. 2022), or because of the lack of modeling of Pop III stars. For this work, we emphasize that we do not require quantitative agreement with simulated and observed abundances. The relations found in this paper between (luminous) haloes and their respective chemical abundances should be treated qualitatively, and are intended for use within the simulations only. However, although the *normalization* of the various abundances is not always in good agreement with observations, we expect the *trends* we identify in this paper to be robust.

3 DEFINING A PROTO-MILKY WAY

Before performing any analyses, it is imperative that we make clear our definition of a proto-Milky Way. To do so, we set out to answer the following two questions:

- (1) When does a proto-Milky Way form?
- (2) What constitutes a proto-Milky Way?

For this work, we define the time in which a system becomes a proto-Milky Way when the main halo in the zoom-in region of the simulation box ($\sim 2 \text{ Mpc}$ side box or up to $\sim 6 R_{\text{vir}}$ for *Latte*, and approximately double for *ELVIS*) reaches a stellar mass ratio of 3:1 with the second most luminous halo⁶ ($t_{\text{MR}_{3:1}}$). We note that for the *ELVIS* galaxies, as there are two main haloes in each simulation, we take the ratio of stellar mass between the two main host haloes and the third most luminous subhalo within the simulation. Albeit arbitrary, we argue that this definition is intuitively sensible as: (i) it defines a point in time in which a system is dominant in its environment and (ii) is it quantifiable and repeatable across different simulations? It has also been reasoned to be a sensible way of pinpointing the time in which a galaxy becomes dominant (Santistevan et al. 2020).⁷ Given our definition, it is then straight forward to answer question (ii); the proto-Milky Way is defined as the stellar population resulting from the amalgamation between the main branch (i.e. the halo tracing the formation of the main host in the simulation) and building blocks (i.e. all the haloes that join with the main branch) before $t_{\text{MR}_{3:1}}$. Fig. 1 shows a schematic of our definitions, where the main branch is shown in red and building blocks as other colours. Moreover, a list of definitions is provided in Table 1; Table 2 displays the $t_{\text{MR}_{3:1}}$ times, the number of systems that coalesce to form a proto-Milky Way (given our definitions), and the stellar/virial masses for each proto-Milky Way system.

Furthermore, in order to track haloes with a high enough number of star particles to be resolvable in *Latte*/*ELVIS*, we choose to only track

⁶This second most luminous halo is by definition not in our sample of systems that comprise the proto-Milky Way.

⁷We note that Santistevan et al. (2020) also use another sensible choice, defined as the time in which the main halo begins forming the majority of its present day stars, signifying a dominant star formation episode of sustainable growth from an *in situ* channel.

Assembly of the proto-Milky Way in m12b

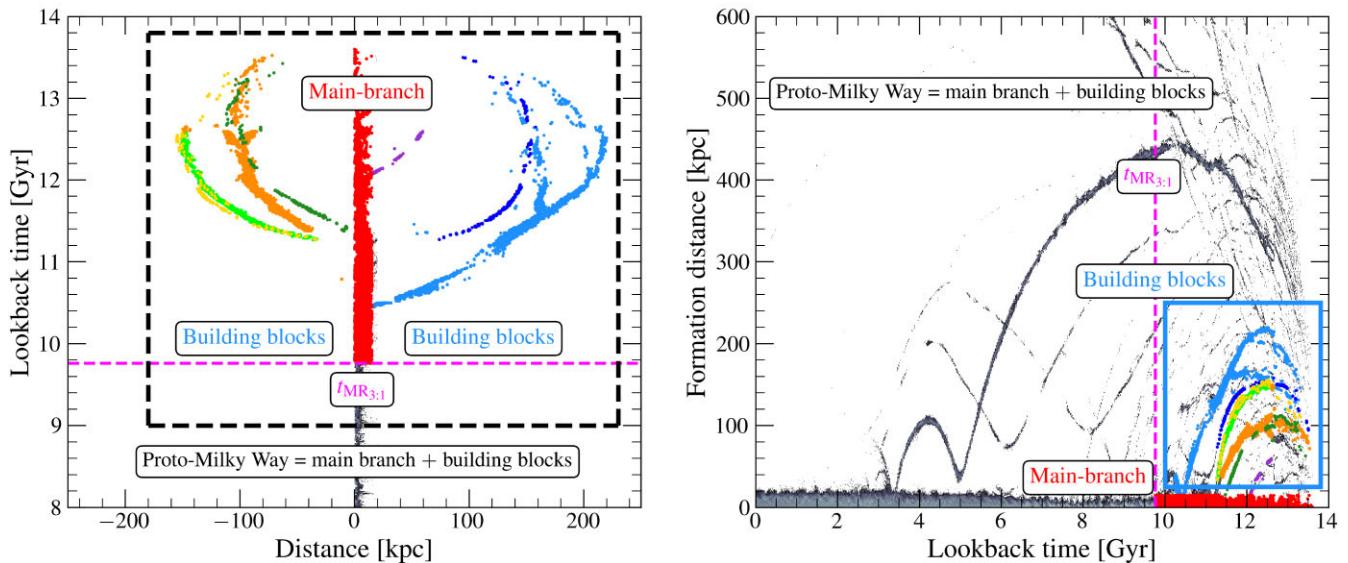


Figure 1. Left: Diagram of the merger tree of the m12b simulation in *Latte* up to a lookback time of 8 Gyr. In this work, a proto-Milky Way is defined as the amalgamation of the main branch halo (red) in a simulation plus all the building blocks (other colours) that coalesce onto it before $t_{\text{MR3:1}}$ (dashed magenta line, see Table 1 for details). Right: Distance at which a star particle in the simulation is formed with respect to the centre of the main host as a function of lookback time (i.e. age) for the m12b simulation in *Latte*. Highlighted in red are the star particles associated with the main branch, and as other colours the star particles associated with the resolvable building blocks (i.e. luminous subhaloes) that join with the main branch before $t_{\text{MR3:1}}$. By tracking each system over time, we are able to identify the star particles associated with all the proto-Milky Way fragments.

Table 1. List of definitions used in this article. See also Fig. 1.

Name	Definition
$t_{\text{MR3:1}}$	Lookback time in the simulation we define the proto-Milky Way to emerge, defined as the time the main branch reaches a stellar mass ratio of 3:1 with the second most massive luminous subhalo in the simulation volume (i.e. ~ 2 Mpc or up to $\sim 6 R_{\text{vir}}$ for <i>Latte</i> , and approximately double for <i>ELVIS</i>).
Main branch	Star particles formed in the main halo (as defined by the simulation) before $t_{\text{MR3:1}}$
Building block	Star particles formed in luminous haloes that join with the main branch halo before $t_{\text{MR3:1}}$
Proto-Milky Way	Star particles formed in the main branch and building block systems, that coalesce into a single galaxy before $t_{\text{MR3:1}}$

systems with 150 star particles or more, using a similar technique to previous studies (e.g. Necib et al. 2019; Panithanpaisal et al. 2021; Horta et al. 2023b). More specifically, we track the evolution of each system (i.e. the star particles) at every snapshot in the simulation over time until $t_{\text{MR3:1}}$ or until the system no longer exists (i.e. it has merged with the main branch system) using the `halo` catalogues, instead of resorting to the merger trees. This allows us to identify all the star particles in every halo, and to assign star particles to individual building blocks. Our choice to only track systems with 150 star particles or more leads to a minimum stellar mass of $M_* \sim 1 \times 10^6 M_\odot$ for subhaloes in *Latte*, and $M_* \sim 5 \times 10^5 M_\odot$ for *ELVIS*, given the slight differences in particle resolution between these two sets of simulations. For more information on the limitations of this choice, see Section 6.

3.1 When does a proto-Milky Way form?

Given our assumptions, we find that on average, proto-Milky Way populations are old (see Table 2). These values range from as late as $t_{\text{MR3:1}} = 8.05$ Gyr ($z \sim 1$) to as early as $t_{\text{MR3:1}} = 12.8$ Gyr ($z \sim 6$). We find that overall the proto-Milky Way systems can be grouped into three main camps: an early forming group, an intermediate

forming group, a late forming one. The difference in formation times of these Milky Way-mass galaxies has also been divided into three similar groups based on the time in which their stellar discs settle (McCluskey et al. 2023), and based on the transition from spheroids to thick and thin discs (Yu et al. 2023). These results are also consistent with the results from Santistevan et al. (2020) when they use the same definition as used here ($t_{\text{MR3:1}}$) (though we note that they find that Milky Way-mass galaxies emerge around $z \sim 3$ –4 when using a definition based on in-situ star formation).

3.2 What constitutes a proto-Milky Way?

Fig. 2 shows the stellar mass ratio between every main branch (diamonds) and building block (circles) with the overall proto-Milky Way population as a function of the stellar mass of each main branch/building block at $t_{\text{MR3:1}}$. In this diagram, there are proto-Milky Way populations formed by one clearly dominant halo (e.g. m12i), and populations formed by two main systems (namely, the main branch and a massive building block with a mass ratio of greater than 1:5; e.g. m12m). To guide the eye, in Fig. 2 we have highlighted the dominant systems as the shaded region, above the dashed line. Here, there are five building block systems (circles) with mass ratios

Table 2. List of approximate times in the simulation in which we define the proto-Milky Way to form ($t_{\text{MR3:1}}$), as well as the number of events (i.e. main branch + building blocks) that constitute the proto-Milky Way (n_{systems}), and the stellar and virial mass of the proto-Milky Way at $t_{\text{MR3:1}}$. We note here that the number of building blocks we find is bounded by our choice to track only systems with 150 star particles or more (see Santistevan et al. (2020) for a comparison when tracking lower mass systems). We also list the corresponding references for each of the *Latte/ELVIS* simulated haloes: (A) Hopkins et al. (2018b); (B) Garrison-Kimmel et al. (2019a); (C) Garrison-Kimmel et al. (2019b); (D) Garrison-Kimmel et al. (2017); (E) Wetzel et al. (2016); and (F) Samuel et al. (2020). These (lookback) times should be interpreted as ages, where 13.8 Gyr is old and 0 Gyr is young. The average values for n_{systems} have been rounded to the closest integer. The $t_{\text{MR3:1}}$ agree well with the results found in Santistevan et al. (2020) (see their Table 1).

Host	$t_{\text{MR3:1}}$ [Gyr]	$t_{\text{MR3:1}}$ [z]	n_{systems}	$M_{\star,3:1} [\times 10^9 M_{\odot}]$	$M_{\text{vir},3:1} [\times 10^{11} M_{\odot}]$
(isolated)					
m12b ^C	9.76	1.59	8	8.80	4.43
m12c ^C	9.05	1.32	5	3.56	4.93
m12f ^D	12.15	3.77	4	0.38	2.86
m12i ^E	11.80	3.18	6	0.35	1.12
m12m ^A	9.94	1.68	5	3.69	5.00
m12r ^F	8.05	1.02	7	4.29	2.61
m12w ^F	11.60	2.92	9	0.35	1.19
(pairs)					
Juliet ^C	12.55	4.72	4	0.31	0.93
Louise ^C	11.90	3.32	4	0.99	1.02
Remus ^B	7.90	0.98	9	20.14	6.41
Romeo ^C	12.81	5.70	4	0.12	0.33
Romulus ^B	10.00	1.70	6	6.85	3.40
Thelma ^C	12.40	4.29	2	0.11	0.78
Average (isolated)	10.33	1.87	6	3.06	3.16
Average (pairs)	11.26	2.56	5	4.75	2.14
Average (total)	10.76	2.15	6	3.90	2.69

Stellar mass ratio of proto-Milky Way fragments

● m12b ● m12m ● Romulus ● Louise
 ● m12c ● m12r ● Remus ● Romeo
 ● m12f ● m12w ● Thelma ● Juliet
 ● m12i

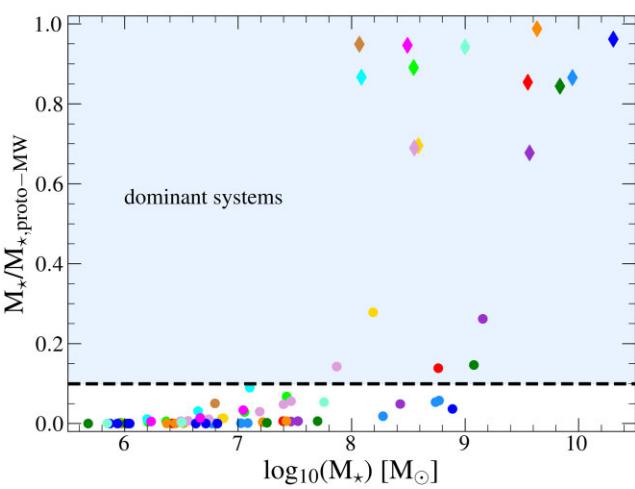


Figure 2. Stellar mass ratio between each main branch (diamonds) or building block (circles) and the proto-Milky Way (i.e. main branch+building blocks) at $t_{\text{MR3:1}}$ as a function of the stellar mass of each main branch/building block. There are five clear cases (namely, m12c, m12f, m12m, m12w, and Romulus) which have a building block on the order of $\gtrsim 1:5$ mass ratio with the proto-Milky Way population (i.e. blue shaded region). This indicates that ~ 40 per cent of the 13 proto-Milky Way systems studied have a massive/dominant building block in addition to the dominant main branch halo.

of $\gtrsim 1:5$ in addition to the dominant main branch (diamonds). Thus, for ~ 40 per cent of our sample (5/13 galaxies), the proto-Milky Way system is comprised of two dominant populations. Conversely, the other ~ 60 per cent (8/13 galaxies) host only one dominant main branch system.

Given this finding, it is interesting to ask what fraction of the proto-galaxy's (stellar) mass is contributed by the main branch/building block progenitors? To answer this question, in Fig. 3 we show the mass difference between each main branch progenitor and its counterpart building blocks as a function of the mass of the main branch progenitor. We find that the majority of the building blocks are of lower mass when compared to the main branch progenitor, on the order of one to four orders of magnitude difference, with a stellar mass ranging between $5 \times 10^5 < M_{\star} < 1 \times 10^8 M_{\odot}$. However, Fig. 3 confirms the findings from Fig. 2, highlighting that for 5/13 galaxies in our sample, in addition to the main branch system, there is a building block whose stellar mass is of the same order of magnitude.

Our findings suggest that on average the proto-galaxy of a Milky Way-mass halo is comprised of five to six systems with $M_{\star} \gtrsim 5 \times 10^5 M_{\odot}$ and one to two systems with $M_{\star} \gtrsim 1 \times 10^8 M_{\odot}$ ⁸. In the following sections, we set out to study the chemical-kinematic properties of these systems at $z = 0$ to see if the different systems that form proto-Milky Way populations can be distinguished.

⁸However, these results are subject to our choice to only study systems with 150 star particles. If one was to lower this mass limit and was to look at all systems that coalesce with the main branch before $z = 0$ (e.g. Santistevan et al. 2020), this number grows significantly, up to ~ 100 building blocks.

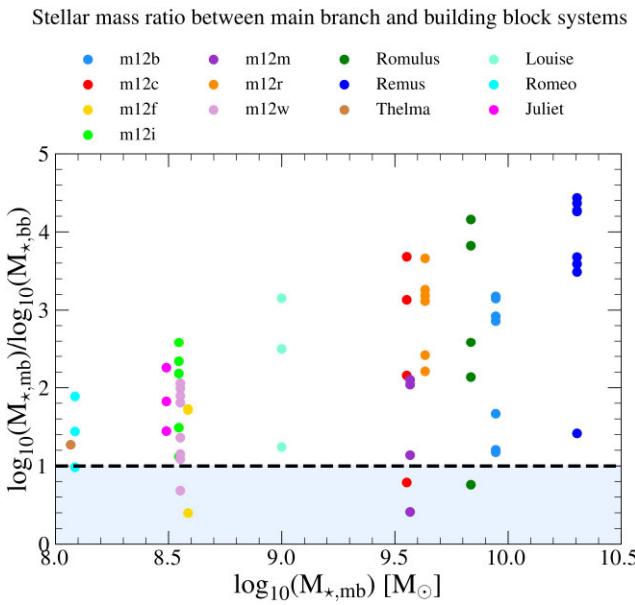


Figure 3. Ratio of the stellar mass between main branch progenitors and their building block counterparts as a function of the main branch progenitor's stellar mass for each Milky Way-mass simulation at $t_{\text{MR3:1}}$. 5 out of 13 proto-Milky Way's host a building block of similar mass to the main branch progenitor (blue shaded region).

4 RESULTS

In this section, we consider each main branch and building block population individually in order to examine how the mass, age, spatial distribution, morphology, kinematics, and abundance patterns of these systems differ. We also aim to examine the role of environment by comparing isolated Milky Way-mass haloes with ones in Local Group environments.

4.1 Stellar mass and age

We begin by examining the stellar mass and the minimum age of a star particle in each main branch and building block separately, shown in Fig. 4. We choose to study the minimum age instead of the mean age as we believe that it is a better constraint for the time in which a system quenches star formation, and thus ceases to evolve. The questions we aim to answer are: What age are the systems that form a proto-Milky Way? How massive are the main branch and building block systems that constitute a proto-Milky Way?

The left panel of Fig. 4 shows the relationship between the minimum star particle age and the stellar mass at $z = 0$ of the main branch (diamonds) and building blocks (circles) from each simulation. The middle and right panels show histograms for stellar mass and minimum star particle age, respectively. Here, we show the frequency of all systems together in black, isolated haloes (i.e. *Latte*) in green, systems in Local Group environments (i.e. *ELVIS*) in yellow, main branch systems in red, and building blocks in blue. We recall that the resolution of the *Latte* and *ELVIS* suites are different (see Section 2 and the figure caption for details).

From inspection of the middle and right panels of Fig. 4, we find that, overall (black solid line), the mean stellar mass of the subhaloes that comprise proto-Milky Way systems is $\langle M_* \rangle \sim 4 \times 10^7 M_\odot$, and the mean minimum age is $\langle \text{age}_{\text{min}} \rangle \sim 11.4$ Gyr (or $\langle z \rangle \sim 2.8$). However, the range in these parameters is significantly large, and for both cases, we find that the distribution is skewed (or for the case of the

stellar mass, even possibly bimodal). Given our set of choices and assumptions, we find that the stellar masses for all these systems ranges from $\sim 5 \times 10^5 < M_* < 2 \times 10^{10} M_\odot$, and the minimum age can reach anything between $\sim 8 < \text{age}_{\text{min}} < 13$ Gyr (or $\sim 0.7 < z < 6.5$). Furthermore, when splitting the distributions by environment and comparing the haloes that live in isolated environments from those that live in a Local Group-like environment, we find that the mean values of the stellar masses of systems in Local Group-like environments is slightly lower than for systems in isolation. The difference in the median stellar mass is on the order of half a magnitude. Furthermore, there are also some slight differences in the distribution of the minimum star particle age, whereby the pairs tend to favour older populations. Statistically, the mean values show no clear differences ($\langle \text{age}_{\text{min}, \text{pairs}} \rangle = 11.5$ Gyr and $\langle \text{age}_{\text{min}, \text{isolated}} \rangle = 11.26$ Gyr). However, the median differs by approximately 0.5 Gyr for both the stellar mass and minimum age (see Table 3).

When comparing the main branch populations (red) with their building block counterparts (blue), we see substantial differences in their stellar masses. Specifically, we find that main branch systems tend to be more massive, approximately two orders of magnitude larger (i.e. $\langle M_{*, \text{mb}} \rangle = 1 \times 10^9 M_\odot$ and $\langle M_{*, \text{bb}} \rangle = 1 \times 10^7 M_\odot$). However, we note that some building blocks do reach high-stellar masses, on the order of $M_* \sim 2 \times 10^9 M_\odot$, making the range in the distribution for building blocks much larger than for main branch debris. We see similar differences in the mean and spread of the minimum star particle age between main branch and building blocks debris as we did when comparing environment, on the order of ~ 0.4 Gyr.

Our results thus imply that proto-Milky Way populations are predominantly comprised by one or two major systems of similar mass to the LMC (i.e. $M_* \sim 1 \times 10^9 M_\odot$) and 3–5 smaller mass building blocks of approximately ~ 2 orders of magnitude smaller in stellar mass (i.e. $M_* \sim 4 \times 10^7 M_\odot$). The massive systems typically arise from the main branch progenitor, and in the case where there are two dominant systems, also from a massive building block.

The left panel of Fig. 4 shows the distribution of minimum star particle age (i.e. the youngest) as a function of stellar mass for each event in each Milky Way-mass halo separately, where here we distinguish main branch populations (diamonds) and building blocks (circles). There is a relation between the stellar mass of a system and the minimum star particle age, whereby a system's minimum stellar age decreases with increasing stellar mass. This is likely because those systems that are forming stars for longer are able to build up more mass (a similar argument as for the mass–metallicity relation of galaxies, see also fig. 3 of Cunningham et al. 2022). These results from this section are summarized in Table 3.

4.2 Spatial distribution and morphology

We now set out to examine the spatial distribution of the different contributors to a proto-Milky Way. In doing so, we aim to tackle the following questions: Where is most of the mass contained in the main host at $z = 0$? What is the morphology of the debris at $z = 0$?

Fig. 5 characterizes where mass is deposited by showing the total (cumulative) mass fraction of the debris of every main branch (dashed) and building block (solid) event comprising the proto-Milky Way systems as a function of present day spherical radius from the centre of the Milky Way-mass host. Each main branch/building block event is colour coded by their respective stellar mass. To guide the readers eye, we also plot a vertical line at 5 kpc (cyan) and 20 kpc (grey).

Age and stellar mass properties of proto-Milky Way populations

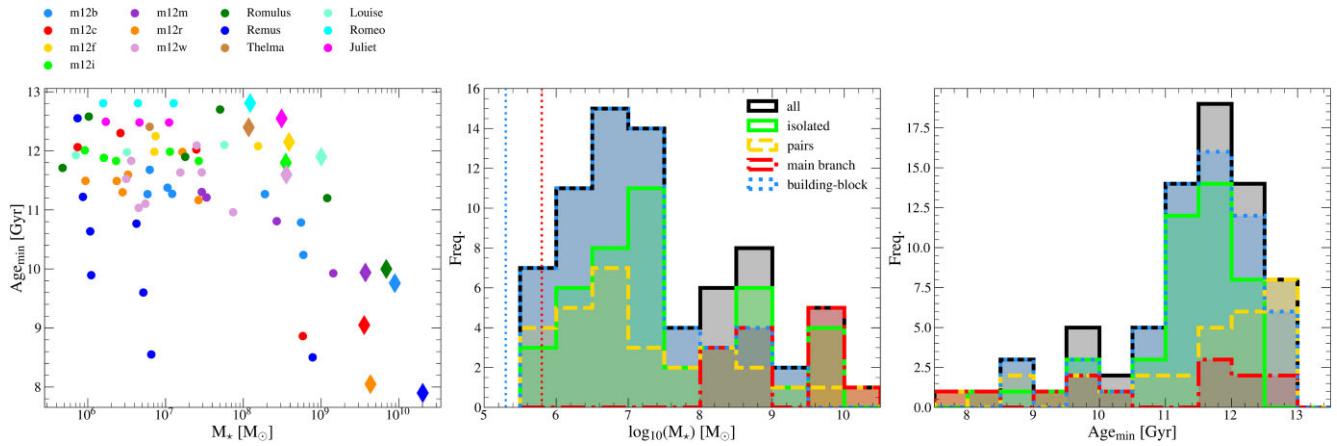


Figure 4. Left: minimum star particle age (i.e. the youngest star particle) in each main branch (diamond) and building block (circle) event as a function of its stellar mass for all 13 Milky Way-mass haloes. Middle: histogram of the stellar mass of each system, split into environment and main branch/building block populations. The vertical dotted lines demarcate the minimum possible stellar mass of a halo in the simulation given our choice to track luminous subhaloes with 150 star particles or more and the simulations resolution, for *Latte* (red) and *ELVIS* (blue). Right: histogram of the minimum star particle age, illustrated as in the middle panel. In each panel, the label ‘pairs’ corresponds to the systems studied in *ELVIS*, and in a Local Group-like environment at $z = 0$.

Table 3. Summary of the mean, median, and 1σ values for the stellar mass and minimum star particle age for our sample of events comprising proto-Milky Way systems.

Sample	$\langle \log_{10}(M_*) \rangle [M_\odot]$	$med(\log_{10}(M_*) [M_\odot]$	$\sigma_{\log_{10}(M_*)} [M_\odot]$	$\langle age_{min} \rangle [Gyr]$	$med(age_{min}) [Gyr]$	$\sigma_{age_{min}} [Gyr]$
Proto-Milky Way (all)	7.39	7.08	1.17	11.36	11.64	1.16
Environmental difference						
Proto-galaxy (pairs)	7.21	6.79	1.25	11.50	11.97	1.41
Proto-galaxy (isolated)	7.50	7.31	1.09	11.26	11.51	0.94
Classification difference						
Main branch	9.09	8.99	0.71	10.76	11.60	1.66
Building block	7.02	6.81	0.88	11.10	11.20	1.31
All						
Main branch (pairs)	8.96	8.74	0.85	11.26	12.15	1.76
Main branch (isolated)	9.19	9.55	0.56	10.33	9.94	1.43
Building block (pairs)	6.75	6.64	0.88	11.57	11.97	1.29
Building block (isolated)	7.178	7.05	0.84	11.43	11.52	0.68

As is to be expected, there is a range of spatial distributions for all the main branch and building block events. However, the majority of the mass from these systems is pre-dominantly contained within ~ 10 kpc from the centre of the host halo. This is especially the case when examining either main branch progenitors (dashed lines) and/or more massive building block debris (darker solid lines). For all Milky Way-mass galaxies the main branch system contains ~ 50 per cent of its mass within ~ 10 kpc from the host’s centre, and ~ 95 per cent within ~ 30 –40 kpc. For the case of the building blocks, the most massive events ($M_* \gtrsim 5 \times 10^8 M_\odot$) typically contain ~ 50 per cent of their mass within ~ 5 –20 kpc, and ~ 95 per cent of their mass within ~ 20 –40 kpc, in a similar fashion to the main branch population. This is especially the case for m12f, m12m, and Romulus, where the main branch progenitor follows a very similar spatial profile to the most massive building block in that system, making these almost indistinguishable spatially. For the lower mass building blocks ($M_* \lesssim 5 \times 10^6 M_\odot$), we see a wide range of profiles, ranging from ~ 10 to 50 kpc for 50 per cent of their enclosed mass and ~ 20 –100 kpc for 95 per cent of their enclosed mass. This result

suggests that the innermost regions of the Milky Way-mass galaxies is where you would expect to find the oldest populations in the galaxy (El-Badry et al. 2018; Fragkoudi et al. 2020) that comprise the proto-Milky Way, arising from both a main branch progenitor and (possibly) the most massive building blocks (Horta et al. 2021a; Rix et al. 2022). Due to the strong spatial overlap between main branch systems and massive building blocks, it would be difficult to distinguish these based on spatial distribution information alone.

We find a small difference in the spatial distribution of the debris of an event that occurs in a halo that is isolated versus a halo that is in a Local Group environment, whereby the latter tend to present proto-Milky Way populations more concentrated toward the host’s centre. These results can be more easily digestible in Fig. 6, where we show histograms of r_{50} and r_{95} (i.e. the 50th and 95th percentiles of the spherical radii for each system), following the colour coding from Fig. 4.

Fig. 7 provides a summary of morphology by showing the aspect ratio (c/a) subtracted from unity, as a function of their stellar mass. As in previous figures, the main branch populations are shown as

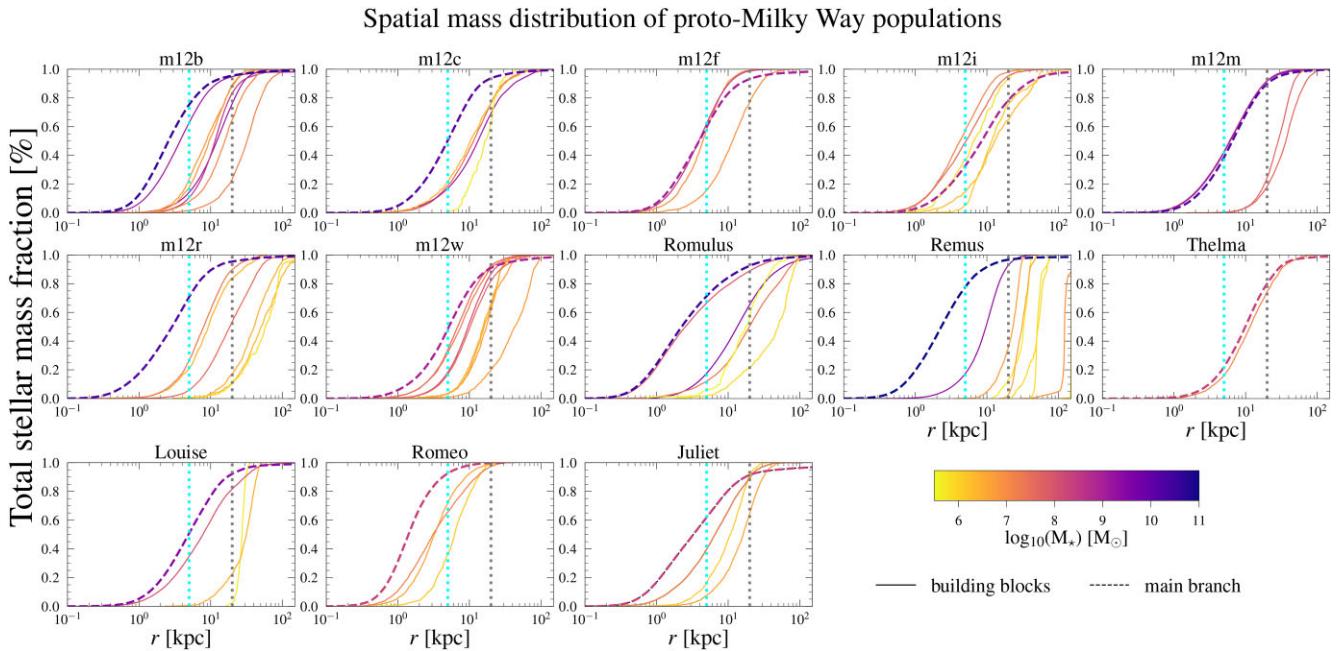


Figure 5. Total stellar mass fraction as a function of spherical radius (at $z = 0$) for all the main branch (dashed) and building block (solid) events in each Milky Way-mass halo. Each profile is colour coded by the systems' respective stellar mass. The vertical dashed lines mark 5 kpc (cyan) and 20 kpc (grey). The majority of the proto-Milky Way material (i.e. main branch and massive building blocks) are contained within a small spatial volume, close to the host's centre. However, there is a range of spatial profiles for lower mass building blocks.

diamonds and building block systems as circles. Given that the 95th percentiles represent almost the extent of the distribution, we use these values to define two axes: a semimajor one ($a = R_{95}$) and a semiminor one ($c = z_{95}$), both in units of kpc. We define these quantities so that we can measure the aspect ratio (c/a) and in turn their ellipticity, defined as $\varepsilon = 1 - c/a$. Given this definition, a value of $\varepsilon = 1$ marks a perfect circle, and an ε value closer to 0 corresponds to a more squashed ellipse. We note that these aspect ratios are defined with respect to the principal axis of the host at $z = 0$.

We find that the there is a dependence on ε with stellar mass, whereby more massive systems tend to adopt a more oblate distribution at present day when compared to their lower mass counterparts, which adopt a wider range of morphologies. As we saw in subsection 4.1, the main branch progenitors adopt a more oblate morphology when compared to the lower mass building block counterparts. However, we find that the more massive building block debris also adopt an oblate distribution, following the main branch progenitors.

4.3 Kinematic properties

In this section, we set out to examine the kinematic properties of populations comprising proto-Milky Way systems. Specifically, we aim to answer the following questions: how rotationally supported are the main branch and building block systems that form the proto-Milky Way at present day? Are proto-Milky Way populations rotating on prograde or retrograde orbits?

To quantify the amount of rotational support in each system, we compute the ratio of the rotational velocity over the total velocity for all star particles in a given population, $\kappa_{\text{rot}}/\kappa_{\text{tot}}$. These two velocity quantities are defined in the coordinate system centred on the host

Milky Way-mass galaxy's disc at $z = 0$, and are computed by finding the centre of the Milky Way-mass host using its baryonic particles at that redshift. This can be estimated by taking the ratio of the kinetic energy in the rotational direction over the total kinetic energy (McCarthy et al. 2012), such that

$$\kappa_{\text{rot}} = \frac{1}{N} \sum_i^N \frac{(L_{z_i}/R_i)^2}{2}, \quad (1)$$

assuming $R = \sqrt{X^2 + Y^2}$, $L_z = |\vec{R} \times \vec{v}_\phi|$, and

$$\kappa_{\text{tot}} = v_{\text{tot}}^2/2, \quad (2)$$

where

$$v_{\text{tot}} = \sqrt{v_X^2 + v_Y^2 + v_Z^2}. \quad (3)$$

We normalize this quantity by taking the ratio of this value with the amount of rotational support determined in the young (age < 4 Gyr) disc ($d_{\text{form}} < 30$ kpc) of the host of each Milky Way-mass halo, $\kappa/\kappa_{\text{disc}}$ (where $\kappa = \kappa_{\text{rot}}/\kappa_{\text{tot}}$).

Fig. 8 shows the mean value of $\kappa/\kappa_{\text{disc}}$ for all the main branch (diamonds) and building block (circles) systems as a function of their mean ellipticity. Milky Way-mass haloes in isolation (pairs) are shown as full (empty) markers. A value of $\kappa/\kappa_{\text{disc}} = 1$ signifies that a system is as rotationally supported as the young disc in that simulation. A value of $\kappa/\kappa_{\text{disc}} > 1$ implies that it is more rotationally supported, and a value of $\kappa/\kappa_{\text{disc}} < 1$ that it is less rotationally supported. In right panel, we plot the mean azimuthal velocity of every proto-Milky Way population.

We find that the majority of the debris from both the main branch and building block systems have a mean $\kappa/\kappa_{\text{disc}}$ value between 0.25

⁹ R here is the cylindrical galactocentric radius, and X and Y are the galactocentric cartesian coordinates.

Radius enclosing 50% and 95% of stellar mass

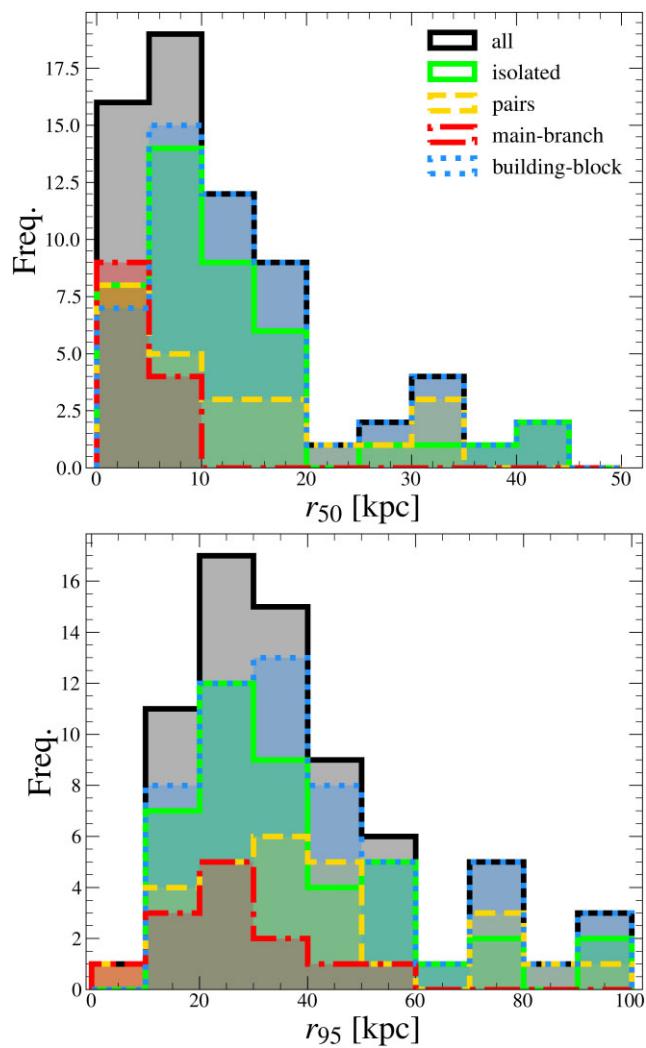


Figure 6. Histograms of the 50th (top) and 95th (bottom) percentiles of the spherical radii for all (black), isolated haloes (green), haloes in pairs (yellow), main branch systems (red), and building blocks (blue). The majority of the stellar populations of proto-Milky Ways are contained within ~ 40 kpc, with 50 per cent of the mass contained within ~ 5 –10 kpc from the host's centre at present day. In each panel, the label 'pairs' corresponds to the systems studied in *ELVIS*, and in a Local Group-like environment at $z = 0$.

and 0.8, indicating not a strong amount of rotational support in the system when compared to the host's young disc. However, their rotational support is not 0, indicating that particles are not on purely radial orbits. In fact, their mean azimuthal velocities show that the majority of these systems have pre-dominantly prograde orbits ($\langle v_\phi \rangle > 0$ km s $^{-1}$). This means that they are rotating in the same direction as the disc, although at a much slower pace. Our results suggest that all these systems, either defined as main branch progenitor or building block, show weak but systematic net rotation in the plane of the host's disc at $z = 0$ despite many of them appearing flattened/oblate in morphology (see subsection 4.2). We find no dependence of the mean $\kappa/\kappa_{\text{disc}}$ value of proto-Milky Way populations with environment (see the left panel of Fig. 8).

It is important to note that recent studies have reported that Milky Way-mass galaxies in FIRE experience different phases of growth

Shape of proto-Milky Way populations

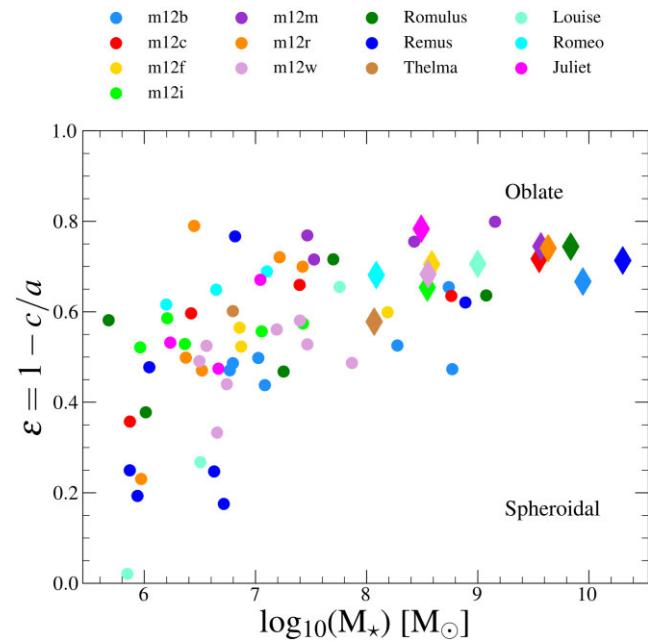


Figure 7. Ellipticity (i.e. the ratio of 95th percentiles between cylindrical height and radius – that is, the aspect ratio – subtracted from unity) as a function of the stellar mass for main branch debris (diamonds) and building block events (circles). More massive systems tend to adopt a more oblate shape.

(Yu et al. 2021; Gurvich et al. 2023; Hopkins et al. 2023; McCluskey et al. 2023; Semenov et al. 2023; Yu et al. 2023), which can be characterized based on differences in their stellar kinematics and amount of rotational support. Yu et al. (2023) find that the orbits of star particles formed in the main branch spheroid at early times are more radial than those formed at later times in a more settled disc (see also Gurvich et al. 2023 and McCluskey et al. 2023). This result is related to our finding, and suggests that populations formed at early times are likely to not be on as rotationally supported orbits when compared to populations formed later in settled discs.

4.4 Chemical compositions

In this section, we examine what is likely to be the most pristine observable tracer of stellar populations: their chemical compositions. While FIRE tracks eleven different elemental species, they trace three nucleosynthetic channels: contributions from CCSNe, Type Ia supernova, and stellar winds. We set out to explore the distribution of the debris of these events in the chemical plane tracing the contribution of CCSN and Type Ia supernova, choosing Mg as our α tracer. The main question we aim to tackle in this section is: what differences in the chemical compositions (and thus, the star formation histories) can we expect from main branch progenitors when compared to their building block counterparts?

Fig. 9 shows the median [Mg/Fe] and [Fe/H] values for building blocks (circles) and main branch debris (diamonds), where each system is colour coded by their mean stellar mass (left) and minimum star particle age (right). Empty markers correspond to systems in Local Group-like environments (i.e. the *ELVIS* suite) and filled markers correspond to events in isolated haloes (i.e. the *Latte* suite).

Rotational support and azimuthal kinematics of proto-Milky Way populations

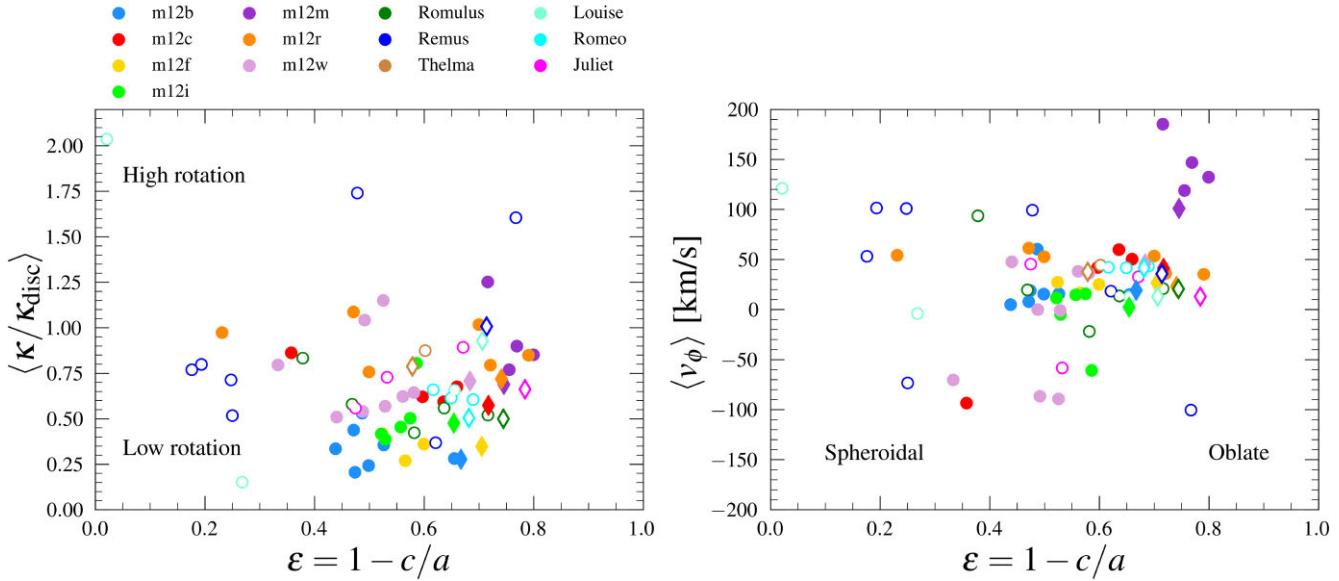


Figure 8. Left: mean of the rotational support of each proto-Milky Way population normalized by the rotational support of its host's disc ($\kappa / \kappa_{\text{disc}}$) as a function of ellipticity. Rotational support is defined as the ratio of rotational energy (κ_{rot}) in the direction of the host's galactic disc at present day and the total kinetic energy (κ_{tot}). The disc population is comprised by star particles with age < 4 Gyr formed in the main host, $d_{\text{form}} < 30$ kpc. Right: mean azimuthal velocity in the direction of the host's disc at present day as a function of ellipticity. Systems in isolation (pairs) are shown as full (empty) markers. The majority of main branch and building block debris show low level of systematic net rotation ($0.25 \lesssim \langle \kappa / \kappa_{\text{disc}} \rangle \lesssim 0.8$) when compared to their host present day disc. However, this rotational support is not zero. In fact, the majority of proto-Milky Way populations show prograde motion ($0 \lesssim \langle v_\phi \rangle \lesssim 50$ km s $^{-1}$), that can reach up to $\langle v_\phi \rangle \sim 100$ –150 km s $^{-1}$ (m12i).

[α/Fe]-[Fe/H] compositions of proto-Milky Way populations

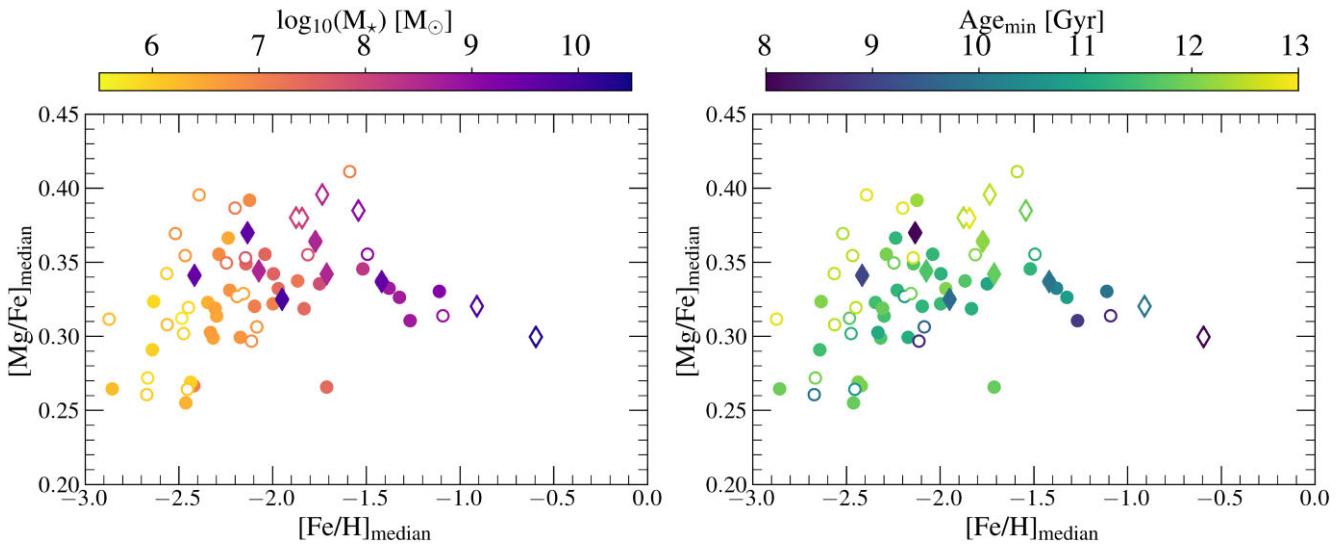


Figure 9. Median [Mg/Fe] and [Fe/H] values for main branch (diamonds) and building block (circles) populations for isolated Milky Way-mass haloes (filled markers) and those in pairs (empty markers), colour coded by stellar mass (left) and minimum star particle age (right). The average 1σ is 0.33 dex for [Fe/H], and 0.08 dex for [Mg/Fe]. On average, main branch progenitors and the most massive building blocks present more enriched chemical compositions when compared to lower mass building blocks; this is a result of the galaxy mass–metallicity relation.

Fig. 9 demonstrates that, on average, the main branches are more metal-rich than the building blocks. Here, main branch progenitors either have a higher [Mg/Fe] value at fixed [Fe/H], or higher [Fe/H] overall. However, we find that this is also the case for the

most massive (and youngest) building blocks. This is a natural consequence of the mass–metallicity relation (e.g. Kirby et al. 2013, 2020). More massive systems are able to form stars for longer, thus enriching their interstellar medium with more metals and evolving

chemically faster than lower mass systems that quench star formation earlier. This fact could be leveraged to disentangle the lower mass building blocks from their main branches using their abundances (e.g. employing methods presented in Cunningham et al. 2022, Horta et al. 2023a, Deason et al. 2023, for example).

However, some of the more massive building blocks have chemical compositions consistent with the main branches. As a result, it could be challenging to disentangle populations from the main branch from populations from the most massive building block when a proto-Milky Way has two significant contributors (which is the case for roughly ~ 40 per cent of our Milky Way-mass galaxy sample). We investigate this further in Fig. 10, in which we compare the metallicity distribution functions (MDFs) for the main branch (dashed) and most massive building block (solid) in both m12f (black) and m12m (red). In the case of m12f, the mean of the main branch MDF is ~ 0.1 – 0.2 dex higher compared to the most massive building block. Conversely, the main branch in m12m is identical in [Fe/H] when compared to its massive building block counterpart. These results show that, quantitatively, it would be extremely difficult to distinguish massive building blocks from their main branch system counterparts using their MDFs. More detailed chemical abundance information from elemental species synthesized in more exotic nucleosynthetic channels, which we have not been able to examine in this work (but see Horta et al. 2023a), may hold the clues to disentangling these dominant proto-Milky Way fragments.

When comparing the debris from host haloes that evolve in different environments, we find that there are possible subtle differences. Specifically, we find that the main branch and building block events in host haloes simulated in Local Group-like environments (pairs) present on average slightly higher median [Mg/Fe] and/or [Fe/H] values when compared to isolated hosts. This result is consistent with our finding that systems in Local Group-like environments evolve either faster and/or earlier, when compared to systems in isolated hosts (Santistevan et al. 2020). However, within the spread of the distributions (i.e. the uncertainties in Fig. 9), which is on average ~ 0.05 – 0.1 dex for [Mg/Fe] and ~ 0.3 dex for [Fe/H], we note that this result is tentative.

5 DISCUSSION

5.1 Can we distinguish if a proto-Milky way formed from one or two dominant systems?

Fig. 11 shows the X-Z positions, Toomre diagram distribution, and [Mg/Fe]-[Fe/H] density contour distributions for the main branch (red), the most massive building block (black), the old disc (blue), and young disc (green) in the m12i and m12m simulations. Disc stars are selected to be formed within 30 kpc of the main host after $t_{\text{MR3:1}}$, where the old (young) disc is older (younger) than 4 Gyr. We choose to compare m12i with m12m, as m12i is a clear case where the proto-Milky Way formed from one dominant main branch system ($M_\star = 3.51 \times 10^8 M_\odot$), and m12m is a clear example of a proto-Milky Way formed from two dominant systems (a main branch of mass $M_\star = 3.69 \times 10^9 M_\odot$ and a massive building block of mass $M_\star = 1.43 \times 10^9 M_\odot$). As can be seen in Fig. 11, there are subtle differences in the spatial distribution (at $z = 0$) for all populations examined between m12i and m12m. More specifically, m12i presents a clear thin young disc population in addition to a spherical old disc, main branch, and building block (of mass $M_\star = 2.67 \times 10^7 M_\odot$). Conversely, m12m presents a much flatter distribution, where the main branch and massive building block systems present an oval

Metallicity distribution of massive proto-Milky Way fragments in m12f & m12m

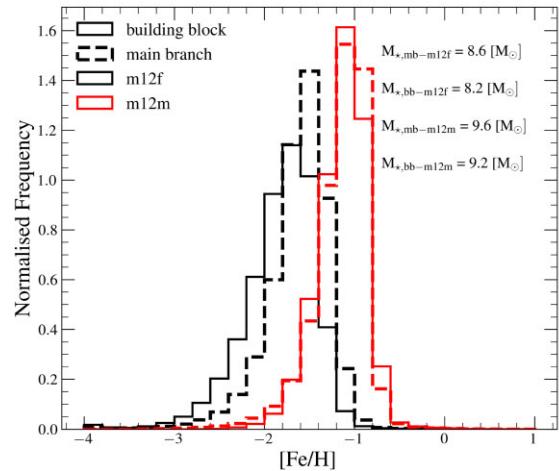


Figure 10. Histograms of the MDFs of main branch progenitors (dashed) and the most massive building blocks (solid) events in the m12f (black) and m12m (red) simulations. The MDF profiles are qualitatively the same for these populations. This result highlights the difficulty of distinguishing main branch from massive building block populations based on their MDFs.

shape, in a similar fashion to the old disc in this Milky Way-mass galaxy.

Moreover, we find that in m12i, the main branch and building block overlap in the Toomre diagram and are largely non-rotational ($v_\phi \sim 0 \text{ km s}^{-1}$), and are different to the old/young disc, which show a more extended distribution rotating at higher v_ϕ . Conversely, m12m reveals that its main branch and massive building block also overlap in kinematic space, but rotate at a higher tangential velocity of $v_\phi \sim 100 \text{ km s}^{-1}$, lagging behind the young disc by $\sim 150 \text{ km s}^{-1}$. In this halo, the main branch and massive building block also overlap with the old disc. The difference in the v_ϕ magnitude between the proto-Milky Way system in m12i and m12m is interesting. However, it is likely due to m12i being an outlier in terms of the rotational velocities of its metal-poor stars (Santistevan et al. 2022). All the other *Latte* Milky Way-mass galaxies show a preference for prograde disc orbits for older and/or lower metallicity stars, similar to m12m (although this system also shows higher than average rotation, see the right panel of Fig. 8). Santistevan et al. (2022) argue that metal-poor/old stars on prograde disc orbits are a consequence of major building blocks depositing stars/gas on prograde orbits, which typically set the orientation of the resulting Milky Way-mass galaxy disc at $z = 0$.

In terms of their [Mg/Fe]-[Fe/H] compositions, we find again that for both m12i and m12m, the main branch and building block populations overlap. This is to be expected for m12m (see Figs 9 and 10), but is a surprise for m12i. Interestingly, the [Mg/Fe]-[Fe/H] compositions of these systems are clearly different from that of the old/young discs in m12i, which present a much higher [Fe/H] distribution. However, we note that there is an overlap between the metal-rich sequence of the main branch/building block and the metal-poor tail of the old disc. Conversely, for m12m this overlap between the main branch and massive building block is more pronounced. This highlights that the dominant proto-Milky Way populations are likely to overlap with the metal-poor/old disc (Conroy et al. 2021; Horta et al. 2021a; Mardini et al. 2022; Horta et al. 2023b).

In a similar vein, another interesting diagram to investigate relates to the time difference between proto-Milky Way systems that form

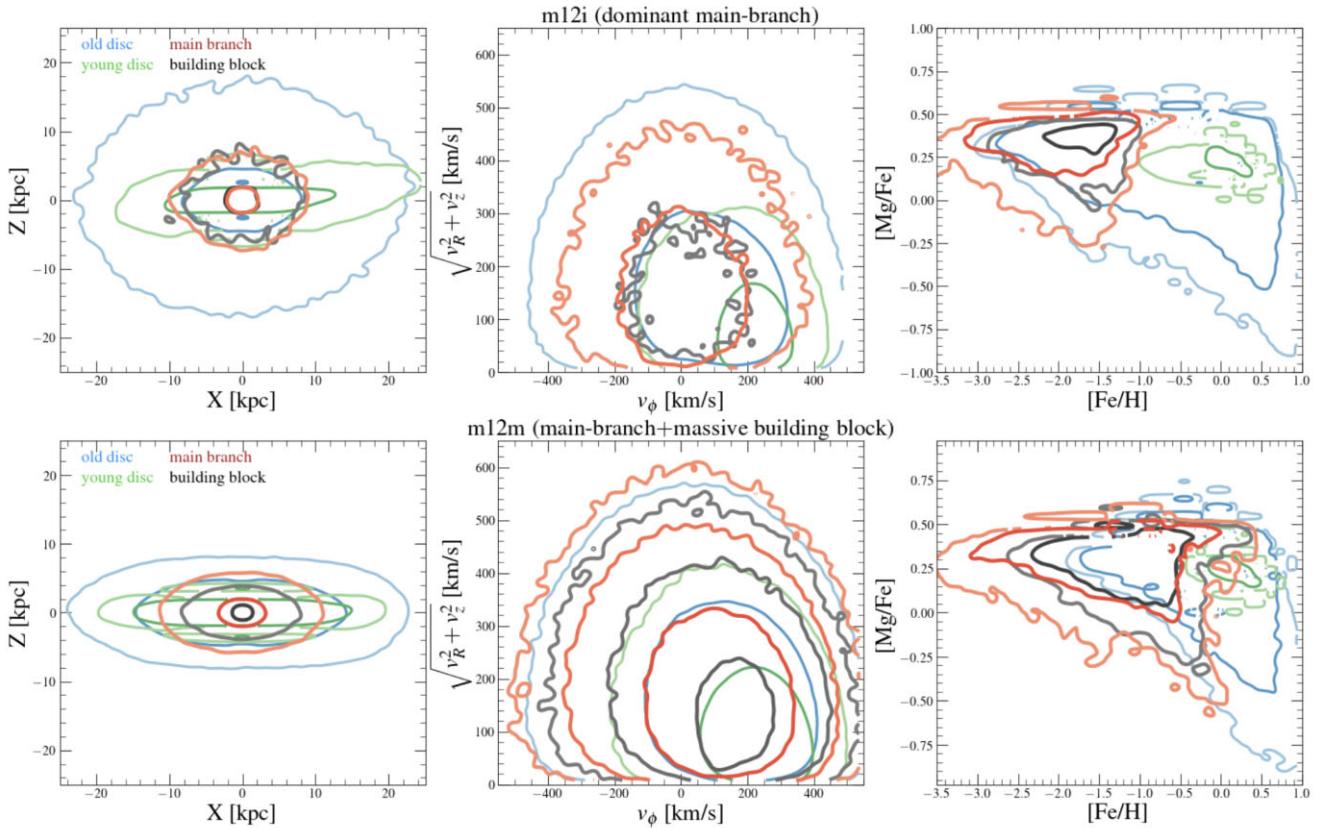


Figure 11. Left: Density level contours of the X-Z positions (i.e. edge-on projections) at $z = 0$ for star particles belonging to the main branch system (red), most massive building block (black), the old disc (blue), and the young disc (green) in m12i. Here, the old (young) disc is defined as star particles formed in the main host halo between $4 < \tau [\text{Gyr}] < t_{\text{MR3:1}}$ ($4 < \tau [\text{Gyr}]$). Middle: Same as left, but now in the cylindrical Toomre diagram. Right: The same as left, but now in the $[\text{Mg}/\text{Fe}]\text{-}[\text{Fe}/\text{H}]$ plane. m12i and m12m differ in the fact that the former proto-Milky Way is comprised primarily by one main branch system (~ 90 per cent of the stellar mass) and m12m is comprised by two systems, a main branch system (~ 65 per cent of M_*) and a massive building block (~ 35 per cent of M_*). The kinematic distributions of main branch, building block, and old disc are qualitatively similar and are different from the young disc. This is more pronounced in m12i than m12m. The $[\text{Mg}/\text{Fe}]\text{-}[\text{Fe}/\text{H}]$ compositions of the main branch and building block system are also extremely similar, but are different from the young disc. The main branch and building block overlap with the metal-poor old-disc; this overlap is bigger for m12m than for m12i.

from one main system versus two main haloes. To investigate this point further, in Fig. 12 we show the main branch, (massive) building block, and old/young disc in the age–metallicity plane. Here the data is displayed in the same way as in Fig. 11. We find that for this particular comparison, a Milky Way-mass halo with a proto-galaxy population formed primarily by one massive and dominant main branch halo, m12i (but also Thelma, Louise, Romeo, and Juliet, see Fig. 4) is older than the proto-galaxy population of a Milky Way-mass halo formed from one dominant main branch halo and a massive building block halo, m12m (but also m12c and Romulus). This difference is on the order of ~ 2 Gyr. Furthermore, the peak in the metallicity distribution for the proto-Milky Way population in m12i is more metal-poor than the one in m12m, on the order of ~ 1 dex. Although this comparison has only been shown for two haloes, we find that it is qualitatively satisfied for 8 of the 13 Milky Way-mass galaxies. We argue that this result is potentially very important, and suggests that age differences in metal-poor stars in the inner regions of Milky Way-mass haloes could possibly help decipher if proto-Milky Way systems formed from one or two main haloes. However, we do note that for m12b, m12f, m12r, m12w, and Remus, this is not the case.

In summary, we argue that disentangling if a proto-Milky Way system formed from one or two dominant systems is going to be challenging, as their observable properties are going to be similar. However, we suggest that with large and complete samples of metal-poor stars, that include elemental abundances synthesized in nucleosynthetic sites not explored in this work, as well as accurate age estimates, may hold the clues to answering this question.

5.2 Hunting for the proto-galaxy in the Milky Way

Given all our findings, we now provide a list of ideas/pointers we suggest one to follow if aiming to identify the majority of the populations belonging to the proto-Milky Way:

(i) Mass and age: we suggest that the best possible way to find the proto-galaxy in the Milky Way would be to identify stellar populations older than $\tau \gtrsim 8$ Gyr, that amount to a mass smaller than $M_* \lesssim 10^9 - 10^{10} M_\odot$.

(ii) Spatial distribution: this stellar population would primarily be concentrated towards the inner regions of the galaxy (95 per cent of the mass within $r \sim 30-40$ kpc), with 50 per cent of the mass contained within $\sim 5-10$ kpc. It would also likely have an oblate profile ($\varepsilon \sim 0.7$).

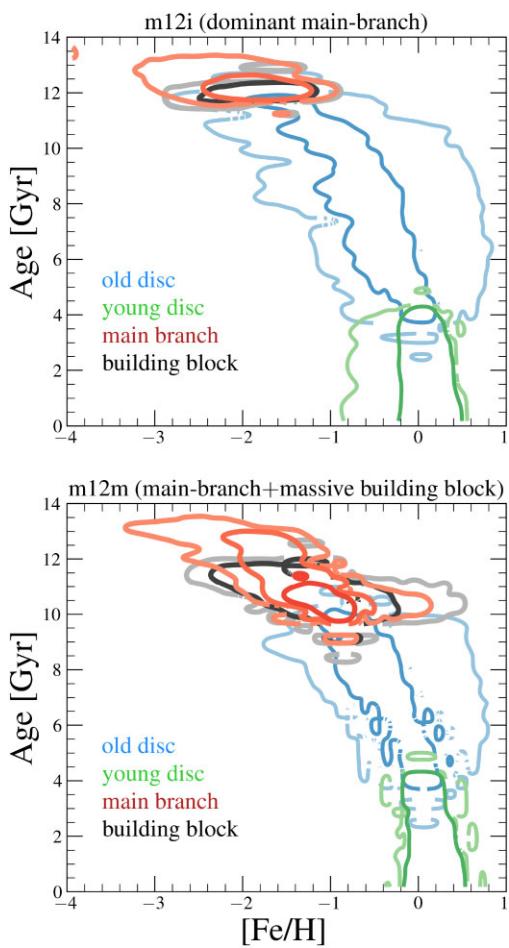


Figure 12. Age–metallicity relation for the same samples as shown in Fig. 11. For this particular comparison we see that m12i, a Milky Way-mass halo with a proto-galaxy population formed primarily by one massive and dominant halo (i.e. main branch), is older than the proto-galaxy population of m12m, a Milky Way-mass halo formed from two dominant haloes (i.e. a main branch and a massive building block). We argue that this ~ 2 Gyr difference should be detectable in relative ages of metal-poor stars. Moreover, the peak in the metallicity distribution for the proto-Milky Way population in m12i is more metal-poor than the one in m12m, on the order of ~ 1 dex. These subtle differences are also seen for ~ 60 per cent of the parent Milky Way-mass galaxy sample (see subsection 5.1 for details). These results hint that age estimates and $[\text{Fe}/\text{H}]$ information for large samples of metal-poor stars in the inner regions of the Milky Way could possibly help answer if the galaxy formed from one dominant halo or from two.

(iii) Kinematics: the proto-Milky Way would not be a strongly rotating population (with respect to the present day Galactic disc, $0.25 \lesssim \langle \kappa/\kappa_{\text{disc}} \rangle \lesssim 0.8$). However, it is still likely to host prograde orbits and manifest moderate tangential velocity values ($0 \lesssim v_{\phi} \lesssim 60 \text{ km s}^{-1}$, see Fig. 8), matching that of an old and metal-poor disc (Fig. 11).

(iv) Chemical compositions: the proto-Milky Way could have a wide range of $[\text{Fe}/\text{H}]$ and $[\alpha/\text{Fe}]$ values. We find that the majority of the stars comprising the proto-Milky Way (either from one main branch system or a main branch and a massive building block) are likely to overlap with the metal-weak old disc in $[\alpha/\text{Fe}]$ and $[\text{Fe}/\text{H}]$. However, additional elemental abundance ratios, which have not been explored in this work, may provide additional separation between proto-galaxy fragments and other co-spatial populations.

Hunts for the proto-galaxy and/or the building blocks that formed it have been performed recently in observational studies (Horta et al.

2021a; Belokurov & Kravtsov 2022; Rix et al. 2022) using chemical-kinematic information. These results are shedding light on the earliest stages of formation of the Milky Way. However, open questions still remain, such as: how many systems comprise the proto-Milky Way? When did the proto-Milky Way emerge? What caused the proto-galaxy to emerge and morph into the metal-poor disc? We believe that this study has provided some intuition on how to answer some of these questions, as we have been able to assess: (a) what proto-Milky Way populations are made of? (b) How massive and/or old proto-Milky Way systems are? (c) How and if different proto-Milky Way fragments can be distinguishable in chemical-kinematic samples.

The advent of the SDSS-V project Milky Way Mapper (Kollmeier et al. 2017) will deliver precise elemental abundance ratios for over $\sim 50\,000$ stars with $[\text{Fe}/\text{H}] < -1$, that when complemented with the *Gaia* mission, and other upcoming massive spectroscopic surveys (e.g. WEAVE: Dalton et al. 2012; 4MOST: de Jong et al. 2019), will provide an unprecedented amount of chemical-kinematic information for metal-poor stars in the innermost galaxy. Along those lines, recent work with the *Gaia* XP spectra are delivering a colossal amount of metallicities for stars in the inner regions of the galaxy (Andrae, Rix & Chandra 2023), which are also helping resolve populations in this region (Rix et al. 2022). In a similar vein, detailed spectroscopic follow up (e.g. PRISTINE: Starkenburg et al. 2017) of metal-poor stars in the innermost regions of the galaxy can also help disentangle the earliest stages of formation of the Milky Way (Lucey et al. 2020; Arentsen et al. 2020a, b; Sestito et al. 2023).

Given our results, we suggest that with these data it should be possible to pick out the massive contributors to proto-Milky Way systems from the smaller building blocks. We are only scratching the surface, but we are on the right path to finding the Milky Way’s heart and understanding its early assembly history.

6 LIMITATIONS AND FURTHER CONSIDERATIONS

Before listing our conclusions, it is imperative we discuss the limitations of our work. Further, we provide a summary of the limitations and considerations for the interpretations of our findings:

(i) The new aspect of this work has been the ability to track the systems that comprise proto-Milky Way populations. However, in doing so, we have decided to track only those luminous haloes that are resolvable given the resolution limits of FIRE-2. Specifically, we have tracked the populations from haloes with 150 star particles or more, leading to a minimum stellar mass of $\sim 1 \times 10^6 M_{\odot}$ for the *Latte* suite, and $\sim 5 \times 10^5 M_{\odot}$ in the *ELVIS* suite¹⁰. Albeit our hands being tied with the ability to resolve haloes, we have been cautious in our choices to be able to track as many resolvable systems as possible in these simulations. However, it is likely that in reality there are more luminous haloes of lower masses that contribute to the build-up of proto-Milky Way populations. We argue that the contribution in mass of these lower mass building blocks is small, but cannot rule out the possibility of it being non-negligible (see Santistevan et al. 2020 and Gandhi et al. 2023 for an accounting of lower mass building blocks). Furthermore, the kinematic properties of the lower mass haloes may not be fully resolved with 150 star particles. Although this only affects a small fraction of our sample, it is another limitation to keep

¹⁰The small difference in the resolution between the two suites is small enough to not have any impact on our results, as we are tracking haloes with 150 star particles or more.

in mind. Studies focusing on tackling the assembly history of proto-Milky Way populations, and the properties of their constituent main branch and building block systems, may need to take this issue into account when comparing to our findings.

(ii) A key property we have defined in this work has been $t_{\text{MR}_{3:1}}$, the time at which a proto-Milky Way emerges. Although well reasoned (see Section 3 for details), this choice is arbitrary, and has ramifications on all the present day properties of the proto-Milky Way populations, as well as the number of building block systems each proto-Milky Way inherits. It could have also been equally as valid to define this time in another well-motivated way (for example, the time in which the host halo peaks in star formation). This is beyond the scope of this work, but could be an interesting way of expanding on these results.

(iii) Here, we have only studied the properties of the field stellar components of proto-Milky Way populations. However, galaxies across the cosmos contain globular clusters (GCs). In the Milky Way, it has been shown that the disruption of GCs contribute a significant amount to the total stellar halo mass budget (Martell et al. 2017; Schiavon et al. 2017; Koch, Grebel & Martell 2019; Horta et al. 2021b; Belokurov & Kravtsov 2023). This would imply that in addition to the field components comprising proto-Milky Way systems, one must also take into account the contribution from disrupted/evaporated GCs. For this work, this limitation is due to FIRE-2 not including prescriptions for the formation and evolution of GCs. However, we argue that it is an important point that needs to be considered for observational and potential future simulation work.

(iv) When comparing the observable properties of main branch and building block events, we have primarily only examined qualitatively the mean/median values. It would be interesting to investigate how the average and full distribution of the spatial, kinematic, and chemical properties of these systems compare quantitatively (following methods and tools that already exist; e.g. Cunningham et al. 2022; Horta et al. 2023a).

7 CONCLUSIONS

At the earliest stages of formation, galaxies experience rapid and chaotic growth, either by coalescence of low-mass galaxies/clumps and/or filamentary supply of gas. In the FIRE-2 simulations, bursty stellar feedback that repeatedly blows apart the ISM at early times also appears to be critical to set the properties of early-stellar populations (e.g. Yu et al. 2021; Gurvich et al. 2023; Hopkins et al. 2023). The remains of the stars born during this phase constitute the proto-galaxy, and should retain the clues to understanding galaxy formation at these earliest stages. In this work, we have searched for the fragments (namely, the main branch and building blocks) that constitute the proto-galaxy in 13 Milky Way-mass haloes from the FIRE-2 simulations. We then examined their observable properties at present day, with the aim of answering the following questions:

(i) What constitutes a proto-Milky Way? We find that proto-Milky Way populations are made of either one (~ 60 per cent) or two (~ 40 per cent) dominant systems of similar mass to the LMC (i.e. $M_\star \sim 1 \times 10^9 M_\odot$) and $\sim 3\text{--}5$ other lower-mass building blocks with an average stellar mass of $M_\star \sim 4 \times 10^7 M_\odot$ (see Fig. 2, Fig. 4, and Fig. 3). The case of two clear dominant systems comprising the proto-Milky Way is especially clear in m12f and m12m. However, the number of building blocks we find in this study that comprise a proto-Milky Way is grounded by our choice to only track systems with 150 star particles or more.

(ii) When does a proto-Milky Way form? Given our assumptions (Section 3) we find that on average, proto-Milky Way populations are old (see Table 2). Their minimum age can range from $\text{Age}_{\text{min}} \gtrsim 8.05$ Gyr ($z = 1.02$) to $\text{Age}_{\text{min}} \lesssim 12.9$ Gyr ($z = 6.08$). We find that overall the proto-Milky Way systems can be grouped into three main camps: an early-forming group, an intermediate forming group, a late-forming one.

(iii) Does environment play a role? The noticeable differences found between galaxies in different environments are the times in which proto-Milky Way systems assemble, and the sizes of the average building block. Table 2 shows that on average, systems in pairs assemble earlier and from smaller mass systems than proto-Milky Way populations in isolation, in line with results from Santistevan et al. (2020). We also find that pairs tend to contain 50 per cent of their stellar populations closer to the host's centre when compared to isolated systems (Fig. 6), and that pairs tend to present slightly more enriched median $[\alpha/\text{Fe}]$ and/or $[\text{Fe}/\text{H}]$ composition values.

(iv) Where are the debris of proto-Milky Way systems spatially contained? The dominant components of the proto-Milky Way (namely, the main branch population and the most massive building blocks) contain 50 per cent of their stellar mass within $r \lesssim 5\text{--}10$ kpc, and 95 per cent within $r \lesssim 40\text{--}60$ kpc (see Figs 5 and 6).

(v) What shape do debris from the proto-Milky Way have? Although different main branch/building blocks adopt a range of morphologies, the dominant components of proto-Milky Way systems adopt an oblate shape ($\varepsilon \sim 0.7$, see Fig. 7).

(vi) What kinematics do the debris of proto-Milky Way systems have? All the fragments of proto-Milky Way systems show low level of systematic net rotation with respect to the present day disc of the host galaxy (i.e. $\langle \kappa/\kappa_{\text{disc}} \rangle \lesssim 0.8$), but are also not purely isotropic (Fig. 8). The majority of these stellar populations rotate on prograde orbits, and can reach average azimuthal velocities of up to $v_\phi \sim 100\text{--}150$ km s $^{-1}$.

(vii) What are the chemical compositions of proto-Milky Ways? The main branch and building block components of proto-Milky Way systems can present a wide range of $[\text{Fe}/\text{H}]$ and $[\alpha/\text{Fe}]$ values, and can adopt high $[\alpha/\text{Fe}]$ values (Fig. 9). This would make it difficult to distinguish the dominant proto-Milky Way populations from populations formed later in the disc using the average value of these abundances alone (see Fig. 11). However, disentangling the massive fragments from the lower mass ones is possible with $[\alpha/\text{Fe}]$ and $[\text{Fe}/\text{H}]$ compositions; similarly, additional element abundances may also help distinguish the larger mass fragments (e.g. Horta et al. 2023a).

(viii) Can we distinguish the fragments that build up proto-Milky Way systems? On the whole, it is possible to separate the dominant components of proto-Milky Way systems (i.e. the main branch) from the non-dominant (low-mass building blocks) components using chemical-kinematic samples. However, distinguishing stars formed in the main branch progenitor from the most massive building blocks will likely be difficult owing to the big overlap in all chemical and kinematic planes shown in this work. However, studies focusing on other chemical abundance measurements and/or studies with larger samples may be able to disentangle the dominant proto-Milky Way fragments based on chemical abundance measurements.

(ix) How do we hunt for the proto-Milky Way? We suggest that metal-poor stars confined to the inner galaxy are likely to be the easiest to find, as they are the debris from the more dominant fragments that formed the proto-Milky Way. These stars should have prograde orbits that are not strongly rotating with the Milky Way's disc, but are also not purely isotropic. They should present, on

average, more enriched chemical abundance ratios when compared to lower mass building blocks and later accreted satellite galaxies, and are likely to overlap in chemical space with the metal-poor tail of the old disc. Thus, we suggest that additional chemical abundance information, likely probing different nucleosynthetic channels may help disentangle different fragments of the proto-Milky Way.

(x) Is the proto-Milky Way formed from one or two dominant haloes? It may be possible to answer this question by examining relative age differences between metal-poor stars in the central regions of the galaxy. From our comparison of m12i and m12m in Fig. 12, proto-Milky Way systems formed from one dominant halo may tend to assemble earlier, and are thus older and more metal-poor, when compared to proto-Milky Way systems formed from two dominant haloes. However, we do stress that this result is from one comparison alone, and is only applicable to ~ 60 per cent of the full sample (8 of the 13 Milky Way-mass galaxies studied).

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8 DATA AVAILABILITY

FIRE-2 simulations are publicly available (Wetzel et al. 2023) at <http://flathub.flatironinstitute.org/fire>. Additional FIRE simulation data are available at <https://fire.northwestern.edu/data>. A public version of the GIZMO code is available at <http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html>.

REFERENCES

Abadi M. G., Navarro J. F., Steinmetz M., 2006, *MNRAS*, 365, 747

Amorisco N. C., 2017, *MNRAS*, 464, 2882

Andrae R., Rix H.-W., Chandra V., 2023, preprint ([arXiv:2302.02611](https://arxiv.org/abs/2302.02611))

Arentsen A., et al., 2020a, *MNRAS*, 491, 11

Arentsen A., et al., 2020b, *MNRAS*, 496, 4964

Behroozi P. S., Wechsler R. H., Wu H.-Y., 2013, *ApJ*, 762, L109

Bell E. F., et al., 2008, *ApJ*, 680, L295

Bellardini M. A., Wetzel A., Loebman S. R., Faucher-Giguère C.-A., Ma X., Feldmann R., 2021, *MNRAS*, 505, 4586

Belokurov V., Kravtsov A., 2022, *MNRAS*, 514, 689

Belokurov V., Kravtsov A., 2023, preprint ([arXiv:2306.00060](https://arxiv.org/abs/2306.00060))

Belokurov V., et al., 2007, *ApJ*, 658, L337

Belokurov V., Erkal D., Evans N. W., Koposov S. E., Deason A. J., 2018, *MNRAS*, 478, 611

Belokurov V., Sanders J. L., Fattah A., Smith M. C., Deason A. J., Evans N. W., Grand R. J. J., 2020, *MNRAS*, 494, 3880

Bonaca A., Conroy C., Wetzel A., Hopkins P. F., Kereš D., 2017, *ApJ*, 845, L101

Brown T. M., Smith E., Ferguson H. C., Rich R. M., Guhathakurta P., Renzini A., Sweigart A. V., Kimble R. A., 2006, *ApJ*, 652, L323

Bullock J. S., Johnston K. V., 2005, *ApJ*, 635, L931

Carollo D., et al., 2007, *Nature*, 450, 1020

Chiba M., Beers T. C., 2000, *AJ*, 119, 2843

Conroy C., Naidu R. P., Garavito-Camargo N., Besla G., Zaritsky D., Bonaca A., Johnson B. D., 2021, *Nature*, 592, 534

Cooper A. P., et al., 2010, *MNRAS*, 406, 744

Cunningham E. C., et al., 2022, *ApJ*, 934, L172

Dalton G., et al., 2012, in McLean I. S., Ramsay S. K., Takami H., eds, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series Vol. 8446, Ground-based and Airborne Instrumentation for Astronomy IV. SPIE, Bellingham, p. 84460

de Jong R. S., et al., 2019, *The Messenger*, 175, 3

Deason A. J., Belokurov V., Evans N. W., 2011, *MNRAS*, 416, 2903

Deason A. J., Koposov S. E., Fattah A., Grand R. J. J., 2023, *MNRAS*, 520, 6091

Di Matteo P., Haywood M., Lehnert M. D., Katz D., Khoperskov S., Snaith O. N., Gómez A., Robichon N., 2019, *A&A*, 632, 4

Donlon Thomas I., Newberg H. J., Kim B., Lépine S., 2022, *ApJ*, 932, L16

El-Badry K., et al., 2018, *MNRAS*, 480, 652

Escala I., et al., 2018, *MNRAS*, 474, 2194

Escala I., Kirby E. N., Gilbert K. M., Cunningham E. C., Wojno J., 2019, *ApJ*, 878, L42

Escala I., Gilbert K. M., Kirby E. N., Wojno J., Cunningham E. C., Guhathakurta P., 2020, *ApJ*, 889, L177

Faucher-Giguère C.-A., Lidz A., Zaldarriaga M., Hernquist L., 2009, *ApJ*, 703, L1416

Ferguson A. M. N., Irwin M. J., Ibata R. A., Lewis G. F., Tanvir N. R., 2002, *AJ*, 124, 1452

Font A. S., Johnston K. V., Ferguson A. M. N., Bullock J. S., Robertson B. E., Tumlinson J., Guhathakurta P., 2008, *ApJ*, 673, L215

Font A. S., McCarthy I. G., Crain R. A., Theuns T., Schaye J., Wiersma R. P. C., Dalla Vecchia C., 2011, *MNRAS*, 416, 2802

Forbes D. A., 2020, *MNRAS*, 493, 847

Fragkoudi F., et al., 2020, *MNRAS*, 494, 5936

Vallenari A., et al., 2023, *A&A*, 674, 1

Gandhi P. J., Wetzel A., Hopkins P. F., Shappee B. J., Wheeler C., Faucher-Giguère C.-A., 2022, *MNRAS*, 516, 1958

Gandhi P. J., et al., 2023, preprint ([arXiv:2309.09940](https://arxiv.org/abs/2309.09940))

Garrison-Kimmel S., et al., 2017, *MNRAS*, 471, 1709

Garrison-Kimmel S., et al., 2019a, *MNRAS*, 487, 1380

Garrison-Kimmel S., et al., 2019b, *MNRAS*, 489, 4574

Grillmair C. J., Dionatos O., 2006, *ApJ*, 643, L17

Gurvich A. B., et al., 2023, *MNRAS*, 519, 2598

Hahn O., Abel T., 2011, *MNRAS*, 415, 2101

Haywood M., Di Matteo P., Lehnert M. D., Snaith O., Khoperskov S., Gómez A., 2018, *ApJ*, 863, L113

Helmi A., 2020, *ARA&A*, 58, 256

Helmi A., Babusiaux C., Koppelman H. H., Massari D., Veljanoski J., Brown A. G. A., 2018, *Nature*, 563, 85

Hopkins P. F., 2015, *MNRAS*, 450, 53

Hopkins P. F., 2016, *MNRAS*, 455, 89

Hopkins P. F., et al., 2018a, *MNRAS*, 477, 1578

Hopkins P. F., et al., 2018b, *MNRAS*, 480, 800

Hopkins P. F., et al., 2023, *MNRAS*

Horta D., et al., 2021a, *MNRAS*, 500, 1385

Horta D., et al., 2021b, *MNRAS*, 500, 5462

Horta D., et al., 2023a, *MNRAS*, 520, 5671

Horta D., et al., 2023b, *ApJ*, 943, L158

Ibata R. A., Gilmore G., Irwin M. J., 1994, *Nature*, 370, 194

Johnston K. V., Bullock J. S., Sharma S., Font A., Robertson B. E., Leitner S. N., 2008, *ApJ*, 689, L936

Khoperskov S., et al., 2022a, preprint ([arXiv:2206.04521](https://arxiv.org/abs/2206.04521))

Khoperskov S., et al., 2022b, preprint ([arXiv:2206.04522](https://arxiv.org/abs/2206.04522))

Kirby E. N., Cohen J. G., Guhathakurta P., Cheng L., Bullock J. S., Gallazzi A., 2013, *ApJ*, 779, L102

Kirby E. N., Gilbert K. M., Escala I., Wojno J., Guhathakurta P., Majewski S. R., Beaton R. L., 2020, *AJ*, 159, 46

Koch A., Grebel E. K., Martell S. L., 2019, *A&A*, 625, 75

Kollmeier J. A., et al., 2017, *SDSS-V: Pioneering Panoptic Spectroscopy*, preprint (arXiv:1711.03234)

Kroupa P., 2001, *MNRAS*, 322, 231

Kruijssen J. M. D., et al., 2020, *MNRAS*, 498, 2491

Krumholz M. R., Gnedin N. Y., 2011, *ApJ*, 729, L36

Leitherer C., et al., 1999, *ApJS*, 123, 3

Lucey M., et al., 2021, *MNRAS*, 501, 5996

Ma X., Hopkins P. F., Wetzel A. R., Kirby E. N., Anglés-Alcázar D., Faucher-Giguère C.-A., Kereš D., Quataert E., 2017, *MNRAS*, 467, 2430

Mackereth J. T., et al., 2019, *MNRAS*, 482, 3426

Mardini M. K., Frebel A., Chiti A., Meiron Y., Brauer K. V., Ou X., 2022, *ApJ*, 936, L78

Martell S. L., et al., 2017, *MNRAS*, 465, 3203

McCarthy I. G., Font A. S., Crain R. A., Deason A. J., Schaye J., Theuns T., 2012, *MNRAS*, 420, 2245

McCluskey F., Wetzel A., Loebman S. R., Moreno J., Faucher-Giguere C.-A., 2024, *MNRAS*, 527, 6949

Necib L., Lisanti M., Garrison-Kimmel S., Wetzel A., Sanderson R., Hopkins P. F., Faucher-Giguère C.-A., Kereš D., 2019, *ApJ*, 883, L27

Newberg H. J., Yanny B., Willett B. A., 2009, *ApJ*, 700, L61

Orkney M. D. A., et al., 2023, preprint (arXiv:2303.02147)

Panithanpaisal N., Sanderson R. E., Wetzel A., Cunningham E. C., Bailin J., Faucher-Giguère C.-A., 2021, *ApJ*, 920, L10

Planck Collaboration et al., 2020, *A&A*, 641, 6

Rix H.-W., et al., 2022, *ApJ*, 941, L45

Samuel J., et al., 2020, *MNRAS*, 491, 1471

Sanderson R. E., et al., 2018, *ApJ*, 869, L12

Sanderson R. E., et al., 2020, *ApJS*, 246, 6

Santistevan I. B., Wetzel A., El-Badry K., Bland-Hawthorn J., Boylan-Kolchin M., Bailin J., Faucher-Giguère C.-A., Benincasa S., 2020, *MNRAS*, 497, 747

Santistevan I. B., Wetzel A., Tollerud E., Sanderson R. E., Samuel J., 2023, *MNRAS*, 518, 1447

Schiavon R. P., et al., 2017, *MNRAS*, 465, 501

Semenov V. A., Conroy C., Chandra V., Hernquist L., Nelson D., 2023, preprint (arXiv:2306.13125)

Sestito F., et al., 2023, *MNRAS*, 518, 4557

Shipp N., et al., 2023, *ApJ*, 949, L44

Starkenburg E., et al., 2017, *MNRAS*, 471, 2587

Su K.-Y., Hopkins P. F., Hayward C. C., Faucher-Giguère C.-A., Kereš D., Ma X., Robles V. H., 2017, *MNRAS*, 471, 144

Wetzel A., Garrison-Kimmel S., 2020a, *HaloAnalysis: Read and analyze halo catalogs and merger trees*, preprint (ascl:2002.014)

Wetzel A., Garrison-Kimmel S., 2020b, *GizmoAnalysis: Read and analyze Gizmo simulations*, preprint (ascl:2002.015)

Wetzel A. R., Hopkins P. F., Kim J.-h., Faucher-Giguère C.-A., Kereš D., Quataert E., 2016, *ApJ*, 827, L23

Wetzel A., et al., 2023, *ApJS*, 265, 44

Wheeler C., et al., 2019, *MNRAS*, 490, 4447

White S. D. M., Frenk C. S., 1991, *ApJ*, 379, L52

White S. D. M., Rees M. J., 1978, *MNRAS*, 183, 341

Yu S., et al., 2021, *MNRAS*, 505, 889

Yu S., et al., 2023, *MNRAS*, 523, 6220

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