

Search for prompt production of pentaquarks in charm hadron final states

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A search for hidden-charm pentaquark states decaying to a range of $\Sigma_c \bar{D}$ and $\Lambda_c^+ \bar{D}$ final states, as well as doubly charmed pentaquark states to $\Sigma_c D$ and $\Lambda_c^+ D$, is made using samples of proton-proton collision data corresponding to an integrated luminosity of 5.7 fb^{-1} recorded by the LHCb detector at $\sqrt{s} = 13 \text{ TeV}$. Since no significant signals are found, upper limits are set on the pentaquark yields relative to that of the Λ_c^+ baryon in the $\Lambda_c^+ \rightarrow p K^- \pi^+$ decay mode. The known pentaquark states are also investigated, and their signal yields are found to be consistent with zero in all cases.

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I. INTRODUCTION

Since the formulation of the quark model [1,2], hadronic states beyond the conventional $q\bar{q}$ mesons and qqq baryons have been proposed. Hadrons with different combinations of quarks q and gluons g , such as pentaquarks ($q\bar{q}qqq$), tetraquarks ($q\bar{q}q\bar{q}$) [1,2], six-quark H-dibaryons ($qq\bar{q}q\bar{q}q\bar{q}$) [3], hybrids ($q\bar{q}g$) [4] and glueballs (ggg) [5], have been predicted by QCD-based models. The existence of such “exotic” hadrons had been debated for several years without a consensus being reached. In the early 2000s, new hadrons with unexpected features were observed, such as the $D_{s0}^*(2317)^+$ [6] and $\chi_{c1}(3872)$ [7] mesons, followed shortly after by the discovery of many other charmonium-like and bottomoniumlike states. While it is still not possible to rule out firmly a conventional nature for the majority of such states, the observation of manifestly exotic hadrons such as the $Z_c(4430)^+$ meson [8], an electrically charged charmoniumlike state, three P_c^+ baryons [9–11], with a minimal quark content $c\bar{c}uud$, and the T_{cc}^+ state [12,13], a meson containing two charm quarks, established the existence of QCD exotics. Many models have been proposed to explain the exotic nature of such states: *hadronic molecules* [14,15], whose constituents are color-singlet hadrons bound by residual nuclear forces; *tetraquarks and pentaquarks* [16,17], bound states where diquarks and diantiquarks are building blocks; *hadro-quarkonium* [18], a cloud of light quarks and gluons bound to a heavy $Q\bar{Q}$ core state via van der Waals forces (Q represents a heavy quark, such as the b quark), and

threshold effects, enhancements caused by threshold cusps or rescattering processes [19,20]. An intriguing feature of many exotic hadrons is the proximity to hadron-hadron thresholds. For example, the three pentaquark states $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$, observed in the $J/\psi p$ projection of $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays [11], have masses that are just below the $\Sigma_c^+ \bar{D}^0$ and $\Sigma_c^+ \bar{D}^{*0}$ thresholds.¹ More experimental and theoretical scrutiny is required to understand if this is just coincidental or related to the internal structure of the states as bound systems of a baryon and a meson. As for the conventional hadrons, the observation of new decay modes can shed light on the binding mechanism of exotic hadrons. In addition, many models predict doubly charmed pentaquark states, where doubly charmed refers to a state with two units of charm quantum number, decaying to a range of $\Sigma_c D$ and $\Lambda_c^+ D$ combinations [21]. Excited Ξ_{cc} baryons could be observed in such final states as well [22].

This paper presents a search for the $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$ baryons and other pentaquarks with hidden charm, meaning charm quantum number equal to zero, in the prompt $\Sigma_c \bar{D}^{(*)}$, $\Sigma_c^* \bar{D}^{(*)}$, $\Lambda_c^+ \bar{D}^{(*)}$, and $\Lambda_c^+ \pi \bar{D}^{(*)}$ mass spectra.² A search for pentaquarks containing two charm quarks has also been carried out in the $\Sigma_c D^{(*)}$, $\Sigma_c^* D^{(*)}$, $\Lambda_c^+ D^{(*)}$ and $\Lambda_c^+ \pi D^{(*)}$ mass spectra. Upper limits on the yields in these spectra relative to the $\Lambda_c^+ \rightarrow p K^- \pi^+$ normalization channel are presented. The measurements are based on samples of proton-proton (pp) collision data corresponding to an integrated luminosity of 5.7 fb^{-1} at center-of-mass energies of 13 TeV recorded by the LHCb experiment between 2016 and 2018.

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¹The $\Sigma_c(2455)$ and $\Sigma_c(2520)$ baryons are referred to as Σ_c and Σ_c^* , respectively.

²The inclusion of charge-conjugate processes is implied throughout.

II. THE LHCb DETECTOR

The LHCb detector [23,24] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. The tracking system provides a measurement of the momentum p of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/ c . The minimum distance of a track to a primary pp collision vertex (PV), the impact parameter, is measured with a resolution of $(15 + 29/p_T) \mu\text{m}$, where p_T is the component of the momentum transverse to the beam, in GeV/ c . Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photons, electrons and hadrons are identified by a calorimeter system consisting of scintillating-pad and pre-shower detectors, an electromagnetic and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers.

The online event selection is performed by a trigger, which consists of a hardware stage followed by a two-level software stage [25]. At the hardware trigger stage, events are required to have a muon with high p_T or hadron, photon or electron with high transverse energy in the calorimeters. In between the two software trigger stages, an alignment and calibration of the detector is performed in near real time and their results are used in the trigger [26]. The same alignment and calibration information is propagated to the offline reconstruction, ensuring consistent and high-quality particle identification (PID) information between the trigger and offline software. The identical performance of the online and offline reconstruction offers the opportunity to perform physics analyses directly using candidates reconstructed in the trigger [27,28]. This analysis exploits this by using D^0 , D^+ and Λ_c^+ candidates fully reconstructed in the trigger, as well as single pions for certain final states.

Simulated pp collisions are generated using PYTHIA [29] with a specific LHCb configuration [30]. Decays of hadronic particles are described by EVTGEN [31], in which final-state radiation is generated using PHOTOS [32]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [33] as described in Ref. [34].

III. SELECTION

All signal mode combinations are listed in Table I. It is interesting to note that the quark content of each of these states is comparable to the quark content of the $J/\psi p$

TABLE I. All possible combinations of Σ_c or Λ_c^+ baryons with $D^{(*)}$ mesons to produce the isospin multiplet. Combinations of Λ_c^+ baryons, pions and D mesons are also considered. From each Σ_c D combination the corresponding $\Lambda_c^+ \pi D$ combination can be derived. The charge of the corresponding pentaquark state is given, along with the isospin, hypercharge and charm quantum numbers. The last column indicates whether a mode has an upper limit set in this paper. The combinations are split by the charm value.

Hadron 1	Hadron 2	Charge	I_3	Y	C	Limit set
Λ_c^+	$\bar{D}^0$	+1	1/2	1	0	✓
Λ_c^+	D^-	0	-1/2	1	0	✓
Λ_c^+	D^{*-}	0	-1/2	1	0	✓
Σ_c^{++}	$\bar{D}^0$	+2	3/2	1	0	✓
Σ_c^{++}	D^-	+1	1/2	1	0	✓
Σ_c^{++}	D^{*-}	+1	1/2	1	0	×
Σ_c^0	$\bar{D}^0$	0	-1/2	1	0	✓
Σ_c^0	D^-	-1	-3/2	1	0	✓
Σ_c^0	D^{*-}	-1	-3/2	1	0	×
Σ_c^{*++}	$\bar{D}^0$	+2	3/2	1	0	✓
Σ_c^{*++}	D^-	+1	1/2	1	0	✓
Σ_c^{*++}	D^{*-}	+1	1/2	1	0	✓
Σ_c^{*0}	$\bar{D}^0$	0	-1/2	1	0	✓
Σ_c^{*0}	D^-	-1	-3/2	1	0	✓
Σ_c^{*0}	D^{*-}	-1	-3/2	1	0	✓
Λ_c^+	D^0	+1	-1/2	3	2	✓
Λ_c^+	D^+	+2	1/2	3	2	✓
Λ_c^+	D^{*+}	+2	1/2	3	2	✓
Σ_c^{++}	D^0	+2	1/2	3	2	×
Σ_c^{++}	D^+	+3	3/2	3	2	×
Σ_c^{++}	D^{*+}	+3	3/2	3	2	×
Σ_c^0	D^0	0	-3/2	3	2	×
Σ_c^0	D^+	+1	-1/2	3	2	×
Σ_c^0	D^{*+}	+1	-1/2	3	2	×
Σ_c^{*++}	D^0	+2	1/2	3	2	✓
Σ_c^{*++}	D^+	+3	3/2	3	2	✓
Σ_c^{*++}	D^{*+}	+3	3/2	3	2	×
Σ_c^{*0}	D^0	0	-3/2	3	2	✓
Σ_c^{*0}	D^+	+1	-1/2	3	2	✓
Σ_c^{*0}	D^{*+}	+1	-1/2	3	2	×

combination ($c\bar{c}uud$), since all combinations consist of only the up, down and charm quarks. In the selection process, open-charm hadrons are selected by the trigger. The Λ_c^+ baryon is reconstructed in the $\Lambda_c^+ \rightarrow pK^-\pi^+$ decay mode for both signal and normalization channels, the D^0 meson in the decay $D^0 \rightarrow K^-\pi^+$ and the D^+ meson in the decay $D^+ \rightarrow K^-\pi^+\pi^+$. To improve the signal purity, stringent PID and vertex quality requirements are imposed. To further suppress the background in the Λ_c^+ decay mode, the gradient-boosted decision tree classifier trained on data for the analysis described in Ref. [35] is used. This identifies Λ_c^+ candidates with high efficiency by combining information on the vertex quality and the PID. The classifier is applied directly in the case of the modes

involving a direct Λ_c^+ decay and is used as an input to the multivariate algorithm that is used to select Σ_c candidates in the $\Sigma_c \rightarrow \Lambda_c^+ \pi^\pm$ decay mode. In Fig. 1 the invariant mass distribution for each of these open-charm hadrons is shown. Candidate D^* (Σ_c) hadrons are built by combining the D^0 (Λ_c^+) candidates with a well-identified charged pion with p_T above 200 MeV/ c .

To improve the purity of the Σ_c selection, a multilayer perceptron algorithm provided by the TMVA package [36] is trained using the $\Sigma_c^{*++} \rightarrow \Lambda_c^+ \pi^+$ simulated signal sample and a data sample at high mass, well above the expected signal, in order to describe the shape of the combinatoric background events. As input, the network uses the p_T and

rapidity of the pion and of the Σ_c^{*++} and Λ_c^+ baryons, together with information on the pion PID and the Λ_c^+ classifier response described above.

Once the corresponding baryon and meson combinations have been built, the signal regions are selected. These regions are based on fits to the baryon and meson spectra and require the mass is within a 3σ window around the mean mass value found from the fits, where σ is the resolution of the signal peak. These regions are dependent on the baryon and meson combination the signal mode consists of. The chosen windows are highlighted in Fig. 1. The background regions are selected as a wider window around the fitted mean value to accurately describe the background as close to the signal

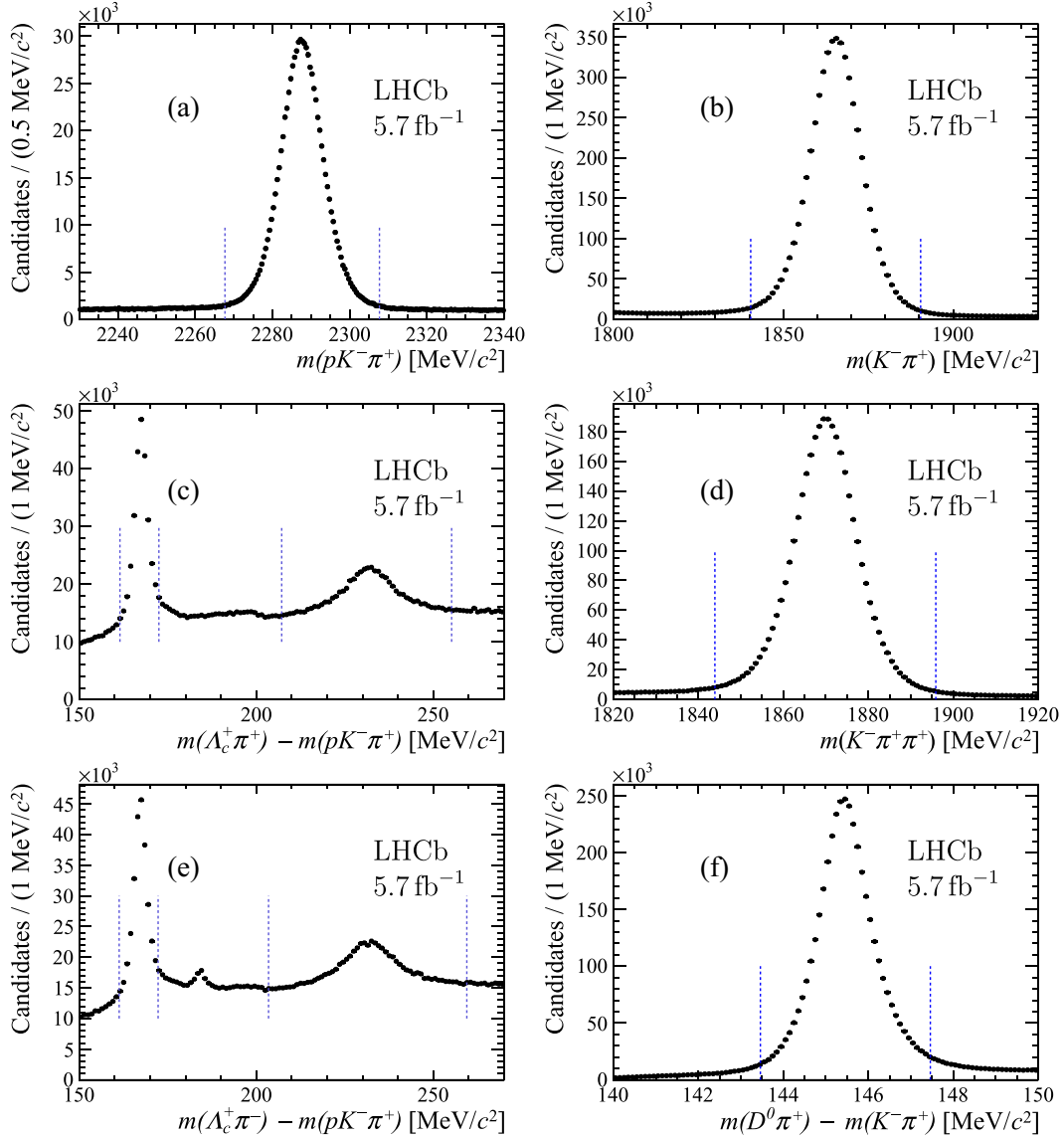


FIG. 1. Invariant mass distributions of the (a) $\Lambda_c^+ \rightarrow p K^- \pi^+$, (b) $D^0 \rightarrow K^- \pi^+$, (c) $\Sigma_c^{*++} \rightarrow \Lambda_c^+ \pi^+$, (d) $D^+ \rightarrow K^- \pi^+ \pi^+$, (e) $\Sigma_c^{*0} \rightarrow \Lambda_c^+ \pi^-$ and (f) $D^{*+} \rightarrow D^0 \pi^+$ decays. Note that in (c), (e) and (f) the mass of the charm hadron is subtracted from the mass distribution to minimize detector resolution effects. In (e) a contribution can also be seen at around 185 MeV/c² from the fully reconstructed $\Xi_c^0 \rightarrow \Lambda_c^+ \pi^-$ decay. The blue dashed lines show the chosen signal windows around the peaks.

region as possible. This corresponds to a $3\text{--}4.5\sigma$ window around the fitted mean value of the mass. Selection criteria are applied on the opening angle between each pair of charged particles to ensure there are no candidates where the same track is used multiple times. If two or more candidates are selected, all but one candidate is discarded at random. Any signal combinations with fewer than 30 candidates within the mass range of interest are not analyzed further. This corresponds to ten modes in total, as summarized in Table I. Note that all $\Lambda_c^+ D \pi$ combinations exceed this threshold.

IV. LIMIT SETTING PROCEDURE

For each mode, a kinematic fit is done to constrain the mass of intermediate charm hadrons to their known values and to constrain them to originate at the same PV. The Q -value spectrum, where the mass of each charmed hadron from the kinematic fit is subtracted from the decaying particle, is fitted using a simultaneous extended unbinned maximum-likelihood fit to the background and signal regions, where the background shape is shared between the two. The background normalization region is a combination of the upper and lower sideband regions and for the $\Sigma_c D$ and $\Sigma_c^* D$ modes is selected from the Σ_c sideband region. For the $\Lambda_c^+ \pi D$ and $\Lambda_c^+ D$ modes the background region used is from the Λ_c^+ sideband region. For the $\Sigma_c D$, $\Sigma_c^* D$ and $\Lambda_c^+ \pi D$ modes, the background model used is a threshold function with all parameters shared between signal and sideband regions, while for the $\Lambda_c^+ D D$ modes, the background model is the sum of a first-order Chebyshev polynomial and a log-normal distribution with all parameters shared between signal and sideband regions apart from the fraction between the two functions, which is independent. An example of the fit in the background-only hypothesis for each signal mode category ($\Sigma_c D$, $\Sigma_c^* D$, $\Lambda_c^+ D$ and $\Lambda_c^+ \pi D$) and the corresponding background is shown in Fig. 2. Four different signal models are investigated: one using a Gaussian function, where the resolution is fixed to the detector resolution found using simulation, and three using Voigtian functions, built from the convolution of the same Gaussian function with a Breit-Wigner distribution, with fixed widths of 5, 10 and 15 MeV/ c^2 , in order to provide greater sensitivity to pentaquark states with broader width. Larger widths are not considered, since the pentaquark states are predicted to be narrow [15].

The invariant mass distribution of $\Lambda_c^+ \rightarrow p K^- \pi^+$ candidates (the normalization channel) is shown in Fig. 3. The distribution is fitted using the sum of a Gaussian function with a Crystal Ball function [37] for the signal model and a first-order Chebyshev polynomial for the background. The obtained signal yield is $789\,200 \pm 1300$.

To search for possible pentaquark contributions, a scan of the Q -value distribution in each signal mode is made from the kinematic threshold up to 600 MeV/ c^2 in steps of 4 MeV/ c^2 , which corresponds roughly to the signal resolution. At each point, an extended unbinned

maximum-likelihood fit is performed. The local p value is determined from the difference between the negative log-likelihood of each fit and a fit with the background-only hypothesis and is assumed to be a one-tailed distribution. An example of the p -value distribution across the scan range is shown for each signal category for the $\Lambda_c^+ \pi^- \bar{D}^0$ mode in Fig. 4. The minimum local p value in each channel varies from 0.041 in the $\Sigma_c^{*++} D^{*-}$ channel with the Voigtian signal model with a 15 MeV/ c^2 width, to 3.36×10^{-6} in the $\Lambda_c^+ \pi^+ D^-$ channel with the Voigtian signal model with a 15 MeV/ c^2 width. The latter corresponds to a local significance of 4.50σ .

The local p value is corrected in order to account for the look-elsewhere effect [38] (LEE) using

$$p_{\text{corr}} = p_{\text{loc}} + \langle N(c_0) \rangle \exp\left(-\frac{c - c_0}{2}\right), \quad (1)$$

where p_{corr} and p_{loc} are the corrected and local p value, respectively, c is the profile likelihood ratio $2\Delta \ln \mathcal{L}$, and c_0 is a reference level set to 0.5 where the average number of “upcrossings” $\langle N(c_0) \rangle$ is found. An upcrossing is defined as when the profile likelihood ratio crosses the chosen threshold with a positive slope. The corrected p value varies from 1 (corresponding to no observation of any significant signal) in many channels, to 1.45×10^{-4} in the $\Lambda_c^+ \pi^+ D^-$ channel with the Voigtian signal model where the width is set to 15 MeV/ c^2 . To evaluate the interpretation of these p values the scanning procedure is repeated using 1000 background-only pseudoexperiments for each channel and the Voigtian signal model with a width of 15 MeV/ c^2 . The average number of fluctuations above 3σ significance across all channels is 7.0 with a standard deviation of 5.0. In the data, five channels, namely the $\Lambda_c^+ \pi^+ \bar{D}^0$, $\Lambda_c^+ \pi^+ D^-$, $\Lambda_c^+ \pi^- \bar{D}^0$, $\Lambda_c^+ \pi^- D^-$ and $\Lambda_c^+ \pi^- D^+$ channels, are observed with local significances greater than 3σ , obtained with the Voigtian signal model with a width of 15 MeV/ c^2 . Thus, we conclude that these significances are consistent with background fluctuations, as determined in the study with pseudoexperiments.

The previously observed pentaquark states are also investigated, namely the $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$ states. This is only carried out for states with the same total charge and hidden-charm quark content. By setting the mass and width in the Voigtian function to the known values of these states [11] and carrying out the same fitting procedure previously described, the significance of the states is found, and the limits are set using the procedure described below.

In this study, several sources of systematic uncertainties are considered. Since the number of tracks is different for signal and normalization, an important source of systematic uncertainty is due to the knowledge of the tracking efficiency, which is affected by hadronic interactions in the detector and overlaps between tracks or occupancy.

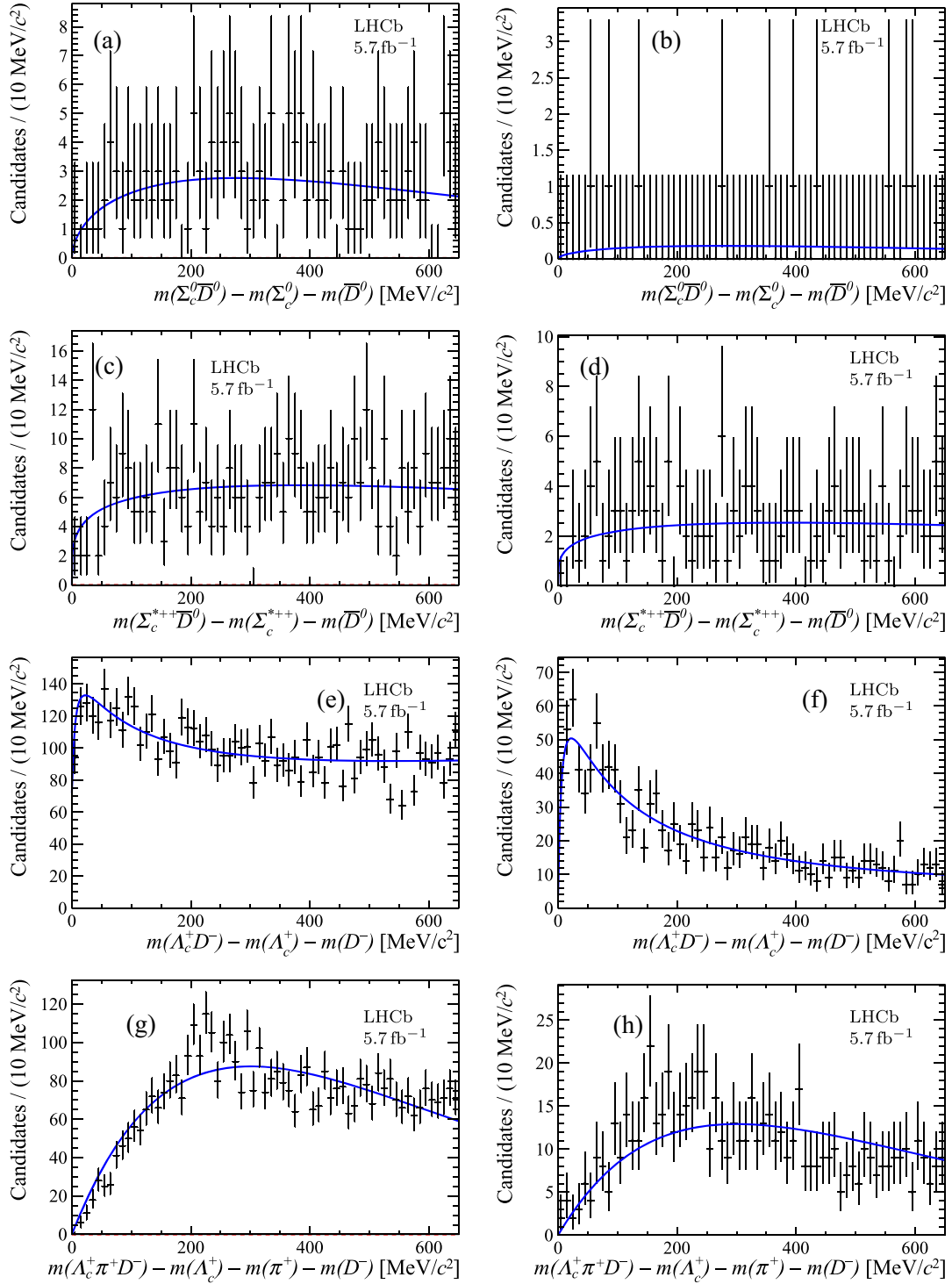


FIG. 2. Distributions of the Q -value spectra for the $\Sigma_c^0 \bar{D}^0$ (a) signal and (b) background regions, for the $\Sigma_c^{*++} \bar{D}^0$ (c) signal and (d) background regions, the $\Lambda_c^+ D^-$ (e) signal and (f) background regions and the $\Lambda_c^+ \pi^+ D^-$ (g) signal and (h) background regions. The fits for the background-only hypotheses are overlaid.

Further uncertainties arise and are quantified from possible differences in the reconstruction between data and simulation, such as differences in selection and PID efficiencies. The performance of the classifier for the Σ_c baryon and the

behavior of the trigger in data and simulation are also considered as sources of uncertainty. The knowledge of the branching fractions of the decay modes used leads to a further uncertainty [39]. The effect of varying the

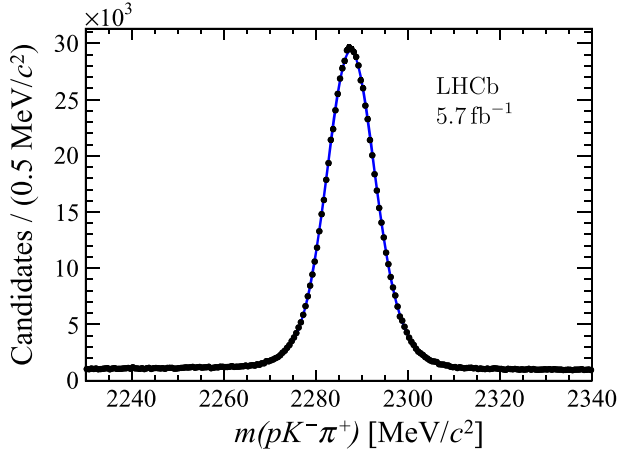


FIG. 3. Invariant mass distribution of the $\Lambda_c^+ \rightarrow p K^- \pi^+$ decay. The fit results are overlaid.

background model on the signal yield is also investigated, e.g., by using either a threshold function or Chebyshev polynomial summed with a log-normal distribution or by varying which background parameters are shared between the signal and background regions. This is done for the combination with the highest signal yield, and the uncertainty is applied for all signal combinations. The range of values found for each contribution is summarized in Table II.

An upper limit (UL) is set on $R(\Lambda_c^+)$, which is defined as

$$R(\Lambda_c^+) = \frac{N_P}{N_{\Lambda_c^+}} \times \frac{\epsilon_{\Lambda_c^+}}{\epsilon_P}, \quad (2)$$

where N represents the Λ_c^+ or pentaquark (P) yield and ϵ is the combined trigger and selection efficiency as found

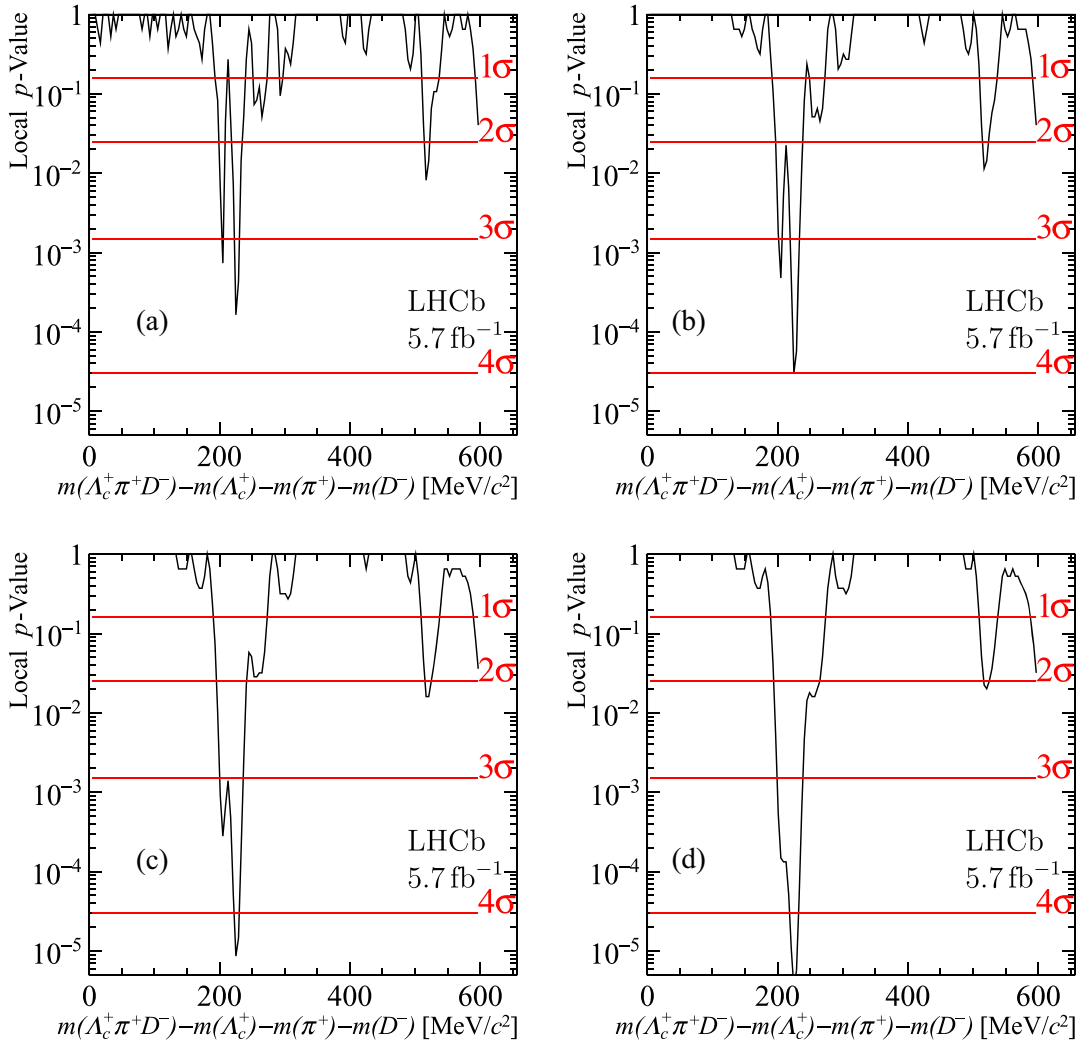


FIG. 4. Local p -value distributions for the $\Lambda_c^+ \pi^+ D^-$ mode with different signal models: (a) Gaussian function, (b) Voigtian function with 5 MeV/c^2 width, (c) Voigtian function with 10 MeV/c^2 width, and (d) Voigtian function with 15 MeV/c^2 width. The red lines correspond to the levels of local significance.

TABLE II. Range of values of each systematic uncertainty contribution and the total combination for the different signal modes.

Source	Uncertainty (%)
Tracking	3.00–6.20
Reconstruction efficiency	0.70–3.70
Generation efficiency	0.10–0.20
Σ_c classifier performance	0.54
L0 trigger efficiency	1.40–7.90
Branching fraction	0.01–0.03
Background model	11.6
Total	12.10–15.79

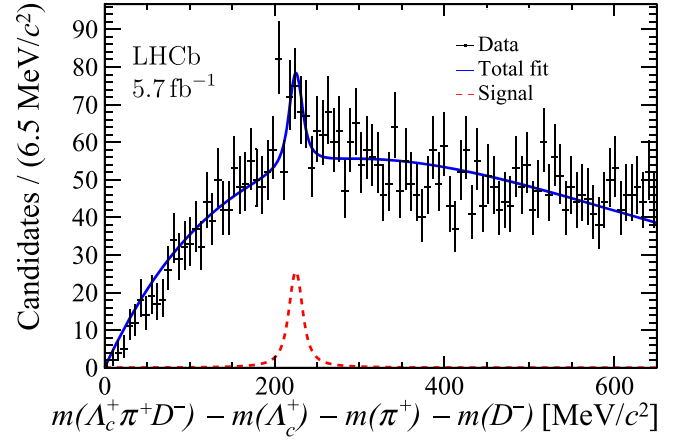


FIG. 6. Distribution of the Q value in the $\Lambda_c^+ \pi^+ D^-$ channel, where the most significant signal is seen. The fit result is overlaid.

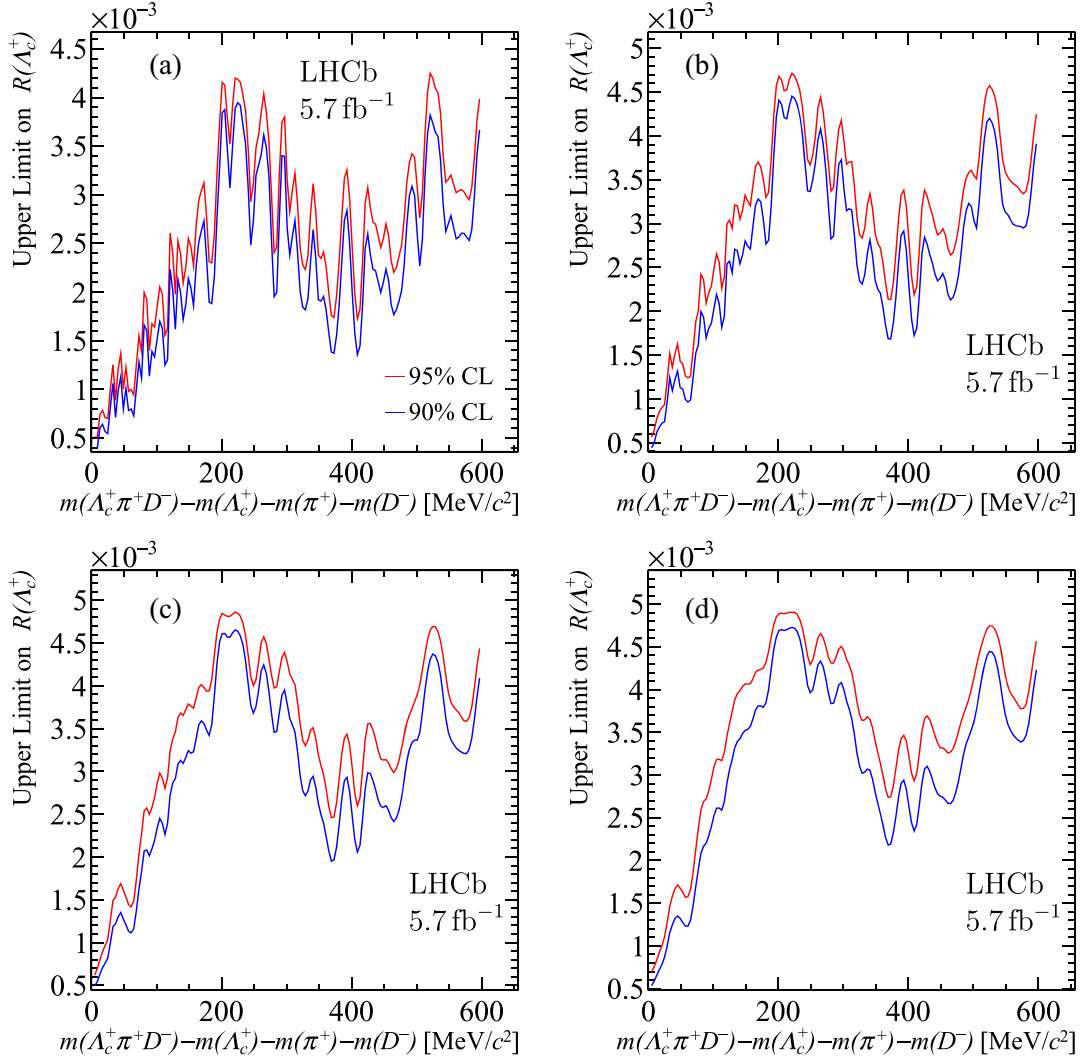


FIG. 5. Upper limits on $R(\Lambda_c^+)$ distribution, at 90% and 95% CL, for the $\Lambda_c^+ \pi^+ D^-$ mode with different signal models: (a) Gaussian function, (b) Voigtian function with 5 MeV/c^2 width, (c) Voigtian function with 10 MeV/c^2 width, and (d) Voigtian function with 15 MeV/c^2 width.

TABLE III. Upper limits on $R(\Lambda_c^+)$ at 90% and 95% CL for the modes with the same total charge as the known pentaquark states and with hidden-charm quark content. The local p value and significance are listed as well as the signal yield, where the error on the signal yield is statistical only.

Decay mode	Pentaquark hypothesis	p value	Significance (σ)	Signal yield	Upper limit ($\times 10^{-3}$)	
					(90% CL)	(95% CL)
$\Lambda_c^+ \bar{D}^0$	$P_c(4312)^+$	0.32	0.48	19.78 ± 22.27	1.17	1.29
	$P_c(4440)^+$	0.44	0.15	26.91 ± 28.17	1.41	1.53
	$P_c(4457)^+$	0.53	0.00	6.20 ± 13.60	1.27	1.43
$\Lambda_c^+ \pi^+ D^{*-}$	$P_c(4440)^+$	1.00	0.00	0.00 ± 0.96	0.72	0.91
	$P_c(4457)^+$	1.00	0.00	0.00 ± 1.73	0.77	0.97
$\Lambda_c^+ \pi^- D^{*-}$	$P_c(4440)^+$	1.00	0.00	0.00 ± 0.80	0.63	0.80
	$P_c(4457)^+$	1.00	0.00	0.00 ± 0.74	0.59	0.74
$\Lambda_c^+ \pi^+ D^-$	$P_c(4312)^+$	1.00	0.00	0.00 ± 1.56	0.69	0.88
	$P_c(4440)^+$	0.65	0.00	4.43 ± 11.67	3.71	4.24
	$P_c(4457)^+$	0.65	0.00	5.94 ± 12.68	3.13	3.61
$\Lambda_c^+ \pi^- D^-$	$P_c(4312)^+$	1.00	0.00	0.00 ± 1.42	0.67	0.86
	$P_c(4440)^+$	0.53	0.00	12.52 ± 15.89	3.91	4.37
	$P_c(4457)^+$	0.53	0.00	8.60 ± 12.22	3.10	3.51
$\Sigma_c^0 D^-$	$P_c(4440)^+$	1.00	0.00	0.00 ± 2.47	0.82	1.03
	$P_c(4457)^+$	1.00	0.00	0.00 ± 1.05	0.63	0.81
$\Sigma_c^{++} D^-$	$P_c(4440)^+$	0.80	0.00	0.61 ± 4.52	1.13	1.37
	$P_c(4457)^+$	0.59	0.00	0.66 ± 1.79	0.80	0.99
$\Sigma_c^{*0} D^-$	$P_c(4440)^+$	0.31	0.49	3.23 ± 3.53	1.89	2.24
	$P_c(4457)^+$	1.00	0.00	0.00 ± 3.09	0.91	1.13
$\Sigma_c^{*++} D^-$	$P_c(4440)^+$	0.75	0.00	1.20 ± 3.81	1.38	1.67
	$P_c(4457)^+$	1.00	0.00	0.00 ± 5.74	0.87	1.08

using simulated events. The limit is then determined at 90% and 95% confidence levels (CL). The likelihood profile is assumed to be parabolic and is determined for five equal-sized steps in the signal yield around the value found from the fit. It is then convolved with a Gaussian function with a mean of zero and a width set to $\sigma = \sigma_{\text{syst}} \cdot \mu$, where σ_{syst} is the systematic uncertainty on the signal yield and μ is the most probable signal yield. The convolved function takes the form

$$L(N') = \int_0^\infty L(N) \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(N - N')^2}{2\sigma^2}\right) dN, \quad (3)$$

where $L(N)$ is the normalized likelihood function. This likelihood profile is numerically integrated to find the value of the integral at 90% or 95% of the physical region, corresponding to the 90% and 95% CL upper limits on the signal yield, and is then converted to an upper limit on $R(\Lambda_c^+)$ using Eq. (2). An example of the upper limit for each signal category is shown for the $\Lambda_c^+ \pi^- \bar{D}^0$ mode in Fig. 5.

The results for the scan across the Q -value spectrum in each signal combination are summarized in the Appendix.

All channels show a signal yield consistent with the background-only hypothesis. The most significant deviation is seen in the $\Lambda_c^+ \pi^+ D^-$ channel. The fit result for this channel is shown in Fig. 6. When fitting with the mass and width of the known pentaquark states, the local significance in these spectra is found to be close to (or equal to) zero in all cases and is summarized in Table III.

V. CONCLUSION

Using an integrated luminosity of 5.7 fb^{-1} of pp collision data collected by the LHCb detector, a large range of combinations of open-charm and hidden-charm hadronic states are investigated for possible pentaquark decay channels. A signal model based on the known pentaquark states is also fitted, and the signal yield is found to be consistent with zero in all cases. When scanning the Q -value distribution from threshold to $600 \text{ MeV}/c^2$, the upper limit on the yield relative to the normalization channel is set at 90% and 95% confidence levels. The highest significance is seen in the $\Lambda_c^+ \pi^+ D^-$ final state; however, using studies of background-only pseudoexperiments this is found to be consistent with the background-only hypothesis.

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APPENDIX: SUMMARY TABLES

Tables IV–VI summarize the upper limits set for each signal channel, along with the signal yields with corresponding significances, as well as the Q value that these values occur at.

TABLE IV. Upper limits on $R(\Lambda_c^+)$ at 90% and 95% CL are shown for 11 of the hidden-charm modes, for their lowest p value and highest significance (both local and corrected for LEE) found in the mass scan for all signal models. The Q value and signal yield for these points are also summarized, where the error on the signal yield is statistical only. The Q value can be converted to the absolute mass by adding the masses of each decay product in the respective combination.

Decay mode	Width (MeV/ c^2)	Lowest p value		Significance (σ)		Q value (MeV/ c^2)	Signal yield	UL ($\times 10^{-3}$)	
		Local	Corrected	Local	Corrected			90% CL	95% CL
$\Lambda_c^+ \bar{D}^0$	0	4.7×10^{-3}	0.36	2.60	0.36	353	22.7 ± 30.6	1.41	1.54
	5	3.4×10^{-3}	0.20	2.71	0.86	353	31.4 ± 12.8	1.53	1.64
	10	2.7×10^{-3}	0.13	2.78	1.15	349	39.4 ± 34.8	1.54	1.65
	15	2.2×10^{-3}	0.09	2.85	1.36	349	46.8 ± 91.0	1.57	1.67
$\Lambda_c^+ D^-$	0	4.7×10^{-3}	0.38	2.60	0.31	501	24.0 ± 12.9	2.05	2.25
	5	3.7×10^{-3}	0.22	2.67	0.77	497	26.7 ± 22.2	2.09	2.27
	10	2.7×10^{-3}	0.13	2.78	1.15	497	33.1 ± 23.0	2.17	2.35
	15	3×10^{-3}	0.11	2.75	1.21	497	38.0 ± 25.5	2.23	2.39
$\Lambda_c^+ D^{*-}$	0	1.4×10^{-3}	0.12	2.99	1.17	417	17.5 ± 6.9	2.48	2.72
	5	2.2×10^{-3}	0.13	2.85	1.13	417	20.8 ± 9.3	2.74	2.94
	10	3×10^{-3}	0.13	2.75	1.11	421	23.8 ± 9.6	2.80	2.96
	15	4.7×10^{-3}	0.16	2.60	0.99	421	26.3 ± 10.8	2.85	3.00
$\Sigma_c^{++} \bar{D}^0$	0	1.2×10^{-3}	0.10	3.04	1.27	301	7.0 ± 3.2	1.10	1.22
	5	4.3×10^{-3}	0.23	2.63	0.73	301	7.7 ± 3.6	1.23	1.37
	10	1.4×10^{-2}	0.48	2.21	0.04	301	7.9 ± 4.1	1.32	1.49
	15	3.2×10^{-2}	0.81	1.85	0.00	301	7.9 ± 4.5	1.40	1.59
$\Lambda_c^+ \pi^+ \bar{D}^0$	0	7.4×10^{-4}	0.06	3.18	1.58	245	41.9 ± 13.7	2.87	3.06
	5	9.69×10^{-5}	5.76×10^{-3}	3.73	2.53	245	67.6 ± 19.2	3.22	3.35
	10	2.46×10^{-5}	1.12×10^{-3}	4.06	3.06	245	91.6 ± 24.1	3.29	3.39
	15	8.61×10^{-6}	3.11×10^{-4}	4.30	3.42	245	115.0 ± 28.5	3.30	3.40
$\Sigma_c^{++} D^-$	0	5.2×10^{-3}	0.41	2.56	0.24	181	3.9 ± 2.3	1.07	1.21
	5	4.1×10^{-3}	0.22	2.65	0.76	177	6.8 ± 3.3	1.46	1.63
	10	3.7×10^{-3}	0.15	2.68	1.02	177	7.9 ± 3.7	1.64	1.84
	15	4.7×10^{-3}	0.15	2.60	1.03	177	8.4 ± 4.0	1.76	1.98
$\Lambda_c^+ \pi^+ D^-$	0	1.6×10^{-4}	0.01	3.59	2.21	225	41.6 ± 12.6	3.95	4.19
	5	3.03×10^{-5}	1.96×10^{-3}	4.01	2.89	225	64.7 ± 17.4	4.43	4.69
	10	8.61×10^{-6}	4.44×10^{-4}	4.30	3.32	225	87.1 ± 21.6	4.64	4.85
	15	3.36×10^{-6}	1.45×10^{-4}	4.50	3.62	225	108.2 ± 25.3	4.72	4.90
$\Lambda_c^+ \pi^+ D^{*-}$	0	2.7×10^{-3}	0.20	2.78	0.86	213	12.8 ± 5.3	3.42	3.75
	5	4.5×10^{-4}	0.02	3.32	1.96	213	22.3 ± 7.8	4.52	4.76
	10	1.45×10^{-4}	6.29×10^{-3}	3.62	2.50	213	30.4 ± 9.7	4.75	4.93
	15	7.42×10^{-5}	2.60×10^{-3}	3.79	2.79	209	37.7 ± 11.4	4.85	5.02
$\Sigma_c^0 \bar{D}^0$	0	1.3×10^{-2}	0.95	2.22	0.00	65	2.9 ± 2.0	0.68	0.78
	5	1.7×10^{-2}	0.79	2.13	0.00	65	3.7 ± 68.8	0.90	1.03
	10	2.2×10^{-2}	0.74	2.02	0.00	65	4.4 ± 4.3	1.02	1.18
	15	2.8×10^{-2}	0.74	1.90	0.00	65	4.8 ± 4.2	1.13	1.29
$\Lambda_c^+ \pi^- \bar{D}^0$	0	4.8×10^{-4}	0.04	3.30	1.72	597	54.0 ± 17.2	2.79	2.98
	5	9.65×10^{-5}	7.11×10^{-3}	3.73	2.45	597	78.8 ± 21.9	3.02	3.20
	10	2.71×10^{-5}	1.63×10^{-3}	4.04	2.94	597	104.0 ± 26.3	3.15	3.30
	15	9.50×10^{-6}	4.83×10^{-4}	4.28	3.30	597	128.5 ± 30.4	3.20	3.33
$\Sigma_c^0 D^-$	0	2.3×10^{-3}	0.19	2.84	0.88	261	4.4 ± 2.7	1.24	1.39
	5	3.4×10^{-3}	0.18	2.71	0.90	261	5.7 ± 3.0	1.50	1.69
	10	6×10^{-3}	0.23	2.51	0.74	261	6.4 ± 3.4	1.66	1.87
	15	1×10^{-2}	0.30	2.32	0.53	261	7.0 ± 3.8	1.78	2.03

TABLE V. Upper limits on $R(\Lambda_c^+)$ at 90% and 95% CL are shown for eight of the hidden-charm modes, for their lowest p value and highest significance (both local and corrected for LEE) found in the mass scan for all signal models. The Q value and signal yield for these points are also summarized, where the error on the signal yield is statistical only. The Q value can be converted to the absolute mass by adding the masses of each decay product in the respective combination.

Decay mode	Width (MeV)	Lowest p value		Significance (σ)		Q value (MeV/ c^2)	Signal yield	UL ($\times 10^{-3}$)	
		Local	Corrected	Local	Corrected			90% CL	95% CL
$\Lambda_c^+ \pi^- D^-$	0	3.9×10^{-4}	0.03	3.36	1.90	257	38.1 ± 12.4	4.28	4.56
	5	5.71×10^{-5}	3.33×10^{-3}	3.86	2.71	253	62.1 ± 17.1	4.62	4.83
	10	1.45×10^{-5}	6.92×10^{-4}	4.18	3.20	249	83.7 ± 21.2	4.72	4.88
	15	4.59×10^{-6}	1.83×10^{-4}	4.44	3.56	249	103.5 ± 24.6	4.77	4.92
$\Lambda_c^+ \pi^- D^{*-}$	0	4.4×10^{-3}	0.31	2.62	0.48	197	12.0 ± 5.3	3.11	3.45
	5	7.1×10^{-3}	0.31	2.45	0.51	197	16.8 ± 7.3	4.08	4.53
	10	8.6×10^{-3}	0.27	2.38	0.61	197	21.2 ± 9.1	4.69	5.15
	15	8.9×10^{-3}	0.22	2.37	0.78	197	25.5 ± 10.8	5.11	5.56
$\Sigma_c^{*++} \bar{D}^0$	0	1×10^{-2}	0.75	2.32	0.00	37	5.0 ± 2.8	0.96	1.09
	5	1.2×10^{-2}	0.62	2.24	0.00	37	7.8 ± 4.0	1.32	1.49
	10	2.7×10^{-2}	0.92	1.92	0.00	205	7.0 ± 20.6	1.57	1.78
	15	2.7×10^{-2}	0.73	1.92	0.00	485	12.5 ± 6.7	2.23	2.49
$\Sigma_c^{*++} D^-$	0	1.2×10^{-3}	0.11	3.03	1.21	537	6.5 ± 3.3	1.63	1.82
	5	1.6×10^{-3}	0.10	2.95	1.30	497	11.8 ± 5.0	2.52	2.79
	10	2.5×10^{-3}	0.11	2.81	1.24	497	13.0 ± 5.7	2.82	3.12
	15	4.3×10^{-3}	0.14	2.63	1.07	497	13.9 ± 6.3	3.02	3.37
$\Sigma_c^{*++} D^{*-}$	0	2.3×10^{-2}	1.40	2.00	0.00	193	2.5 ± 1.8	1.08	1.23
	5	3.5×10^{-2}	1.44	1.81	0.00	449	2.9 ± 2.1	1.26	1.45
	10	3.5×10^{-2}	1.08	1.81	0.00	453	3.2 ± 2.3	1.36	1.57
	15	4.1×10^{-2}	0.99	1.74	0.00	453	3.3 ± 2.4	1.45	1.66
$\Sigma_c^{*0} \bar{D}^0$	0	3.4×10^{-3}	0.27	2.71	0.63	341	11.4 ± 5.0	1.64	1.83
	5	2.6×10^{-3}	0.14	2.80	1.07	341	16.8 ± 6.8	2.29	2.56
	10	2.2×10^{-3}	0.09	2.84	1.31	341	21.3 ± 8.3	2.73	3.00
	15	1.8×10^{-3}	0.06	2.90	1.52	337	26.0 ± 9.6	3.02	3.27
$\Sigma_c^{*0} D^-$	0	7.2×10^{-3}	0.53	2.45	0.00	113	6.2 ± 3.2	1.44	1.62
	5	1.4×10^{-3}	0.08	2.99	1.40	537	11.5 ± 4.8	2.60	2.85
	10	1.1×10^{-3}	0.05	3.06	1.66	537	13.6 ± 5.4	2.99	3.27
	15	1.2×10^{-3}	0.04	3.02	1.70	537	15.1 ± 6.0	3.23	3.54
$\Sigma_c^{*0} D^{*-}$	0	9.9×10^{-3}	0.51	2.33	0.00	109	2.6 ± 1.7	0.96	1.11
	5	3.2×10^{-3}	0.16	2.73	0.99	17	2.8 ± 1.9	1.07	1.22
	10	4.1×10^{-3}	0.16	2.64	1.01	17	2.9 ± 2.1	1.13	1.30
	15	3.1×10^{-3}	0.17	2.51	0.94	17	3.0 ± 2.4	1.18	1.34

TABLE VI. Upper limits on $R(\Lambda_c^+)$ at 90% and 95% CL are shown for each doubly charmed mode, for their lowest p value and highest significance (both local and corrected for LEE) found in the mass scan for all signal models. The Q value and signal yield for these points are also summarized, where the error on the signal yield is statistical only. The Q value can be converted to the absolute mass by adding the masses of each decay product in the respective combination.

Decay mode	Width (MeV)	Lowest p value		Significance (σ)		Q value (MeV/ c^2)	Signal yield	UL ($\times 10^{-3}$)	
		Local	Corrected	Local	Corrected			90% CL	95% CL
$\Lambda_c^+ D^0$	0	8.2×10^{-3}	0.59	2.40	0.00	37	15.0 ± 7.3	0.97	1.06
	5	4.7×10^{-3}	0.26	2.60	0.64	153	26.8 ± 11.0	1.19	1.26
	10	2.7×10^{-3}	0.12	2.78	1.17	153	36.5 ± 14.0	1.27	1.35
	15	2.4×10^{-3}	0.09	2.82	1.34	153	45.0 ± 16.5	1.33	1.43
$\Lambda_c^+ D^+$	0	2×10^{-2}	1.43	2.05	0.00	133	9.4 ± 5.0	1.01	1.13
	5	4.7×10^{-3}	0.27	2.60	0.61	169	11.0 ± 9.9	1.25	1.41
	10	4.2×10^{-3}	0.18	2.64	0.90	169	13.5 ± 24.5	1.52	1.72
	15	5.8×10^{-3}	0.20	2.52	0.85	169	14.9 ± 7.6	1.71	1.92
$\Lambda_c^+ D^{*+}$	0	2.1×10^{-2}	1.25	2.04	0.00	29	3.5 ± 2.3	0.69	0.80
	5	1×10^{-2}	0.49	2.31	0.02	33	6.2 ± 4.2	1.15	1.32
	10	8.1×10^{-3}	0.31	2.41	0.51	33	8.8 ± 5.3	1.45	1.64
	15	7.1×10^{-3}	0.22	2.45	0.76	33	10.5 ± 6.2	1.66	1.88
$\Lambda_c^+ \pi^+ D^0$	0	2.7×10^{-3}	0.22	2.78	0.77	193	18.0 ± 7.2	2.02	2.19
	5	1.6×10^{-3}	0.09	2.95	1.32	193	28.0 ± 10.4	2.32	2.46
	10	1.4×10^{-3}	0.07	2.99	1.51	193	36.7 ± 12.9	2.46	2.62
	15	1.4×10^{-3}	0.05	2.99	1.61	197	44.8 ± 15.3	2.70	2.87
$\Lambda_c^+ \pi^+ D^+$	0	8.7×10^{-3}	0.49	2.38	0.03	225	12.2 ± 5.9	2.04	2.29
	5	2.5×10^{-3}	0.11	2.81	1.23	229	21.8 ± 8.5	3.05	3.32
	10	9.9×10^{-4}	0.03	3.09	1.81	229	29.1 ± 10.3	3.44	3.70
	15	5.9×10^{-4}	0.02	3.25	2.12	229	35.3 ± 11.9	3.70	3.96
$\Lambda_c^+ \pi^+ D^{*+}$	0	5.9×10^{-3}	0.39	2.52	0.28	77	1.9 ± 1.5	0.84	0.95
	5	4.5×10^{-3}	0.22	2.61	0.77	161	6.5 ± 3.6	1.81	2.04
	10	2.9×10^{-3}	0.11	2.76	1.23	161	9.2 ± 4.4	2.31	2.58
	15	1.5×10^{-3}	0.05	2.96	1.64	165	12.2 ± 5.1	2.80	3.10
$\Lambda_c^+ \pi^- D^0$	0	7.3×10^{-4}	0.06	3.18	1.53	593	20.3 ± 7.4	2.11	2.25
	5	6.6×10^{-4}	0.04	3.21	1.78	593	26.3 ± 9.3	2.26	2.38
	10	5.9×10^{-4}	0.03	3.24	1.95	593	32.3 ± 11.0	2.35	2.47
	15	4.8×10^{-4}	0.02	3.30	2.13	593	38.3 ± 12.5	2.42	2.54
$\Lambda_c^+ \pi^- D^+$	0	1.2×10^{-4}	0.01	3.67	2.32	153	21.4 ± 6.9	2.99	3.24
	5	2.07×10^{-5}	1.36×10^{-3}	4.10	3.00	153	33.3 ± 9.5	3.65	3.88
	10	9.44×10^{-6}	4.93×10^{-4}	4.28	3.29	153	43.1 ± 11.6	4.06	4.28
	15	5.96×10^{-6}	2.54×10^{-4}	4.38	3.48	153	51.7 ± 13.4	4.29	4.48
$\Lambda_c^+ \pi^- D^{*+}$	0	2.3×10^{-3}	0.17	2.84	0.97	73	3.2 ± 3.0	1.19	1.35
	5	6.8×10^{-4}	0.04	3.20	1.76	73	5.7 ± 3.3	1.71	1.92
	10	8.5×10^{-4}	0.04	3.14	1.79	73	7.0 ± 3.8	1.94	2.19
	15	1.3×10^{-3}	0.04	3.01	1.70	73	7.6 ± 4.2	2.10	2.36
$\Sigma_c^{*++} D^0$	0	1.2×10^{-2}	0.88	2.27	0.00	113	2.5 ± 1.8	0.63	0.72
	5	9.4×10^{-3}	0.50	2.35	0.00	113	3.2 ± 2.2	0.76	0.87
	10	1.3×10^{-2}	0.48	2.23	0.04	113	3.6 ± 2.4	0.87	1.00
	15	1.8×10^{-2}	0.52	2.11	0.00	113	3.9 ± 2.7	0.95	1.11
$\Sigma_c^{*++} D^+$	0	6×10^{-3}	0.48	2.51	0.05	133	1.9 ± 1.5	0.70	0.81
	5	6.8×10^{-3}	0.37	2.47	0.34	133	2.7 ± 1.9	0.89	1.02
	10	8.8×10^{-3}	0.34	2.37	0.41	133	3.0 ± 2.1	0.97	1.11
	15	1.2×10^{-2}	0.35	2.27	0.38	133	3.2 ± 2.2	1.03	1.18

(Table continued)

TABLE VI. (Continued)

Decay mode	Width (MeV)	Lowest p value		Significance (σ)		Q value (MeV/ c^2)	Signal yield	UL ($\times 10^{-3}$)	
		Local	Corrected	Local	Corrected			90% CL	95% CL
$\Sigma_c^{*0} D^0$	0	1.52×10^{-5}	1.67×10^{-3}	4.17	2.93	89	3.9 ± 2.0	0.68	0.76
	5	5.13×10^{-5}	3.70×10^{-3}	3.88	2.68	89	5.3 ± 2.6	0.90	0.99
	10	1.06×10^{-4}	5.47×10^{-3}	3.70	2.54	89	6.2 ± 3.0	1.03	1.14
	15	1.66×10^{-4}	6.69×10^{-3}	3.59	2.47	89	6.8 ± 3.2	1.13	1.25
$\Sigma_c^{*0} D^+$	0	1.8×10^{-2}	1.20	2.10	0.00	325	2.6 ± 1.8	0.88	1.01
	5	1.3×10^{-2}	0.61	2.23	0.00	73	3.5 ± 2.4	1.12	1.29
	10	1.3×10^{-2}	0.48	2.21	0.06	73	3.8 ± 3.2	1.29	1.50
	15	1.5×10^{-2}	0.41	2.18	0.22	69	4.7 ± 3.7	1.51	1.75

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