



Article

High Modulus, Strut-like poly(ether ether ketone) Aerogels Produced from a Benign Solvent

Glenn A. Spiering , Garrett F. Godshall and Robert B. Moore *

* Correspondence: rbmoore3@vt.edu

Abstract: Poly(ether ether ketone) (PEEK) was found to form gels in the benign solvent 1,3-diphenylacetone (DPA). Gelation of PEEK in DPA was found to form an interconnected, strut-like morphology composed of polymer axialites. To our knowledge, this is the first report of a strut-like morphology for PEEK aerogels. PEEK/DPA gels were prepared by first dissolving PEEK in DPA at 320 °C. Upon cooling to 50 °C, PEEK crystallizes and forms a gel in DPA. The PEEK/DPA phase diagram indicated that phase separation occurs by solid-liquid phase separation, implying that DPA is a good solvent for PEEK. The Flory–Huggins interaction parameter, calculated as $\chi_{12} = 0.093$ for the PEEK/DPA system, confirmed that DPA is a good solvent for PEEK. PEEK aerogels were prepared by solvent exchanging DPA to water then freeze-drying. PEEK aerogels were found to have densities between 0.09 and 0.25 g/cm³, porosities between 80 and 93%, and surface areas between 200 and 225 m²/g, depending on the initial gel concentration. Using nitrogen adsorption analyses, PEEK aerogels were found to be mesoporous adsorbents, with mesopore sizes of about 8 nm, which formed between stacks of platelike crystalline lamellae. Scanning electron microscopy and X-ray scattering were utilized to elucidate the hierarchical structure of the PEEK aerogels. Morphological analysis found that the PEEK/DPA gels were composed of a highly nucleated network of PEEK axialites (i.e., aggregates of stacked crystalline lamellae). The highly connected axialite network imparted robust mechanical properties on PEEK aerogels, which were found to densify less upon freeze-drying than globular PEEK aerogel counterparts gelled from dichloroacetic acid (DCA) or 4-chlorphenol (4CP). PEEK aerogels formed from DPA were also found to have a modulus-density scaling that was far more efficient in supporting loads than the poorly connected aerogels formed from PEEK/DCA or PEEK/4CP solutions. The strut-like morphology in these new PEEK aerogels also significantly improved the modulus to a degree that is comparable to high-performance crosslinked aerogels based on polyimide and polyurea of comparable densities.

Keywords: aerogel; semicrystalline polymer aerogel; solvents; poly(ether ether ketone); Hansen solubility parameters; X-ray scattering; hierarchical morphology; axialite



Citation: Spiering, G.A.; Godshall, G.F.; Moore, R.B. High Modulus, Strut-like poly(ether ether ketone) Aerogels Produced from a Benign Solvent. *Gels* 2024, 10, 283. https://doi.org/10.3390/gels10040283

Academic Editor: Luísa Durães

Received: 28 March 2024 Revised: 10 April 2024 Accepted: 15 April 2024 Published: 22 April 2024



Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/4.0/).

1. Introduction

Polymer gels are substantially dilute materials containing a continuous polymer network that exhibits solid-like behavior, while physically retaining liquids or gases within their three-dimensional macromolecular framework. The gel network can be held together with covalent chemical bonds, as in the case of crosslinked gels, or by physical interactions, in the case of physical gels. The physical interactions that compose a physical gel network include hydrogen bonding, helix formation, phase separation, polymer entanglements, ionic aggregation, π – π interactions, and polymer crystallites [1–7]. Physical gels are also known as thermoreversible, as their physical interactions are thermally labile.

Semicrystalline polymers can form thermoreversible gels from suitable solvents, where polymer crystallites form the physical network. Thermoreversible gelation has been reported for numerous semicrystalline polymers including poly(vinyl chloride) [7,8],

polyethylene [9–11], isotactic polypropylene [12,13], syndiotactic polystyrene [4,14–17], poly(L-lactic acid) [18], polyoxymethylene [19], polyamide-6 [20], poly(vinylidene fluoride) [21,22], poly(ethylene terephthalate) [23], poly(phenylene oxide) [24,25], syndiotactic poly(methyl methacrylate) [26,27], and poly(phenylene sulfide) [28]. The choice of solvent can also lead to differences in the gel morphology and properties [29–31]. Previously, our group has reported the thermoreversible gelation of poly(ether ether ketone) (PEEK) in dichloroacetic acid (DCA) [32–34] and 4-chlorophenol (4CP) [34]. The gelation of PEEK from DCA or 4CP was found to form gels with a mass-fractal globular morphology consisting of lamellar stacks with limited lateral dimension.

DPA is of particular interest as a gel-forming solvent for PEEK since it is non-hazardous and benign, even being a flavoring additive approved by the U.S. Food and Drug Administration [35]. In contrast, 4CP and DCA are both acutely toxic, corrosive, and environmentally hazardous. Using DPA, we have previously reported the gelation of two other aromatic semicrystalline polymers: poly(phenylene sulfide) [28] (PPS) and poly(ether ketone ketone) [36] (PEKK). PPS and PEKK gels from DPA were found to contain fibrillar morphologies composed of crystalline axialites.

Thermoreversible gelation of semicrystalline polymers can be viewed as a thermally induced phase separation (TIPS) process [37]. TIPS is a widely utilized technique to yield porous membranes [38-40], hollow fibers [41-43], and foams [44-46]. In this process, a polymer is dissolved in a solvent at an elevated temperature. Cooling down this solution reduces the polymer miscibility, inducing phase separation and subsequent solidification. In the case of a semicrystalline polymer system, the polymer can additionally crystallize during cooling. Solvent quality largely informs if phase separation is induced through spinodal decomposition (liquid-liquid phase separation) or by a direct crystallization (solid-liquid phase separation) route [37]. Liquid-liquid phase separation tends to have considerable composition dependence and can lead to morphologies such as powders [47] and bicontinuous structures [48,49]. Solid-liquid phase separation can lead to crystalline textures, such as spherulites [50–53] and axialites [28,52,53]. Porous PEEK systems have been prepared using solvents including 4-phenylphenol [54], diphenyl sulfone [55,56], and benzophenone [57]. Interestingly, TIPS of PEEK in diphenyl sulfone has been shown to yield fibrillar foams [56] or powders [55], depending on the preparation. TIPS of PEEK in 4-phenylphenol or benzophenone appear to form fibrillar morphologies composed of thin fibers. Removal of solvents from TIPS foams is often executed by evaporative drying, whereas to prepare a highly porous aerogel, gentler solvent extraction methods are often required.

When the solvent in a gel network is replaced with air, it becomes an aerogel. Evaporative drying, freeze-drying, and supercritical fluid extraction are commonly employed methods for removing a solvent from a gel [58,59]. Evaporative drying can induce a significant collapse of aerogel structures due to strong capillary forces and is not often used in aerogel preparation [58]. While freeze-drying is preferred as a gentler route to aerogel preparation, solvent crystallization can disrupt the gel morphology [60]. Supercritical fluid extraction requires considerable setup but is the gentlest route for preserving the gel structure [58]. Aerogels have many fascinating properties, including low density, high porosity, high surface area, and low thermal conductivity [61,62]. These properties make aerogels suitable for many applications such as thermal insulation [63–66], chemical adsorbents [46,67–70], catalyst supports [71,72], air filtration [73,74], and heterogeneous platforms for blocky copolymer functionalization [36,75,76].

This work reports the gelation of PEEK in a new, benign gelation solvent, 1,3-diphenyl acetone (DPA). The gelation of PEEK in DPA yields a strut-like morphology consisting of polymer axialites. To our knowledge, this is the first report of PEEK gelation in DPA and the first report of a strut-like PEEK aerogel morphology. Building on our previous work on PEEK gels formed from dichloroacetic acid (DCA) [32–34] and 4-chlorophenol (4CP) [34], this work highlights structure–property comparisons between the strut-like morphology of PEEK aerogels formed from DPA and the globular morphologies of PEEK

aerogels gelled in DCA and 4CP. In this work, we investigate the gelation mechanism of the PEEK/DPA system by constructing a phase diagram and investigating melting point depression. Furthermore, we perform a thorough morphological analysis including scanning electron microscopy and X-ray scattering analysis. In our scattering analysis, we are able to assign scattering features to the hierarchical structure of PEEK aerogels. Finally, we investigate the effects of polymer composition and selection of the gelation solvent on network morphology, mechanical properties, and mesoporosity. The broader scope of this work is to emphasize the role of phase separation route and morphology on aerogel properties for the field of semicrystalline polymer aerogels.

2. Results and Discussion

2.1. Gelation of PEEK in DPA

Previously, our group has reported the gelation of PEEK from solutions in DCA [32,33] and 4CP [34]. Using a similar TIPS procedure, we have now found that PEEK also undergoes gelation when cooled after dissolution in DPA at elevated temperatures. PEEK/DPA solutions with polymer concentrations from 8 to 22 wt.% were found to form monolithic, thermoreversible gels when cooled from 320 °C to 50 °C. In order to understand the process—morphology relationships in forming PEEK aerogels, the phase separation process over a range of temperatures and polymer concentrations must be evaluated.

A polymer solution may undergo thermally induced phase separation (TIPS) upon cooling. TIPS for semicrystalline polymers can either occur through solid-liquid (S-L) phase separation or liquid-liquid (L-L) phase separation [37]. For S-L phase separation upon cooling, the polymer crystallizes from the solution and organizes into crystalline lamellae, which tend to stack in large lamellar aggregates called axialites. Given sufficient room to grow (i.e., low nucleation density), the lamella can branch, splay, and induce the formation of large spherulites. However, if the nucleation density is high, the lateral growth of the lamella is limited, resulting in a dense collection of axialites (i.e., immature spherulites). The lamellar aggregates (axialites or spherulites) are large relative to the wavelength of light and thus scatter light. Upon cooling the polymer solution from an elevated temperature, crystallization and turbidity will occur at approximately the same temperature for S–L phase separation. In L–L phase separation, when the polymer solution is cooled, it becomes unstable and undergoes spinodal decomposition and separates into polymer-rich and polymer-poor phases. This phase separation is observed as upper critical solution temperature (UCST) behavior. For L-L phase separation, turbidity occurs as the temperature is lowered into the unstable region below the spinodal curve once the different phases (having different refractive indices) become large relative to the wavelength of light. Following this L–L phase separation, crystallization within the polymer-rich phase may occur at a lower temperature or later time (depending on crystallization kinetics) as cooling continues. Thus, turbidity generally precedes crystallization in the L-L process, while turbidity and crystallization are concurrent in the S-L process. In addition, L-L phase separation generally occurs when polymer-solvent interactions are poor, whereas S-L phase separation is expected when polymer–solvent interactions are favorable [37,45,77].

To determine the phase separation mechanism, a phase diagram was constructed. The phase diagram (Figure 1) shows the crystallization temperature and the cloud point for PEEK/DPA solutions at various PEEK compositions. With increasing PEEK content, both the cloud point temperature and crystallization temperature increase. There is good agreement between PEEK crystallization temperature and cloud point across the PEEK compositions investigated. Since turbidity coincides with PEEK crystallization, the PEEK/DPA system undergoes S–L phase separation, where PEEK crystallizes from the PEEK/DPA solution without ever undergoing spinodal decomposition. Phase separation occurring through a S–L phase separation mechanism suggests that DPA has favorable interactions with PEEK.

Gels **2024**, 10, 283 4 of 22

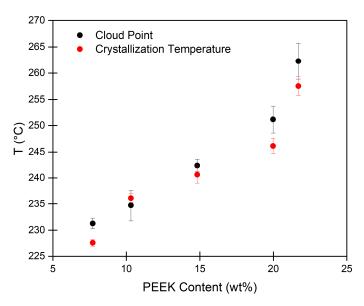


Figure 1. Poly(ether ether ketone) (PEEK)/1,3-diphenylacetone (DPA) phase diagram, showing cloud point and PEEK crystallization temperature for PEEK/DPA solutions. Each data point represents the average of 3 measurements with corresponding error bars (sample standard deviation).

In order to verify that DPA is a good solvent for PEEK, the Flory–Huggins interaction parameter, χ_{12} , was calculated. When χ_{12} is large, it indicates poor interactions between the polymer and solvent, whereas when χ_{12} is small, it indicates favorable solvent–polymer interactions [78]. The Hansen solubility parameters (HSPs) quantify the dispersive, polar, and hydrogen-bonding contributions to intermolecular interactions and may be used to probe the compatibility of polymer and solvent mixtures. For example, the Flory–Huggins interaction parameter can be calculated knowing the HSP as [79]:

$$\chi_{12} = \frac{VA_{1,2}}{RT},\tag{1}$$

with

$$A_{1,2} = \left[(\delta_{D2} - \delta_{D1})^2 + 0.25(\delta_{P2} - \delta_{P1})^2 + 0.25(\delta_{H2} - \delta_{H1})^2 \right]$$
 (2)

where V is the molar volume of the solvent; R is the universal gas constant; T is the absolute temperature; and δ_{Di} , δ_{Pi} , and δ_{Hi} are the dispersive, polar, and hydrogen-bonding partial solubility parameters for either the polymer or solvent, respectively. While the customary form of equation 1, utilizing the Hildebrand solubility parameter, adds an empirical term $\beta = 0.34$ that is proposed to correct for combinatorial entropy, Hansen argues that it instead corrects primarily for neglected polar and hydrogen-bonding terms [79]. As these terms are already considered through the use of the HSP, β is excluded from equation 1.

The partial Hansen solubility parameters for PEEK or DPA are not readily available, so they are calculated using group contribution methods. The details on the HSP calculations can be found in the Supplementary Materials. The solubility parameters for PEEK were calculated using the group contribution method of van Krevelen [80] as δ_{D1} = 18.8 MPa^{1/2}, δ_{P1} = 4.3 MPa^{1/2}, and δ_{H1} = 5.9 MPa^{1/2}. Similarly, the solubility parameters for DPA were previously calculated by our group [28] using the group contribution method of Stefanis and Panayiotou [81]. The solubility parameters of DPA are δ_{D2} = 19.6 MPa^{1/2}, δ_{P2} = 3.5 MPa^{1/2}, and δ_{H2} = 4.7 MPa^{1/2}. Using the calculated solubility parameters for PEEK and DPA, at 25 °C, χ_{12} is calculated to be 0.093. As this χ_{12} is low, DPA is confirmed to be a good solvent for PEEK, in agreement with the experimental result of S–L phase separation.

Gels **2024**, 10, 283 5 of 22

Knowing that PEEK and DPA have favorable interactions, the melting point depression for the PEEK/DPA system can be calculated using Flory's melting point depression equation [82]:

 $\frac{1}{T_m} - \frac{1}{T_{m,b}} = \frac{RV_p}{\Delta H_f V_s} \left[(\phi_s) - \chi_{12} (\phi_s)^2 \right]$ (3)

where T_m is the melting temperature of the mixture, $T_{m,b}$ is the bulk melting temperature of the pure polymer, V_p is the molar volume of the polymer repeat unit ($V_p = 205.8 \, \mathrm{cm}^3/\mathrm{mol}$), V_s is the molar volume of the solvent ($V_s = 196.7 \, \mathrm{cm}^3/\mathrm{mol}$), ΔH_f is PEEK's enthalpy of fusion per mol repeat unit (37.48 kJ/mol) [83], and φ_s is the volume fraction of the solvent. Considering the temperature dependence of χ_{12} , an initial input of $\chi_{12} = 0.047$ (at T = 320 °C) was used. Then, T_m was calculated using χ_{12} , and this T_m value was used to find χ_{12} again. Using the experimentally determined melting temperature of pure PEEK (Figure S1), $T_{m,b} = 343 \, ^{\circ}\mathrm{C}$, χ_{12} was found to range from 0.045 to 0.051 over the temperature range 343–269 °C.

Figure 2 shows the experimental melting temperatures for PEEK/DPA solutions at different PEEK compositions. The prediction from Flory's melting point depression equation is plotted for comparison. The melting point depression curve is in excellent agreement with the experimental data. This agreement is further confirmation that DPA is a good solvent for PEEK and that the calculation of χ_{12} using the calculated Hansen solubility parameters for PEEK and DPA is valid.

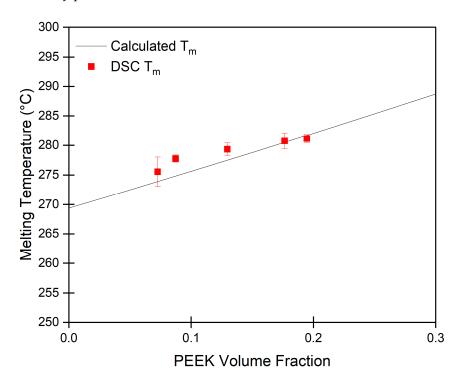


Figure 2. Melting temperature of PEEK in DPA versus PEEK volume fraction. Each data point represents the average of 3 measurements with corresponding error bars (sample standard deviation).

2.2. Morphology of PEEK Aerogels

In order to prepare PEEK aerogels, DPA is removed from the gel structure with ethanol, and the ethanol is replaced with water. The water is frozen and subsequently freeze-dried to yield the solvent-extracted aerogels. To investigate the internal morphology of these PEEK aerogels, microscopy was performed on freeze-fractured aerogels. SEM micrographs of a 15 wt.% PEEK aerogel are shown in Figure 3. PEEK aerogels gelled in DPA consist of a network of struts of a relatively uniform size. The struts are elongated and have branching and splaying at the ends, which is consistent with premature spherulites, or axialites. The layered texture of the axialites implies that they consist of stacks of crystalline polymer lamellae. As S–L phase separation is driven by polymer crystallization, it is not

unexpected to observe axialite morphologies when nucleation density is high. Indeed, axialites [28,52,53] or spherulites [50–53] have been observed as a product of solid–liquid phase separation for other polymer systems.

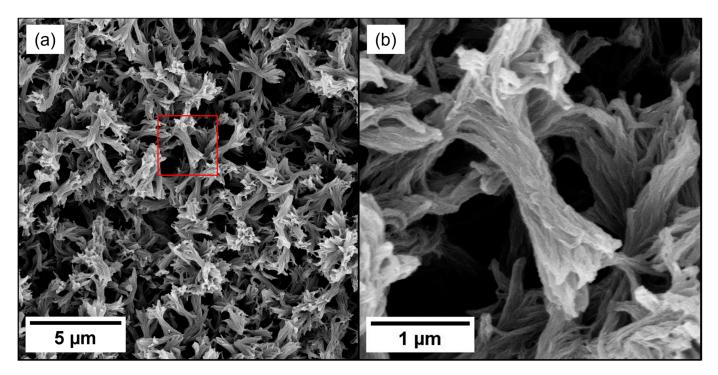


Figure 3. Scanning electron microscopy (SEM) micrographs of a 15 wt.% PEEK aerogel gelled in DPA at (a) 10 kx magnification and (b) 20 kx magnification. The location of (b) is shown in the red box in (a).

Axialite dimensions were quantified using SEM image analysis. Figure 4 compares the size distribution for axialite thickness (Figure 4a) and axialite length (Figure 4b) across differing PEEK concentrations. SEM micrographs are shown for each PEEK concentration in Figure 4c. Across all the polymer concentrations investigated, PEEK aerogels gelled in DPA display strut-like morphologies consisting of PEEK axialites. SEM image analysis is summarized in Table 1. The axialite width remains consistent across all PEEK concentrations, while the axialite length tends to increase slightly with increasing PEEK concentrations. It is interesting that the axialite dimensions only vary minimally with changing PEEK content. These axialite PEEK morphologies have not been observed in other PEEK aerogel systems. Only globular morphologies [32–34] or open cellular structures [44,54,56] have been reported previously.

Table 1. SEM image analysis.

PEEK Concentration (wt.%)	Average Strut Thickness (μm)	Average Strut Length (μm)	
8	0.471 ± 0.094	2.57 ± 0.38	
10	0.499 ± 0.110	3.12 ± 0.49	
15	0.418 ± 0.083	2.39 ± 0.31	
20	0.470 ± 0.111	3.07 ± 0.59	
22	0.476 ± 0.089	3.48 ± 0.70	

To further investigate the hierarchical morphology of PEEK aerogels, X-ray scattering experiments were performed. Aerogels often exhibit a hierarchical structure, where small primary particles form larger aggregates. Performing X-ray scattering experiments across a wide range of length scales can allow for the evaluation of each structural level separately. Merged ultra-small angle X-ray scattering (USAXS)/small angle X-ray scattering

(SAXS)/wide angle X-ray scattering (WAXS) profiles for PEEK aerogels gelled in DPA are shown in Figure 5. Multiple structural features are observed across the length scales probed, indicating the presence of a hierarchical morphology. A knee is observed below 0.03 nm⁻¹. Based on our recent studies of PPS aerogels with similar morphologies [28], this feature is assigned to the thickness of the axialites. This assignment is reasonable, as both the pore size between the lamellar aggregates and the strut length are far too large to correspond to this feature. Between 0.2 nm⁻¹ and 0.8 nm⁻¹, another knee is observed. This feature is associated with the scattering of PEEK crystalline lamellae [34], as the long period of PEEK lamellae is commonly observed at these scattering vectors [84–86]. Following the lamellar knee, oscillations are observed beginning around 0.7 nm⁻¹ and persist to 4 nm⁻¹. These oscillations are likely due to the structure factor that arises due to the periodic spacing of PEEK lamellae within the axialites.

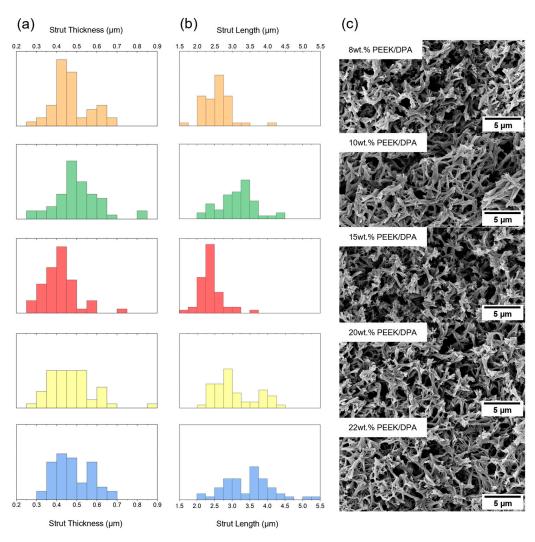


Figure 4. SEM analysis of PEEK aerogels. Histograms of (a) strut thickness and (b) strut length, taken from 50 measurements of strut dimensions from the SEM images. Orange, green, red, yellow, and blue histograms correspond with PEEK aerogels gelled in DPA at PEEK concentrations of 8 wt.%, 10 wt.%, 15 wt.%, 20 wt.%, and 22 wt.%, respectively. (c) SEM images of PEEK aerogels showing the strut-like nature of PEEK aerogels gelled in DPA.

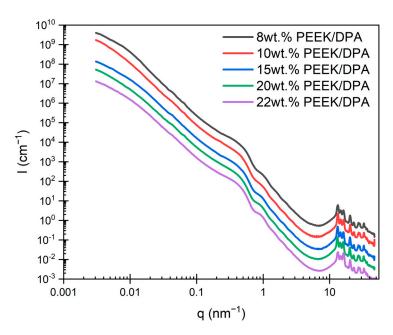


Figure 5. Merged ultra-small angle X-ray scattering (USAXS)/small angle X-ray scattering (SAXS)/ wide angle X-ray scattering (WAXS) profiles for solvent-extracted PEEK aerogels gelled in DPA at different PEEK concentrations.

To differentiate the oscillations from the power-law scattering, the scattering profiles are plotted in a Porod plot (Figure 6b). In the Porod plots, peaks are observed at values of q^* , 2 q^* , 3 q^* , 4 q^* , and 5 q^* . These values are consistent with a lamellar morphology and confirm the periodic ordering of the stacks of chain-folded lamellae within the axialitic aggregates. The Bragg spacing of this feature can be calculated by $d^* = 2 \pi/q^*$, where $q^* \approx 0.47 \text{ nm}^{-1}$, yielding $d^* = 13 \text{ nm}$. This Bragg spacing is consistent with the long period reported for melt crystallized PEEK, which is on the order of 12–16 nm [84,87]. This agreement strengthens the argument that the oscillations originate from a structure factor contribution of the stacked PEEK lamellae. Above 7 nm $^{-1}$, Bragg reflections are observed, corresponding to specific families of planes associated with the orthorhombic crystal structure of PEEK [85,86,88]. Representative WAXS profiles with Bragg reflection assignments are found in Figure S2.

The USAXS/SAXS curves were fit with the unified function [89] in order to quantify the hierarchical morphology of the PEEK aerogels. The unified function is used to analyze each structural level of a complex, hierarchical scattering pattern and extract structural parameters: the radius of gyration (R_g) and Porod exponent (P). Details on the analysis of scattering data using the unified function can be found in the Supplementary Materials.

The radius of gyration (R_{g2}) and the Porod exponent (P_2) were obtained for the feature observed below 0.03 nm⁻¹, which is assigned to the axialite thickness. Strut thickness is obtained by the relation $t_2 = 2\sqrt{4/3}R_{g2}$, assuming that the axialites are approximately rod-shaped [89]. Tabulated values for R_{g2} , P_2 , and t_2 can be found in Table S2. Axialite thickness is relatively consistent across all PEEK contents. Axialite thickness determined from the unified function is in excellent agreement with thickness from SEM image analysis (Table 1), confirming the assignment of the SAXS feature to axialite thickness. Aggregate size, or, specifically, axialite thickness, for PEEK aerogels gelled in DPA was found to be on a comparable length scale to the aggregate size of the other PEEK aerogels gelled in DCA or 4CP [34]. PEEK aerogels gelled in DPA were found to have Porod exponents, or P_2 , greater than 3, which is consistent with a surface fractal. In our previous work, it was found that PEEK aerogels gelled in DCA or 4CP had Porod exponents, or P_2 , associated with surface fractals (P > 3) or mass fractals (A > P > 1) [34].

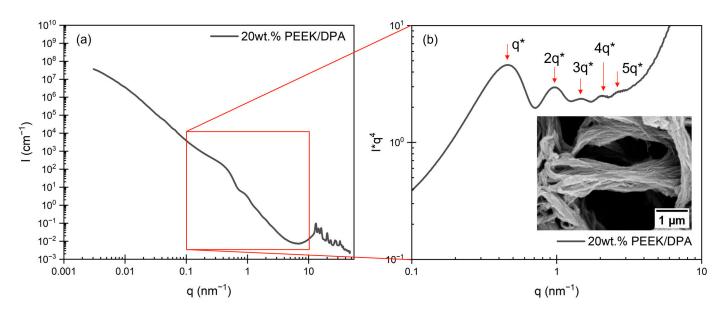


Figure 6. (a) USAXS/SAXS/WAXS profile for a 20 wt.% PEEK aerogel gelled in DPA presented as I vs. q and (b) Porod plot of USAXS/SAXS/WAXS profile for the 20 wt.% PEEK aerogel. Red arrows note the higher order reflections, as multiples of the primary peak found at q^* , associated with a lamellar morphology. The inset is an SEM image of an axialite at high magnification, showing its texture, which is associated with lamellar stacking.

The radius of gyration (R_{g1}) and Porod exponent (P_1) were obtained for the feature observed between 0.2 nm⁻¹ and 0.8 nm⁻¹, which is assigned to the lamellar thickness. Lamellar thickness is obtained using the relation $t_1 = 2R_{g1}$ [89]. Tabulated values for R_{g1} , P_1 , and t_1 can be found in Table S2. The lamellar thickness tends to slightly increase with increasing PEEK content. P_1 was found to be 4.0 for all PEEK aerogels gelled in DPA. Previously, it was found that P_1 was 4.0 for all PEEK aerogels gelled in DCA or 4CP [34]. A Porod exponent of 4 is characteristic of smooth surfaces, which is consistent with the flat interface between crystalline lamellae and amorphous material [90].

At wide angles, PEEK aerogels display diffraction peaks associated with the orthorhombic unit cell characteristic of PEEK crystals. Absolute crystallinity is determined through the use of Vonk's procedure [91]. Figure 7 shows the crystallinity of PEEK aerogels gelled in DPA versus PEEK content, and tabulated values for crystallinity can be found in Table S3. Figure 7 also compares crystallinity determined through integrating DSC melting endotherms (shown in Figure S1) to absolute crystallinity determined by WAXS. While the absolute crystallinity was found to be slightly higher than DSC crystallinity for all PEEK aerogels, it is clear that the degree of crystallinity (about 40%) is typical for melt crystallized PEEK [92-94] and independent of the PEEK content in the gels. The crystallinity values for the PEEK aerogels gelled in DPA are also similar to those reported for PEEK aerogels gelled in DCA but were about 10% higher than the crystallinity of aerogels gelled in 4CP [34]. Crystalline imperfection factor k versus PEEK content is shown in Figure S4. A decreasing value (from about 1.7 to 1) suggests that crystalline order generally tended to increase with increasing PEEK content. All values of *k* found here are comparable to values previously reported for melt crystallized PEEK [92,93].

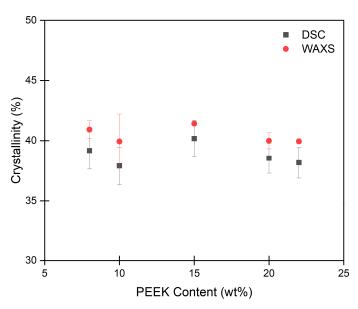


Figure 7. Crystallinity versus PEEK content for PEEK aerogels gelled in DPA. Each data point represents the average of 3 measurements with corresponding error bars (sample standard deviation).

2.3. Porosity and Surface Area of PEEK Aerogels

Nitrogen adsorption is particularly powerful in characterizing nanometer-size pores which are otherwise difficult to characterize. Figure 8a shows nitrogen adsorption isotherms for PEEK aerogels gelled in DPA at different PEEK concentrations. The shapes of the isotherms are characteristic of the pore size and shape. All nitrogen adsorption isotherms collected on PEEK aerogels have a knee at low relative pressure (below $p/p^o = 0.05$) which is associated with the transition between monolayer and multilayer adsorption. Also present is a sickle-shaped hysteresis between 0.4 and 1.0 p/p^o , which is associated with capillary condensation in mesopores [95]. Both of these features are indicative of a IUPAC type IV isotherm, which is characteristic of a mesoporous adsorbent with 2–50 nm pores [95]. Additionally, the hysteresis of the isotherms can be characterized as IUPAC type H3 hysteresis, which is characteristic of slit-like mesopores formed from aggregates of platelike particles [95]. These slit-like mesopores are likely attributed to the nanometer-scale spacing between lamella within the stacks of platelike crystallites of the axialitic aggregates, observed in the PEEK aerogels (Figure 3b).

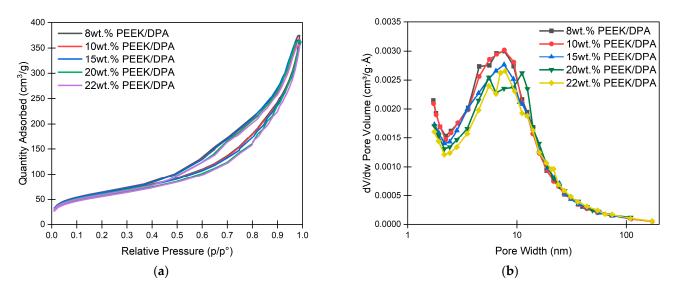
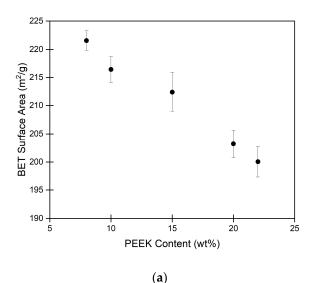


Figure 8. (a) Nitrogen adsorption isotherms for PEEK aerogels gelled in DPA, and (b) pore size distribution versus pore width for PEEK aerogels gelled in DPA.

Pore size distribution can be calculated from nitrogen adsorption isotherms by applying the Barrett–Joyner–Halenda (BJH) method [96]. Figure 8b shows the pore size distributions for PEEK aerogels gelled in DPA. The pore size distributions for all PEEK aerogels gelled in DPA all have a maximum at about 7.5 nm. This pore width is on a similar length scale as what is expected for the amorphous thickness, reported as 4–5 nm in melt crystallized PEEK [84,87]. As the amorphous thickness is the average distance between lamellar surfaces, these pore size measurements are consistent with the pores originating from stacks of lamella.

The application of the Brunauer–Emmett–Teller (BET) theory to nitrogen adsorption isotherms yields the specific surface area of porous materials [97]. The BET surface areas for the PEEK aerogels are shown in Figure 9a. Tabulated values for the surface area can be found in Table S3. PEEK aerogels were found to have high surface areas between 200 and 225 $\rm m^2/g$, which tend to decrease somewhat as the PEEK content increases. Figure 9b compares the BET surface area for each PEEK aerogel system to the aerogel density. PEEK aerogels gelled in DPA were found to have surface areas that were consistently lower than values around 325 $\rm m^2/g$ reported previously for PEEK aerogels gelled in DCA or 4CP [34]. The PEEK aerogels gelled in DCA or 4CP have a higher surface area due to a finer aggregate size and mass fractal structure [34] compared to those of the PEEK aerogels gelled in DPA, as seen in supplemental Figure S3.



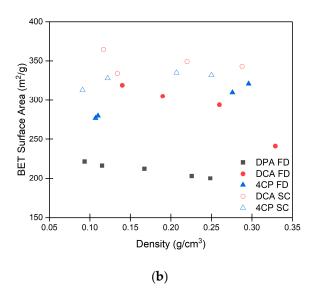
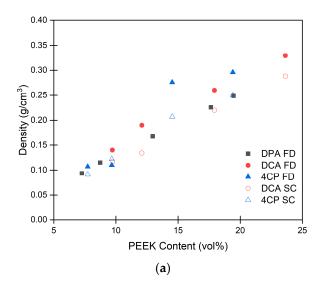


Figure 9. (a) Surface area of PEEK aerogels gelled in DPA vs. PEEK content. (b) Surface area of PEEK aerogels gelled in DPA, dichloroacetic acid (DCA), or 4-chlorophenol (4CP) [34]. Aerogels prepared by freeze-drying (FD) are indicated by a filled symbol, whereas aerogels prepared by extraction with supercritical CO₂ (SC) are indicated by an open symbol. Each data point represents the average of 3 measurements with corresponding error bars (sample standard deviation).

The density of PEEK aerogels formed over a range of PEEK/DPA contents is compared to the density of PEEK aerogels formed from DCA and 4CP in Figure 10a. As expected for all aerogels and solvents, an increase in PEEK content yielded a near-linear increase in the bulk density of the aerogels. For PEEK aerogels gelled in DPA, the densities were found to increase from 0.09 to 0.25 g/cm³ with increasing concentrations (Table S3). The strong correlation between PEEK concentration and density indicates that there is good control of aerogel density for the PEEK/DPA system.



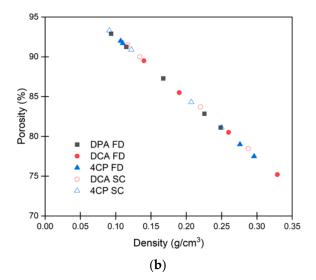


Figure 10. Comparison of density and porosity between aerogels prepared from PEEK/DPA, PEEK/DCA [34], and PEEK/4CP [34] solutions. (a) Density versus PEEK content for PEEK aerogels. Each data point represents the average of 6 density measurements. (b) Porosity versus density for PEEK aerogels. Each data point represents the average of porosity calculated using average density and average crystallinity. Aerogels prepared by freeze-drying (FD) are indicated by a filled symbol, whereas aerogels prepared by extraction with supercritical CO₂ (SC) are indicated by an open symbol.

To compare the effects of gel network morphology on density, strut-like PEEK aerogels prepared from DPA are compared to the globular aerogels prepared from DCA or 4CP (Figure 10a). Freeze-dried PEEK aerogels gelled in DPA tend to have a lower density at a given PEEK content than the freeze-dried PEEK aerogels prepared in DCA or 4CP. When PEEK aerogels gelled in DCA or 4CP are dried using an extraction with supercritical $\rm CO_2$, lower densities are achieved, and these densities are comparable to the densities of freeze-dried PEEK aerogels gelled in DPA at similar PEEK compositions.

The comparison of the solvent extraction methods suggests that the strut-like morphology of the PEEK aerogels formed from DPA resists densification during solvent extraction and thus is more stable to less-rigorous extraction methods (i.e., freeze-drying versus supercritical CO₂ extraction). While freeze-drying is regarded as a relatively gentle extraction route compared to the capillary stresses exerted during evaporative drying, the growth of crystals during freezing can exert stress on the gel structure [60]. Meanwhile, extraction with supercritical CO₂ is the gentlest method for preparing aerogels, since the supercritical route transforms the liquid phase into gas without experiencing the capillary forces associated with a direct transformation between liquid and gas [58]. Apparently, the globular structure of PEEK aerogels prepared from DCA and 4CP is not robust enough to avoid densification caused by the forces exerted during freeze-drying. However, the strut-like morphology of PEEK aerogels prepared from DPA appears to be considerably more stable to the freeze-drying process, as they have similar densities and porosities to the supercritically extracted PEEK aerogels at comparable PEEK contents. This focus on comparing solvent extraction methods will be the subject of a subsequent study.

To determine the effects of aerogel morphology on porosity, porosity is compared to solvent content for the different aerogel systems (Figure S6). PEEK aerogels gelled in DPA were found to be highly porous with porosities ranging between 80 and 93% (Table S3). Generally, aerogel porosity tends to increase with increasing solvent content. Freeze-dried PEEK aerogels prepared from DPA tended to have higher porosity at a given PEEK content than the freeze-dried PEEK aerogels prepared from DCA or 4CP. When aerogels prepared from DCA or 4CP were dried using an extraction with supercritical CO₂, higher porosities were achieved, and these porosities are comparable to the porosity of freeze-dried PEEK aerogels prepared from DPA at similar PEEK compositions.

The relationship between porosity and density was compared to determine if there were significant differences between the different aerogel morphologies. Figure 10b shows aerogel porosity versus aerogel density for aerogels prepared from DPA, DCA, and 4CP. As expected, porosity tends to decrease with increasing aerogel density. All aerogels follow the same linear relationship between density and porosity despite the different aerogel morphologies and the different drying methods. The slight differences in crystallinity and thus, skeletal density, between the systems also appear to have little effect on this relationship.

2.4. Mechanical Properties of PEEK Aerogels

As evidenced above, the strut-like morphology of PEEK aerogels prepared from DPA is believed to lead to robust mechanical properties that resist deformation. To verify this, compression testing was performed on the PEEK aerogels gelled in DPA. Figure 11 shows the modulus versus density plot for PEEK aerogels. Tabulated values for the modulus can be found in Table S3. The strut-like PEEK aerogels formed from DPA had a significantly higher modulus than the globular PEEK aerogels formed from DCA across the investigated densities. At the lowest densities, PEEK aerogels gelled in DPA had a modulus an order of magnitude greater than the PEEK aerogels gelled in DCA. Thus, the strut-like morphology of PEEK aerogels gelled in DPA appears to be more efficient at distributing mechanical stress than the globular morphology of PEEK aerogels prepared in DCA. This behavior may be attributed to a higher inter-particle connectivity of the strut-like morphology compared to weaker network connections in the globular morphology. With greater connectivity, a more efficient stress transfer is produced during compressive deformation.

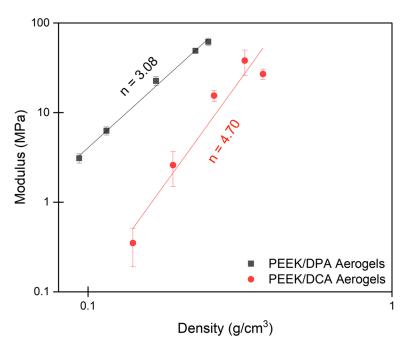


Figure 11. Modulus versus density of PEEK aerogels gelled in DPA compared to PEEK aerogels gelled in DCA [32]. Each data point represents the average of 5 measurements with corresponding error bars (sample standard deviation).

As reported in many other porous systems, PEEK aerogels display a power–law relationship between modulus and density. This relationship is commonly represented as:

$$\frac{E}{E_{solid}} \sim \left(\frac{\rho}{\rho_{solid}}\right)^n \tag{4}$$

where *E* is the modulus of the porous material, E_{solid} is the modulus of the non-porous solid material ($E_{solid,PEEK}$ = 3600 MPa) [98], ρ is the density of the porous material, ρ_{solid}

is the density of the non-porous solid material ($\rho_{solid,PEEK} = 1.3 \text{ g/cm}^3$) [98], and n is the scaling exponent. For cellular materials, Gibson and Ashby found that the scaling exponent was dependent on the mechanism of stress distribution [99]. For cellular materials where bending is the primary deformation mode, n = 2. Aerogels commonly have a scaling relationship that deviates from this ideal behavior due to low mechanical connectivity causing inefficiencies in stress distribution [100,101]. For aerogels, n has been reported to be between 3 and 4. Strut-like PEEK aerogels prepared from DPA were found to have a scaling relationship of 3.08, whereas globular PEEK aerogels prepared from DCA were found to have a scaling relationship of about three [28]. A smaller n indicates that changes in density have a lesser effect on modulus. Indeed, as the density decreases compared to the bulk density, the modulus of the strut-like aerogels decreases from the modulus of PEEK less quickly than for the globular aerogels. It is likely that this improvement in network efficiency imparts strut-like PEEK aerogels prepared from DPA with the ability to better resist the forces of freeze-drying compared to the globular PEEK aerogels prepared from DCA.

This new strut-like morphology greatly improves the mechanical properties of PEEK aerogels. To contextualize the effects of the strut-like morphology, the mechanical properties of PEEK aerogels are compared to those of other aerogels found in the literature. Figure 12 shows the modulus versus density of PEEK aerogels gelled in DPA compared to those of other aerogels in the field. Compared to our previous work on PEEK aerogels formed from DCA and 4CP solutions, the strut-like morphology created by gelation in DPA now elevates PEEK aerogels into a similar modulus and density range as that of the crosslinked polyimide and polyurea aerogels formed by complex chemistry and solvent extraction methods.

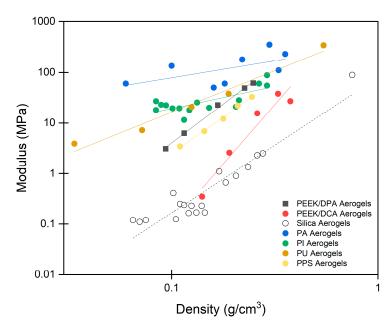


Figure 12. Modulus versus density for strut-like PEEK aerogels prepared in DPA compared to other aerogels from the literature on PEEK aerogels prepared in DCA [32], silica aerogels [102], polyamide (PA) aerogels [103], polyimide (PI) aerogels [104], polyurea (PU) aerogels [105], and polyphenylene sulfide (PPS) aerogels [28].

3. Conclusions

The gelation of PEEK in the benign solvent, DPA, and the preparation of PEEK aerogels composed of crystalline axialites have been demonstrated. The construction of a phase diagram confirmed solid–liquid phase separation as the gelation mechanism, where PEEK crystallization on cooling induces gelation. Solid–liquid phase separation implies that DPA is a good solvent for PEEK. The Flory–Huggins interaction parameter was calculated as $\chi_{12} = 0.093$ for PEEK/DPA, which confirmed that DPA is a good solvent for PEEK.

The evidence from microscopy, X-ray scattering, and nitrogen adsorption was consistent with the aerogel having a hierarchical structure consisting of a network of PEEK axialites, which are composed of stacks of crystalline lamellae. The high connectivity of the axialite network leads to robust PEEK aerogels, which appear to have low densification on freezedrying and an improved compressive modulus compared to the poorly connected globular aerogels derived from PEEK/DCA and PEEK/4CP systems. The low density, high modulus, high surface area, and high porosity of PEEK aerogels prepared from DPA indicate their suitability for lightweight structural applications. The axialite morphology was consistent across all PEEK compositions, displaying similar axialite dimensions and crystallinity, while the density, porosity, surface area, and modulus are able to be tuned by changing the PEEK composition. The gelation of PEEK in DPA leads to strong, low-density aerogels with properties that rival those of high-performance crosslinked aerogels, while utilizing a simpler preparation pathway. This work emphasizes that solvent selection has a significant impact on process-morphology-property relationships in semicrystalline polymer aerogels. Future work will involve a deeper investigation into the effects of the solvent extraction process and a deeper scattering analysis.

4. Materials and Methods

4.1. Materials

PEEK (Victrex 150P) was provided by Solvay Specialty Polymers (Alpharetta, GA, USA). The 1,3-diphenylacetone (DPA) was purchased from Oakwood Chemical (Estill, SC, USA). Ethanol (200 proof, 100% USP, Decon Labs, King of Prussia, PA, USA) was purchased from Fisher Scientific Company LLC (Suwanee, GA, USA). Water-based conductive graphene carbon paint was purchased from Electron Microscopy Sciences (Hatfield, PA, USA). All polymers and chemicals were used as received.

4.2. PEEK Gel Preparation

PEEK and DPA were loaded into a three-neck round-bottomed flask equipped with an argon inlet, an overhead stirrer, and a condenser. The flask was placed in a metal bath set at 320 °C. Argon was allowed to purge the flask during dissolution. Dissolution of PEEK in DPA took place for between 1 and 5 h, depending on PEEK concentration. The solution was stirred using a mechanical stirrer for the final 20 min of dissolution. The hot PEEK solution was poured into open-ended cylindrical glass tubes, which were held in a well heater (Hart Scientific 9122, Everett, WA, USA) set at 50 °C. The tubes had a nominal inner diameter of 9 mm and a length of 100 mm, and to prevent solvent leakage, the bottom end of each tube was closed with a rubber septum. Gelation of the PEEK solution was allowed to occur for over 20 min. Gelation of the solution occurred within 5 min. Samples of the solidified PEEK/DPA gel were taken to measure cloud point and crystallization temperature.

4.3. PEEK Aerogel Preparation

After 20 min of gelation in the tubes, the PEEK/DPA gels, still within the tubes, were placed in an ethanol bath to exchange the DPA with ethanol. The ethanol bath was set to 50 $^{\circ}$ C to prevent DPA crystallization. The ethanol was exchanged with fresh ethanol after 24 h, and the gels were pushed out of the tubes. After an additional 24 h in the ethanol bath, the gels were moved to a Soxhlet extractor to replace any residual DPA with ethanol. Soxhlet extraction was allowed to occur over 4 days. The ethanol-soaked gels were exchanged with deionized water for 4 days in a water bath. The water was replaced with fresh deionized water daily. The hydrogels were frozen overnight at -18 $^{\circ}$ C and were then lyophilized (Labconco Corporation, Kansas City, MO, USA) over 24 h to yield freeze-dried PEEK aerogels.

4.4. Characterization

Cloud point measurements were performed on a Nikon Eclipse LV100 optical microscope (Nikon Corporation, Tokyo, Japan) equipped with a Linkam HFSX350-CAP

temperature stage (Linkam Scientific Instruments, Salfords, UK) with a 1.7 mm diameter capillary port. The turbidity of PEEK/DPA solutions was recorded using an AmScope MU503B digital CMOS camera (AmScope, Irvine, CA, USA) and AmScope software version 4.11.20671.20220413. Solidified PEEK/DPA gels were packed into 1.5 mm diameter Pyrex capillaries, which were sealed with a torch. Capillaries were heated in the hot stage to 320 °C at 60 °C/min, held isothermally for 3 min, and cooled at 10 °C/min to 50 °C. Images of the capillary were taken once per second. Images were processed in ImageJ image analysis software version 1.53q to yield the average brightness of each image. Average brightness versus temperature was plotted (see Figure S7), and the cloud point temperature was taken as the temperature where brightness was reduced 50%.

Differential scanning calorimetry (DSC) experiments were performed on the solidified PEEK/DPA gels using a TA Instruments Q1000 DSC (TA Instruments, New Castle, DE, USA). The PEEK/DPA gels were sealed in hermetic pans to prevent solvent evaporation. Samples were heated at 10 °C/min to 320 °C, where they were isothermally held for 1 min. Samples were then cooled at 10 °C/min to 50 °C, where they were isothermally held for 20 min. Crystallization temperature (T_c) was recorded as the minimum of the crystallization exotherm during this cooling scan. Samples were again heated at 10 °C/min to 320 °C, where they were isothermally held for 1 min. Melting temperature (T_m) was recorded as the maximum of the melting endotherm during this heating scan.

The morphology of PEEK aerogels was evaluated with scanning electron microscopy (SEM) using a LEO (Zeiss, Jena, Germany) 1550 field-emission scanning electron microscopy (FE-SEM) with in-lens detection. Samples were freeze-fractured by immersing them in liquid nitrogen for 15 min followed by shattering with a hammer to reveal internal aerogel surfaces of small fragments. These aerogel fragments were mounted on a stub using conductive graphene carbon paint. The paint was allowed to dry prior to sputter-coating. Mounted samples were sputter-coated with a 5 nm thick layer of iridium with a Leica EM ACE600 sputter coater (Leica, Wetzlar, Germany). SEM images were analyzed using the image analysis software ImageJ to measure the structural features of the PEEK aerogels. To ensure statistical significance of measurements, 50 features were measured.

Small angle X-ray scattering (SAXS) experiments were performed using a Xeuss 3.0 SAXS/WAXS beamline (Xenocs, Genoble, France), equipped with a GeniX 3D Cu HFVLF microfocus X-ray source with a wavelength of 0.154 nm (Cu K_{α}). The sample-todetector distance was 1800 mm for extra-small angle X-ray scattering (ESAXS), 900 mm for SAXS, 370 mm for mid angle X-ray scattering (MAXS), and 43 mm for wide angle X-ray scattering (WAXS). A Bonse-Hart camera was used to collect ultra-small angle Xray scattering (USAXS) data. The q-range was calibrated using a lanthanum hexaboride standard for WAXS and a silver behenate standard for ESAXS, SAXS, and MAXS. Twodimensional scattering patterns were obtained using a Dectris EIGER 4M detector, with an exposure time of 4 h for USAXS, 4 h for ESAXS, 2 h for SAXS, 1 h for MAXS, and 1 h for WAXS. The scattering data were reduced and corrected for background, thickness, and transmission using the XSACT software version 2.10.3. Slit-smeared USAXS data were desmeared using XSACT, yielding pinhole equivalent data. ESAXS, SAXS, MAXS, and WAXS data were output on an absolute scale using direct beam intensity. USAXS, ESAXS, SAXS, MAXS, and WAXS profiles were merged using the XSACT software. The scattering profiles were vertically shifted to facilitate comparison. Scattering plots are presented as scattering intensity, I(q), versus scattering vector q, where $q = (4\pi/\lambda)\sin(\theta)$; θ is one half of the scattering angle, and λ is the X-ray wavelength. Merged USAXS/SAXS/WAXS scattering profiles were fit to the unified function [89] using Irena [106].

Absolute crystallinity was determined using WAXS data corrected for background, thickness, transmission, absorption, and polarization using the XSACT software. Excess power law scattering at low q was subtracted from the WAXS data. This excess scattering, associated with crystalline lamellae, was found in fitting the USAXS/SAXS/WAXS profiles to the Unified Function. Vonk's procedure [91] for determining absolute crystallinity was used. Corrected WAXS profiles were normalized to electron units, and the incoherent

scattering intensity was subtracted. Then, absolute crystallinity was determined using Vonk's graphical method. Full details on the procedure are found in the Supplementary Materials. Amorphous PEEK was prepared by melting PEEK at $400\,^{\circ}\text{C}$ for 3 min, then pressing it into a film and quenching it into liquid nitrogen.

DSC experiments were performed on PEEK aerogels using a TA Instruments Q1000 DSC (TA Instruments, New Castle, DE, USA). The PEEK aerogels were sealed in standard DSC pans. Samples were heated at 10 °C/min to 400 °C. Crystallinity ($\%X_c$) was determined by:

$$\%X_c = \frac{\Delta H_m}{\Delta H_m^0} \times 100 \tag{5}$$

where ΔH_m is the integral of the experimental melting endotherm on first heating, and ΔH_m^o is the melting enthalpy for PEEK, 130 J/g [83].

Nitrogen porosimetry experiments were performed using a Micromeritics 3 Flex gas adsorption analyzer (Micromeritics Instrument Corporation, Norcross, GA, USA). Samples were outgassed at $100\,^{\circ}\text{C}$ for 24 h. Adsorption and desorption isotherms were collected using nitrogen as the adsorbent at $-196\,^{\circ}\text{C}$ (77 K). Surface area was calculated using the Brunauer–Emmett–Teller (BET) method [97], and pore size distribution was calculated using the Barrett–Joyner–Halenda (BJH) method [96].

Compression testing experiments were performed on aerogels using an Instron 3340 Universal Testing System (Instron, Norwood, MA, USA) with a 5 kN load cell. Samples were tested in accordance with ASTM D695-23 [107]. Aerogel samples for compression testing were cylinders with nominal dimensions of 9 mm diameter to 18 mm length (Figure S12). Samples for compression testing were cut to length in the hydrogel state, prior to freeze-drying. Aerogel bulk density, ρ_b , was calculated as:

$$\rho_b = \frac{m}{\pi r^{2l}} \tag{6}$$

where m is the mass of a cylindrical aerogel, r is the cylinder radius, and l is the cylinder length. Porosity, Π , was calculated as:

$$\Pi = \frac{\frac{1}{\rho_b} - \frac{1}{\rho_s}}{\frac{1}{\rho_b}} \times 100\% \tag{7}$$

where ρ_b is the bulk density, and ρ_s is skeletal density, calculated as:

$$\rho_s = \frac{\% X_c \rho_c + (100 - \% X_c) \rho_a}{100} \tag{8}$$

where $%X_c$ is the crystallinity determined by DSC, ρ_c is the crystalline density of PEEK (1.400 g/cm³), and ρ_a is the amorphous density of PEEK (1.263 g/cm³) [83].

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/gels10040283/s1, Details on the HSP group contribution calculation [108–112]; Figure S1: Representative differential scanning calorimetry curves taken on first heating of PEEK aerogels; Figure S2: Wide angle X-ray scattering patterns for PEEK aerogels gelled in DPA and melt crystallized PEEK; Details on the unified function analysis; Table S2: Radius of gyration (R_g), Porod exponent (P), axialite thickness (t_2), and lamellar thickness (t_1) derived from application of the unified function to USAXS/SAXS profiles collected for PEEK aerogels gelled in DPA; Figure S3: SEM micrographs of freeze dried PEEK aerogels at 15 wt.% PEEK gelled in DPA, 4CP, and DCA; Table S3: Density, porosity, surface area, modulus, and crystallinity of PEEK aerogels gelled in DPA; Figure S4: Crystalline imperfection factor, k, versus PEEK content; Figure S5: Bulk density of PEEK aerogels gelled in DPA versus PEEK content; Figure S6: Porosity versus gelation solvent content for PEEK aerogels; Figure S7: Representative average brightness versus temperature profile for cloud point determination; Details on absolute crystallinity determination using Vonk's

procedure; Figure S12: A PEEK aerogel cylinder for compression testing prepared from a 15 wt.% PEEK/DPA solution.

Author Contributions: Conceptualization, G.A.S. and R.B.M.; methodology, G.A.S. and G.F.G.; validation, G.A.S. and G.F.G.; formal analysis, G.A.S.; investigation, G.A.S.; resources, R.B.M.; data curation, G.A.S.; writing—original draft preparation, G.A.S.; writing—review and editing, G.A.S. and R.B.M.; visualization, G.A.S.; supervision, R.B.M.; project administration, R.B.M.; funding acquisition, R.B.M. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Science Foundation under Grant No. DMR-2104856.

Data Availability Statement: Dataset available on request from the authors.

Acknowledgments: This material is based upon work supported by the National Science Foundation under Grant No. DMR-2104856. Purchase of the Xenocs Xeuss 3.0 SAXS/WAXS instrument used to obtain results included in this publication was supported by the National Science Foundation under the award DMR MRI 2018258. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the author(s) and do not necessarily reflect the views of the National Science Foundation. This work used shared facilities at the Nanoscale Characterization and Fabrication Laboratory, which is funded and managed by Virginia Tech's Institute for Critical Technology and Applied Science. Additional support is provided by the Virginia Tech National Center for Earth and Environmental Nanotechnology Infrastructure (NanoEarth), a member of the National Nanotechnology Coordinated Infrastructure (NNCI), supported by NSF (ECCS 1542100 and ECCS 2025151). This work was made possible by the use of Virginia Tech's Materials Characterization Facility, which is supported by the Institute for Critical Technology and Applied Science, the Macromolecules Innovation Institute, and the Office of the Vice President for Research and Innovation.

Conflicts of Interest: The authors declare no conflicts of interest.

References

- 1. Nijenhuis, K.t. Thermoreversible networks: Viscoelastic properties and structure of gels. In *Advances in Polymer Science*; Springer: Berlin/Heidelberg, Germany, 1997; Volume 130.
- 2. Song, G.; Zhang, L.; He, C.; Fang, D.-C.; Whitten, P.G.; Wang, H. Facile fabrication of tough hydrogels physically cross-linked by strong cooperative hydrogen bonding. *Macromolecules* **2013**, *46*, 7423–7435. [CrossRef]
- 3. Wen, J.; Jiang, S.; Wang, J.; Li, X.; Bi, Z.; Jin, Y.; Fan, L.; Wang, L.; Wu, Y.; Gan, F. Polyimide solution with reversible sol-gel transition by construction of dynamic *π*-*π* stacking. *Polymer* **2023**, *278*, 126006. [CrossRef]
- 4. Itagaki, H.; Tokami, T.; Mochizuki, J. A trial to clarify a cause of forming physical gels: Morphology of syndiotactic polystyrene in n-alkylbenzene. *Polymer* **2012**, *53*, *5304*–*5312*. [CrossRef]
- 5. Cirkel, P.A.; Okada, T. A comparison of mechanical and electrical percolation during the gelling of Nafion solutions. *Macromolecules* **2000**, 33, 4921–4925. [CrossRef]
- 6. Hikmet, R.; Callister, S.; Keller, A. Thermoreversible gelation of atactic polystyrene: Phase transformation and morphology. *Polymer* 1988, 29, 1378–1388. [CrossRef]
- 7. Guenet, J.-M. Thermoreversible Gelation of Polymers and Biopolymers; Academic Press: London, UK, 1992.
- 8. Hong, P.-D.; Chen, J.-H. Structure and properties of polyvinyl chloride physical gels. *Polymer* 1998, 39, 711–717. [CrossRef]
- 9. Matsuo, M.; Miyoshi, S.; Azuma, M.; Bin, Y.; Agari, Y.; Sato, Y.; Kondo, A. Phase separation of several kinds of polyethylene solution under the gelation/crystallization process. *Macromolecules* **2005**, *38*, 6688–6699. [CrossRef]
- 10. Daniel, C.; Longo, S.; Guerra, G. High porosity polyethylene aerogels. Polyolefins J. 2015, 2, 49–55.
- 11. Domszy, R.; Alamo, R.; Edwards, C.; Mandelkern, L. Thermoreversible gelation and crystallization of homopolymers and copolymers. *Macromolecules* **1986**, *19*, 310–325. [CrossRef]
- 12. Matsuda, H.; Inoue, T.; Okabe, M.; Ukaji, T. Study of polyolefin gel in organic solvents I. Structure of isotactic polypropylene gel in organic solvents. *Polym. J.* 1987, 19, 323–329. [CrossRef]
- 13. Xiao, Z.; Sun, N. Crystallization behavior for metallocene-catalyzed isotactic polypropylene in alkane solvents of various molecular sizes. *J. Therm. Anal. Calorim.* **2016**, 124, 295–303. [CrossRef]
- 14. Daniel, C.; Dammer, C.; Guenet, J.-M. On the definition of thermoreversible gels: The case of syndiotactic polystyrene. *Polymer* **1994**, *35*, 4243–4246. [CrossRef]
- 15. Daniel, C.; Deluca, M.; Guenet, J.-M.; Brulet, A.; Menelle, A. Thermoreversible gelation of syndiotactic polystyrene in benzene. *Polymer* 1996, 37, 1273–1280. [CrossRef]
- 16. Daniel, C.; Menelle, A.; Brulet, A.; Guenet, J.-M. Thermoreversible gelation of syndiotactic polystyrene in toluene and chloroform. *Polymer* **1997**, *38*, 4193–4199. [CrossRef]

17. D'Aniello, C.; Daniel, C.; Guerra, G. ε form gels and aerogels of syndiotactic polystyrene. *Macromolecules* **2015**, 48, 1187–1193. [CrossRef]

- 18. Ma, P.X.; Zhang, R. Synthetic nano-scale fibrous extracellular matrix. J. Biomed. Mater. Res. Off. J. Soc. Biomater. Jpn. Soc. Biomater. Aust. Soc. Biomater. 1999, 46, 60–72. [CrossRef]
- 19. Fang, X.; Wyatt, T.; Shi, J.; Yao, D. Fabrication of high-strength polyoxymethylene fibers by gel spinning. *J. Mater. Sci.* **2018**, *53*, 11901–11916. [CrossRef]
- 20. Stamhuis, J.E.; Pennings, A.J. Gelation and Crystallisation of Nylon-6 from Dilute Solution. *Br. Polym. J.* **1978**, *10*, 221–225. [CrossRef]
- 21. Tazaki, M.; Wada, R.; Abe, M.O.; Homma, T. Crystallization and gelation of poly(vinylidene fluoride) in organic solvents. *J. Appl. Polym. Sci.* **1997**, *65*, 1517–1524. [CrossRef]
- 22. Yadav, P.J.P.; Patra, A.K.; Sastry, P.U.; Ghorai, B.K.; Maiti, P. Solvent Retention, Thermodynamics, Rheology and Small Angle X-ray Scattering Studies on Thermoreversible Poly(vinylidene fluoride) Gels. *J. Phys. Chem. B* **2010**, *114*, 11420–11429. [CrossRef]
- 23. Xue, G.; Ji, G.; Li, Y. Rapid crystallization and thermoreversible gelation of poly(ethylene terephthalate) in polymer/oligomer binary system. *J. Polym. Sci. Part B Polym. Phys.* **1998**, *36*, 1219–1225. [CrossRef]
- 24. Daniel, C.; Longo, S.; Fasano, G.; Vitillo, J.G.; Guerra, G. Nanoporous Crystalline Phases of Poly(2,6-Dimethyl-1,4-phenylene)oxide. *Chem. Mater.* 2011, 23, 3195–3200. [CrossRef]
- 25. Daniel, C.; Longo, S.; Cardea, S.; Vitillo, J.G.; Guerra, G. Monolithic nanoporous–crystalline aerogels based on PPO. *RSC Adv.* **2012**, 2, 12011–12018. [CrossRef]
- 26. Buyse, K.; Berghmans, H.; Bosco, M.; Paoletti, S. Mechanistic aspects of the thermoreversible gelation of syndiotactic poly(methyl methacrylate) in toluene. *Macromolecules* **1998**, *31*, 9224–9230. [CrossRef]
- 27. Saiani, A.; Spěváček, J.; Guenet, J.-M. Phase behavior and polymer/solvent interactions in thermoreversible gels of syndiotactic poly(methyl methacrylate). *Macromolecules* **1998**, *31*, 703–710. [CrossRef]
- 28. Godshall, G.F.; Spiering, G.A.; Crater, E.R.; Moore, R.B. Low-Density, Semicrystalline Poly(phenylene sulfide) Aerogels Fabricated Using a Benign Solvent. *ACS Appl. Polym. Mater.* **2023**, *5*, 7994–8004. [CrossRef]
- 29. Mochizuki, J.; Sano, T.; Tokami, T.; Itagaki, H. Decisive properties of solvent able to form gels with syndiotactic polystyrene. *Polymer* **2015**, *67*, 118–127. [CrossRef]
- 30. Kobayashi, M. Structure of gels, characterization techniques. In *Gels Handbook*; Elsevier: Amsterdam, The Netherlands, 2001; pp. 172–412.
- 31. Okabe, M.; Wada, R.; Tazaki, M.; Homma, T. The Flory-Huggins interaction parameter and thermoreversible gelation of poly(vinylidene fluoride) in organic solvents. *Polym. J.* **2003**, *35*, 798–803. [CrossRef]
- 32. Talley, S.J.; AndersonSchoepe, C.L.; Berger, C.J.; Leary, K.A.; Snyder, S.A.; Moore, R.B. Mechanically robust and superhydrophobic aerogels of poly(ether ether ketone). *Polymer* **2017**, *126*, 437–445. [CrossRef]
- 33. Talley, S.J.; Yuan, X.; Moore, R.B. Thermoreversible Gelation of Poly(ether ether ketone). *ACS Macro Lett.* **2017**, *6*, 262–266. [CrossRef]
- 34. Talley, S.J.; Vivod, S.L.; Nguyen, B.A.; Meador, M.A.B.; Radulescu, A.; Moore, R.B. Hierarchical Morphology of Poly(ether ether ketone) Aerogels. *ACS Appl. Mater. Interfaces* **2019**, *11*, 31508–31519. [CrossRef]
- 35. Substances Added to Food (Formerly EAFUS): 1,3-Diphenyl-2-propanone. Available online: https://www.cfsanappsexternal.fda. gov/scripts/fdcc/index.cfm?set=FoodSubstances&id=DIPHENYLPROPANONE (accessed on 27 March 2024).
- 36. Pomatto, M.E.; Crater, E.R.; Godshall, G.F.; Moore, R.B. Blocky bromination of poly(ether ketone ketone) as a means to preserve crystallizability and rapid crystallization kinetics. *Polym. Chem.* **2024**, *15*, 609–621. [CrossRef]
- 37. Kim, S.S.; Lloyd, D.R. Microporous membrane formation via thermally-induced phase separation. III. Effect of thermodynamic interactions on the structure of isotactic polypropylene membranes. *J. Membr. Sci.* **1991**, *64*, 13–29. [CrossRef]
- 38. Matsuyama, H.; Maki, T.; Teramoto, M.; Asano, K. Effect of polypropylene molecular weight on porous membrane formation by thermally induced phase separation. *J. Membr. Sci.* **2002**, 204, 323–328. [CrossRef]
- 39. Gu, M.; Zhang, J.; Wang, X.; Tao, H.; Ge, L. Formation of poly(vinylidene fluoride) (PVDF) membranes via thermally induced phase separation. *Desalination* **2006**, *192*, 160–167. [CrossRef]
- 40. Tanaka, T.; Lloyd, D.R. Formation of poly(l-lactic acid) microfiltration membranes via thermally induced phase separation. *J. Membr. Sci.* **2004**, 238, 65–73. [CrossRef]
- 41. Matsuyama, H.; Okafuji, H.; Maki, T.; Teramoto, M.; Kubota, N. Preparation of polyethylene hollow fiber membrane via thermally induced phase separation. *J. Membr. Sci.* **2003**, 223, 119–126. [CrossRef]
- 42. Jeon, S.; Karkhanechi, H.; Fang, L.-F.; Cheng, L.; Ono, T.; Nakamura, R.; Matsuyama, H. Novel preparation and fundamental characterization of polyamide 6 self-supporting hollow fiber membranes via thermally induced phase separation (TIPS). *J. Membr. Sci.* 2018, 546, 1–14. [CrossRef]
- 43. Yang, Z.; Li, P.; Xie, L.; Wang, Z.; Wang, S.-C. Preparation of iPP hollow-fiber microporous membranes via thermally induced phase separation with co-solvents of DBP and DOP. *Desalination* **2006**, *192*, 168–181. [CrossRef]
- 44. Rusakov, D.; Menner, A.; Bismarck, A. High-Performance Polymer Foams by Thermally Induced Phase Separation. *Macromol. Rapid Commun.* **2020**, *41*, 2000110. [CrossRef]
- 45. Onder, O.C.; Yilgor, E.; Yilgor, I. Critical parameters controlling the properties of monolithic poly(lactic acid) foams prepared by thermally induced phase separation. *J. Polym. Sci. Part B Polym. Phys.* **2019**, *57*, 98–108. [CrossRef]

46. Su, M.; Pan, Y.; Zheng, G.; Liu, C.; Shen, C.; Liu, X. An ultra-light, superhydrophobic and thermal insulation ultra-high molecular weight polyethylene foam. *Polymer* **2021**, *218*, 123528. [CrossRef]

- 47. Su, D.; Yang, J.; Liu, S.; Ren, L.; Qin, S. Preparation of polyamide 12 powder for additive manufacturing applications via thermally induced phase separation. *e-Polymers* **2022**, 22, 553–565. [CrossRef]
- 48. Lin, Y.; Chen, G.; Yang, J.; Wang, X. Formation of isotactic polypropylene membranes with bicontinuous structure and good strength via thermally induced phase separation method. *Desalination* **2009**, 236, 8–15. [CrossRef]
- 49. Lin, Y.; Tang, Y.; Ma, H.; Yang, J.; Tian, Y.; Ma, W.; Wang, X. Formation of a bicontinuous structure membrane of polyvinylidene fluoride in diphenyl carbonate diluent via thermally induced phase separation. *J. Appl. Polym. Sci.* **2009**, *114*, 1523–1528. [CrossRef]
- 50. Lloyd, D.R.; Kinzer, K.E.; Tseng, H. Microporous membrane formation via thermally induced phase separation. I. Solid-liquid phase separation. *J. Membr. Sci.* **1990**, *52*, 239–261. [CrossRef]
- 51. Caplan, M.R.; Chiang, C.-Y.; Lloyd, D.R.; Yen, L.Y. Formation of microporous Teflon[®] PFA membranes via thermally induced phase separation. *J. Membr. Sci.* **1997**, 130, 219–237. [CrossRef]
- 52. Chiang, C.-y.; Lloyd, D.R. Effects of process conditions on the formation of microporous membranes via solid-liquid thermally induced phase separation. *J. Porous Mater.* **1996**, *2*, 273–285. [CrossRef]
- 53. Rezabeigi, E.; Drew, R.A.L.; Wood-Adams, P.M. Highly Porous Polymer Structures Fabricated via Rapid Precipitation from Ternary Systems. *Ind. Eng. Chem. Res.* **2017**, *56*, 11451–11459. [CrossRef]
- 54. Rusakov, D.; Menner, A.; Spieckermann, F.; Wilhelm, H.; Bismarck, A. Morphology and properties of foamed high crystallinity PEEK prepared by high temperature thermally induced phase separation. *J. Appl. Polym. Sci.* **2022**, *139*, 51423. [CrossRef]
- 55. Wang, Y.; Shen, J.; Yan, M.; Tian, X. Poly ether ether ketone and its composite powder prepared by thermally induced phase separation for high temperature selective laser sintering. *Mater. Des.* **2021**, 201, 109510. [CrossRef]
- 56. Meng, L.; Zhang, J.; Zhao, S.; Qi, D.; Xu, P.; Wu, S.; Wang, L.; Yue, X.; Jiang, Z. A Novel PEEK Foam with Ultra-High Temperature-Resistant by Temperature Induced Phase Separation. *Macromol. Mater. Eng.* **2023**, *308*, 2200559. [CrossRef]
- 57. Ding, H.; Zhang, Q.; Tian, Y.; Shi, Y.; Liu, B. Preparation of porous structure in the system of PEEK/PPS/diphenyl ketone via thermally induced phase separation. *J. Appl. Polym. Sci.* **2007**, *104*, 1523–1530. [CrossRef]
- 58. Bisson, A.; Rigacci, A.; Lecomte, D.; Rodier, E.; Achard, P. Drying of silica gels to obtain aerogels: Phenomenology and basic techniques. *Dry. Technol.* **2003**, *21*, 593–628. [CrossRef]
- 59. Job, N.; Pirard, R.; Marien, J.; Pirard, J.-P. Porous carbon xerogels with texture tailored by pH control during sol–gel process. *Carbon* **2004**, 42, 619–628. [CrossRef]
- 60. Scherer, G.W. Freezing gels. J. Non-Cryst. Solids 1993, 155, 1–25. [CrossRef]
- 61. Hüsing, N.; Schubert, U. Aerogels—Airy materials: Chemistry, structure, and properties. *Angew. Chem. Int. Ed.* **1998**, 37, 22–45. [CrossRef]
- 62. Pierre, A.C.; Pajonk, G.M. Chemistry of aerogels and their applications. Chem. Rev. 2002, 102, 4243-4266. [CrossRef]
- 63. Fesmire, J.E. Aerogel insulation systems for space launch applications. Cryogenics 2006, 46, 111–117. [CrossRef]
- 64. Baetens, R.; Jelle, B.P.; Gustavsen, A. Aerogel insulation for building applications: A state-of-the-art review. *Energy Build.* **2011**, 43, 761–769. [CrossRef]
- 65. Cuce, E.; Cuce, P.M.; Wood, C.J.; Riffat, S.B. Toward aerogel based thermal superinsulation in buildings: A comprehensive review. *Renew. Sustain. Energy Rev.* **2014**, *34*, 273–299. [CrossRef]
- 66. Randall, J.P.; Meador, M.A.B.; Jana, S.C. Tailoring Mechanical Properties of Aerogels for Aerospace Applications. *ACS Appl. Mater. Interfaces* **2011**, *3*, 613–626. [CrossRef]
- 67. Liu, Y.; Hao, M.; Chen, Z.; Ramakrishna, S.; Liu, Y.; Wang, X.; Hu, X.; Wei, Y. Recent advances in the development of nanofiber-based aerogel for oil-water separation: A review. *Fuel* **2023**, *354*, 129338. [CrossRef]
- 68. Zhang, J.; Qin, L.; Yang, Y.; Liu, X. Porous carbon nanospheres aerogel based molecularly imprinted polymer for efficient phenol adsorption and removal from wastewater. *Sep. Purif. Technol.* **2021**, 274, 119029. [CrossRef]
- 69. Tian, C.; She, J.; Wu, Y.; Luo, S.; Wu, Q.; Qing, Y. Reusable and cross-linked cellulose nanofibrils aerogel for the removal of heavy metal ions. *Polym. Compos.* **2018**, *39*, 4442–4451. [CrossRef]
- 70. Maatar, W.; Boufi, S. Microporous cationic nanofibrillar cellulose aerogel as promising adsorbent of acid dyes. *Cellulose* **2017**, 24, 1001–1015. [CrossRef]
- 71. Hees, T.; Zhong, F.; Rudolph, T.; Walther, A.; Mülhaupt, R. Nanocellulose aerogels for supporting iron catalysts and in situ formation of polyethylene nanocomposites. *Adv. Funct. Mater.* **2017**, 27, 1605586. [CrossRef]
- 72. Yu, H.; Oh, S.; Han, Y.; Lee, S.; Jeong, H.S.; Hong, H.-J. Modified cellulose nanofibril aerogel: Tunable catalyst support for treatment of 4-Nitrophenol from wastewater. *Chemosphere* **2021**, *285*, 131448. [CrossRef]
- 73. Kim, S.J.; Chase, G.; Jana, S.C. Polymer aerogels for efficient removal of airborne nanoparticles. *Sep. Purif. Technol.* **2015**, *156*, 803–808. [CrossRef]
- 74. Zhai, C.; Jana, S.C. Tuning porous networks in polyimide aerogels for airborne nanoparticle filtration. *ACS Appl. Mater. Interfaces* **2017**, *9*, 30074–30082. [CrossRef]
- 75. Noble, K.F.; Troya, D.; Talley, S.J.; Ilavsky, J.; Moore, R.B. High-Resolution Comonomer Sequencing of Blocky Brominated Syndiotactic Polystyrene Copolymers Using 13C NMR Spectroscopy and Computer Simulations. *Macromolecules* **2020**, *53*, 9539–9552. [CrossRef]

76. Kasprzak, C.R.; Anderson, L.J.; Moore, R.B. Tailored sequencing of highly brominated Poly(ether ether ketone) as a means to preserve crystallizability and enhance Tg. *Polymer* **2022**, 251, 124918. [CrossRef]

- 77. Tang, Y.; Lin, Y.; Ma, W.; Wang, X. A review on microporous polyvinylidene fluoride membranes fabricated via thermally induced phase separation for MF/UF application. *J. Membr. Sci.* **2021**, *639*, 119759. [CrossRef]
- 78. Lloyd, D.R.; Kim, S.S.; Kinzer, K.E. Microporous membrane formation via thermally-induced phase separation. II. Liquid—Liquid phase separation. *J. Membr. Sci.* **1991**, *64*, 1–11. [CrossRef]
- 79. Hansen, C.M. Hansen Solubility Parameters: A User's Handbook; CRC Press: Boca Raton, FL, USA, 2007.
- 80. Van Krevelen, D.W.; Te Nijenhuis, K. *Properties of Polymers: Their Correlation with Chemical Structure*; Their Numerical Estimation and Prediction from Additive Group Contributions; Elsevier: Amsterdam, The Netherlands, 2009.
- 81. Stefanis, E.; Panayiotou, C. Prediction of Hansen solubility parameters with a new group-contribution method. *Int. J. Thermophys.* **2008**, 29, 568–585. [CrossRef]
- 82. Flory, P.J. Thermodynamics of crystallization in high polymers. IV. A theory of crystalline states and fusion in polymers, copolymers, and their mixtures with diluents. *J. Chem. Phys.* **1949**, *17*, 223–240. [CrossRef]
- 83. Blundell, D.J.; Osborn, B.N. The morphology of poly(aryl-ether-ether-ketone). Polymer 1983, 24, 953–958. [CrossRef]
- 84. Verma, R.; Marand, H.; Hsiao, B. Morphological changes during secondary crystallization and subsequent melting in poly(ether ether ketone) as studied by real time small angle X-ray scattering. *Macromolecules* **1996**, *29*, 7767–7775. [CrossRef]
- 85. Wang, W.; Schultz, J.M.; Hsiao, B.S. Time-resolved simultaneous SAXS/WAXS studies of PEEK during isothermal crystallization, melting, and subsequent cooling. *J. Macromol. Sci. Part B Phys.* **1998**, 37, 667–682. [CrossRef]
- 86. Fougnies, C.; Damman, P.; Dosiere, M.; Koch, M. Time-resolved SAXS, WAXS, and DSC study of melting of poly(aryl ether ether ketone)(PEEK) annealed from the amorphous state. *Macromolecules* **1997**, *30*, 1392–1399. [CrossRef]
- 87. Hsiao, B.S.; Sauer, B.B.; Verma, R.K.; Zachmann, H.G.; Seifert, S.; Chu, B.; Harney, P. New Insight of Isothermal Melt Crystallization in Poly(aryl ether ether ketone) via Time-Resolved Simultaneous Small-Angle X-ray Scattering/Wide-Angle X-ray Diffraction Measurements. *Macromolecules* 1995, 28, 6931–6936. [CrossRef]
- 88. Hay, J.; Langford, J.; Lloyd, J. Variation in unit cell parameters of aromatic polymers with crystallization temperature. *Polymer* **1989**, *30*, 489–493. [CrossRef]
- 89. Beaucage, G. Approximations leading to a unified exponential/power-law approach to small-angle scattering. *J. Appl. Crystallogr.* **1995**, *28*, 717–728. [CrossRef]
- 90. Ogawa, T. Small-angle X-ray scattering from the surfaces of polymer crystals. J. Phys. Soc. Jpn. 1990, 59, 3642–3649. [CrossRef]
- 91. Vonk, C.G. Computerization of Ruland's X-ray method for determination of the crystallinity in polymers. *J. Appl. Crystallogr.* **1973**, *6*, 148–152. [CrossRef]
- 92. James, M.; Anderson, D. Determination of crystallinity in graphite fiber-reinforced thermoplastic composites. *Adv. X-ray Anal.* **1985**, *29*, 291–303. [CrossRef]
- 93. Kumar, S.; Anderson, D.P.; Adams, W.W. Crystallization and morphology of poly(aryl-ether-ether-ketone). *Polymer* **1986**, 27, 329–336. [CrossRef]
- 94. Spahr, D.; Schultz, J.M. Determination of matrix crystallinity of composites by X-ray diffraction. *Polym. Compos.* **1990**, *11*, 201–210. [CrossRef]
- 95. Sing, K.S.; Everett, D.; Haul, R.; Moscou, L.; Pierotti, R.; Rouquerol, J.; Siemieniewska, T. Reporting physisorption data for gas/solid systems with special reference to the determination of surface area and porosity (Recommendations 1984). *Pure Appl. Chem.* **1985**, 57, 603–619. [CrossRef]
- 96. Barrett, E.P.; Joyner, L.G.; Halenda, P.P. The determination of pore volume and area distributions in porous substances. I. Computations from nitrogen isotherms. *J. Am. Chem. Soc.* **1951**, *73*, 373–380. [CrossRef]
- 97. Brunauer, S.; Emmett, P.H.; Teller, E. Adsorption of gases in multimolecular layers. J. Am. Chem. Soc. 1938, 60, 309–319. [CrossRef]
- 98. Nikonovich, M.; Costa, J.F.S.; Fonseca, A.C.; Ramalho, A.; Emami, N. Structural, thermal, and mechanical characterisation of PEEK-based composites in cryogenic temperature. *Polym. Test.* **2023**, *125*, 108139. [CrossRef]
- 99. Gibson, I.; Ashby, M.F. The mechanics of three-dimensional cellular materials. *Proc. R. Soc. Lond. A Math. Phys. Sci.* **1982**, 382, 43–59.
- 100. Woignier, T.; Reynes, J.; Alaoui, A.H.; Beurroies, I.; Phalippou, J. Different kinds of structure in aerogels: Relationships with the mechanical properties. *J. Non-Cryst. Solids* **1998**, 241, 45–52. [CrossRef]
- 101. Fan, H.; Hartshorn, C.; Buchheit, T.; Tallant, D.; Assink, R.; Simpson, R.; Kissel, D.J.; Lacks, D.J.; Torquato, S.; Brinker, C.J. Modulus–density scaling behaviour and framework architecture of nanoporous self-assembled silicas. *Nat. Mater.* **2007**, *6*, 418–423. [CrossRef] [PubMed]
- 102. Fricke, J. Aerogels—highly tenuous solids with fascinating properties. J. Non-Cryst. Solids 1988, 100, 169–173. [CrossRef]
- 103. Williams, J.C.; Meador, M.A.B.; McCorkle, L.; Mueller, C.; Wilmoth, N. Synthesis and Properties of Step-Growth Polyamide Aerogels Cross-linked with Triacid Chlorides. *Chem. Mater.* **2014**, *26*, 4163–4171. [CrossRef]
- 104. Guo, H.; Meador, M.A.B.; McCorkle, L.; Quade, D.J.; Guo, J.; Hamilton, B.; Cakmak, M.; Sprowl, G. Polyimide Aerogels Cross-Linked through Amine Functionalized Polyoligomeric Silsesquioxane. *ACS Appl. Mater. Interfaces* **2011**, *3*, 546–552. [CrossRef] [PubMed]
- 105. Leventis, N.; Sotiriou-Leventis, C.; Chandrasekaran, N.; Mulik, S.; Larimore, Z.J.; Lu, H.; Churu, G.; Mang, J.T. Multifunctional polyurea aerogels from isocyanates and water. A structure—property case study. *Chem. Mater.* **2010**, 22, 6692–6710. [CrossRef]

106. Ilavsky, J.; Jemian, P.R. Irena: Tool suite for modeling and analysis of small-angle scattering. *J. Appl. Crystallogr.* **2009**, *42*, 347–353. [CrossRef]

- 107. ASTM D695-23; Standard Test Method for Compressive Properties of Rigid Plastics. American Society for Testing and Materials: West Conshohocken, PA, USA, 2023.
- 108. Ruland, W. X-ray determination of crystallinity and diffuse disorder scattering. Acta Crystallogr. 1961, 14, 1180–1185. [CrossRef]
- 109. Roe, R.-J. Methods of X-ray and Neutron Scattering in Polymer Science; Oxford University Press: New York, NY, USA, 2000.
- 110. Tence-Girault, S.; Quibel, J.; Cherri, A.; Roland, S.; Fayolle, B.; Bizet, S.; Iliopoulos, I. Quantitative structural study of cold-crystallized PEKK. ACS Appl. Poly. Mater. 2021, 3, 1795–1808. [CrossRef]
- 111. Prince, E. *International Tables for Crystallography, Volume C: Mathematical, Physical and Chemical Tables;* Springer Science & Business Media: Berlin/Heidelberg, Germany, 2004.
- 112. Hubbell, J.H.; Veigele, W.J.; Briggs, E.; Brown, R.; Cromer, D.; Howerton, d.R. Atomic form factors, incoherent scattering functions, and photon scattering cross sections. *J. Phys. Chem. Ref. Data* **1975**, *4*, 471–538. [CrossRef]

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.

Supporting Information

High Modulus, Strut-Like poly(ether ether ketone) Aerogels Produced from a Benign Solvent

Glenn A. Spiering, Garrett F. Godshall and Robert B. Moore *

Department of Chemistry, Macromolecules Innovation Institute, Virginia Tech, Blacksburg, VA 24061, USA

*rbmoore3@vt.edu

Keywords: aerogel; semicrystalline polymer aerogel; solvents; poly(ether ether ketone); Hansen solubility parameters; X-ray scattering; hierarchical morphology; axialite

HSP Group Contribution Calculation

The Van Krevelen group contribution method [1] was used to estimate the Hansen solubility parameters for PEEK. The following equations are used to estimate the Hansen solubility parameters for PEEK:

$$\delta_d = \frac{\sum F_{di}}{V} \tag{S1}$$

$$\delta_p = \frac{\sqrt{\sum F_{pi}^2}}{V} \tag{S2}$$

$$\delta_h = \sqrt{\frac{\sum E_{hi}}{V}} \tag{S3}$$

where F_{di} is the dispersion component for the *i*th structural group, F_{pi} is the polar component for the *i*th structural group, E_{hi} is the hydrogen bonding energy for the *i*th structural group, and V is the molar volume of PEEK, calculated as 228.3 cm³/mol from the molecular weight of PEEK (288.3 g/mol) and the amorphous density of PEEK (1.263 g/cm³) [2].

Table S1. Group contribution for the atomic composition of PEEK

Group	Number	F_d	F_p^2	Eh
Disubstituted phenyl	3	1270	12100	0
Ether	2	100	160000	3000
Carbonyl	1	290	592900	2000
Sum		4300	949200	8000
		$\delta_{ m d}$	$\delta_{ m p}$	δ_{h}
Calc	ulated HSP	18.8	4.3	5.9

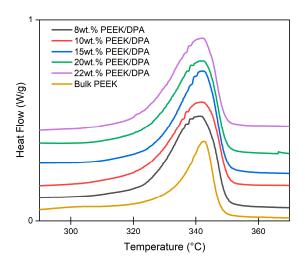


Figure S1. Representative differential scanning calorimetry curves taken on first heating of PEEK aerogels. Endotherm is positive on the y-axis. For comparison, a differential scanning calorimetry curve taken on second heating of a bulk PEEK pellet is shown. Melt crystallized PEEK was prepared by melting PEEK at 400 °C for 3 min, then cooling to 50 °C at 10 °C/min then heating to 400 °C at 10 °C/min.

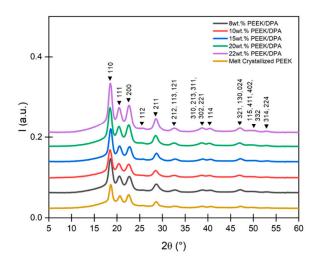


Figure S2. Wide angle X-ray scattering patterns for PEEK aerogels gelled in DPA and melt crystallized PEEK. Diffraction peaks are characteristic of the orthorhombic crystal structure of PEEK [3]. Melt crystallized PEEK was prepared by melting PEEK at 400 °C for 3 min, then cooling to 315 °C and crystallizing for 10 min. The cooling rate used was 10 °C/min.

Unified Function Analysis

The USAXS/SAXS curves were fit with the unified function [4] in order to quantify the hierarchical morphology of the PEEK aerogels. The unified function is used to analyze each structural level of a complex, hierarchical scattering pattern and extract structural parameters, the radius of gyration (R_g) and Porod exponent (P). Details on the unified function can be found in the Supporting Information of Talley et al [5].

Radius of gyration (R_{gl}) and Porod exponent (P_l) were obtained for the feature observed between 0.2 nm⁻¹ – 0.8 nm⁻¹, which is assigned to the lamellar thickness. Lamellar thickness is obtained using the relation $t_1 = 2R_{g1}$ [4]. Tabulated values for R_{gl} , P_l , and t_l can be found in **Table S2**. The lamellar thickness tends to slightly increase with increasing PEEK content. The convolution of structure factor (**Figure 6b**) with the form factor of the lamellae makes a definite extraction of lamellar thickness using the unified function challenging. While the 1D correlation function is often used to find lamellar thickness for PEEK [6], it was not found to be suitable for this system, as the scattering feature associated with the lamellae is in the form of a broad knee instead of an intense scattering maxima. As they crystallize, stacks of lamellae grow and splay, forming axialites, which can be observed at lower scattering vectors.

Table S2. Radius of Gyration (R_g), Porod Exponent (P), Axialite Thickness (t_2), and Lamellar Thickness (t_1) derived from application of the unified function to USAXS/SAXS profiles collected for PEEK aerogels gelled in DPA.

PEEK Concentration (wt%)	R _{g2} (nm)	t ₂ (nm)	P ₂	R _{g1} (nm)	tı (nm)	P ₁
8	218 ± 19	503 ± 45	3.48 ± 0.01	5.45 ± 0.25	10.9 ± 0.5	4.0
10	241 ± 40	555 ± 92	3.51 ± 0.04	5.87 ± 0.12	11.7 ± 0.2	4.0
15	182 ± 15	421 ± 35	3.52 ± 0.09	5.89 ± 0.03	11.8 ± 0.1	4.0
20	220 ± 9	508 ± 22	3.26 ± 0.16	5.75 ± 0.12	11.5 ± 0.2	4.0
22	207 ± 21	477 ± 47	3.29 ± 0.24	6.09 ± 0.19	12.2 ± 0.4	4.0

Radius of gyration (R_{g2}) and Porod exponent (P_2) were obtained for the feature observed below 0.03 nm⁻¹, which is assigned to the axialite thickness. Strut thickness is obtained by the relation $t_2 = 2\sqrt{4/3}R_{g2}$, assuming that the axialites are approximately rod-shaped [4]. Tabulated values for R_{g2} , P_2 , and t_2 can be found in **Table S2**. Axialite thickness is relatively consistent across all PEEK contents. Axialite thickness determined from the unified function is in excellent agreement with thickness from SEM image analysis, confirming the assignment of the SAXS feature to axialite thickness.

SAXS analysis allows for the facile comparison of the PEEK aerogel gelled in DPA to the previously reported PEEK aerogel systems using DCA and 4CP as solvents [5]. **Figure S3** compares the morphologies of PEEK aerogels gelled in different solvents. **Figure S3a-c** shows SEM micrographs of the different PEEK aerogel systems. The strut-like axialites of PEEK aerogels gelled in DPA (**Figure S3a**) are considerably larger than the globular aggregates found in PEEK aerogels gelled in 4CP (**Figure S3b**) and DCA (**Figure S3c**).

The feature observed between $0.2 \text{ nm}^{-1} - 0.8 \text{ nm}^{-1}$ is assigned to PEEK lamellae in the PEEK aerogel systems. **Table S2** shows the crystallite dimension, R_{gl} , ranges from about 5-6 nm for PEEK aerogels gelled in DPA. The crystallite dimension for PEEK aerogels gelled in DPA was found to be comparable to previous work in our group on PEEK aerogels gelled in DCA and 4CP [5]. Previous work in our group on PEEK aerogels gelled in DCA and 4CP used small-angle neutron scattering to confirm this origins of this scattering feature are due to PEEK lamellae [5]. As the feature, assigned to the lamellae in PEEK aerogels gelled in DPA, is on a similar length scale as the feature confirmed to be due to PEEK lamellae in the PEEK/DCA and PEEK/4CP systems, the assignment of the feature observed between $0.2 \text{ nm}^{-1} - 0.8 \text{ nm}^{-1}$ to lamellae in PEEK aerogels gelled in DPA is reasonable.

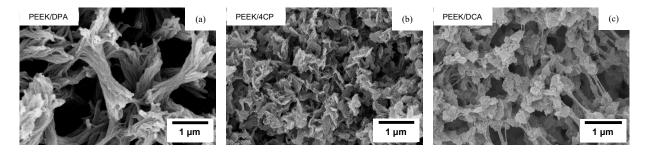


Figure S3. SEM micrographs of freeze dried PEEK aerogels at 15wt.% PEEK gelled in (a) DPA, (b) 4CP, and (c) DCA [5].

The feature observed below 0.03 nm^{-1} is assigned to aggregates of PEEK lamellae in the PEEK aerogel systems. **Table S2** shows the aggregate size, R_{g2} , ranges from about 180-240 nm for PEEK aerogels gelled in DPA. Aggregate size, or specifically, axialite thickness, for PEEK aerogels gelled in DPA, was found to be on a comparable length scale to the aggregate size of the other PEEK aerogel systems gelled in DCA or 4CP [5]. While the aggregates are in the form of either strut-like axialites for PEEK/DPA systems, globules for PEEK/DCA systems, or platelets for PEEK/DCA systems, strut thickness and aggregate size both tend to be on the same length scale of hundreds of nanometers (**Figure S3a-c**). Good agreement between the SEM micrographs and the unified function analysis for each aerogel system confirms the assignment of R_{g2} to aggregate size.

Power law scattering observed in aerogels is indicative of the fractality of their scattering features. These power laws are quantified by the Porod exponent. **Table S2** shows the Porod exponent associated with the aggregate feature (P_2) for PEEK aerogels gelled in DPA. In our previous work, it was found that PEEK aerogels gelled in DCA or 4CP had Porod exponents, P_2 , associated with surface fractals (P > 3) or mass fractals (P > 1) [5]. PEEK aerogels gelled in DPA were found to have Porod exponents greater than 3, which is consistent with surface fractals. P_1 was also found to be 4.0 for all PEEK aerogels gelled in DPA. Previously, it was found that P_1 was 4.0 for all PEEK aerogels gelled in DCA or 4CP. A Porod exponent of 4 is characteristic of smooth surfaces, which is consistent with the flat interface between crystalline lamellae and amorphous material [7].

Table S3. Density, porosity, surface area, modulus, and crystallinity of PEEK aerogels gelled in DPA

PEEK Concentration (wt%)	Density (g/cm ³)	Average Porosity (%)	BET Surface Area (m ² /g)	Modulus (MPa)	WAXS Crystallinity (%)
8	0.094 ± 0.002	92.9	222 ± 2	3.10 ± 0.37	40.9 ± 0.7
10	0.115 ± 0.002	91.3	216 ± 2	6.27 ± 0.66	39.9 ± 2.3
15	0.167 ± 0.001	87.3	212 ± 3	22.64 ± 2.64	41.4 ± 0.2
20	0.226 ± 0.002	82.8	203 ± 2	49.00 ± 3.13	40.0 ± 0.7
22	0.249 ± 0.003	81.1	200 ± 3	61.72 ± 6.08	39.9 ± 0.2

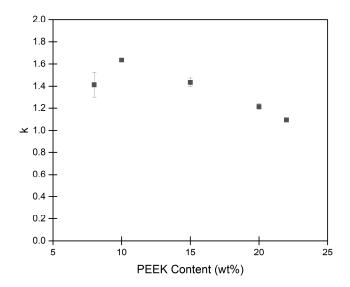


Figure S4. Crystalline imperfection factor, *k*, versus PEEK content.

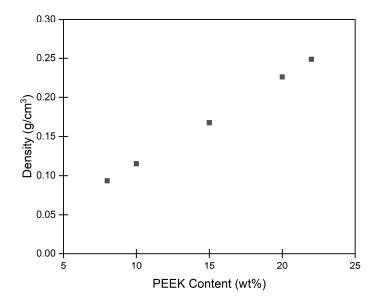


Figure S5. Bulk density of PEEK aerogels gelled in DPA versus PEEK content.

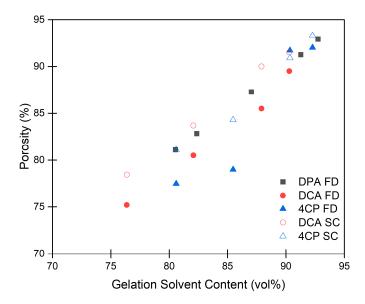


Figure S6. Porosity versus gelation solvent content for PEEK aerogels. Aerogels prepared by freeze-drying (FD) are indicated by a filled symbol, whereas aerogels prepared by extraction with supercritical CO₂ (SC) are indicated by an open symbol.

Cloud point determination:

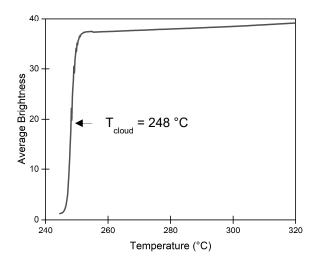


Figure S7. Representative average brightness versus temperature profile for cloud point determination. The sample is a 20wt.% PEEK/DPA gel. Cloud point is determined as the temperature where brightness drops 50%.

Absolute Crystallinity Determination using Vonk's Procedure

Vonk's computerization [8] of the Ruland method [9] for determining crystallinity yields both absolute crystallinity and the crystalline imperfection factor from wide angle X-ray scattering (WAXS) data. Lattice imperfections and thermal vibrations caused crystalline scattering to deviate and be incorrectly attributed to amorphous scattering [10]. Diffuse scattering caused by these imperfections can reduce crystalline diffraction peak height and broaden the diffraction peak. The corrections used in absolute crystallinity determination also correct for many experimental effects which are not often considered in standard crystallinity determination by WAXS [11]. Corrections for transmission, background, polarization and absorption must be applied prior to absolute crystallinity determination.

Scattering intensity must be converted to electron units using the fact that the total scattering intensity in all reciprocal space is constant. First, $T(s_p)$ is calculated:

$$T(s_p) = \frac{\int_0^{s_p} (\overline{f^2} + \overline{f}) s^2 ds}{\int_0^{s_p} I_{corr} s^2 ds}$$
 (S4)

where s is the scattering vector ($s=2\frac{sin\theta}{\lambda}$), s_p is the upper limit of integration, I_{corr} is the corrected scattering intensity, θ is one half of the scattering angle and λ is the X-ray wavelength. The weighted mean-square atomic scattering factor is calculated as $\overline{f^2(s)}=\frac{\sum N_i f_i^2}{\sum N_i}$, and the weighted average incoherent atomic scattering intensity is calculated as $\overline{J(s)}=\frac{\sum N_i J_i}{\sum N_i} \left(\frac{\lambda}{\lambda'}\right)^3$, where N_i is the number of atoms of type i, f_i is the atomic scattering factor of an atom of type i, and J_i is the incoherent atomic scattering intensity of an atom of type i. The Breit-Dirac recoil factor, $\left(\frac{\lambda}{\lambda'}\right)^3$, is evaluated as [10]:

$$\left(\frac{\lambda}{\lambda'}\right)^3 = \left(1 + \frac{2h}{mc\lambda}\sin^2\theta\right)^{-3} \tag{S5}$$

where $\frac{h}{mc} = 0.02426$ Å. The functions of $\overline{f^2(s)}$ and $\overline{J(s)}$ for the atomic composition of PEEK (C₁₉H₁₂O₃) were determined using the tabulated values for f [12] and J [13]. The shift factor α is evaluated at $s_p = 0.65$ Å⁻¹ (shown in **Figure S8**), which is a reasonable assumption [8]. Scattering intensity normalized for electron units is then given as:

$$I_{norm}(s) = I_{corr}(s) * \alpha. \tag{S6}$$

Next, the incoherent scattering is subtracted from the scattering profile as it contains no structural information. The coherent and incoherent scattering can be calculated as $I_{coh} = \overline{f^2(s)} * s^2$ and $I_{incoh} = \overline{J(s)} * s^2$, respectively. Subtraction of incoherent scattering is shown in **Figure S9**.

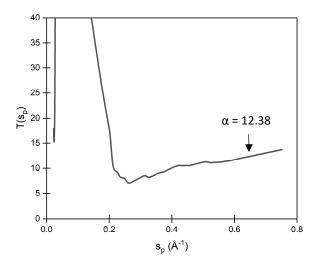


Figure S8. A plot showing T_{sp} vs s_p , used to determine shift factor α to convert intensity to electron units. The sample is a 22 wt.% PEEK aerogel gelled in DPA.

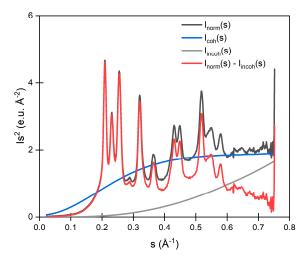


Figure S9. WAXS scattering profiles showing experimental scattering data after normalization to electron units, calculated coherent scattering, calculated incoherent scattering, and experimental data with incoherent scattering subtracted. The sample is a 22 wt.% PEEK aerogel gelled in DPA.

Next, crystalline scattering must be differentiated from the amorphous scattering. Amorphous scattering intensity is separated from the crystalline scattering intensity using Vonk's separation procedure [8]. Briefly, the experimentally recorded amorphous background, $I_{amorphous}(s)$, is multiplied by a shift factor to equal $I_{norm}(s) - I_{incoh}(s)$ for s values where there is assumed to be no crystalline intensity. Over s values where crystalline reflections exist, the shift factor is linearly extrapolated between shift factors in the nearest neighboring s values where no crystalline intensity is expected. Through this procedure, the amorphous intensity is separated from crystalline intensity using the experimentally determined amorphous profile (as shown in **Figure S10**).

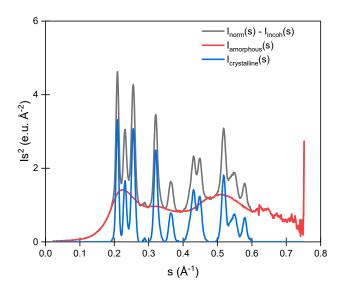


Figure S10. WAXS scattering profiles showing experimental scattering data after subtraction of incoherent scattering, separated amorphous intensity, and separated crystalline intensity. The sample is a 22 wt.% PEEK aerogel gelled in DPA.

Vonk proposed that the expression $R(s_p)$ oscillates about $\frac{K}{x_c}$, where

$$R(s_p) = \frac{\int_0^{s_p} I s^2 ds}{\int_0^{s_p} I_{crystalline} s^2 ds'}$$
 (S7)

and

$$K = \frac{\int_0^{sp} \overline{f^2} s^2 ds}{\int_0^{sp} \overline{f^2} s^2 D(s) ds},$$
 (S8)

where x_c is the absolute crystallinity, s_p is the upper limit of integration, I is the total coherent scattering intensity (I_{norm} - I_{incoh}), $I_{crystalline}$ is the coherent intensity in crystalline peaks, and D(s) is the disorder function. The disorder function is approximated with a Debye-Waller factor, $D(s) = e^{-ks^2}$, where k is the crystalline imperfection factor. Use of the Debye-Waller factor assumes that crystalline disorder can be primarily attributed to atomic displacements due to thermal fluctuations (crystalline imperfections of the first kind). Then, K can be approximated as:

$$K \approx 1 + \frac{k}{2} s_p^2. \tag{S9}$$

Thus, a plot of $R(s_p)$ vs s_p^2 should oscillate about:

$$y = \frac{1}{x_c} + \frac{k}{2x_c} s_p^2.$$
 (S10)

Experimental data is then fit with a line, and x_c and k are solved for, as shown in **Figure S11**.

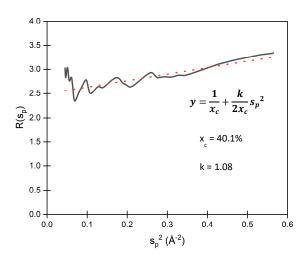


Figure S11. Plot of $R(s_p)$ versus s_p^2 . The black solid line is the experimental data displayed as $R(s_p)$ and the red dotted line is the linear fit. The sample is a 22 wt.% PEEK aerogel gelled in DPA.



Figure S12. A PEEK aerogel cylinder for compression testing prepared from a 15 wt.% PEEK/DPA solution.

References

- 1. Van Krevelen, D.W.; Te Nijenhuis, K. *Properties of polymers: their correlation with chemical structure; their numerical estimation and prediction from additive group contributions*; Elsevier: 2009.
- 2. Blundell, D.J.; Osborn, B.N. The morphology of poly (aryl-ether-ether-ketone). *Polymer* **1983**, *24*, 953-958.
- 3. Hay, J.; Langford, J.; Lloyd, J. Variation in unit cell parameters of aromatic polymers with crystallization temperature. *Polymer* **1989**, *30*, 489-493.
- 4. Beaucage, G. ②pproximations leading to a unified exponential/power-law approach to small-angle scattering. *J. Appl. Crystallogr.* **1995**, *28*, 717-728.
- 5. Talley, S.J.; Vivod, S.L.; Nguyen, B.②.; Meador, M.②.B.; Radulescu, ②.; Moore, R.B. Hierarchical Morphology of Poly(ether ether ketone) ②erogels. *ACS Appl. Mater. Interfaces* **2019**, *11*, 31508-31519, doi:10.1021/acsami.9b09699.
- 6. Verma, R.; Marand, H.; Hsiao, B. Morphological changes during secondary crystallization and subsequent melting in poly (ether ether ketone) as studied by real time small angle X-ray scattering. *Macromolecules* **1996**, *29*, 7767-7775.
- 7. Ogawa, T. Small-angle X-ray scattering from the surfaces of polymer crystals. *Journal of the Physical Society of Japan* **1990**, *59*, 3642-3649.
- 8. Vonk, C.G. Computerization of Ruland's X-ray method for determination of the crystallinity in polymers. *J. Appl. Crystallogr.* **1973**, *6*, 148-152.
- 9. Ruland, W. X-ray determination of crystallinity and diffuse disorder scattering. *Acta Crystallographica* **1961**, *14*, 1180-1185.
- 10. Roe, R.-J. *Methods of X-ray and neutron scattering in polymer science*; Oxford University Press on Demand: 2000.
- 11. Tence-Girault, S.; Quibel, J.; Cherri, D.; Roland, S.; Fayolle, B.; Bizet, S.; Iliopoulos, I. Quantitative structural study of cold-crystallized PEKK. ACS Applied Polymer Materials 2021, 3, 1795-1808.
- 12. Prince, E. International Tables for Crystallography, Volume C: Mathematical, physical and chemical tables; Springer Science & Business Media: 2004.
- 13. Hubbell, J.H.; Veigele, W.J.; Briggs, E.; Brown, R.; Cromer, D.; Howerton, d.R. ②tomic form factors, incoherent scattering functions, and photon scattering cross sections. *Journal of physical and chemical reference data* 1975, 4, 471-538.