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Shear annealing of a self-interacting sheet[†]

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2D materials such as graphene, graphene oxide, transition metal dichalcogenides, and 2D polymers have unique properties which allow them to be used in many applications from electronics to energy to biotechnology. Producing and applying these materials often involves solution processing. Previous computational studies have observed 2D sheets in shear and extensional flows, but have focused on steady flows, even though the dynamics of these materials might exhibit hysteresis. In this work, we study 2D sheets with short-ranged attractive interactions with time-varying shear. We show that, even with relatively simple protocols, the properties of sheet suspensions can be tuned.

1 Introduction

2D materials, or sheets, such as graphene, graphene oxide, transition metal dichalcogenides, and, more recently, synthetic 2D polymers, have a wide breadth of applications due to their unique properties. Graphene and graphene oxide, for example, possess high surface areas, tunability (e.g. through functionalization), and favorable electrical, optical, and catalytic properties while being lightweight, flexible, and mechanically stable, allowing them to see success as membranes for separations², in biomedical applications such as drug delivery^{3,4}, in flexible electronic devices⁵, and more^{6–8}.

In order to apply graphene and its derivatives to industrial and commercial use, it is important to be able to produce them at high quality and with relatively low cost. Many of the methods of producing graphene such as mechanical exfoliation⁹ and various bottom-up synthesis strategies^{10–12}, have been restricted by high costs and/or limited scalability^{13–16}. Liquid exfoliation, which typically involves using either sonication or shear of a material in solution to separate its stacked layers, represents a cheap, facile, and easily scalable method for producing 2D materials for certain applications^{16–21}. Furthermore, many of the applications of graphene involve the use a suspension precursor regardless of the synthesis method (e.g. graphene inks for the printing of flexible electronics²²). Therefore, in order to optimize the production and application of graphene as well as other 2D materials, it is important to understand how suspensions of 2D materials behave in flow.

Theoretical and computational studies have shown that the properties of sheets are greatly impacted by both their own attrac-

tive interactions^{23–27} and the flow fields applied to them^{28–35}. In our previous paper¹, we showed combined these features and discovered a rich conformational properties which, when combined with the rotational behavior of the sheets, showed that the non-monotonic rheological properties and sheet orientations observed in dilute sheet suspensions^{36,37} could be explained by attractive interactions in the athermal, dilute limit.

One question that arises when looking at our previous results is that of initial condition. Our simulations began with an initially flat sheet, but our results suggest that, for sufficiently low bending rigidities relative to interaction strength, such a state might not be accessible for a long period of time at any shear rate. It was observed that the final conformation of the sheets was highly dependent on the initial condition, leading naturally to the question of whether these sorts of conformations can be observed in real systems. More broadly, we can ask questions about how the conformations of these systems can be controlled over time by applying non-steady flows or, more generally, by varying the parameters of the system over time.

This idea is not without precedent. Suspensions of colloidal particles exhibit different microstructures depending on factors such as the shear rate and volume fraction, analogous to sheet conformations. These microstructures, in turn, result in unique macroscopic material properties (liquids, gels, glasses, and crystals) which can be tuned for a particular application. Notably, colloidal suspensions with attractive interactions, even at volume fractions much lower than the glass transition, exhibit the same characteristic shear-thinning into shear-thickening rheological behavior seen in sheet suspensions due to the breakdown and formation of particle clusters^{38–42}. The time scales for these microstructural changes cause the material to have memory of the flow history⁴³. This memory allows for tuning of the final microstructure of a material through control of the applied flow protocol, for example by varying the "quenching" time from a high-shear "rejuvenation" (memoryless) regime^{44,45}. Similarly,

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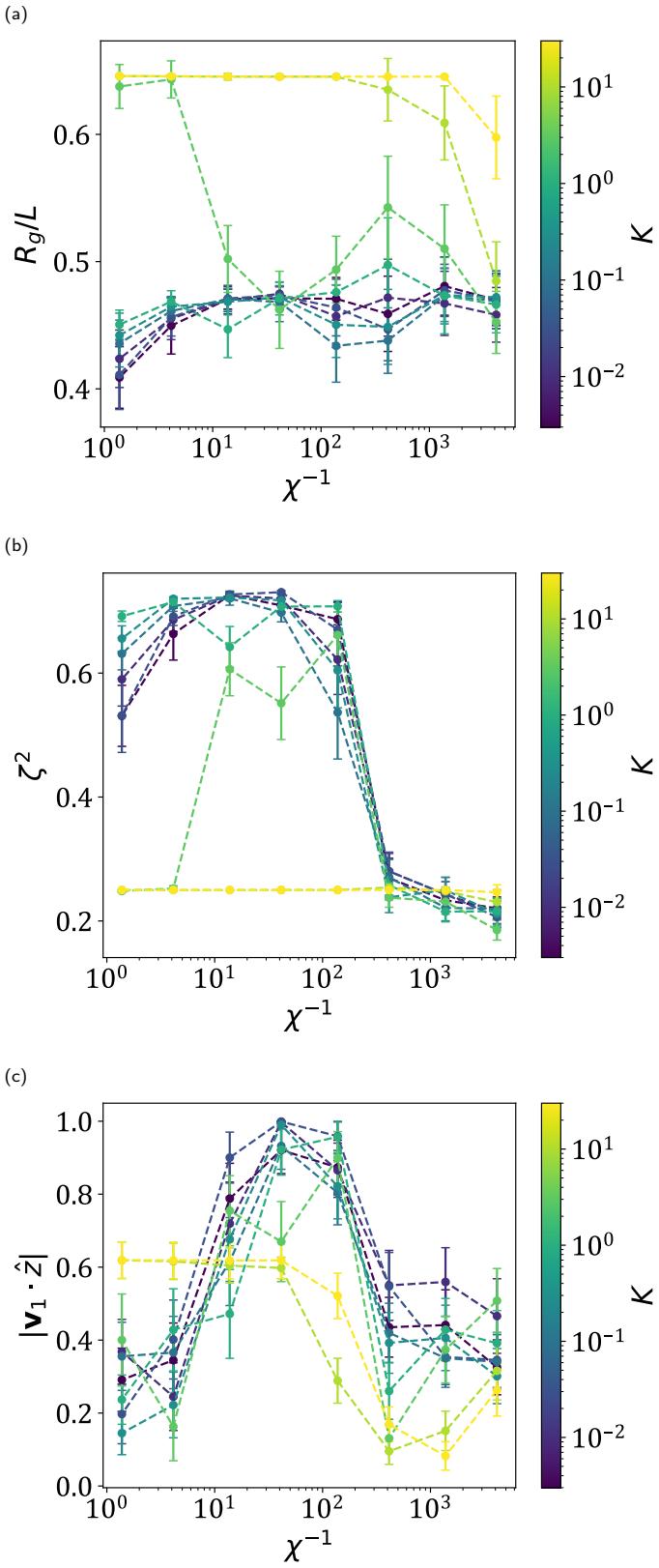


Fig. 1 (a) Radius of gyration, (b) relative shape anisotropy, and (c) alignment (from the minimum bounding ellipsoid) starting from flat initial configurations and averaged over the last $200\gamma t$ of $2000\gamma t$ and all ϕ . Error bars are 95% confidence intervals. Dotted lines drawn to guide the eye. Recreated from previous work¹

the tumbling regime for 2D sheets, which appears at high shear rates, represents a region where the conformation of sheets is continuously changing (i.e., they have access to many conformations, similar to a rejuvenation regime)^{1,34}. The folded regime similarly represents a regime where sheet conformation and rotation does not change significantly with time and where the final conformational and rotational properties of sheets possibly depends highly on the initial condition/flow history¹. Thus, it makes sense to examine the 2D sheet system from a similar framework as that used for colloidal suspensions.

The remainder of the paper will be divided as follows. First, we explain our models and methods. Next, we show that the final conformation of sheets can be controlled by varying the quench time in a linear annealing simulation. Then, we implement simple step protocols utilizing the features of the phase plot discovered in previous work¹ to control both the conformation and orientation of sheets. Finally, we summarize our results and give our concluding remarks.

2 Models and methods

2.1 Simulation methodology

We employ the same model used in previous work¹ which we will describe briefly here. For more details, please see the model description given by Silmore, Strano, and Swan^{34,35} and our previous publication¹.

We generate hexagonal sheets with circumradius $L = 39a$, where a is the bead radius, such that each interior bead has 6 tangent neighbors, totalling $N = 1141$ beads. Between neighboring beads, we apply a harmonic potential with spring constant (in-plane stiffness) k . Between triangles of neighboring beads which share an edge, we apply a dihedral potential with bending rigidity (out-of-plane stiffness) κ . As is true in many real systems, we set the in-plane stiffness to be much higher than the out-of-plane stiffness, such that the Föppl-von Kármán number, $FvK \sim kL^2/\kappa$ is large (in this case, $FvK > 10^3$). Between pairs of non-neighboring beads, we apply a truncated Lennard-Jones potential with interaction strength ϵ and interaction range σ . We use a turn-on distance of $r_{on} = 2a$ and a cut-off radius of $r_{cut} = 2.5\sigma$. For all simulations, we set $\sigma = 4\sqrt{6}a/3$. We also apply a hard-sphere potential between pairs of non-neighboring beads.

We integrate the system forward in time with an Euler-Maruyama integrator following the equations of motion

$$d\mathbf{x}_i = \left(-\sum_j \mathcal{M}_{ij} \frac{\partial U_i}{\partial \mathbf{x}_j} + \mathbf{L} \mathbf{x}_i \right) dt, \quad (1)$$

where \mathbf{L} is the velocity gradient tensor, $(\mathbf{L})_{mn} = \dot{\gamma} \delta_{m1} \delta_{n2}$, $\dot{\gamma}$ is the shear rate, and U_i is the sum of the applied potentials on bead i . To achieve long-range hydrodynamics, we use the Rotne-Prager-Yamakawa tensor for \mathcal{M}_{ij} ⁴⁶.

We previously identified two relevant dimensionless groups for this system. First, the relative strength of shear to interactions:

$$\chi^{-1} \equiv \frac{6\pi\eta\dot{\gamma}L^2\sigma}{\tilde{\epsilon}\sigma^2} \left(\frac{L}{a} \right)^{-1} \quad (2)$$

where $\tilde{\epsilon} = \epsilon/2\sqrt{3}a^2$ is the interaction energy density of the sheet.

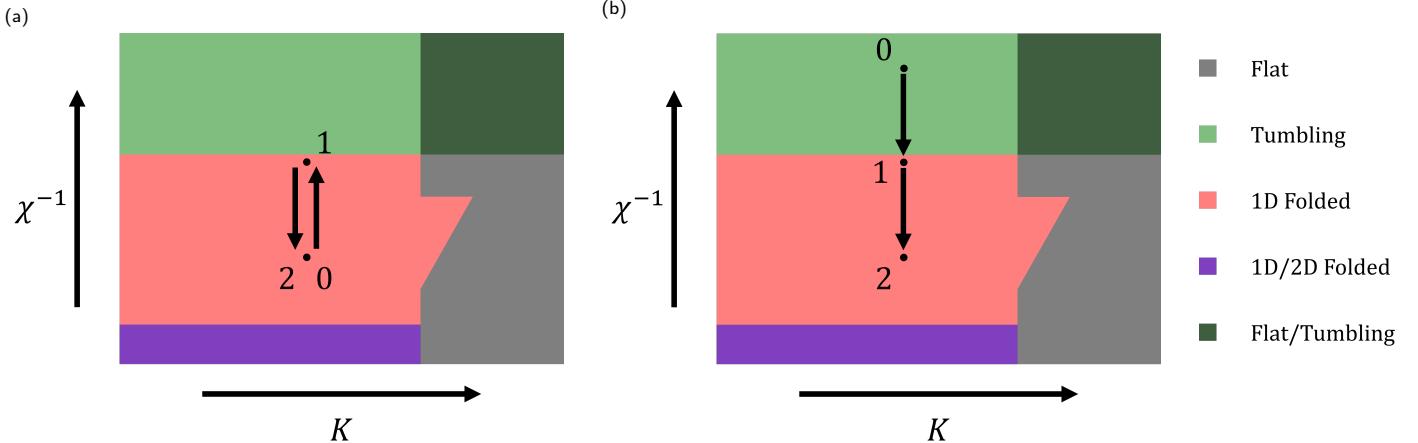


Fig. 2 Abstractions of different annealing protocols. Shaded regions denote the steady state conformational phase map discovered in our prior study¹. Dots with numbers indicate constant χ^{-1} simulations run for $2000\dot{\gamma}t$. Arrows represent a factor of 10 change in χ^{-1} . (a) Protocol 1, which starts at $\chi^{-1} = 1.4 \times 10^1$. (b) Protocol 2, which starts at $\chi^{-1} = 1.4 \times 10^3$.

Second, the relative strength of bending rigidity to interactions:

$$K \equiv \frac{\kappa}{\tilde{\epsilon}\sigma^2}. \quad (3)$$

We note again in this paper that the pair of dimensionless groups χ^{-1}, K have a convenient physical interpretation. Varying χ^{-1} at constant K corresponds to changing experimental conditions (i.e. shear rate) at constant material conditions, whereas varying K corresponds to changing the material conditions (e.g. sheet composition or solvent).

We generate initial conditions by generating a flat sheet in the flow-vorticity plane then rotating by a constant angle $\theta = 5^\circ$ about the vorticity axis and a variable angle ϕ degrees about the flow axis. We then run a shear simulation at constant χ^{-1}, K to generate an initial conformation. We then implement several protocols varying χ^{-1} , performing a constant χ^{-1} simulation at the end of each protocol to gather statistics for sheet properties. These protocols are detailed in the following sections.

Simulations were run using HOOMD-blue on NVIDIA GeForce GTX 1080 Ti's⁴⁷ with a custom package from Ref.³⁴ which was adapted from Ref.⁴⁸. Averages were taken from every $100\dot{\gamma}t$ due to the autocorrelation of tumbling sheets, as discussed in previous work. All images of sheets were rendered using Ovito⁴⁹.

2.2 Annealing simulations

Similarly to shear protocols applied to attractive colloidal suspensions⁴⁵, we apply a linear annealing shear protocol to sheets. First, we run a constant shear simulation at $\chi^{-1} = 4.1 \times 10^2$ for $2000\dot{\gamma}t$, where $\dot{\gamma}_0$ is the initial shear rate. Then, the shear rate is decreased linearly to zero over a variable quench time $\dot{\gamma}_0 t_q$, relative to the initial shear rate, where the sheet is allowed to equilibrate for another $2000\dot{\gamma}t$. Averages are taken over the last $500\dot{\gamma}t$ of the constant shear and no shear portions. We expect that, by varying the quench time, the final conformation of the sheets will vary. Specifically, as quench time increases, sheets will have more time at moderate shear rates to rearrange themselves into more

energetically favorable conformations.

We measure several properties of the final conformation: the radius of gyration, R_g , and the relative shape anisotropy, ζ^2 . The radius of gyration is a measure of the size of a sheet. Flat sheets have the largest possible radius of gyration for an inextensible sheet ($R_g \approx 0.65L$). 1D folded sheets have moderate $R_g \approx 0.5L$ and 2D folded sheets have smaller $R_g \lesssim 0.4$. Tumbling sheets have widely varying values of R_g but tend to average around the value for 1D folded sheets, $R_g \approx 0.5$.

The relative shape anisotropy is a measure of the shape of a sheet. It ranges from 0 to 1, which 0 corresponding to a spherically symmetric sheet and 1 corresponding to a linear sheet. 1D folded sheets, who have a single large axis and are therefore "line-like," have large values of $\zeta^2 \approx 0.7$. Flat sheets have low values of $\zeta^2 \approx 0.25$. Different 2D folded sheets can have very different values of ζ^2 corresponding to different fold patterns. Tumbling sheets again have widely varying values of ζ^2 , but tend to average with very low values of $\zeta^2 \lesssim 0.2$, corresponding to a more "sphere-like" sheet.

These properties therefore give a more detailed description of sheets than just their conformations. Flat sheets have large R_g and low ζ^2 , 1D folded sheets have moderate R_g and high ζ^2 , 2D folded sheets have lower R_g and ζ^2 values than 1D folded sheets, and tumbling sheets typically have moderate R_g and low ζ^2 , with larger variances in these values. The behavior of an individual sheet is dependent on the initial condition, necessitating averages over many initial conditions, given by ϕ .

2.3 Step protocols

Next, we show that the features of the phase plot can be exploited to tune the final properties of a dilute suspension of sheets. As a target, we choose 1D folded, high alignment sheets, which we would like to achieve at low shear rates. The alignment varies from 0 to 1 and is a measure of the orientation of a sheet with respect to the vorticity axis. This value was shown previously¹ to correspond to the viscosity of a dilute suspension of sheets, with

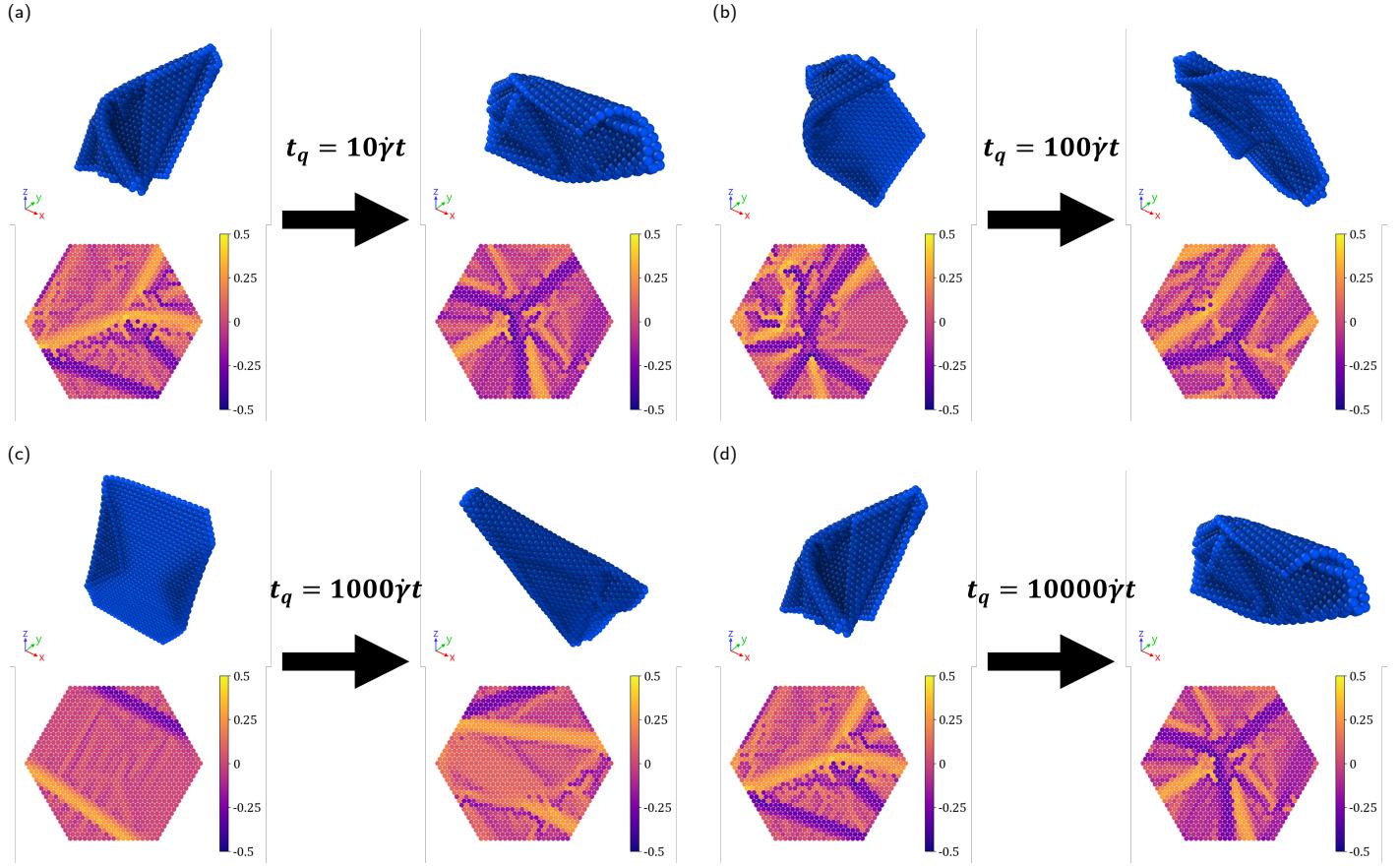


Fig. 3 Sample configurations (top) and their corresponding signed local mean curvatures (bottom), shown before (left) and after (right) annealing, for $K = 0.03$ and (a) $t_q = 10\dot{\gamma}t$, (b) $t_q = 100\dot{\gamma}t$, (c) $t_q = 1000\dot{\gamma}t$, and (d) $t_q = 10000\dot{\gamma}t$. Before annealing, sheets are sheared with a constant $\chi^{-1} = 4.1 \times 10^2$, which is in the tumbling regime. In configurations, x is the flow direction and y is the shear direction. Signed local curvature plots are all drawn to the same scale.

high alignments corresponding to lower viscosities. In this work, we use the eigenvector of the gyration tensor corresponding to its largest eigenvalue as opposed to the largest semi-axis of the minimum bounding ellipsoid, as it points in a similar direction and is much cheaper to calculate.

Flat sheets have alignments which depend on their orientation. Flat sheets which rotate about the vorticity axis have alignments close to 0 while flat sheets in the flow-vorticity plane can have a range of alignments. 2D folded sheets similarly have a range of alignments corresponding to the particular orbit they occupy. Tumbling sheets, on the other hand, tend to have alignments close to what would be achieved with a random sheet orientation, $|\mathbf{v}_1 \cdot \hat{\mathbf{z}}| \approx 0.52$. This makes sense, as these sheets tend to have low values of ζ^2 and therefore little preference for different alignments in shear. 1D folded sheets tend to have alignments close to 0 or 1 depending on the initial condition, with 1 being more likely for higher shear rates¹.

A suspension with high alignment might have favorable macroscopic properties. For example, this suspension would have the minimal viscosity for a dilute suspension for a particular value of K as seen in previous work¹. In addition, this suspension would be highly ordered and thus might carry favorable electronic properties, packing properties when concentrated, etc.. We would like

to achieve this state from both the high-shear tumbling regime and from folded sheets with lower alignments, which would suggest that this desired state could be achieved from many initial conditions. In particular, achieving this state from tumbling would be desirable as tumbling accesses many different configurations.

To achieve this, we note the features of Figure 7 from previous work¹, recreated in Figure 1. In particular, this figure shows that high alignment for sheets with relatively low values of K is achieved at values of χ^{-1} just before the tumbling transition ($1.4 \times 10^1 \lesssim \chi^{-1} \lesssim 1.4 \times 10^2$). While these results were achieved from flat initial configurations, it is likely that these shear rates have the effect of creating 1D folded, high alignment sheets. The mechanism for changing average alignments was discussed in previous work, having to do with the deformability of these sheets allowing sheets to shift Jeffrey orbits⁵⁰⁻⁵². As χ^{-1} increases, the low alignment state becomes less favorable due to its higher stress, causing an increase in the high alignment state. However, it remains to be seen if this high alignment can be achieved from 1D folded sheets which are already in low alignment orbits. Because sheet sections can slide along each other, this region likely has the additional effect of rearranging 2D folded sheets into lower stress, more energetically favorable 1D folded sheets. At

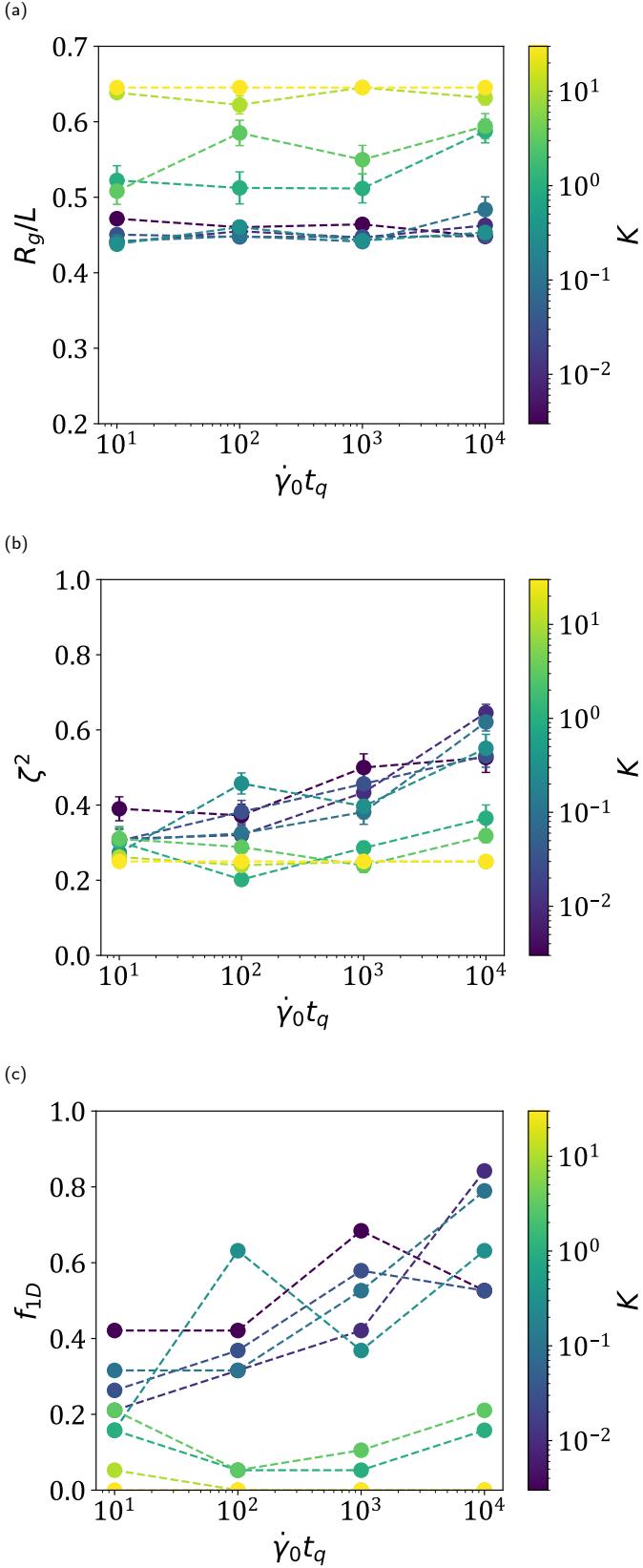


Fig. 4 Sheet (a) radius of gyration and (b) relative shape anisotropy as a function of quench time, averaged over the last $500\gamma_0 t$ of the no shear portion of annealing simulations and all ϕ . Error bars indicate 95% confidence intervals and dotted lines are drawn to guide the eye. (c) The fraction of sheets which were 1D folded after annealing.

large enough values of χ^{-1} , the sheets tumble and alignment is broken down due to the low relative shape anisotropy of tumbling sheets, leading to this Goldilocks zone for alignment. Therefore, targeting this region requires knowledge of the tumbling transition for sheets.

We design two step protocols to target this region. Protocol 1 starts in the 1D folded regime at moderate alignments, $\chi^{-1} = 1.4 \times 10^1$ (Step 0), and steps into the high alignment zone, $\chi^{-1} = 1.4 \times 10^2$ (Step 1), before stepping back down to the original $\chi^{-1} = 1.4 \times 10^1$ (Step 2). Each step is run for equal strains of $2000\dot{\gamma}\tau$, where $\dot{\gamma}$ is the shear rate at each step. This protocol is run at a variety of K . We visualize this protocol on an abstraction of the phase plot from previous work¹, seen in Figure 2. The shape of this abstraction is explained in previous work¹.

For tunability, it is important that high alignment is achieved upon increasing χ^{-1} and is maintained upon returning to the lower χ^{-1} . Once sheets are in a high alignment state, we don't expect reducing χ^{-1} to produce a mechanism for alignment to decrease, as the low alignment state still produces higher stresses than the high alignment state, making it likely that the high alignment state can be retained.

Protocol 2 starts in the tumbling regime, $\chi^{-1} = 1.4 \times 10^3$ (Step 0), steps into the high alignment zone, $\chi^{-1} = 1.4 \times 10^2$ (Step 1), then steps down to $\chi^{-1} = 1.4 \times 10^1$. Each step is again run for $2000\dot{\gamma}\tau$ and this protocol is also run at a variety of K . This protocol tests if high alignment, 1D folded sheets can be generated from the tumbling regime, which accesses many more configurations than the 1D folded sheets. We visualize this protocol in Figure 2.

We calculate the radius of gyration, R_g , and relative shape anisotropy, ζ^2 as before as well as the alignment, $|\mathbf{v}_1 \cdot \hat{\mathbf{z}}|$ of these simulations. Again, the behavior of an individual sheet is erratic, necessitating averages over many initial conditions, given by ϕ .

3 Results and discussion

3.1 Annealing simulations

In these simulations, sheets start in the tumbling regime at varying K ($\chi^{-1} = 4.1 \times 10^2$) and are annealed to no shear over a variable quench time t_q . Sample configurations along with their corresponding signed local mean curvature (SLMC, as described in previous work Silmore *et al.*³⁴) at the start and end of annealing are shown in Figure 3. A video of an annealing simulation can be found in the ESI†. While sheets appear to become more compact after annealing due to the presence of attractive interactions, the behavior of an individual sheet depends on its configuration at the onset of annealing. Therefore, it is necessary to look at averages over many initial conditions.

We report summary statistics for the final sheet configurations in Figure 4. For $K \lesssim 1$, the radius of gyration does not change much with quench time. Its approximate value of $0.45L$ is smaller than tumbling sheets, showing that sheets become more compact due to attractive interactions to fairly consistent value, which makes sense for $K \lesssim 1$, as attractive interaction can overcome bending rigidity. For $K \gtrsim 1$, there are flat sheets as well as folded sheets, causing a higher average radius of gyration.

For $K \lesssim 1$, the relative shape anisotropy of the sheets increases

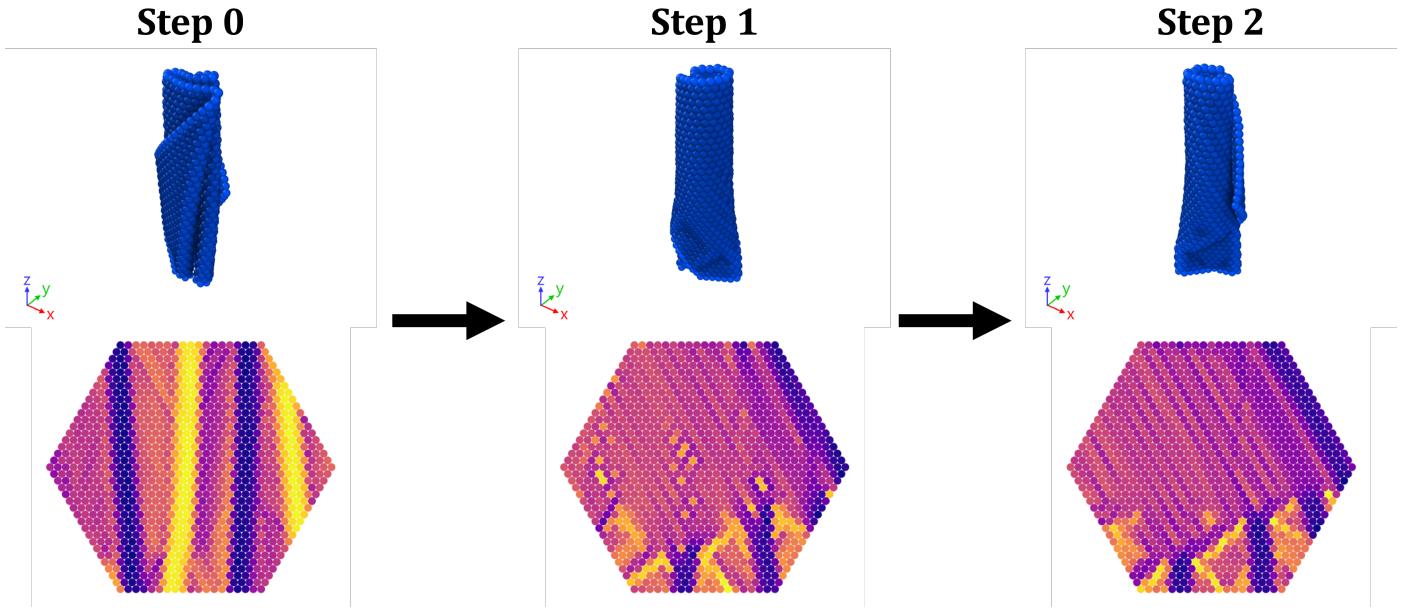


Fig. 5 Sample configurations (top) and their corresponding signed local mean curvatures (bottom), shown at the end of each constant χ^{-1} step for Protocol 1. In configurations, x is the flow direction and y is the shear direction. Signed local mean curvature plots are all drawn to the same scale.

on average with quench time. This indicates that sheets on average exhibit more 1D folded conformations. Indeed, Figure 4c calculates the fraction of sheets which are 1D folded, which matches with the relative shape anisotropy. This makes sense, as 1D folded sheets are slightly more energetically favorable than 2D folded sheets. Longer quench times gives more time for sheets which were more 2D folded-like to anneal towards this more energetically favorable conformation. For moderate $K \sim 1$, the relative shape anisotropy and fraction of 1D folded sheets also increased with quench time due to increased annealing, although the trend is suppressed because most sheets were flat in this regime. We suspect the initial decrease to be due to the relatively small number of annealing strain cycles causing larger variance in the final sheet conformations. For $K \gtrsim 10$, the relative shape anisotropy is relatively constant, corresponding to nearly all sheets being flat.

These results show that controlling quench time can indeed influence the final conformations of sheets. While the size of the sheets, even in the athermal limit, seems to depend on the material properties of the sheet (i.e. low or high K), the average relative shape anisotropy of the sheets increases significantly with quench time. For the shortest quench times, about 40% of sheets were 1D folded. For the longest quench times studied here, most sheets (about 50% to 85%) were 1D folded. It is unknown if long enough quench times would produce nearly 100% 1D folded sheets or if there is an asymptote with this shear protocol.

3.2 Step protocols

3.2.1 Protocol 1

Next, we implement step changes in χ^{-1} to try to achieve high alignment and 1D folding. In Protocol 1, sheets are in the 1D folded regime for the whole simulation. Sample configurations at the end of each constant χ^{-1} step are shown in Figure 5. A sample

video for a Protocol 1 simulation can be found in the ESI†.

We report summary statistics for the sheets averaged over the last 500yr of each step in Figure 6. These plots for different values of K showing all simulations are provided in the ESI†. For all K , the radius of gyration and relative shape anisotropy do not change significantly, showing that most sheets remained 1D folded throughout the simulations. Furthermore, the average alignment of these sheets shows that sheets are indeed aligned upon moving to the high alignment region at Step 1. This is despite many sheets having near-zero average alignments during Step 0. This confirms that this region can induce alignment in sheets from a variety of initial conditions. Significantly, this high alignment is maintained upon returning to the original χ^{-1} in Step 2, as expected and desired. This shows that this regime indeed shows hysteresis and the final properties of the suspension can be changed by modifying protocol.

For large enough $K \gtrsim 3$, the average radius of gyration is higher, the average relative shape anisotropy is lower, and the average alignment is lower. Examination of individual simulations reveals that this is due to the presence of a fraction of flat sheets. Some of these flat sheets become 1D folded at Step 1 due to the higher χ^{-1} , as indicated by the decrease in average radius of gyration and increase in relative shape anisotropy. Because flat sheets in the flow-vorticity plane can have a variety of alignments due to having two large axes, this makes the average alignment for large K lower, even though most sheets are either high alignment 1D folded sheets or flat sheets in the flow-vorticity plane.

3.2.2 Protocol 2

In Protocol 2, sheets start in the tumbling regime, are moved to the high alignment region, then χ^{-1} is lowered further. Sample configurations at the end of each constant χ^{-1} step are shown in Figure 7. A sample video for a Protocol 2 simulation can be found

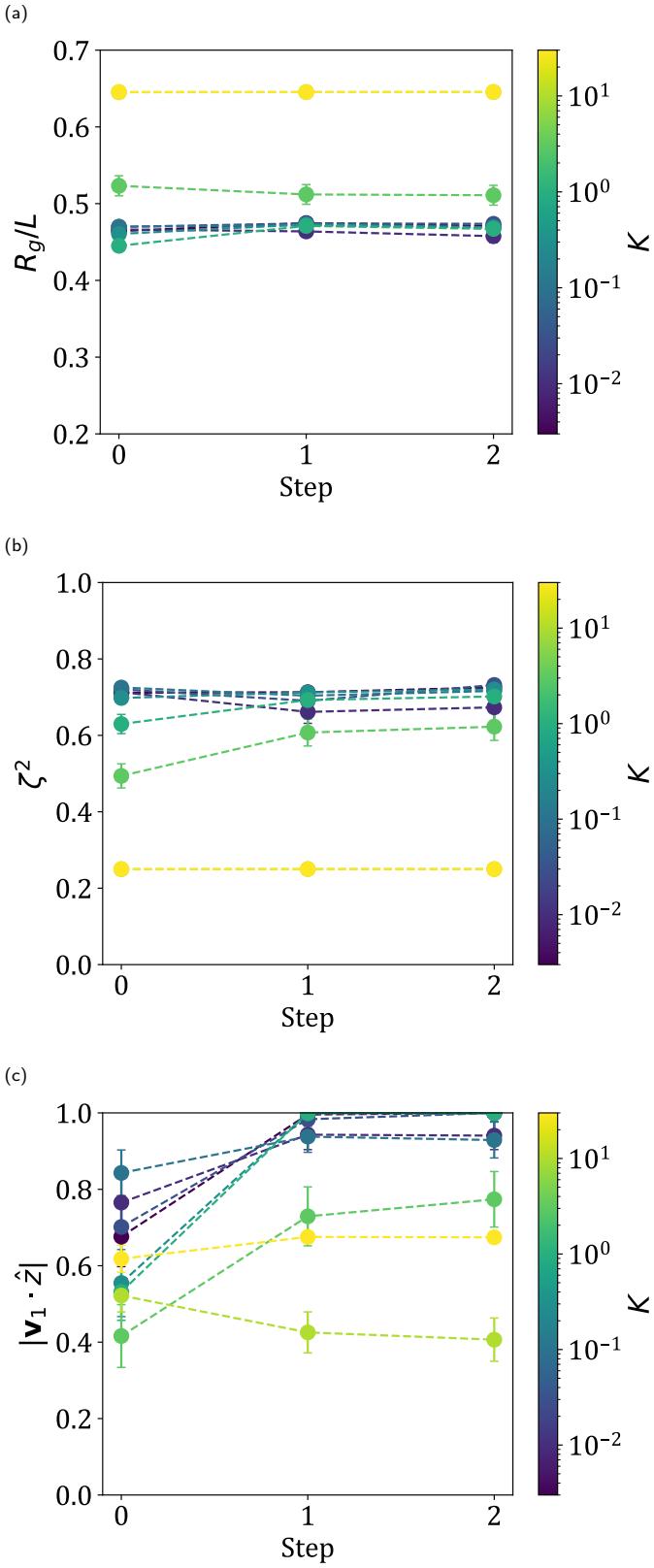


Fig. 6 Sheet (a) radius of gyration, (b) relative shape anisotropy, and (c) alignment averaged over the last $500\gamma t$ of each step for Protocol 1. Error bars indicate 95% confidence intervals and dotted lines are drawn to guide the eye.

in the ESI†.

We report these summary statistics for a range of K in Figure 8. These plots for different values of K showing all simulations are provided in the ESI†. For $K \lesssim 1$ and from Step 0 to Step 1, the radius of gyration of the sheets stays approximately the same while the relative shape anisotropy increases. This shows that sheets are indeed transitioning from tumbling to 1D folded from Step 0 to Step 1. The alignment also increases from Step 0 to Step 1, as expected, with sheets transitioning from a roughly random orientation with tumbling to high alignment 1D folded conformations. Interestingly, this increase also occurs from Step 1 to Step 2. This means that not only does entering the high alignment regime increase alignment, but changing χ^{-1} within the folding regime also can increase the average alignment of sheets. Lower values of χ^{-1} , even outside the high alignment regime, can change the rotational behavior of sheets, evidently allowing sheets to adopt new, lower stress orbits. Notably, the final alignment decreases with increasing K , suggesting that sheet deformability is key for sheet alignment.

Analysis of individual simulations also shows several sheets adopt high average alignment 2D folded behavior, depicted in the ESI†, which originates from teacup tumbling behavior described in previous work¹. This step change from tumbling, therefore, is highly dependent on initial condition, with the final behavior of being either high alignment 1D folded or 2D folded. For $K \gtrsim 3.0$, the behavior is similar, but with the presence of flat sheets causing higher radii of gyration, lower relative shape anisotropies, and lower average alignments. For $K = 30.0$, every sheet is flat throughout the simulation, causing no significant change in any summary statistic.

Together, these data show that, even from the tumbling regime where sheets sample many different configurations, high alignment, 1D folded behavior can be achieved using fairly simple shear protocols.

4 Conclusions

In this work, we examine several time-dependent protocols for self-interacting, semi-flexible sheets in simple shear. Through linear annealing from tumbling to zero shear, we show that the average final properties of the sheets (in the athermal limit) can be tuned through varying the quench time. In particular, while the radius of gyration of sheets remains about the same regardless of quench time, the relative shape anisotropy increases due to the increased presence of 1D folded sheets. For large enough K , sheets are flat instead and these trends disappear.

Next, by implementing step changes in χ^{-1} , we show that sheets can also be aligned. Specifically, we show that sheets in the 1D folded regime can be aligned by increasing χ^{-1} to a value in a high alignment regime, which lies just below the tumbling transition. This alignment is maintained upon returning to a lower value of χ^{-1} , showing hysteresis in the rotational behavior of these sheets. This protocol could be used to tune bulk properties. For example, a suspension of high alignment sheets has a lower viscosity than sheets at the same shear rate but lower average alignments.

We also show that alignment can be achieved from the tum-

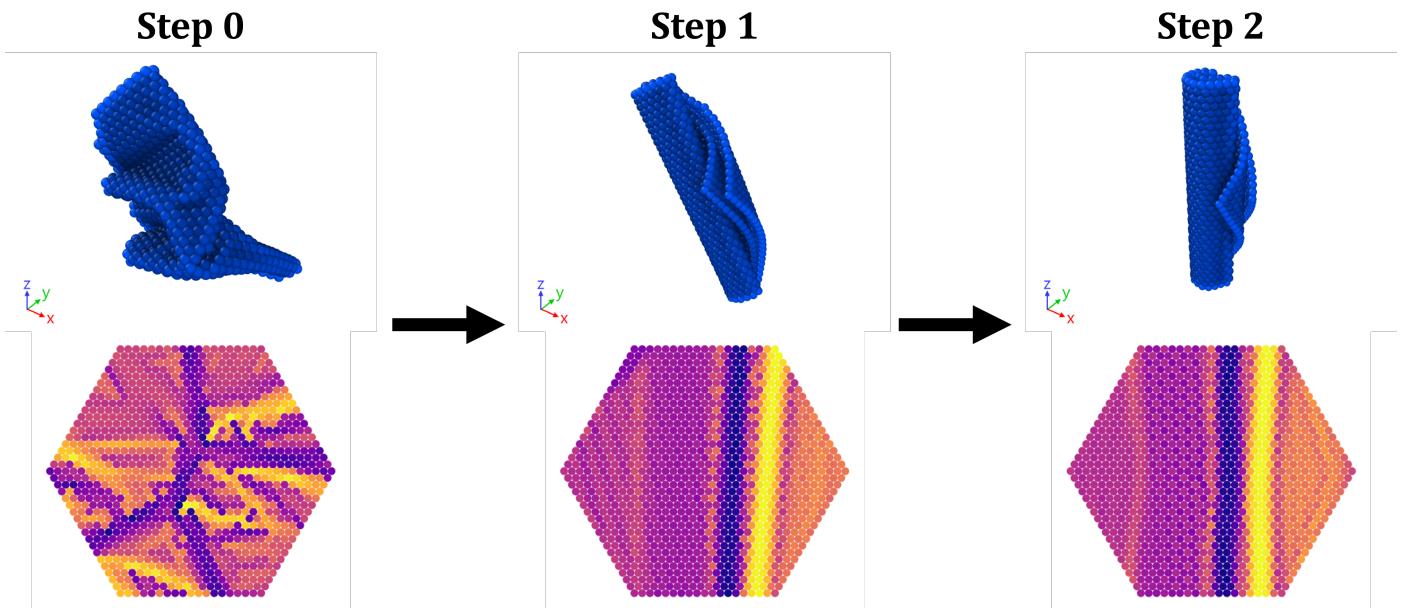


Fig. 7 Sample configurations (top) and their corresponding signed local mean curvatures (bottom), shown at the end of each constant χ^{-1} step for Protocol 2. In configurations, x is the flow direction and y is the shear direction. Signed local mean curvature plots are all drawn to the same scale.

bling regime, again by stepping into the high alignment 1D folding regime before decreasing the value of χ^{-1} lower. Interestingly, the alignment of these sheets increases upon lowering χ^{-1} below the high alignment regime, showing that changing χ^{-1} within the folded regime allows sheets to adopt new, lower stress orbits. The final conformations of these sheets are 1D folded or 2D folded, depending on the initial condition. The final alignment decreasing with K suggests that deformability is vital to achieving high alignment. For high enough values of K , sheets are flat, and the trends disappear.

It is possible that further design is possible through varying the time at each step or values of χ^{-1} at each step, time between steps or applied rate of change of χ^{-1} between steps, or by implementing more complex protocols with more steps. For example, due to the increase in average alignment from Step 1 to Step 2 in Protocol 2, a cyclic shear protocol which avoids the tumbling regime might achieve even better alignments after several cycles.

Furthermore, it might be possible to tune sheet properties even more specifically by introducing changes in K as well as χ^{-1} . This might be achieved experimentally, for example, by changing solvent to induce more or less favorable self-interactions and/or bending rigidities. Studies on the effect of protocols varying K would be valuable.

While thermal energy larger than interaction strength will likely break apart folded conformations in the absence of shear²⁴, the effects of small thermal fluctuations are not considered in this work and would be valuable in future work.

Using simple protocols to traverse the χ^{-1}, K phase space, we show that the conformational and rotational properties of sheets can be tuned with varying degrees of consistency. We hope that this work can help inform the design of such protocols to produce sheets with the desired properties.

Author Contributions

William T. Funkenbusch - methodology, investigation, visualization & writing. Kevin S. Silmore - methodology & writing. Patrick S. Doyle - supervision & writing.

Conflicts of interest

There are no conflicts to declare.

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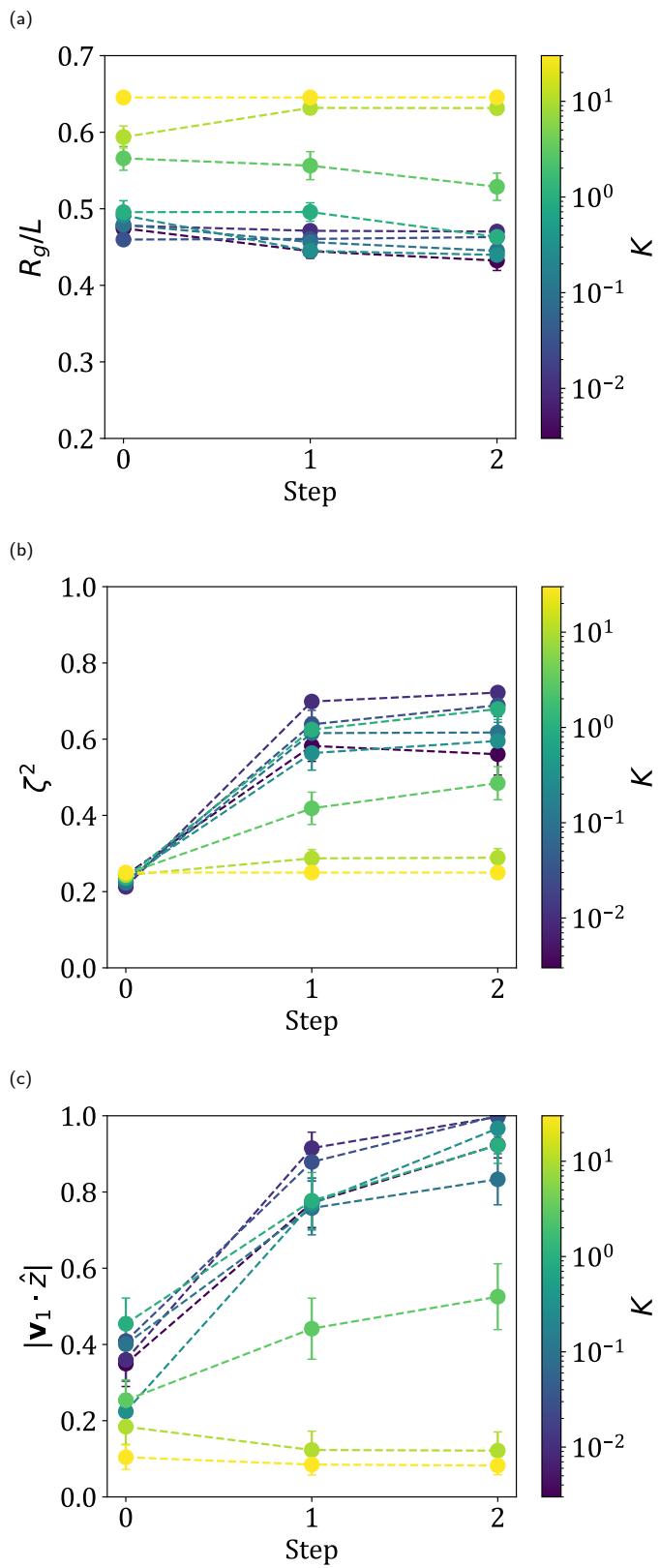


Fig. 8 Sheet (a) radius of gyration, (b) relative shape anisotropy, and (c) alignment averaged over the last $500\gamma t$ of each step for Protocol 2. Error bars indicate 95% confidence intervals and dotted lines are drawn to guide the eye.

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