

Dynamic Diffusive Interfacial Transport (D-DIT): A Novel Quantitative Swelling Technique for Developing Binary Phase Diagrams of Aqueous Surfactant Systems

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Current methods to develop surfactant phase diagrams are time-intensive and fail to capture the kinetics of phase evolution. Here, the design and performance of a quantitative swelling technique to study the dynamic phase behavior of surfactants is described. The instrument combines cross-polarized optical and short-wave infrared (SWIR) imaging to enable high-resolution, high-throughput, and in-situ identification of phases and water compositions. Data across the entire composition spectrum for dynamics and phase evolution of a binary aqueous non-ionic surfactant solution at two isotherms is presented. This instrument provides pathways to develop non-equilibrium phase diagrams of surfactant systems – critical to predicting outcomes of formulation and processing. It can be applied to study time-dependent material relationships across a diverse range of materials and processes including dissolution of surfactant droplets and drying of aqueous polymer films.

I. INTRODUCTION

Surfactants are amphiphilic molecules that reduce surface tension and spontaneously self-assemble above the critical micelle concentration (CMC)¹. In binary aqueous solutions, surfactants form an array of concentration- and temperature-dependent aggregates spanning from low-viscosity micellar phases to pasty, high-viscosity liquid crystalline phases such as hexagonal, cubic, and lamellar². The self-assembly and associated phase information – including the number, structure, and composition of phases is typically documented in phase diagrams which are used to create various commercial products like shampoos and conditioners^{3,4}.

The study of surfactant phases is growing in both significance and complexity. Phase science is an old field^{5–7} and classically, temperature-composition phase diagrams have been determined by sealing a priori known compositions in glass vials and observing the resulting phases. Krafft's pioneering work on the behavior of soap solutions in different solvents and the temperature dependence of soap crystal solubility set the stage for McBain's work leading to the first published

phase diagram for a surfactant system (sodium laurate (dodecanoate)-sodium chloride-water ternary system at 90 °C) in 1922⁸. The first phase diagram for a binary system (potassium oleate-water) was published by McBain and Elford in 1926⁹. Historically, phase diagrams are developed over decades of carefully executed experiments. For example, the phase diagrams of the binary decyl tetraethylene glycol ether (C₁₀E₄)-H₂O¹⁰ and dioctadecyldimethylammonium chloride (DODMAC)-H₂O¹¹ systems have been through numerous revisions. A complete phase diagram for the industrial workhorse sodium lauryl ether sulfate (SLES)-H₂O system has yet to be determined¹².

Current experimental methods for developing surfactant phase diagrams suffer from at least one of the following limitations: (1) the need to test many samples, (2) a low signal-to-noise ratio or poor accuracy, (3) expensive set-up and complicated data analysis, and (4) unable to capture transient phase dynamics. Isoplethal methods, such as polarized optical microscopy^{13–15}, calorimetry¹⁶, and small angle x-ray scattering¹⁷, are widely used but require testing of several samples¹⁸. Isothermal techniques like deuterium-based nuclear magnetic resonance (D-NMR)^{19–21} and swelling (or penetration) experiments^{7,22–24} can examine an wide concentration range but struggle with quantification of phase parameters and high-viscosity liquid crystalline phases²¹.

In 1987, Laughlin and Munyon devised the first in-situ quantitative swelling method termed Diffusive Interfacial Transport (DIT), which overcame many of the limitations of classical techniques⁴. Similar to penetration experiments, the entire composition range could be investigated and all phases along an isotherm were produced. Data for the entire phase diagram could be obtained by conducting studies at several temperatures. In the first iteration of this method (“DIT-NDX”), a Jamin-Lebedeff quantitative split-beam transmission interferometer was coupled to a polarized optical microscope to measure the refractive indices of surfactant phases and determine their compositions^{4,7}. The DIT-NDX technique produced a great deal of useful information^{11,21,25}, but the analytical accuracy of concentrations estimated using this method was poor. For example, the acylmethylglucamine phase diagram had to be adjusted based on separate calorimetric experiments⁷.

The second version (“DIT-NIR”) developed in 2000 used near-infrared (IR) microspectroscopy to measure water compositions instead of interferometry-based refractive index quantification²⁵. The Jamin-Lebedeff optics from the earlier DIT-NDX were retained for qualitative analysis of

surfactant phase textures based on polarized optical microscopy and an FT-NIR spectrophotometer coupled to an IR microscope was used to record IR spectra. DIT-NIR had many advantages over DIT-NDX²⁶ but was expensive to set up²⁷ and had poor signal-to-noise ratio, necessitating up to 128 scans to be co-added²⁵. Further, generating concentrations from IR absorption spectra is difficult and Jamin-Lebedeff interferometers are no longer commercially available²¹, impeding widespread use of this technique. Despite these limitations, the DIT-NIR technique had significant potential and, with appropriate system improvements, could serve as an efficient approach for constructing binary phase diagrams.

This article describes a new instrument called the “Dynamic-DIT” (D-DIT) which couples short-wave infrared (SWIR) imaging and polarized optical imaging to simultaneously track the temporal evolution of water concentration and phase formation. The D-DIT builds upon previous iterations of the Diffusive Interfacial Transport (DIT) methodology^{4,25} and generates previously inaccessible data about kinetic phase transitions and equilibria of binary aqueous surfactant systems. The capability of the instrument is demonstrated by tracking the phase evolution of a binary aqueous non-ionic surfactant solution in a confined rectangular geometry over seven days.

II. EXPERIMENTAL SECTION

A. Experimental Setup

A schematic of the D-DIT is shown in **FIG. 1**. Visible light and SWIR radiation is transmitted through the D-DIT sample capillary and imaged with cameras. SWIR radiation is unaffected by polarizers. This experimental setup represents a novel integration of commercial instrumentation: a SWIR camera, an optical camera, an infrared radiation source, and a cold optical light source.

The instrumentation is controlled through a custom Python code that can initiate simultaneous image acquisition through both cameras at intervals as small as six seconds. The frames per second (fps) captured by the camera depend on pixel resolution and should be optimized. Only radiation from the composite light source was allowed to pass through the capillaries and be captured by the cameras. In a Dynamic-DIT experiment, pure or concentrated surfactant at one end (right) was brought in contact with water at the other open end (left) in a long, thin rectangular capillary (1D diffusion) (**supplementary material**)¹⁸. After the capillary was filled with water, the exposed end

was sealed, e.g., with high-vacuum silicone grease. Post-initiation, capillaries were allowed to equilibrate at room temperature (22 °C) or in a refrigerator (4 °C).

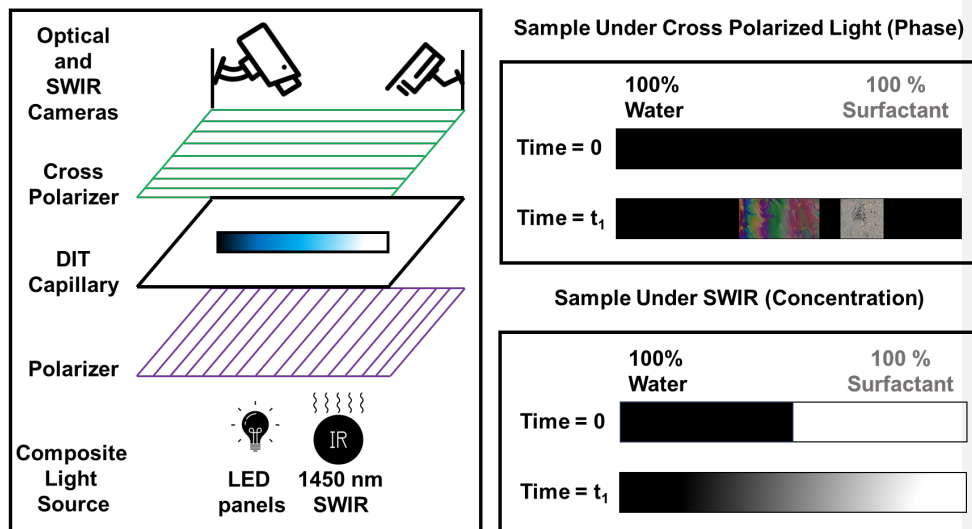


FIG. 1. Schematic of the novel D-DIT with three principal components – (1) composite light source (visible + SWIR), (2) Cross-polarizers and optical camera (phase structure), and (3) short-wave IR (SWIR) camera (water concentration). The instrument is pictured in the **supplementary material**.

1. Short Wave Infrared (SWIR) Camera

SWIR technology has been extensively used in defense applications²⁸ and was only declassified enough for public experimentation ~1995. More recently, it has been used for machine-vision inspection of silicon wafers and agricultural products^{29,30}. An IR spectrum is produced by exciting various vibrational modes of a molecule with IR photons of varying wavelengths. The water molecule, which is a potent IR absorber, has three vibrational degrees of freedom: (1) symmetrical stretching, (2) asymmetric stretching, and (3) in-plane scissoring, with each mode corresponding to a unique wavenumber³¹.

108 At a wavelength of approximately 1450 nm, liquid water exhibits a strong absorption band
109 in the near-infrared region^{32,33}, causing objects with high moisture content to appear black in SWIR
110 images. Surfactants and other molecules commonly encountered in surfactant systems, such as
111 alcohols and carboxylic acids, do not absorb strongly in the same region of the IR spectrum as
112 water²⁵. The Goldeye G-033 TEC1 GigE SWIR camera has indium gallium arsenide (InGaAs)
113 sensors and is sensitive to the SWIR spectrum between 900 and 1700 nanometers. It can capture
114 up to 301 frames per second at 0.3-megapixel resolution and generate 14-bit images.

115 **2. Optical Camera**

116 The optical camera was used for imaging transmitted cross-polarized visible light. This
117 setup utilized the Basler acA1920-50gc GigE color camera. It can capture 50 frames per second at
118 a resolution of 2.3-megapixels and produce 12-bit images.

119 **3. Composite Light source**

120 The composite light source was a straightforward integration of commonly available cold
121 LED panels and a 1450 nm SWIR backlight developed by EFFILUX. Both the sources were
122 focused to get maximum radiation through the capillaries. Polarizing sheets were integrated above
123 and below the capillaries to ensure cross-polarization of visible light.

124 **4. DIT capillaries**

125 Rectangular glass capillaries manufactured by Vitrocom with chamber dimensions 50 mm
126 x 10 mm x 1 mm (length x width x thickness) were used in this study. The originally received
127 capillaries were sealed at one end and displayed no strain birefringence. Capillaries were selected
128 based on principles established by Laughlin et al.^{4,25} – they were geometrically constrained to
129 ensure that concentration gradients along the two short dimensions vanished, while the gradient
130 along the longest dimension persisted. An additional consideration was IR transmission. The
131 chamber had to be sufficiently thick for SWIR imaging with high contrast, but small enough to
132 eliminate hydrodynamic effects.

133 **B. Data Processing**

134 Contrary to previous iterations of DIT, analyzing data from the D-DIT was straightforward
135 and based on the Beer-Lambert Law³⁴ (**Equation (1)**). An empty capillary and a capillary filled

with water were used as controls. Only water, and not the surfactant absorbed IR resulting in an intense black color that was tracked. A single sequence of images was sufficient and multiple scans were not necessary.

$$A = \text{Log}_{10} \frac{I_o}{I} = \epsilon l c \quad (1)$$

I_o was the baseline intensity for the black capillary or capillary filled only with surfactant while I corresponded to the measured intensity post-initiation. The extinction coefficient ϵ for water was calculated from the loaded capillary at $t = 0$. The control capillary can also be used. Knowing the absorbance (A) and path length through the capillary ($l = 1$ mm), water concentration was determined and normalized to the length of the capillary (50 mm). Qualitative identification of surfactant phases from cross-polarized optical images was based on the classical work of Rosevear¹⁵.

III. RESULTS AND DISCUSSION

To demonstrate the diverse capabilities of the D-DIT, simultaneous cross-polarized optical and SWIR imaging data is provided for the dynamic phase behavior of the non-ionic surfactant pentaethylene glycol monodecyl ether ($C_{10}E_5$) - linear formula $\text{CH}_3(\text{CH}_2)_9(\text{OCH}_2\text{CH}_2)_5\text{OH}$. An optically clear, liquid solution of $C_{10}E_5$ (BioXtra, $\geq 97.0\%$ - Millipore Sigma) was used as received.

FIG. 2 shows high-resolution cross-polarized micrographs of capillaries seven days post-initiation of the DIT experiment.¹⁵ Micellar and cubic phases appear dark under cross-polarizers¹⁵. At both temperatures, birefringent regions in **FIG. 2** (a – i) and (b – i) represented co-existing hexagonal and lamellar phases. The hexagonal phase could be identified by its characteristic fan-like structures **FIG. 2** (b – ii), while lamellar phases were determined by the presence of multilamellar vesicles (MLVs) (**FIG. 2** (a – ii) and (a – iii)).

Water concentration evolution data at two isotherms across the entire composition spectrum (0-100% water concentration) is presented in **FIG. 3** (a) and dynamic data over the initial 8 hours post-initiation at 22 °C is available (**multimedia view**). As expected⁷, the concentration gradient was initially steep (**FIG. 3** (a): $t = 0$ days) and gradually started to smoothen (**FIG. 3** (a) – $t = 1$ day) with countercurrent diffusion of solute and solvent. Seven days after initiation at 22 °C (**FIG. 3** (a) – $t = 7$ days), water diffused to the closed end of the capillary and resulted in two

163 distinct phase regions (Micelles > Birefringent region (co-existing lamellar and hexagonal phases))
164 as seen in **FIG. 2** (b - i).

165 At 4 °C, five distinct phase bands – Micelles > Hexagonal > Cubic > Birefringent region
166 (co-existing lamellar and hexagonal phases) > micelles (**FIG. 2** (b - i)) – were observed with
167 decreasing water concentration. Water concentration at boundaries of phase bands is presented in
168 **FIG. 3** (b). At this temperature, interdiffusion across the capillary was slower, and needle-like
169 structures were observed at the liquid crystalline/ micellar interface (**FIG. 2** (b - iii)).

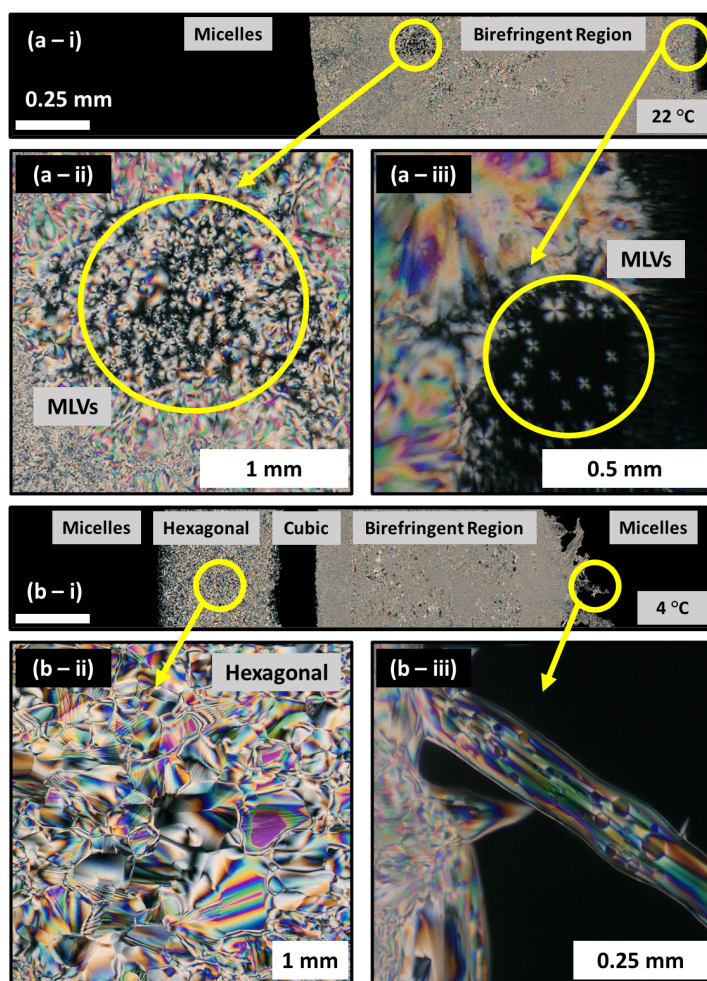


FIG. 2. C₁₀E₅ – water capillaries at $t = 7$ days at (a - i) 22 °C, and (b - i) 4 °C. Specific features of interest shown in (a - ii), (a - iii), (b - ii), and (b - iii). Scale bars in (a - i) and (b - i) indicate 2.5 mm. High-resolution cross-polarized micrographs captured using a Keyence VHX-F series microscope equipped with a Dual-Objective VH-ZST Zoom Lens (magnification range

20x to 2000x) with polarizers). Full images from the D-DIT are presented in the **supplementary material**.

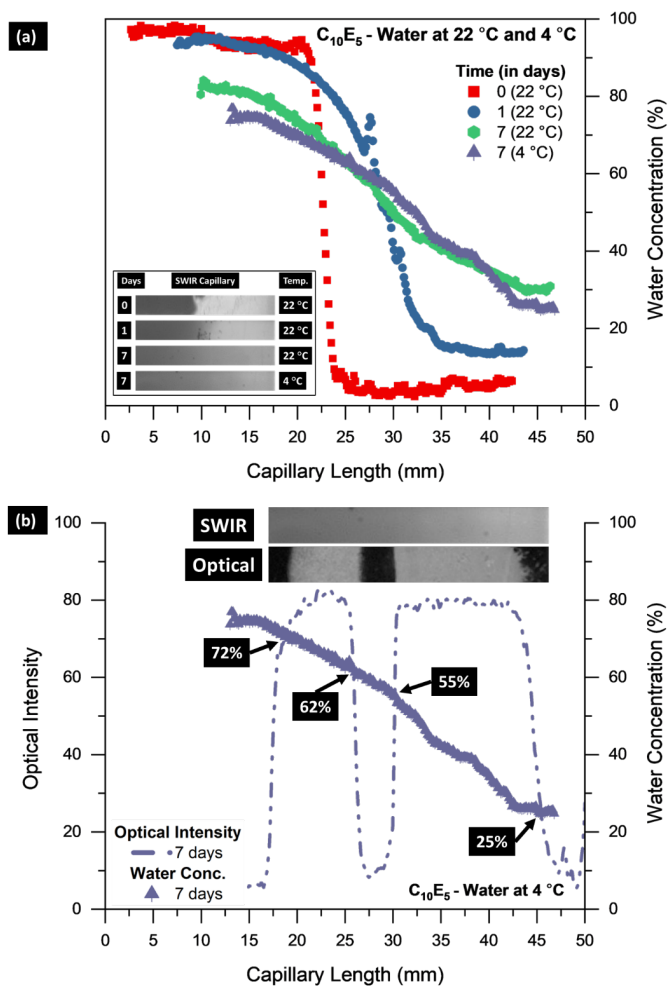
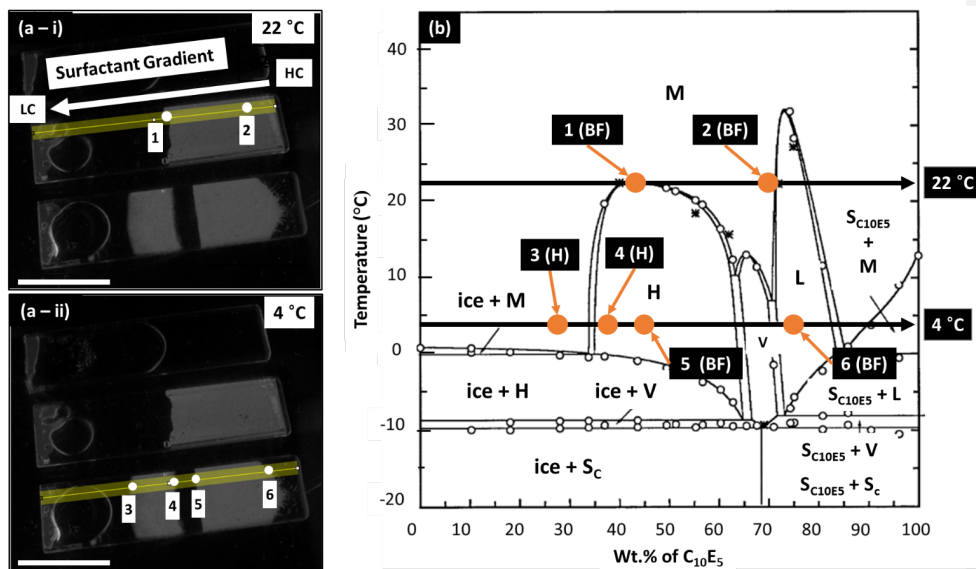


FIG. 3. (a) Evolution of water concentration profiles. (Inset) SWIR images of line scans across the capillary (**multimedia view**). (b) Optical intensity and water concentration profile across the length of the capillary at 4 °C. (Inset) corresponding line scans from SWIR and optical images.

181 Width of the phase bands can be determined from points of intersection of intensity and
 182 concentration profiles (intersections indicated by arrows). A complete set of profiles is shown in
 183 the **supplementary material**.

184 Water concentrations at selected points of interest and comparisons to the equilibrium
 185 phase diagram developed by Nibu and Inoue¹⁶ are presented in **FIG. 4** (b). There was good
 186 correlation between water content and predicted phases at 22 °C, with the exception of an optically
 187 isotropic micellar phase formed between the hexagonal and lamellar phases¹⁶. In this study, no
 188 such phase was found. The absence of this micellar phase and the presence of a coexisting
 189 birefringent region were attributed to two key factors: (1) the high degree of packing of lamellar
 190 and hexagonal phases leading to slower water diffusion; and (2) extremely high viscosity of the
 191 hexagonal phase restricting flow and movement in the capillary. The complexity is further
 192 increased by the fact that the 22 °C isotherm is close to the upper limit of the hexagonal phase
 193 boundary.



195 **FIG. 4.** (a-i) and (a-ii) Cross-polarized optical images at 22 °C and 4 °C after 7 days with water
 196 gradient from left to right and corresponding C₁₀E₅ gradient from right to left (HC - high
 197 concentration and LC - low concentration). Points of interest are marked 1-6. Scale bars (lower
 198 left) indicate 20 mm. (b) Comparison between selected points of interest (1-6) from D-DIT
 199 capillaries and equilibrium C₁₀E₅ – water phase diagram adapted from Nibu and Inoue¹⁶. Legend:
 200 M – Micelles, H – Hexagonal phase, V – Cubic phase, L – Lamellar phase, S_c – solid phase
 201 hydrated compound, S_{C₁₀E₅} - solid of pure C₁₀E₅, and BF – birefringent region (with coexisting
 202 Hexagonal (H) and Lamellar (L) phases). Phases identified are written in circular brackets (E.g.,
 203 1(BF) indicates point 1 from (a-i) and its phase BF.)

204 All expected phases were observed at 4 °C. However, the water concentration and the
 205 resulting phases, along with the position of the phase bands did not align with those predicted by
 206 the equilibrium phase diagram¹⁶. This was extremely interesting and alluded to the interplay
 207 between the kinetics of mass transport across interfaces to reach equilibrium in a confined
 208 environment and the dynamic nature of the measurements. Small temperature changes developed
 209 while imaging the capillary at room temperature (22 °C) could have also induced another non-
 210 equilibrium effect - efforts were made to minimize time spent outside the temperature conditioning
 211 environment. Over time, it is expected that the phase bands will asymmetrically widen⁴ and the
 212 capillary will equilibrate to a uniform concentration.

213 IV. DISCUSSION

214 The Dynamic-DIT can develop non-equilibrium phase diagrams of surfactant systems,
 215 which are fundamentally distinct from equilibrium temperature-concentration diagrams. By
 216 considering the time required for a system to reach equilibrium, non-equilibrium phase diagrams
 217 can be used to predict the outcomes of various processes like dilution, mixing, and temperature
 218 changes. Additionally, the dynamics of phase transitions in geometrically constrained
 219 environments can be utilized in products and flow processes to kinetically trap the surfactant in
 220 desired non-equilibrium states³⁵.

221 It can also be used to quantify the dissolution and drying of surfactant or polymer solutions.
 222 Aqueous surfactant solutions, especially the low-viscosity micellar phases, are commonly used in
 223 personal care products like shampoos and detergents². To lower a product's carbon and water

footprint, global consumer product companies are striving to formulate, and ship concentrated products with high-viscosity liquid crystalline or gel phases³⁶. However, such concentrated materials can reduce mixing and pumping efficiency during formulation and slow production^{37,38}. During the processing of surfactant solutions, knowledge of the temperature-concentration phase diagram (hydration) and transformation kinetics from one phase to another (dissolution) is of paramount importance^{39,40}. Other applications such as paper coatings^{41,42}, adhesives^{43,44}, pharmaceutical packaging⁴⁵, and printed circuit boards⁴⁶ make extensive use of water-based polymer films. Drying (inverse hydration) time is an essential processing and performance criterion for these films^{47,48}. Additional studies are in progress.

This technique can be extended to multicomponent mixtures by running full 900 nm - 1700 nm absorption spectrums for each component using broadband SWIR excitation light sources and selective bandpass filters in front of the cameras. Certain components could also be tagged with dyes and markers sensitive to specific wavelengths. However, diffusion of more than two components can get extremely complicated since the third (or higher) component may diffuse separately from its starting location (tie-line crossing is common in ternary systems and tie-triangles must be constructed^{21,49,50}), and must be carefully considered. The capabilities of the D-DIT can be enhanced by the addition of an environmental chamber to enable in-situ temperature ramps. As some SWIR signals are temperature dependent, proper calibrations must be performed at each temperature of interest.

V. SUMMARY

The Dynamic-DIT (D-DIT) enables the simultaneous in-situ measurement of water concentration and surfactant phase evolution. The system benefits from the coupling of commercially available instruments to perform a diverse array of experiments on aqueous solutions. The aqueous surfactant system characterized in this study is intended to demonstrate the capability of the Dynamic-DIT to characterize dynamic phase transitions and develop non-equilibrium phase diagrams. Experiments performed thus far represent only a small subset of the instrument's full capabilities as the SWIR camera can also be used for dissolution and drying studies. With further system improvements, the effects of various confining geometries and in-situ temperature variations on the dynamic behavior of surfactant phases can be investigated.

253 **SUPPLEMENTARY MATERIAL**

254 See supplementary material for optical and SWIR images from D-DIT, and complete
255 coupled optical intensity and water concentration profiles. Multimedia files include D-DIT data
256 over the initial eight hours at 22 °C.

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261 **CONFLICTS OF INTEREST**

262 There are no conflicts of interest to declare.

263 **AUTHOR CONTRIBUTIONS**

264 P.U.K.: data curation, formal analysis, investigation, methodology, visualization, writing -
265 original draft; K.A.E.: conceptualization, data curation, funding acquisition, project
266 administration, visualization, supervision, writing - original draft, writing – review & editing; S.L.:
267 conceptualization, data curation, methodology, funding acquisition, resources, supervision,
268 writing – review & editing.

269 **DATA AVAILABILITY**

270 The data that support the findings of this study are available from the corresponding author
271 upon reasonable request.

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