

Testing Dirac leptogenesis with the cosmic microwave background and proton decay

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The nature of neutrino masses and the matter–antimatter asymmetry of our universe are two of the most important open problems in particle physics today and are notoriously difficult to test with current technology. Dirac neutrinos offer a solution through a leptogenesis mechanism that hinges on the smallness of neutrino masses and resultant non-thermalization of the right-handed neutrino partners in the early universe. We thoroughly explore possible realizations of this Dirac leptogenesis idea, revealing new windows for highly efficient asymmetry generation. In many of them, the number of relativistic degrees of freedom, N_{eff} , is severely enhanced compared to standard cosmology and offers a novel handle to constrain Dirac leptogenesis with upcoming measurements of the cosmic microwave background. Realizations involving leptoquarks even allow for low-scale post-sphaleron baryogenesis and predict proton decay. These novel aspects render Dirac leptogenesis surprisingly testable.

I. INTRODUCTION

Neutrino oscillations have established neutrinos to be massive particles, albeit much lighter than all other fermions: $m_\nu \lesssim 0.8$ eV [1]. The Standard Model (SM) of particle physics needs to be extended by additional particles to accommodate non-zero m_ν , the simplest extension being three right-handed neutrinos ν_R that form massive Dirac particles together with the familiar ν_L . This is sufficient to explain all neutrino data and makes the mass generation for leptons analogous to that of quarks. The Higgs then couples to neutrinos with coupling strength $m_\nu/174$ GeV, too feeble to be detectable in experiments or even to ever thermalize the ν_R in the early universe [2–4], assuming a vanishing abundance after the Big Bang. Only an undetectably small ν_R abundance is created through the Higgs interactions [5, 6].

The tiny ν_R coupling and consequent non-thermalization was used to great effect in Ref. [7] for *Dirac leptogenesis*: Similar to standard leptogenesis [8, 9], a *lepton* asymmetry is created in the early universe through the decay of new heavy particles that is then converted to the observed *baryon* asymmetry by sphalerons [10]. Where standard leptogenesis creates the lepton asymmetry through explicit lepton number violation, Dirac leptogenesis creates two exactly opposite lepton asymmetries for left- and right-handed neutrinos. Since the latter are invisible to the sphalerons inside the SM plasma, only the left-handed asymmetry is converted into baryons. The asymmetry within the ν_R , and indeed the ν_R themselves, are seemingly impossible to observe.

In this article, we provide an exhaustive list of Dirac leptogenesis realizations and study their phenomenology. By solving the relevant Boltzmann equations we show that this mechanism is far more efficient than previously estimated. Furthermore, we show that large regions of

parameter space are surprisingly testable or already excluded by measurements of N_{eff} in cosmic microwave background (CMB) experiments, going far beyond earlier estimates [11, 12]. Realizations involving leptoquarks do not even require sphalerons and can thus work at low scales, unavoidably generating proton decay as a consequence.

The rest of this article is structured as follows: in Sec. II we describe the ingredients necessary for Dirac leptogenesis and describe the mechanism qualitatively. In Sec. III we study the simplest realization quantitatively to confirm the qualitative picture from before. Sec. IV is devoted to a discussion of qualitatively different Dirac-leptogenesis realizations that do not require sphalerons and simultaneously generate proton decay. We conclude in Sec. V. Some technical details and additional information have been relegated to the appendix: the details of our N_{eff} calculation can be found in App. A and the full derivation of our Boltzmann equations in App. B. App. C lists the relevant scattering cross sections for the model discussed in the main text. We illustrate some numerical solutions to the Boltzmann equations in App. D.

II. INGREDIENTS FOR DIRAC LEPTOGENESIS

For the simplest Dirac leptogenesis setup, we need several copies of a heavy new particle X that decays – typically before sphaleron freeze-out, but at least before Big Bang nucleosynthesis – into a non-thermalized ν_R plus an SM particle. Since ν_R is a spin-1/2 gauge singlet, X carries the same gauge quantum numbers as the SM particle but has a different spin. Borrowing language from supersymmetry, X is hence either a slepton, a squark, or a Higgsino. Consequently, any supersymmetric Dirac-neutrino model automatically provides the necessary ingredients for Dirac leptogenesis. The different quantum number assignments for X are listed in Tab. I; case b is the one originally discussed in Ref. [7]. The same models were identified in Ref. [13] as interesting additions to Majorana-neutrino leptogenesis. In all cases we can con-

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Case	$SU(3) \times SU(2) \times U(1)$	spin	g_X	$(B - L)(X)$	Relevant Lagrangian terms that induce X decay	$\varepsilon_{\text{wave}}$	$\varepsilon_{\text{vertex}}$	ΔB
<i>a</i>	$(\mathbf{1}, \mathbf{1}, -1)$	0	1	-2	$\nu_R e_R \bar{X}, LL \bar{X}$	✓	✗	0
<i>b</i>	$(\mathbf{1}, \mathbf{2}, 1/2)$	0	2	0	$\bar{H}X, \bar{\nu}_R LX, \bar{L}e_RX, \bar{Q}_L d_RX, \bar{u}_R Q_L X, X^\dagger H^\dagger HH$	✓	✓ or ✗	0
<i>c</i>	$(\mathbf{3}, \mathbf{1}, -1/3)$	0	3	-2/3	$d_R \nu_R X^\dagger, u_R e_R X^\dagger, Q_L LX^\dagger, u_R d_RX, Q_L Q_L X$	✓	✓ or ✗	0 or 1
<i>d</i>	$(\mathbf{3}, \mathbf{1}, 2/3)$	0	3	-2/3	$u_R \nu_R X^\dagger, d_R d_RX$	✓	✗	1
<i>e</i>	$(\mathbf{3}, \mathbf{2}, 1/6)$	0	6	4/3	$\bar{Q}_L \nu_R X, \bar{d}_R LX$	✓	✗	0
<i>f</i>	$(\mathbf{1}, \mathbf{2}, -1/2)$	1/2	2	-1	$\bar{X}L, \bar{\nu}_R XH, \bar{X}e_R H$	✓	✓	0

TABLE I: Quantum numbers for particle X whose decay gives Dirac leptogenesis. $\varepsilon_{\text{wave}}$ and $\varepsilon_{\text{vertex}}$ indicate one-loop contributions from wave-function and vertex renormalization. Case *c* and *d* can lead to $\Delta B = 1$ proton decay (last column).

sistently assign a conserved $B - L$ quantum number to X , which allows us to protect the Dirac nature of neutrinos by imposing $U(1)_{B-L}$ [14] or a subgroup [15] either globally or locally. X always has additional decay modes exclusively into SM particles besides the one into ν_R . These are crucial for Dirac leptogenesis because otherwise we would have an additional global $U(1)_{\nu_R}$ symmetry that would lead to CP conservation.

Assuming hierarchical X , a CP asymmetry ε in the decays of the lightest X will create a ν_R asymmetry

$$Y_{\Delta\nu_R} \equiv \frac{n_{\nu_R} - n_{\bar{\nu}_R}}{s} \Big|_{\text{today}} \equiv \varepsilon \eta \frac{n_X^{\text{eq}} + n_{\bar{X}}^{\text{eq}}}{s} \Big|_{T \gg M_X} \quad (1)$$

for every multiplet component of X , where $s \propto g_\star T^3$ is the entropy density and n_A the number density of A . The above corresponds to the standard definition of the efficiency factor η [16], which is however *not* restricted to $|\eta| \leq 1$ for Dirac leptogenesis, although we have $|\varepsilon\eta| \leq 1$.

Following the ν_R asymmetry generation through X decays, the ν_R will be out of contact with the SM plasma. Since $B - L$ is conserved in our Dirac-neutrino model, we have the asymmetry $Y_{\Delta(B-L_{\text{SM}})} = Y_{\Delta\nu_R}$ in the SM bath. There, sphalerons break $\Delta(B+L_{\text{SM}}) = 6$, converting the $B - L_{\text{SM}}$ asymmetry into a baryon asymmetry [10, 17]

$$Y_{\Delta B} = \frac{28}{79} Y_{\Delta(B-L_{\text{SM}})} = \frac{28}{79} Y_{\Delta\nu_R} \simeq 10^{-3} g_X \varepsilon \eta, \quad (2)$$

where in the last equation we have assumed only the SM degrees of freedom, $g_\star = 106.75$, as we will in all numerical examples. To obtain the measured baryon asymmetry [9, 18] we thus need $g_X \varepsilon \eta \sim 10^{-7}$. In cases *c* and *d*, X decays can *directly* produce a baryon asymmetry and can be effective *after* sphaleron freeze out; the factor 28/79 then needs to be dropped and no ΔL_{SM} is generated.

With CP asymmetry ε simply generated at one loop in all cases, the only quantity left to calculate is the efficiency η . From Tab. I it is clear that in addition to the desired decay channels, X unavoidably also has gauge interactions, which can quickly deplete the number of X at temperatures $T < M_X$. Naively, this makes it more complicated to generate the baryon asymmetry since it suppresses η . However, in analogy to scalar-triplet leptogenesis [19] there are ways to have very efficient leptogenesis as long as at least some of the inverse decay reactions are out of equilibrium, as already observed in [20].

Depending on the hierarchy of rates, different predictions for N_{eff} emerge:

- (I) If all decay rates of X are out of equilibrium, we have to rely on gauge interactions to produce X , assuming zero initial abundance. Once these scatterings freeze out, the remaining X eventually decay perfectly out of equilibrium at a temperature $T \ll M_X$. The ν_R created in this decay then have a large momentum compared to the SM temperature and thus a potentially large contribution to N_{eff} , reminiscent of the superWIMP mechanism [21], see App. A. This novel observation severely restricts this region of parameter space.
- (II) If the decay rates involving ν_R are in equilibrium but the other ones are not, a large η can be achieved in complete analogy to scalar-triplet leptogenesis. Here, the ν_R are thermalized at $T \sim M_X$, yielding
$$\Delta N_{\text{eff}} \simeq 0.14 (106.75/g_\star(M_X))^{4/3}, \quad (3)$$
an amount testable by CMB-S4 [22] unless $g_\star(M_X)$ far exceeds the SM amount [12]. This is the same contribution as in the $\Delta L = 4$ Dirac-leptogenesis mechanism of Ref. [23].
- (III) If the decay rates involving ν_R are out of equilibrium but the other ones are not, we have efficient asymmetry generation with only a small amount of ν_R generated through freeze-in with typical momenta $p \sim 2.5 T$ [24]. Here, ΔN_{eff} can be unobservably small since both abundance and momenta of ν_R are small. This *freeze-in* Dirac leptogenesis technically differs from the namesake setup of [25].

The above cases allow for large η . Moving away from these extreme cases lowers η and often pushes ΔN_{eff} closer to the thermal value of Eq. (3). The interactions and decays of the heavier X copies – required to exist for non-zero ε – will further increase ΔN_{eff} without contributing to the asymmetry. Even case (III) could therefore generate a testable ΔN_{eff} unless the ν_R couplings of *all* X are suppressed.

Below we quantify the above points for case *a* (cf. Tab. I), arguably the simplest version of Dirac leptogenesis. The other cases give qualitatively similar phenomenology, except for the leptoquark cases *c* and *d*, which are discussed in more detail toward the end.

III. A SIMPLE MODEL

As a simple model that realizes Dirac leptogenesis we introduce two electrically charged scalars $X_{1,2} \equiv X_{1,2}^-$ to the SM (case *a* from Tab. I), in addition to the three right-handed neutrinos necessary to form Dirac neutrinos. The Yukawa couplings of ν_R with the Higgs are minuscule and play no role in the following. The relevant interactions of the charged scalars are

$$\mathcal{L} = \frac{1}{2} \bar{L}^c F_i L \bar{X}_i + \bar{e}^c G_i \nu_R \bar{X}_i + \text{h.c.}, \quad (4)$$

assuming, without loss of generality, that the X_i are mass eigenstates. The matrices $F_{1,2}$ are antisymmetric in their flavor indices due to the antisymmetry of the $SU(2)$ singlet contraction $\bar{L}_\alpha^c L_\beta = \bar{e}_\alpha^c \nu_{L,\beta} - \bar{e}_\beta^c \nu_{L,\alpha}$. The G_i are arbitrary complex Yukawa matrices. Total lepton number is conserved by assigning $L(X_i) = 2$, but, more importantly, ν_R number is explicitly broken by the simultaneous presence of both Yukawas; this allows for the generation of a ν_R asymmetry in the X_i decays.¹

The tree-level decay rates of X_i are given by

$$\Gamma(X_i \rightarrow e_R \nu_R) \simeq \frac{M_i}{16\pi} \text{tr}(G_i G_i^\dagger), \quad (5)$$

$$\Gamma(X_i \rightarrow e_L \nu_L) \simeq \frac{M_i}{16\pi} \text{tr}(F_i F_i^\dagger), \quad (6)$$

summed over all final-state flavors. CPT invariance enforces $\Gamma(X_i) = \Gamma(\bar{X}_i) \equiv \Gamma_{X_i}$ and hence

$$\Gamma(X_i \rightarrow e_{R/L} \nu_{R/L}) = \Gamma_{X_i} (B_{R/L} \pm \varepsilon_i), \quad (7)$$

$$\Gamma(\bar{X}_i \rightarrow \bar{e}_{R/L} \bar{\nu}_{R/L}) = \Gamma_{X_i} (B_{R/L} \mp \varepsilon_i) \quad (8)$$

in the presence of a CP asymmetry

$$\varepsilon_i \equiv \frac{\Gamma(X_i \rightarrow e_R \nu_R) - \Gamma(\bar{X}_i \rightarrow \bar{e}_R \bar{\nu}_R)}{2\Gamma_{X_i}}, \quad (9)$$

where $B_L = 1 - B_R$ and $B_R \equiv \Gamma(X_i \rightarrow e_R \nu_R) / \Gamma_{X_i}$. This definition of ε_i as the average ν_R number per X_i decay immediately implies the absolute upper bound

$$|\varepsilon_i| \leq \min(B_L, B_R), \quad (10)$$

although realistic values for ε_i are far below this limit. This is in complete analogy to triplet-scalar leptogenesis [19]. At one loop, we find from the diagrams in Fig. 1:

$$\varepsilon_i \simeq \frac{\sum_j (M_j^2/M_i^2 - 1)^{-1} \Im [\text{tr}(F_j F_j^\dagger) \text{tr}(G_j G_j^\dagger)]}{8\pi [\text{tr}(G_i G_i^\dagger) + \text{tr}(F_i F_i^\dagger)]}. \quad (11)$$

Again: a non-vanishing CP asymmetry unavoidably requires both decay modes $X_i \rightarrow e_L \nu_L$ and $X_i \rightarrow e_R \nu_R$.

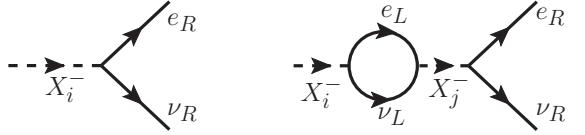


FIG. 1: Tree-level and one-loop wave-function diagram whose interference produces the CP-asymmetry ε_i of Eq. (11).

In the following we will assume a hierarchical X_i spectrum with $X_1 \equiv X$ being the lightest. Any asymmetry generated by the heavier $X_{i>1}$ is expected to be washed out by the interactions of X ; the contribution of the heavier scalars to the ν_R density and thus ΔN_{eff} on the other hand will only increase the final ΔN_{eff} . By neglecting these contributions here we are being conservative.

Provided all leptons except for ν_R are in thermal equilibrium, the Boltzmann equations (derived in App. B) for $\Sigma_A \equiv Y_A + Y_{\bar{A}}$ and $\Delta_A \equiv Y_A - Y_{\bar{A}}$ read

$$\frac{d\Sigma_X}{dy} = \frac{1}{2} \langle \sigma v \rangle_{X\bar{X}} \left(\Sigma_X^2 - \Sigma_X^{\text{eq}2} \right) + \frac{\langle \Gamma_X \rangle}{s} \left[\Sigma_X - \Sigma_X^{\text{eq}} \left(B_L + B_R \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right], \quad (12)$$

$$\frac{d\Sigma_{\nu_R}}{dy} = -\frac{\langle \Gamma_X \rangle}{s} B_R \left(\Sigma_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) + \frac{1}{2} \left(\langle \sigma v \rangle_s \Sigma_{e_R}^{\text{eq}} + \langle \sigma v \rangle_t \Sigma_L^{\text{eq}} \right) \left(\Sigma_{\nu_R} - \Sigma_{\nu_R}^{\text{eq}} \right), \quad (13)$$

$$\frac{d\Delta_X}{dy} = \frac{\langle \Gamma_X \rangle}{s} \left[\Delta_X - \Sigma_X^{\text{eq}} \left\{ B_R \frac{\Delta_{\nu_R} (\Sigma_{e_R}^{\text{eq}} + \Sigma_{\nu_R})}{\Sigma_{\nu_R}^{\text{eq}} \Sigma_{e_R}^{\text{eq}}} - B_L \frac{4(\Delta_X + \Delta_{\nu_R})}{\Sigma_L^{\text{eq}}} - \varepsilon \left(1 - \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right\} \right], \quad (14)$$

$$\frac{d\Delta_{\nu_R}}{dy} = \frac{\langle \Gamma_X \rangle}{s} \left[-\varepsilon \left(\Sigma_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) - B_R \left(\Delta_X - \Sigma_X^{\text{eq}} \frac{\Delta_{\nu_R} (\Sigma_{e_R}^{\text{eq}} + \Sigma_{\nu_R})}{\Sigma_{\nu_R}^{\text{eq}} \Sigma_{e_R}^{\text{eq}}} \right) + \frac{\langle \sigma v \rangle_s}{2} [\Delta_{\nu_R} (\Sigma_{e_R}^{\text{eq}} + \Sigma_{\nu_R}) + 2(\Delta_{\nu_R} + \Delta_X) \Sigma_{\nu_R}^{\text{eq}}] + \langle \sigma v \rangle_t [\Delta_{\nu_R} \Sigma_L^{\text{eq}} + (\Delta_{\nu_R} + \Delta_X) (\Sigma_{\nu_R} + \Sigma_{\nu_R}^{\text{eq}})] \right], \quad (15)$$

where $d/dy \equiv 3\mathcal{H}(ds/dx)^{-1}d/dx$, \mathcal{H} is the Hubble rate and $x \equiv M_X/T$. Neglecting the Yukawa interactions as well as couplings in the scalar potential, the relevant thermally averaged $X\bar{X}$ annihilation cross section $\langle \sigma v \rangle_{X\bar{X}}$ comes from the hypercharge coupling of X see e.g. Ref. [26]. The s - and t -channel X -mediated $|\Delta_{\nu_R}| = 1$ scatterings such as $e_L \nu_L \rightarrow e_R \nu_R$ are encoded in $\langle \sigma v \rangle_{s,t}$ and are typically suppressed compared to the (inverse) decays. Details can be found in App. C.

The above set of Boltzmann equations has already been simplified by setting the linear combinations $\Delta_{\nu_R} - \Delta_{e_R}$ and $\Delta_{\nu_R} + \Delta_{e_R} + \Delta_{\nu_L} + \Delta_{e_L} + 2\Delta_X$, which are conserved due to $U(1)_Y \times U(1)_L$, to zero, and by assuming all Δ to be suppressed by the small ε . We assume van-

¹ These couplings contribute at one-loop level to the Dirac-neutrino mass matrix, $\delta m_\nu \sim F m_\ell G^* v^2 / (16\pi^2 M_X^2)$, which is $\ll m_\nu$ in the region of interest without finetuning.

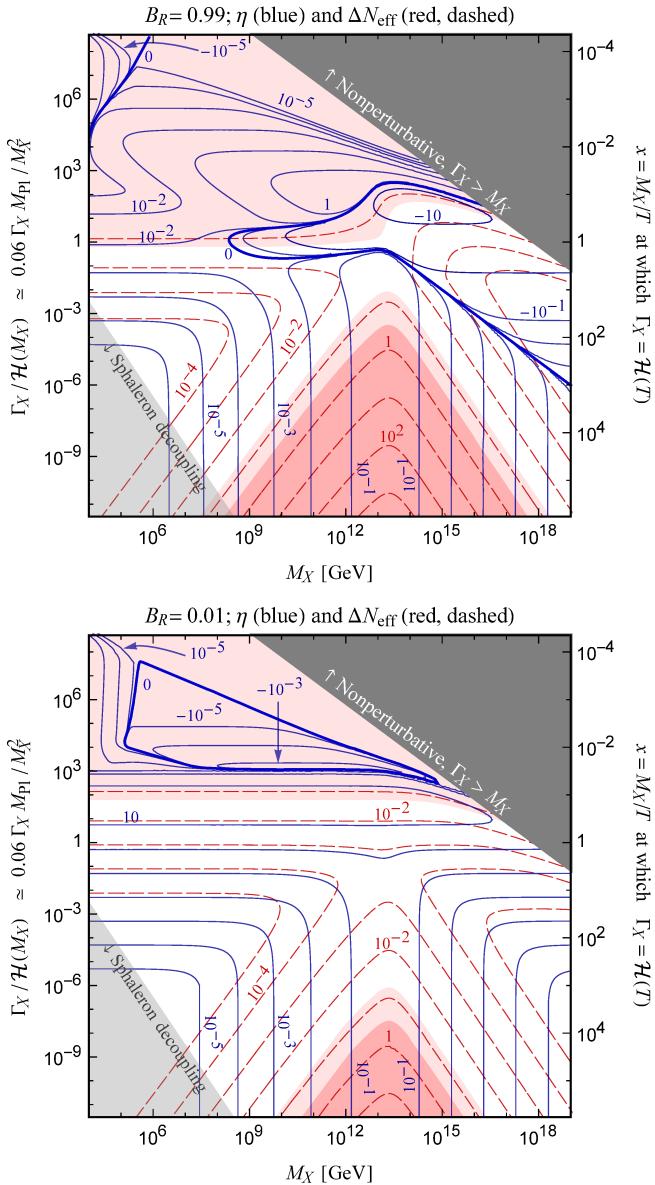


FIG. 2: Contours of ΔN_{eff} (red, dashed) and η (blue) for $B_R = 0.99$ (top) and $B_R = 0.01$ (bottom). In both cases $|\varepsilon| \leq 10^{-2}$ and we require $\varepsilon\eta \sim 10^{-7}$ to explain the baryon asymmetry. The dark red shaded region is excluded by current bounds on ΔN_{eff} [18]; light red shows future reach [22]. The upper-right region has nonperturbative $\Gamma_X > M_X$. In the lower-left region, X decays after sphaleron decoupling.

ishing initial abundances for both X and ν_R . For thermalized ν_R , these equations are similar to those of triplet leptogenesis [19]. We show some numerical solutions to the Boltzmann equations in App. D to illustrate the evolution of ν_R abundance and asymmetry. $\Delta_{\nu_R}(T \rightarrow 0)$ gives the ν_R asymmetry or efficiency parameter η , while $\Sigma_{\nu_R}(T \rightarrow 0)$ is the number of right-handed neutrinos, which gives ΔN_{eff} when multiplied by the characteristic ν_R momentum at production; see appendix A for more details. Some numerical solutions are presented in Fig. 2.

In Fig. 2, we can recognize the behavior mentioned before and can quantify the relations:

(I) For $\Gamma_X \ll \mathcal{H}$, the X freeze in or out and decay at $T \ll M_X$. The efficiency peaks at $M_X \sim 10^{13}$ GeV and then falls off like $M_X^{-1} (M_X \log(M_X/\text{GeV}))$ for larger (smaller) masses. Here,

$$\Delta N_{\text{eff}} \simeq 0.05 B_R \eta / \sqrt{\Gamma_X M_{\text{Pl}} / M_X^2} \quad (16)$$

can become arbitrarily large for small Γ_X due to the large ν_R momentum, leading to strong constraints. A freeze-in component $\Delta N_{\text{eff}} \propto \Gamma_X / M_X^2$ becomes important for larger Γ_X and eventually leads to thermalization.

(II) For $B_L \ll 1$ and thermalized $X \rightarrow \nu_R$, a large $\eta \lesssim 1/B_L$ can be obtained, although $|\varepsilon\eta|$ remains below 1. This is an efficient leptogenesis region with the simple ΔN_{eff} prediction of Eq. (3).

(III) For $B_R \ll 1$, we find $\Delta_{\nu_R} \simeq \Sigma_{\nu_R} \varepsilon / B_R$ and thus a large $\eta \lesssim 1/B_R$, together with a suppressed ΔN_{eff} .

Numerical examples for other branching ratios are given in Fig. 3 and confirm the above picture. The qualitative behavior for the choices $B_R = 1 - 10^{-5}$ (upper panel), and $B_R = 10^{-5}$ (middle panel) is similar to that of Fig. 2 and we can identify the large- η regions already described above. Notice that in these two examples $|\varepsilon|$ is restricted to be below 10^{-5} from Eq. (10), so $|\eta|$ has to be larger than 10^{-2} in order to generate the observed baryon asymmetry. For $\Gamma_X \ll \mathcal{H}(M_X)$, this restricts M_X to the region $10^{11}-10^{15}$ GeV, but the mass is essentially unconstrained in regions (II) and (III), i.e. for larger Γ_X . Realistically, ε is actually much smaller than this upper limit of 10^{-5} and thus η has to be larger still. Nevertheless, we can have successful baryogenesis over a wide region of parameter space. In Fig. 3 (bottom), we show the efficiency for the special case $B_R = B_L = 1/2$. This case is comparably simple because the lack of hierarchy in $X \leftrightarrow e_R \nu_R$ vs. $X \leftrightarrow e_L \nu_L$ precludes the large- η regions (II) and (III). η can at most be of order one here, which however is hardly restrictive because $|\varepsilon|$ can be as large as 1/2 in principle. Even this case allows therefore for efficient baryogenesis, with a large portion of parameter space testable through ΔN_{eff} .

From Figs. 2 and 3 it is clear that Dirac leptogenesis is very efficient, in part because both X and ν_R can be out of equilibrium, allowing for successful baryogenesis even with tiny ε . Since the sign of η depends on the hierarchy of rates we find $\eta = 0$ contours that delineate these regions, not found in other leptogenesis mechanisms [16]. Large regions of the parameter space are already excluded by ΔN_{eff} constraints and even more can be tested with stage-IV CMB data [12, 22], down to $\Delta N_{\text{eff}} \simeq 0.06$.

While we have focused our numerical study on case a, the other cases of Tab. I are qualitatively similar. Their gauge annihilation cross sections will differ somewhat

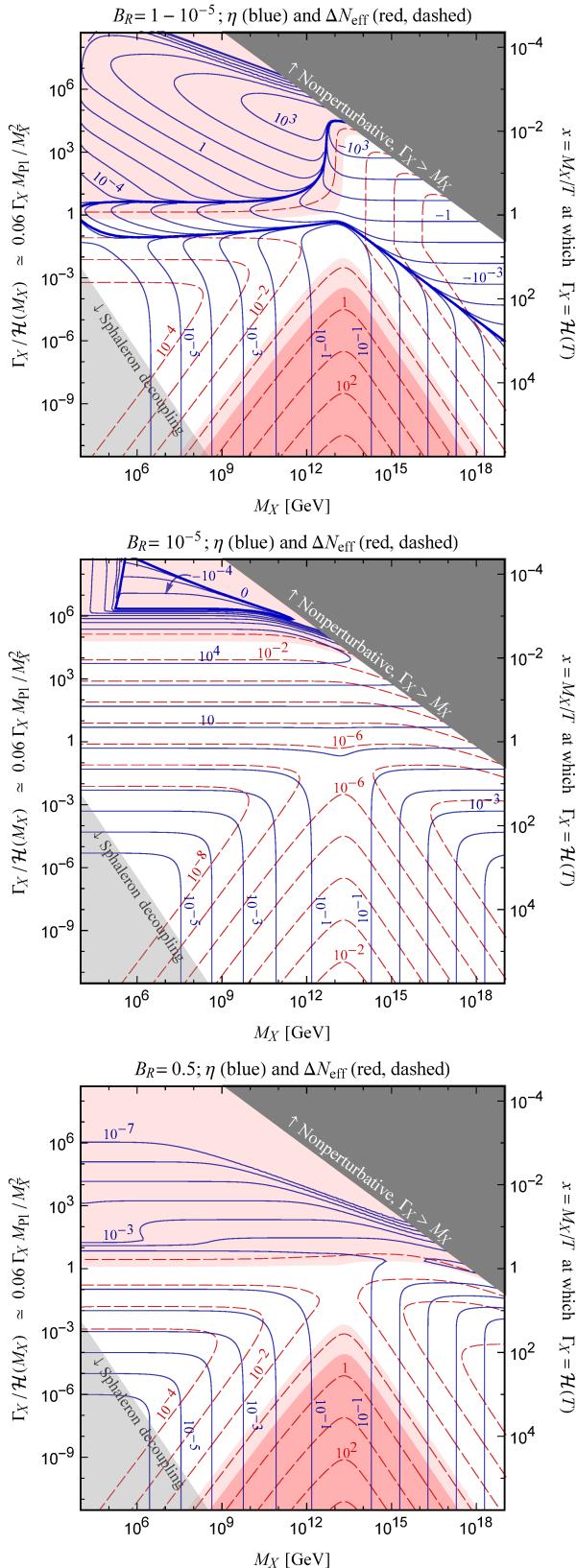


FIG. 3: Same as Fig. 2 but for $B_R = 1 - 10^{-5}$ (top), $B_R = 10^{-5}$ (middle), $B_R = 1/2$ (bottom).

– and might even require corrections due to Sommerfeld [27] and bound-state formation [28] – and there are often more than two relevant decay channels, but the basic picture from, say, Fig. 2 remains correct. Let us briefly mention two cases that induce new effects.

IV. PROTON DECAY

Case *d* (and in general case *c*) of Tab. I is special in that it violates baryon number directly. This makes it possible to circumvent the use of sphalerons in baryogenesis and establish *low-scale* Dirac leptogenesis, sharing similarities with cloistered baryogenesis [29]. The parameter space looks similar to Fig. 2, except that the lower-left sphaleron decay region is now allowed, X only needs to decay before Big Bang nucleosynthesis. This enlarges the allowed parameter space and in particular allows for fairly light leptoquarks X , which could then lead to detectable particle-physics signatures. Interestingly, the fact that a non-zero CP asymmetry ε requires X couplings to both $u_R\nu_R$ and d_Rd_R unequivocally gives rise to proton decay! $B - L$ is conserved in these proton decays and we unavoidably have final states that contain ν_R (see also [30]). For case *d*, we *only* have such ν_R final states, e.g. $p \rightarrow K^+\bar{\nu}_R$, while case *c* also has fully visible final states such as $p \rightarrow \pi^0e^+$.

For case *d*, we have the following Lagrangian for several copies of the leptoquark $X \sim (\mathbf{3}, \mathbf{1}, 2/3)$,

$$\mathcal{L} = \bar{d}_R^c F_i d_R X_i + \bar{u}_R^c G_i \nu_R \bar{X}_i + \text{h.c.}, \quad (17)$$

with implicit contraction of $SU(3)$ indices. This leads to the proton decay rate

$$\Gamma(p \rightarrow K^+\bar{\nu}_R) \simeq \sum_{i,\alpha} \frac{|F_{i,12}G_{i,1\alpha}|^2}{6 \times 10^{33} \text{ yr}} \left(\frac{2 \times 10^{15} \text{ GeV}}{M_{X_i}} \right)^4, \quad (18)$$

using the relevant QCD matrix element from Ref. [31]. Notice that a kaon is produced due to the antisymmetry of the F_i Yukawa couplings in flavor space. The current limit on this proton-decay mode is $1/\Gamma > 6 \times 10^{33}$ yr [32] and will be improved in JUNO [33], Hyper-Kamiokande [34] and DUNE [35]. Baryogenesis does not actually require X couplings to the first quark generation, seemingly allowing for an easy way to evade proton decay. However, *any* nonzero F and G couplings will together – as required for a nonzero CP asymmetry – induce proton decay at higher order in perturbation theory, potentially with more complicated final states [36]. The X masses and couplings required for baryogenesis can easily lead to testable proton decay rates (and ΔN_{eff}).

V. CONCLUSIONS

Massive Dirac neutrinos have Higgs couplings too small to bring the ν_R into thermal equilibrium, which allows

for leptogenesis without $B - L$ violation. In this article, we have shown that there are many simple realizations of this two-decade-old idea and that each one has a much larger viable parameter space than anticipated: Dirac leptogenesis is very efficient. Even more surprisingly, much of this parameter space is testable through the ν_R contribution to N_{eff} , soon to be measured with sub-percent accuracy by CMB stage-IV experiments. A subset of models even allows for post-sphaleron baryogenesis and predict proton decay, making them one of the few known models that link these two baryon number violating observables. With both baryogenesis and Dirac neutrinos notoriously difficult to probe, Dirac leptogenesis provides some novel handles for testability.

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Appendix A: Computation of ΔN_{eff}

At temperature T , the energy density of the universe can be written as

$$\rho = \left[1 + \frac{7}{8} \left(\frac{T_\nu}{T} \right)^4 (N_{\text{eff}} + \Delta N_{\text{eff}}) \right] \rho_\gamma + \dots, \quad (\text{A1})$$

where ρ_γ is the energy density of photons, $N_{\text{eff}} = 3.045$ [37] is the SM's effective number of relativistic degrees of freedom in the active neutrino sector and

$$\Delta N_{\text{eff}} = \frac{8}{7} \left(\frac{T}{T_\nu} \right)^4 \frac{\rho_i}{\rho_\gamma} \quad (\text{A2})$$

is the respective contribution from an additional relativistic species i with energy density ρ_i . In general,

$$\rho_i = g_i \int \frac{d^3 p_i}{(2\pi)^3} E_i f_i, \quad (\text{A3})$$

where g_i is the particle's number of internal degrees of freedom, E_i its energy and f_i its momentum distribution. For ultra-relativistic particles, $E_i = p_i$ and we can

express the energy density as $\rho_i = s^{4/3} \langle q_i \rangle Y_i$, where $\langle q_i \rangle$ is the first moment of the momentum mode, $q_i \equiv p_i/s^{1/3}$,

$$\langle q_i \rangle = \frac{g_i}{s^{4/3} Y_i} \int \frac{d^3 p_i}{(2\pi)^3} p_i f_i, \quad (\text{A4})$$

and Y_i is the comoving number density,

$$Y_i = \frac{g_i}{s} \int \frac{d^3 p_i}{(2\pi)^3} f_i. \quad (\text{A5})$$

In the above expressions, $s = g_* T^3 2\pi^2/45$ denotes the entropy density. Accordingly,

$$\Delta N_{\text{eff}} = \sum_i \frac{\langle q_i \rangle}{\langle q_\nu \rangle} \frac{Y_i}{Y_\nu} N_{\text{eff}}, \quad (\text{A6})$$

where $\langle q_\nu \rangle$ and Y_ν are the respective quantities for the relativistic SM neutrinos:

$$\langle q_\nu \rangle \simeq 3.15 \left(\frac{45}{2\pi^2 g_*(T_{\nu, \text{FO}})} \right)^{1/3}, \quad (\text{A7})$$

$$Y_\nu = \sum_{j=1}^3 Y_{\nu_j}^{\text{eq}}(T_{\nu, \text{FO}}), \quad (\text{A8})$$

with $T_{\nu, \text{FO}}$ being the temperature of neutrino decoupling.

In Eq. (A6), the sum runs over the involved production modes of right-handed neutrinos with characteristic $\langle q_i \rangle$ for which we employ the results of Ref. [21]. For the production in the late decay of the mother particle X (referred to as the superWIMP production mechanism in [21]) we obtain

$$\langle q_{\text{sw}} \rangle = \frac{45^{1/12} \pi^{7/12}}{2^{4/3} g_*^{1/12}} \frac{M_X}{\sqrt{\Gamma_X M_{\text{Pl}}}} \quad (\text{A9})$$

in our notation. Early production around $x \sim 1$ (via freeze-in or close-to-equilibrium processes) gives rise to a moment similar to Eq. (A7). The respective contributions to the comoving number density, Y_i , are obtained from solving the Boltzmann equations.

Appendix B: Boltzmann equations

In this appendix we derive the Boltzmann equations. For the individual abundances Y of particles and antiparticles, the Boltzmann equations read:

$$\frac{dY_X}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \left[\langle \sigma v \rangle_{X\bar{X}} \left(Y_X Y_{\bar{X}} - Y_X^{\text{eq}}{}^2 \right) + \frac{\langle \Gamma_X \rangle (B_R + \varepsilon)}{s} \left(Y_X - Y_X^{\text{eq}} \frac{Y_{\nu_R} Y_{e_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) \right]$$

$$+ \frac{\langle \Gamma_X \rangle (B_L - \varepsilon)}{s} \left(Y_X - Y_X^{\text{eq}} \frac{Y_L^2}{Y_L^{\text{eq}2}} \right) \Bigg], \quad (\text{B1})$$

$$\begin{aligned} \frac{dY_{\bar{X}}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& \langle \sigma v \rangle_{X\bar{X}} \left(Y_X Y_{\bar{X}} - Y_X^{\text{eq}2} \right) + \frac{\langle \Gamma_X \rangle (B_R - \varepsilon)}{s} \left(Y_{\bar{X}} - Y_X^{\text{eq}} \frac{Y_{\bar{\nu}_R} Y_{\bar{e}_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) \\ & + \frac{\langle \Gamma_X \rangle (B_L + \varepsilon)}{s} \left(Y_{\bar{X}} - Y_X^{\text{eq}} \frac{Y_{\bar{L}}^2}{Y_L^{\text{eq}2}} \right) \Bigg], \end{aligned} \quad (\text{B2})$$

$$\begin{aligned} \frac{dY_{\nu_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - \frac{\langle \Gamma_X \rangle (B_R + \varepsilon)}{s} \left(Y_X - Y_X^{\text{eq}} \frac{Y_{\nu_R} Y_{e_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) + \langle \sigma v \rangle_{\nu_R e_R \rightarrow LL} \left(Y_{\nu_R} Y_{e_R} - Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}} \frac{Y_L^2}{Y_L^{\text{eq}2}} \right) \\ & + \langle \sigma v \rangle_{\nu_R \bar{L} \rightarrow \bar{e}_R L} \left(Y_{\nu_R} Y_{\bar{L}} - Y_{\nu_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{\bar{e}_R} Y_L}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) \Bigg], \end{aligned} \quad (\text{B3})$$

$$\begin{aligned} \frac{dY_{\bar{\nu}_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - \frac{\langle \Gamma_X \rangle (B_R - \varepsilon)}{s} \left(Y_{\bar{X}} - Y_X^{\text{eq}} \frac{Y_{\bar{\nu}_R} Y_{\bar{e}_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) + \langle \sigma v \rangle_{\bar{\nu}_R \bar{e}_R \rightarrow \bar{L} \bar{L}} \left(Y_{\bar{\nu}_R} Y_{\bar{e}_R} - Y_{\bar{\nu}_R}^{\text{eq}} Y_{\bar{e}_R}^{\text{eq}} \frac{Y_{\bar{L}}^2}{Y_L^{\text{eq}2}} \right) \\ & + \langle \sigma v \rangle_{\bar{\nu}_R L \rightarrow e_R \bar{L}} \left(Y_{\bar{\nu}_R} Y_L - Y_{\bar{\nu}_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{e_R} Y_{\bar{L}}}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) \Bigg], \end{aligned} \quad (\text{B4})$$

$$\begin{aligned} \frac{dY_{e_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - \frac{\langle \Gamma_X \rangle (B_R + \varepsilon)}{s} \left(Y_X - Y_X^{\text{eq}} \frac{Y_{\nu_R} Y_{e_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) + \langle \sigma v \rangle_{\nu_R e_R \rightarrow LL} \left(Y_{\nu_R} Y_{e_R} - Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}} \frac{Y_L^2}{Y_L^{\text{eq}2}} \right) \\ & - \langle \sigma v \rangle_{\bar{\nu}_R L \rightarrow e_R \bar{L}} \left(Y_{\bar{\nu}_R} Y_L - Y_{\bar{\nu}_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{e_R} Y_{\bar{L}}}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \text{SM gauge interactions} \Bigg], \end{aligned} \quad (\text{B5})$$

$$\begin{aligned} \frac{dY_{\bar{e}_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - \frac{\langle \Gamma_X \rangle (B_R - \varepsilon)}{s} \left(Y_{\bar{X}} - Y_X^{\text{eq}} \frac{Y_{\bar{\nu}_R} Y_{\bar{e}_R}}{Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}}} \right) + \langle \sigma v \rangle_{\bar{\nu}_R \bar{e}_R \rightarrow \bar{L} \bar{L}} \left(Y_{\bar{\nu}_R} Y_{\bar{e}_R} - Y_{\bar{\nu}_R}^{\text{eq}} Y_{\bar{e}_R}^{\text{eq}} \frac{Y_{\bar{L}}^2}{Y_L^{\text{eq}2}} \right) \\ & - \langle \sigma v \rangle_{\nu_R \bar{L} \rightarrow \bar{e}_R L} \left(Y_{\nu_R} Y_{\bar{L}} - Y_{\nu_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{\bar{e}_R} Y_L}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \text{SM gauge interactions} \Bigg], \end{aligned} \quad (\text{B6})$$

$$\begin{aligned} \frac{dY_L}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - 2 \frac{\langle \Gamma_X \rangle (B_L - \varepsilon)}{s} \left(Y_X - Y_X^{\text{eq}} \frac{Y_L^2}{Y_L^{\text{eq}2}} \right) - 2 \langle \sigma v \rangle_{\nu_R e_R \rightarrow LL} \left(Y_{\nu_R} Y_{e_R} - Y_{\nu_R}^{\text{eq}} Y_{e_R}^{\text{eq}} \frac{Y_L^2}{Y_L^{\text{eq}2}} \right) \\ & - \langle \sigma v \rangle_{\nu_R \bar{L} \rightarrow \bar{e}_R L} \left(Y_{\nu_R} Y_{\bar{L}} - Y_{\nu_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{\bar{e}_R} Y_L}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \langle \sigma v \rangle_{\bar{\nu}_R L \rightarrow e_R \bar{L}} \left(Y_{\bar{\nu}_R} Y_L - Y_{\bar{\nu}_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{e_R} Y_{\bar{L}}}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \text{gauge int.} \Bigg], \end{aligned} \quad (\text{B7})$$

$$\begin{aligned} \frac{dY_{\bar{L}}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \Bigg[& - 2 \frac{\langle \Gamma_X \rangle (B_L + \varepsilon)}{s} \left(Y_{\bar{X}} - Y_X^{\text{eq}} \frac{Y_{\bar{L}}^2}{Y_L^{\text{eq}2}} \right) - 2 \langle \sigma v \rangle_{\bar{\nu}_R \bar{e}_R \rightarrow \bar{L} \bar{L}} \left(Y_{\bar{\nu}_R} Y_{\bar{e}_R} - Y_{\bar{\nu}_R}^{\text{eq}} Y_{\bar{e}_R}^{\text{eq}} \frac{Y_{\bar{L}}^2}{Y_L^{\text{eq}2}} \right) \\ & - \langle \sigma v \rangle_{\bar{\nu}_R L \rightarrow e_R \bar{L}} \left(Y_{\bar{\nu}_R} Y_L - Y_{\bar{\nu}_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{e_R} Y_{\bar{L}}}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \langle \sigma v \rangle_{\nu_R \bar{L} \rightarrow \bar{e}_R L} \left(Y_{\nu_R} Y_{\bar{L}} - Y_{\nu_R}^{\text{eq}} Y_L^{\text{eq}} \frac{Y_{\bar{e}_R} Y_L}{Y_{e_R}^{\text{eq}} Y_L^{\text{eq}}} \right) + \text{gauge int.} \Bigg]. \end{aligned} \quad (\text{B8})$$

Notice that $(3\mathcal{H})^{-1}ds/dx = -s/(\mathcal{H}x)$ for constant relativistic degrees of freedom. As we will assume the SM gauge interactions to be fully efficient, we have combined ν_L and e_L in the above equations by defining $Y_L = Y_{\nu_L} + Y_{e_L}$. Now, we define $\Sigma_A \equiv Y_A + Y_{\bar{A}}$ and

$\Delta_A \equiv Y_A - Y_{\bar{A}}$ for any species A and rewrite the Boltzmann equations accordingly. Σ_L and Σ_{e_R} are approximated by their equilibrium values on account of their efficient SM gauge interactions, leaving the following six equations:

$$\frac{d\Sigma_X}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \left[\frac{1}{2} \langle \sigma v \rangle_{X\bar{X}} \left(\Sigma_X^2 - \Sigma_X^{\text{eq}2} \right) + \frac{\langle \Gamma_X \rangle}{s} \left\{ \Sigma_X - \Sigma_X^{\text{eq}} \left(B_L + B_R \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right\} \right], \quad (\text{B9})$$

$$\frac{d\Sigma_{\nu_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \frac{\langle \Gamma_X \rangle}{s} \left[-B_R \left(\Sigma_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) + \frac{1}{2} \langle \sigma v \rangle_s \Sigma_{e_R}^{\text{eq}} (\Sigma_{\nu_R} - \Sigma_{\nu_R}^{\text{eq}}) + \frac{1}{2} \langle \sigma v \rangle_t \Sigma_L^{\text{eq}} (\Sigma_{\nu_R} - \Sigma_{\nu_R}^{\text{eq}}) \right], \quad (\text{B10})$$

$$\frac{d\Delta_X}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \frac{\langle \Gamma_X \rangle}{s} \left[\Delta_X - \Sigma_X^{\text{eq}} \left\{ B_R \frac{\Sigma_{\nu_R} \Delta_{e_R} + \Sigma_{e_R}^{\text{eq}} \Delta_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}} \Sigma_{e_R}^{\text{eq}}} + B_L \frac{2\Delta_L}{\Sigma_L^{\text{eq}}} - \varepsilon \left(1 - \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right\} \right], \quad (\text{B11})$$

$$\begin{aligned} \frac{d\Delta_{\nu_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \frac{\langle \Gamma_X \rangle}{s} & \left[-B_R \left(\Delta_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R} \Delta_{e_R} + \Sigma_{e_R}^{\text{eq}} \Delta_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}} \Sigma_{e_R}^{\text{eq}}} \right) - \varepsilon \left(\Sigma_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right. \\ & \left. + \frac{1}{2} \langle \sigma v \rangle_s \left(\Delta_{\nu_R} \Sigma_{e_R}^{\text{eq}} + \Delta_{e_R} \Sigma_{\nu_R} - 2\Delta_L \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_{e_R}^{\text{eq}}}{\Sigma_L^{\text{eq}}} \right) + \frac{1}{2} \langle \sigma v \rangle_t \left\{ \Delta_{\nu_R} \Sigma_L^{\text{eq}} - \Delta_L (\Sigma_{\nu_R} + \Sigma_{\nu_R}^{\text{eq}}) + \Delta_{e_R} \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_L^{\text{eq}}}{\Sigma_{e_R}^{\text{eq}}} \right\} \right], \end{aligned} \quad (\text{B12})$$

$$\begin{aligned} \frac{d\Delta_{e_R}}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \frac{\langle \Gamma_X \rangle}{s} & \left[-B_R \left(\Delta_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R} \Delta_{e_R} + \Sigma_{e_R}^{\text{eq}} \Delta_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}} \Sigma_{e_R}^{\text{eq}}} \right) - \varepsilon \left(\Sigma_X - \Sigma_X^{\text{eq}} \frac{\Sigma_{\nu_R}}{\Sigma_{\nu_R}^{\text{eq}}} \right) \right. \\ & \left. + \frac{1}{2} \langle \sigma v \rangle_s \left(\Delta_{\nu_R} \Sigma_{e_R}^{\text{eq}} + \Delta_{e_R} \Sigma_{\nu_R} - 2\Delta_L \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_{e_R}^{\text{eq}}}{\Sigma_L^{\text{eq}}} \right) + \frac{1}{2} \langle \sigma v \rangle_t \left\{ \Delta_{\nu_R} \Sigma_L^{\text{eq}} - \Delta_L (\Sigma_{\nu_R} + \Sigma_{\nu_R}^{\text{eq}}) + \Delta_{e_R} \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_L^{\text{eq}}}{\Sigma_{e_R}^{\text{eq}}} \right\} \right], \end{aligned} \quad (\text{B13})$$

$$\begin{aligned} \frac{d\Delta_L}{dx} = \frac{1}{3\mathcal{H}} \frac{ds}{dx} \frac{\langle \Gamma_X \rangle}{s} & \left[-2B_L \left(\Delta_X - 2\Sigma_X^{\text{eq}} \frac{\Delta_L}{\Sigma_L^{\text{eq}}} \right) + 2\varepsilon (\Sigma_X - \Sigma_X^{\text{eq}}) - \langle \sigma v \rangle_s \left(\Delta_{\nu_R} \Sigma_{e_R}^{\text{eq}} + \Delta_{e_R} \Sigma_{\nu_R} - 2\Delta_L \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_{e_R}^{\text{eq}}}{\Sigma_L^{\text{eq}}} \right) \right. \\ & \left. - \langle \sigma v \rangle_t \left\{ \Delta_{\nu_R} \Sigma_L^{\text{eq}} - \Delta_L (\Sigma_{\nu_R} + \Sigma_{\nu_R}^{\text{eq}}) + \Delta_{e_R} \Sigma_{\nu_R}^{\text{eq}} \frac{\Sigma_L^{\text{eq}}}{\Sigma_{e_R}^{\text{eq}}} \right\} \right], \end{aligned} \quad (\text{B14})$$

where we have only kept terms linear in ε , Δ_A and neglected any asymmetry in the s - and t -channel scattering cross sections, $\langle \sigma v \rangle_{\nu_R e_R \rightarrow LL} \simeq \langle \sigma v \rangle_{\bar{\nu}_R \bar{e}_R \rightarrow \bar{L} \bar{L}}$ and $\langle \sigma v \rangle_{\nu_R \bar{L} \rightarrow \bar{e}_R L} \simeq \langle \sigma v \rangle_{\bar{\nu}_R L \rightarrow e_R \bar{L}}$, denoted by $\langle \sigma v \rangle_s$ and $\langle \sigma v \rangle_t$, respectively.

Note that $d(\Delta_{\nu_R} + \Delta_{e_R} + \Delta_L + 2\Delta_X)/dx = 0$ and $d(\Delta_{\nu_R} - \Delta_{e_R})/dx = 0$ due to conservation of hypercharge and lepton number, *i.e.* the set of differential equations is redundant and we can eliminate two of them by plugging in the solutions

$$\Delta_{\nu_R} + \Delta_{e_R} + \Delta_L + 2\Delta_X = \delta_1, \quad (\text{B15})$$

$$\Delta_{\nu_R} - \Delta_{e_R} = \delta_2, \quad (\text{B16})$$

where δ_i are initial conditions (set to zero here assuming vanishing asymmetries in the beginning). We choose to eliminate Eqs. (B13) and (B14) to obtain the Boltzmann equations in the main text. When ν_R is deep in equilibrium the Boltzmann equations simplify and are structurally similar to those of triplet leptogenesis [19]. In that region the equations become symmetric under $L \leftrightarrow R$, $\varepsilon \leftrightarrow -\varepsilon$; for every η at (B_R, ε) there is a solution with $-\eta$ at $(1 - B_R, -\varepsilon)$. This can be observed in the upper-left corners of the two examples in Fig. 2.

Appendix C: Involved cross sections

For case *a* of Tab. I, the relevant annihilation cross sections, summed over final-state spins, are

$$\sigma(X\bar{X} \rightarrow \mathcal{B}^* \rightarrow f\bar{f}) = \frac{(g')^4 Y_f^2}{24\pi s} \sqrt{1 - \frac{4M_X^2}{s}}, \quad (\text{C1})$$

$$\sigma(X\bar{X} \rightarrow \mathcal{B}^* \rightarrow \phi\bar{\phi}) = \frac{(g')^4 Y_\phi^2}{48\pi s} \sqrt{1 - \frac{4M_X^2}{s}}, \quad (\text{C2})$$

$$\begin{aligned} \sigma(X\bar{X} \rightarrow \mathcal{B}\mathcal{B}) = \frac{(g')^4}{16\pi M_X^2} & \left[\frac{\sqrt{(y-1)y^3} + \sqrt{(y-1)y}}{(y-1)y^2} \right. \\ & \left. + \frac{(1-2y) \tanh^{-1} \left(\sqrt{\frac{y-1}{y}} \right)}{(y-1)y^2} \right]_{y=\frac{s}{4M_X^2}}, \end{aligned} \quad (\text{C3})$$

where \mathcal{B} is the hypercharge gauge boson and g' the gauge coupling. f is a massless chiral fermion with hypercharge Y_f and ϕ a massless complex scalar with hypercharge Y_ϕ . The thermally-averaged annihilation rate is approximately

$$\langle \sigma v \rangle_{X\bar{X}} \simeq \frac{10^{-4}}{M_X^2} \begin{cases} 3.5 (M_X/T)^2, & M_X \ll T, \\ 1.2, & M_X \sim T, \\ 5.5, & M_X \gg T. \end{cases} \quad (\text{C4})$$

The thermally-averaged annihilation rate as well as the decay rates are shown in Fig. 4 relative to the Hubble rate $\mathcal{H} = \sqrt{4\pi^3 g_*/45} T^2/M_{\text{Pl}}$. For $M_X \gg 10^{13} \text{ GeV}$, the hypercharge gauge interactions are not sufficient to put X in equilibrium; for $M_X \ll 10^{13} \text{ GeV}$, X reaches equilibrium and freezes out at some temperature $T < M_X$. Decay rates have a different temperature dependence than annihilations.

The X -mediated $\Delta\nu_R = 1$ scattering cross sections consist of s - and t -channel cross sections,

$$\sigma_s(L_\alpha L_\beta \rightarrow e_{R,\gamma} \nu_{R,\sigma}) = \frac{|F_{\alpha\beta} G_{\sigma\gamma}^*|^2}{16\pi} \frac{s}{(s - M_X^2)^2}, \quad (\text{C5})$$

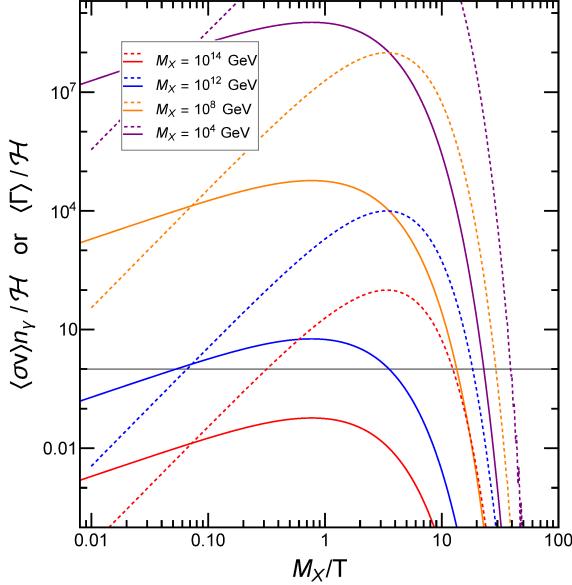


FIG. 4: Thermally averaged annihilation rate $\langle \sigma v \rangle n_\gamma / \mathcal{H}$ (solid lines) and inverse decay rate $\langle \Gamma \rangle / \mathcal{H}$ (dashed lines; for unity Yukawas) compared to the Hubble rate for several X masses.

$$\sigma_t(\bar{L}_\alpha e_{R,\gamma} \rightarrow L_\beta \bar{\nu}_{R,\sigma}) = \frac{|F_{\alpha\beta} G_{\sigma\gamma}^*|^2}{16\pi M_X^2} \times \left[\frac{y(y+2) + 2(y+1) \log\left(\frac{1}{y+1}\right)}{y^2(y+1)} \right]_{y=s/M_X^2} \quad (C6)$$

The former needs to be properly regulated to subtract the on-shell region that is already counted in the Boltzmann equations via (inverse) decays. We follow the procedure from Ref. [19] (see also Refs. [38, 39]) and subtract σ_s by

$$\frac{|F_{\alpha\beta} G_{\sigma\gamma}^*|^2}{16\pi} \frac{\pi s}{M_X \Gamma_X} \delta(s - M_X^2). \quad (C7)$$

For the Boltzmann equations we require the thermally averaged cross sections, summed over initial and final flavors. The relevant coupling trace can then also be written as

$$\text{tr}(F_i F_i^\dagger) \text{tr}(G_i G_i^\dagger) \simeq B_R B_L \Gamma_X^2 \left(\frac{16\pi}{M_X} \right)^2. \quad (C8)$$

Appendix D: Evolution of abundances

In this appendix we show some numerical solutions to the Boltzmann equations. Due to our approximations in App. B, all Δ_A are proportional to ε so we are effectively solving for Δ/ε . Depending on the parameters, some Δ change sign during the evolution.

The two plots in Fig. 5 correspond to case (I), where X reaches equilibrium and freezes out (left) or freezes

in (right) due to its gauge interactions, then decays at $T \ll M_X$. The smaller mass in the left figure results in a (more) efficient annihilation, cf. Fig. 4, leaving few X to eventually decay, which results in a suppressed η . In the right figure, the gauge interactions of X are just too small to thermalize X but still large enough to copiously produce X available to decay, resulting in a large η . For even larger M_X , the production rate of X would decrease, decreasing the abundance of X (and therewith the value of η) again. In these examples, the largest number of ν_R is produced in the final X decay, which also generates these ν_R with a large momentum $p \sim M_X$ relative to the cooled-down SM bath, which leads to fairly large ΔN_{eff} in both examples. Decreasing Γ_X , i.e. increasing the X lifetime, would not change η significantly, but ΔN_{eff} would increase proportional to $1/\sqrt{\Gamma_X}$ due to the increased ν_R momentum relative to the SM bath temperature, following Eq. (16). Changing B_R also does not affect η in this region of parameter space, although it significantly affects $\Delta N_{\text{eff}} \propto B_R$.

Case (I), i.e. the parameter space with $\Gamma_X \ll \mathcal{H}(M_X)$ is relatively easy to describe since η only depends on M_X and ΔN_{eff} follows from Eq. (16). Once we increase Γ_X to values around $\mathcal{H}(M_X)$, the Boltzmann equations become more difficult due to several competing rates.

The two plots in Fig. 6 are for $\Gamma_X / \mathcal{H}(M_X) = 10$ with $B_R = 0.99$ (left) and $B_L = 0.99$ (right). In the left plot, the $X \leftrightarrow e_R \nu_R$ rates are in equilibrium but the $X \leftrightarrow e_L \nu_L$ rates are not [case (II)], whereas the roles are reversed in the right plot [case (III)]. Similar to triplet leptogenesis, one rate being out of equilibrium is sufficient for a large η despite X being virtually in equilibrium. In the left plot, the ν_R reach equilibrium and give a thermal ΔN_{eff} [Eq. (3)], whereas the smaller B_R in the right plot suppresses ΔN_{eff} .

Fig. 7 (left) is another illustration of case (II) with even larger Γ_X . Here, the gauge interactions and ν_R decay rates are strong, but the $X \leftrightarrow e_L \nu_L$ rates are just on the verge of equilibrium: $B_L \Gamma_X / \mathcal{H}(M_X) = 1$. This is still sufficient for a very effective asymmetry generation. Increasing Γ_X further would lead to a decreasing η since the $X \leftrightarrow e_L \nu_L$ would thermalize and wash out the asymmetry. Notice that the large ν_R rates lead to a ΔN_{eff} that is slightly larger than the thermal value. The difference is small though, much larger values for ΔN_{eff} can only be obtained for $\Gamma_X / \mathcal{H} \ll 1$.

Fig. 7 (right) is again case (II) but has a large M_X and thus a much smaller X annihilation rate, leading to out-of-equilibrium X . This leads to an even larger $|\eta|$, notably with a different sign than in Fig. 7 (left).

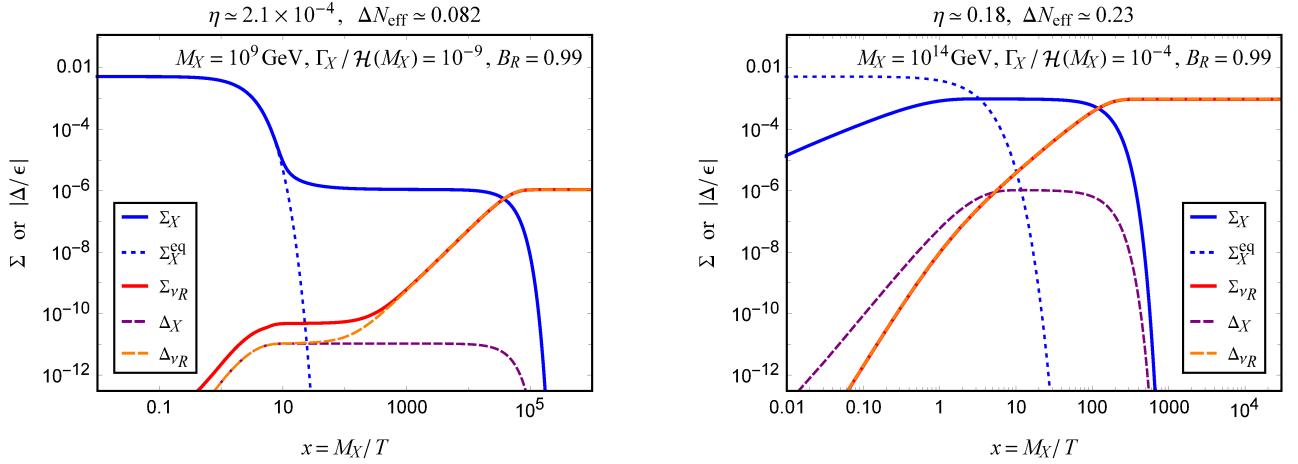


FIG. 5: Evolution of Σ_{X,ν_R} and $|\Delta_{X,\nu_R}/\varepsilon|$ for two parameter points together with the resulting η and ΔN_{eff} . The dashed blue line shows the equilibrium distribution of Σ_X . In the right panel, the curves for Σ_{ν_R} and $|\Delta_{\nu_R}/\varepsilon|$ are on top of each other.

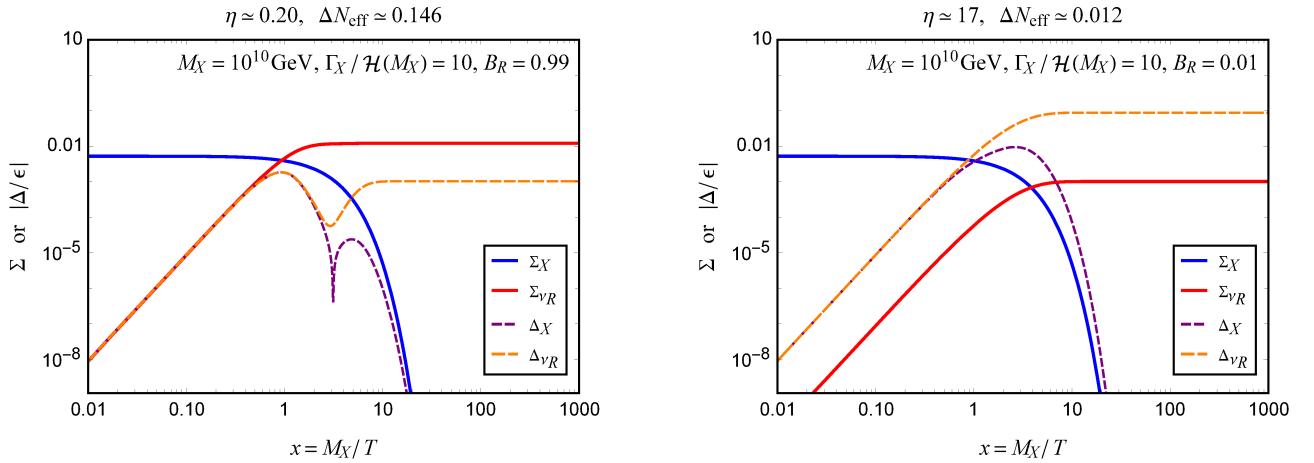


FIG. 6: Evolution of Σ_{X,ν_R} and $|\Delta_{X,\nu_R}/\varepsilon|$ for two parameter points together with the resulting η and ΔN_{eff} . Note that Σ_X is virtually in equilibrium in the considered x range.

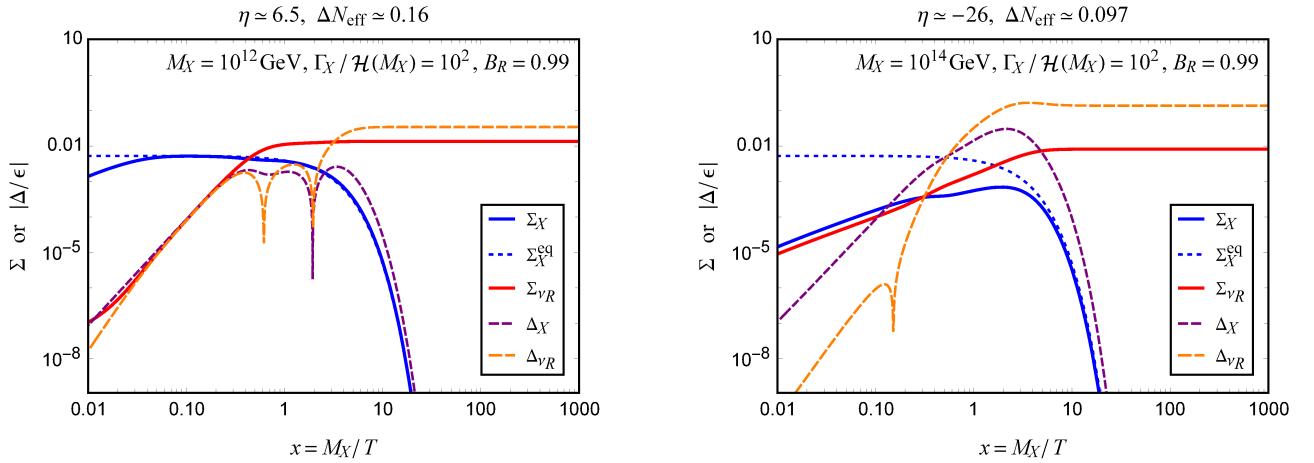


FIG. 7: Evolution of Σ_{X,ν_R} and $|\Delta_{X,\nu_R}/\varepsilon|$ for two parameter points together with the resulting η and ΔN_{eff} . The dotted blue line shows the equilibrium distribution of Σ_X .

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