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Silicon implantation and annealing in β -Ga₂O₃: Role of ambient, temperature, and time


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ABSTRACT

Optimizing thermal anneals of Si-implanted β -Ga₂O₃ is critical for low resistance contacts and selective area doping. We report the impact of annealing ambient, temperature, and time on the activation of room temperature ion-implanted Si in β -Ga₂O₃ at concentrations from 5×10^{18} to 1×10^{20} cm⁻³, demonstrating full activation (>80% activation, mobilities >70 cm²/V s) with contact resistances below 0.29 Ω mm. Homoepitaxial β -Ga₂O₃ films, grown by plasma-assisted molecular beam epitaxy on Fe-doped (010) substrates, were implanted at multiple energies to yield 100 nm box profiles of 5×10^{18} , 5×10^{19} , and 1×10^{20} cm⁻³. Anneals were performed in an ultra-high vacuum-compatible quartz furnace at 1 bar with well-controlled gas compositions. To maintain β -Ga₂O₃ stability, pO₂ must be greater than 10^{-9} bar. Anneals up to pO₂ = 1 bar achieve full activation at 5×10^{18} cm⁻³, while 5×10^{19} cm⁻³ must be annealed with pO₂ $\leq 10^{-4}$ bar, and 1×10^{20} cm⁻³ requires pO₂ < 10^{-6} bar. Water vapor prevents activation and must be maintained below 10^{-8} bar. Activation is achieved for anneal temperatures as low as 850 °C with mobility increasing with anneal temperatures up to 1050 °C, though Si diffusion has been reported above 950 °C. At 950 °C, activation is maximized between 5 and 20 min with longer times resulting in decreased carrier activation (over-annealing). This over-annealing is significant for concentrations above 5×10^{19} cm⁻³ and occurs rapidly at 1×10^{20} cm⁻³. Rutherford backscattering spectrometry (channeling) suggests that damage recovery is seeded from remnant aligned β -Ga₂O₃ that remains after implantation; this conclusion is also supported by scanning transmission electron microscopy showing retention of the β -phase with inclusions that resemble the γ -phase.

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I. INTRODUCTION

Beta-phase gallium oxide (β -Ga₂O₃) has received attention in recent years due to its ultrawide bandgap (~4.8 eV), estimated high breakdown strength (~8 MV/cm), and optical transparency.^{1,2} While other metastable polymorphs are also of interest,^{3,4} the monoclinic β -phase has been extensively studied and the availability of large area melt-grown substrates is a distinct advantage over

other wide and ultra-wide bandgap semiconductors.^{1,5-7} β -Ga₂O₃ can be readily doped with a variety of n-type donors including Si, Ge, and Sn, with Si emerging as the dopant of choice.^{8,9} *In situ* doping during epitaxial growth has been demonstrated during metalorganic chemical vapor deposition (MOCVD), pulsed laser deposition (PLD), and molecular beam epitaxy (MBE) with Si concentrations up to 2×10^{20} cm⁻³.¹⁰⁻¹⁴ Si n-type doping by ion

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implantation has also been demonstrated, providing a controllable method for selective area doping in lateral devices.^{15–20}

Ion implantation requires thermal annealing to remove implantation-induced lattice damage, including point and extended defects as well as radiation-induced phase transformations,^{21–24} and to activate implanted dopants. Processing parameters for annealing include time, temperature, heating and cooling rates, ambient conditions, and the presence of a protective layer during annealing. Ion implantation of Si, Ge, and Sn^{15,16,19} has been reported for n-type doping for channel and contact regions in β -Ga₂O₃, while implants of Mg and N have been investigated as deep acceptors for blocking layers.^{16,25,26} Sasaki, in 2013, reported activation of Si after annealing between 900 and 1100 °C. While increasing temperature improved activation, significant Si diffusion was observed at 1100 °C. Sasaki also reported a decrease in activation fraction as the implanted concentration increased from 1×10^{19} to 1×10^{20} cm⁻³ Si.¹⁵ Tadjer, in 2019, studied the lattice recovery after Si and Sn implant at doses of 2×10^{15} cm⁻², corresponding to peak concentrations of 2×10^{20} cm⁻³. They reported that lattice recovery required anneals at 1150 °C for the highest dose Si implants, with higher temperatures required for Sn implants, consistent with the higher atomic mass implant generating more lattice damage.²⁷ In 2022, Spencer demonstrated activation of Si, Ge, and Sn implants after annealing at 925 °C for 30 min by rapid thermal annealing (RTA), achieving up to 65% activation for the implanted Si, corresponding to 1.3×10^{19} cm⁻³ and a mobility of 93 cm²/V s.¹⁹ Furthermore, by increasing the temperature to 600 °C during implantation, as compared to room temperature, Sardar demonstrated in 2022 an activation fraction of 82% for Si implanted to a peak concentration of 1.2×10^{20} cm⁻³.¹⁷

Annealing under N₂ ambients has been shown to be favorable compared to O₂ ambients, with N₂ anneals activating carriers, while O₂ reversibly deactivates carriers and enhances Si diffusion.^{28,29} Annealing in argon has been reported as similar to annealing in N₂, suggesting that the inert gas does not impact activation.^{30,31} Existing literature does not quantify gas purity, especially trace concentrations of oxygen and water in N₂ or Ar ambients. Some pO₂ is critical for annealing as β -Ga₂O₃ is unstable at high temperatures in the absence of oxygen, decomposing to the volatile Ga₂O sub-oxide or to Ga metal; above 1150 °C, β -Ga₂O₃ has been shown to decompose under nominally pure N₂ and the addition of H₂ lowered the decomposition threshold to 350 °C.³² Lany estimated the equilibrium partial pressure of Ga₂O as a function of temperature and pO₂,⁸ indicating that limiting p_{Ga₂O} to $<10^{-5}$ bar requires that the concentration of O₂ must be maintained above 10^{-14} bar at 900 °C, 10^{-10} bar at 1000 °C, and 10^{-7} bar at 1100 °C. Their DFT calculations⁸ also suggested strong pO₂ dependence for Si activation, especially at high carrier concentrations.

Despite the early successes of Si ion implantation in β -Ga₂O₃, detailed studies on the effects of annealing ambient, temperature, and time are absent from the literature. In this work, we report on the activation fraction and mobility following furnace annealing of room temperature Si implants (from 5×10^{18} to 1×10^{20} cm⁻³) as a function of annealing ambient (controlled pO₂ and pH₂O), temperature (850–1050 °C), and time (2.5–120 min). Under optimized annealing conditions, activation to >80% with mobilities >70 cm²/V s was observed for concentrations up to 1×10^{20} cm⁻³.

II. EXPERIMENTAL

β -Ga₂O₃ films were grown using a Veeco GEN Xcel plasma-assisted MBE (PAMBE) system equipped with a standard effusion cell for Ga and a UNI-Bulb RF plasma source angled at 45° relative to the substrate for oxygen. Tamura Novel Crystal Technology (NCT) Fe-doped β -Ga₂O₃ (010) substrates (23 × 25 mm) were solvent cleaned prior to loading into the growth chamber, with an additional *in situ* oxygen plasma clean prior to growth. Unintentionally doped (UID) films were grown at a substrate temperature of 650 °C with a Ga beam equivalent pressure (BEP) of 6.0×10^{-8} Torr (calibrated to be near the stoichiometric conditions for the chamber), and an oxygen plasma from 2.0 SCCM of O₂ flow and 250 W of RF power. A target film thickness of 400 nm served as a buffer layer to minimize Fe diffusion from the substrate into the surface implanted layer.³³

To compare with implanted samples, an *in situ* doped sample was grown in an Agnitron Agilis 100 MOCVD system on equivalent substrates. A ~50 nm UID layer was first grown at a reactor pressure of 15 Torr and a substrate temperature of 600 °C, followed by the growth of a ~95 nm film doped with Si at 6.9×10^{19} cm⁻³ grown at a pressure of 40 Torr and a substrate temperature of 705 °C. The substrate temperature was measured using a pyrometer aligned to the backside of the SiC-coated graphite susceptor. Triethylgallium (TEGa) and silane (25 ppm SiH₄ in argon) were used as precursors for gallium and silicon, respectively, with argon as the carrier gas and molecular oxygen as the oxidant. The TEGa molar flow was 19 and 39 μ mol/min for the UID and doped layer, respectively. For the doped layer, the silane flow was 27 nmol/min. For the entire growth, the oxygen flow was set at 500 SCCM with a total gas flow of 6000 SCCM.

Prior to ion implantation, films were capped with approximately 20 nm SiO₂ via atomic layer deposition (ALD) in an Oxford FlexAL system at 300 °C using tris(dimethylamino)silane. Ion implantation was performed using three implant energies to form a 100 nm box-shaped concentration profile with straggle to ~200 nm (Fig. 1). Three Si box concentrations of 5×10^{18} , 5×10^{19} , and 1×10^{20} cm⁻³ were formed, all using similar implant energies (modified to compensate for slight variations in the ALD thickness). The nominal energies and doses for the 5×10^{19} cm⁻³ box implant were 15, 45, and 115 keV at 5.6×10^{13} , 1.4×10^{14} , 5.2×10^{14} cm⁻², respectively; specific implant energies for each growth were adjusted based on the measured thickness of the SiO₂ capping layer and are detailed in Table SI in the supplementary material. Figure 1 shows the simulated profile from stopping range of ions in matter (SRIM).³⁴ Secondary ion mass spectrometry (SIMS) measurements (Fig. S1 in the supplementary material) confirm the initial box profile and show slight diffusion after annealing at 1000 °C for 20 min.

After implant, samples were diced into 5 × 5 mm die for anneals. The SiO₂ layer was removed using a 6:1 buffered oxide etchant for 1 min. To account for small differences in UID growth and substrate quality, all trends reported for different activation conditions only include samples from one growth. While rapid thermal annealing (RTA) is often used to activate implants, furnace annealing was chosen to permit careful control of gas purity, furnace cleanliness, purging times, and temperature accuracy.

Annealing was performed in an ultra-high vacuum (UHV) compatible quartz tube furnace, shown schematically in Fig. S2 in

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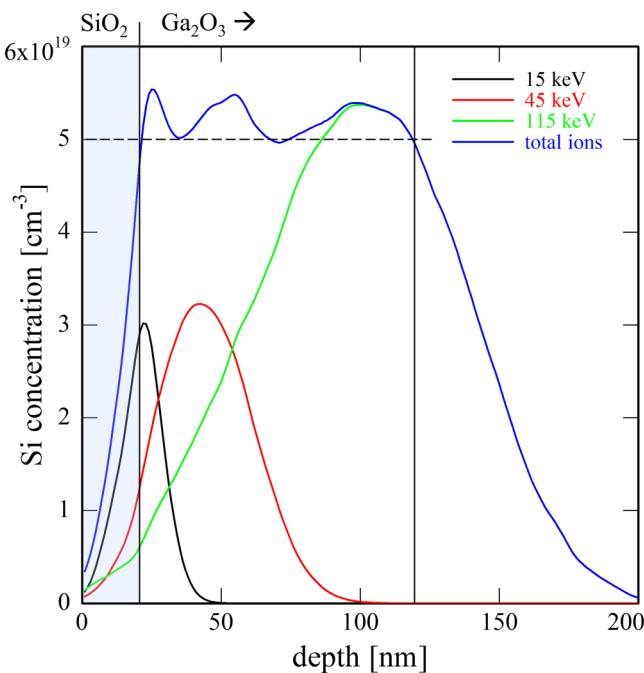


FIG. 1. Simulated implant profile of the $5 \times 10^{19} \text{ cm}^{-3}$ implant with 15, 45, and 115 keV at doses of 5.6×10^{13} , 1.4×10^{14} , $5.2 \times 10^{14} \text{ cm}^{-2}$, respectively, creating a box-shaped implant for the first 100 nm of the film with straggle to 200 nm.

the [supplementary material](#). Gas flows were carefully controlled through flow meters and, to minimize water vapor, the mixed gases were passed over a desiccant to reduce $p_{\text{H}_2\text{O}}$ to below 10^{-8} bar. For annealing experiments in controlled $p_{\text{H}_2\text{O}}$, nitrogen with 10^{-4} bar H_2O was mixed into the gas stream at the inlet of the furnace. Gas from the furnace was passed through a glycerin bubbler and vented to atmosphere ensuring no backflow into the furnace. Unless otherwise specified, all samples were annealed under a 1 bar total pressure (P_{total}). When not in use, the furnace was continuously purged with 1000 SCCM of liquid nitrogen boiloff. All high purity gases were acquired from AirGas and are summarized in [Table I](#). Gas mixtures (1% O_2 in N_2 and 100 ppm H_2O in N_2) do not specify N_2 purity. A vacuum port, open only during sample loading, minimized furnace contamination from ambient air. After loading into

the furnace, a minimum 20-min gas purge with the intended high purity ambient was performed prior to moving the sample into the preheated hot zone. A discussion of the importance of purging times is included in the [supplementary material](#). Unless otherwise stated as a second, subsequent, or staged anneal experiment, all results are for anneals of as-implanted samples.

Electrical activation was determined using a Nanometrics HL5500 Hall system with indium contacts made to the corners in a van der Pauw geometry. The active carrier fraction was defined as the ratio of the measured sheet concentration (n_s) to the total implant dose (Si/cm^2). Free carrier concentrations within the box implant were then estimated by multiplying the active carrier fraction by the total target implant concentration (Si/cm^3). On select samples, contact resistances to the highly doped films were extracted using the transfer length method (TLM). A BCl_3/Ar ICP-RIE dry etch (20 W RF and 250 W ICP) with a Ti/Ni hard mask was used for mesa isolation. The Ti/Ni hard mask was stripped using a 1:1 $\text{HF}:\text{HNO}_3$ solution. A Ti/Al/Ni (50/100/65 nm) stack for metal contacts was deposited by electron-beam evaporation at a base pressure of 4.5×10^{-7} Torr and was patterned via optical lithography and liftoff. TLM samples were annealed in a series of 5 s RTA cycles in N_2 from 300 to 480 °C in steps of 30 °C to ensure ohmic contact formation between the metal and the highly doped films.

X-ray diffraction (XRD) was performed using a PANalytical Empyrean diffractometer with $\text{Cu K}\alpha_1$ radiation. Rutherford backscattering spectrometry in a channeling mode (RBS/c) was performed with a Model 3S-MR10 accelerator from National Electrostatics Corporation (NEC) calibrated using indium zinc oxide (IZO) on glassy carbon. Data were collected for each as-implanted and annealed sample in a 168° backscattering geometry with 2 MeV He^+ beam energy, and $40 \mu\text{C}$ per scan with one scan each in random and channeling configurations. Cross-sectional scanning transmission electron microscopy (STEM) samples were prepared using a Thermo Fisher Helios G4 UX Focused Ion Beam with a final milling step of 5 keV. A carbon layer was deposited to reduce charging during sample preparation. STEM imaging was performed with an aberration corrected Thermo Fisher Spectra 300 CFEG operated at 300 keV.

III. RESULTS AND DISCUSSION

A. Electrical activation

Previous annealing studies using N_2 ambients did not quantify p_{O_2} levels and, as noted earlier, some p_{O_2} is necessary to stabilize

TABLE I. High purity gas specifications from AirGas. All impurity levels are given in ppm. The terms R, RP, and UHP are used in the text to designate the specific gases in this table. N/A, not applicable for specified gas; --, not specified; *, $\text{CO} + \text{CO}_2 \leq 1$ ppm.

Product name	Minimum purity	O_2	H_2O	THC	CO	CO_2	H_2 (for N_2)	N_2 (for Ar)
Research Plus (RP) N_2	99.9999%	≤ 0.2	≤ 0.2	≤ 0.1	≤ 0.3	≤ 0.1	--	N/A
Research (R) N_2	99.9997%	≤ 0.5	≤ 0.5	≤ 0.2	≤ 0.5	≤ 0.5	≤ 2	N/A
Ultra-High Purity (UHP) N_2	99.999%	≤ 1	≤ 1	≤ 0.5	≤ 1	≤ 1	--	N/A
RP Ar	99.9999%	≤ 0.1	≤ 0.2	≤ 0.1	≤ 0.1	≤ 0.1	N/A	≤ 2
100 ppm H_2O in N_2	N/A	N/A	100	N/A	N/A	N/A	N/A	N/A
1% O_2 in N_2	N/A	10 000	N/A	N/A	N/A	N/A	N/A	N/A

Ga₂O₃ against decomposition. To study the pO₂ dependence of electrical activation, samples implanted to each of the three Si concentrations were annealed under varying pO₂ using either UHP O₂ or 1% O₂ in N₂ gas mixed with RP N₂ (P_{total} = 1 bar, p_{H₂O} < 10⁻⁸ bar for all conditions). After sample loading, the furnace was purged for 20 min with 2000 SCCM and samples were annealed for 10 min at 950 °C. For the lowest pO₂ (< 2 × 10⁻⁷ bar, RP N₂), measured sheet resistances (R_s) were 1260, 161, and 199 Ω/□ for 5 × 10¹⁸, 5 × 10¹⁹, and 1 × 10²⁰ cm⁻³ samples, respectively. R_s for the 1 × 10²⁰ cm⁻³ sample was higher than for the 5 × 10¹⁹ sample as 10 min at 950 °C is beyond the optimal time for 1 × 10²⁰ cm⁻³ implants, as discussed later. Figure 2 shows the relative activation as a function of pO₂, with the relative sheet resistance (R_{s,rel}) defined as R_s divided by R_s at pO₂ < 2 × 10⁻⁷ bar (R_{s,low pO₂}); shaded regions correspond to R_{s,rel} > 2. For 5 × 10¹⁸ cm⁻³, implants activated for anneals over the full range of 2 × 10⁻⁷ < pO₂ < 1 bar with no significant change in R_s, mobility, or activation fraction. For 5 × 10¹⁹ cm⁻³ implants, activation was insensitive to pO₂ up to 10⁻⁴ bar, but at 10⁻³ bar, R_s increased by several orders of magnitude. At 1 × 10²⁰ cm⁻³, carriers activated only under RP N₂, pO₂ < 2 × 10⁻⁷ bar; any additional O₂ caused R_s to increase dramatically (an order of magnitude at 10⁻⁵ bar pO₂). The decreased tolerance to oxygen at high doping concentrations is likely due to the increased pO₂ and Fermi level causing an increase in V_{Ga} concentrations.

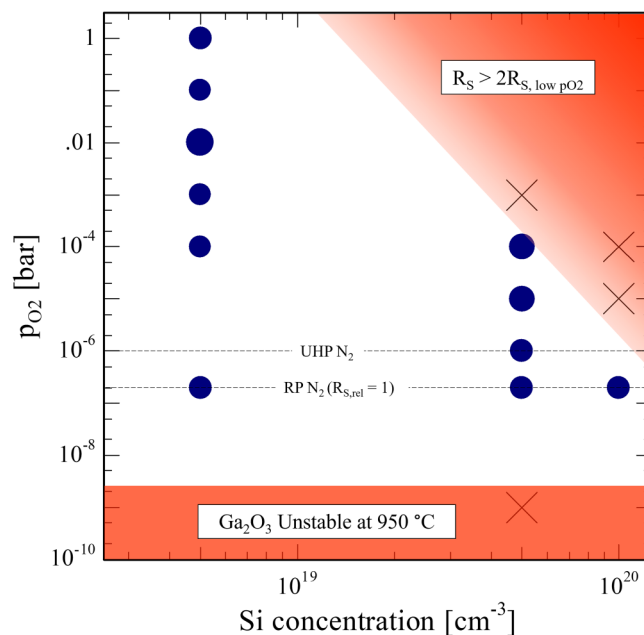


FIG. 2. pO₂ dependence of Si activation at 950 °C for 10 min as a function of implant concentration. Experimental conditions for R_s values below 2R_{s,low pO₂} (pO₂ < 2 × 10⁻⁷ bar) are shown as filled circles with the diameter of the circle representing the R_{s,rel} value (with R_{s,low pO₂} = “1”); black “x” symbols indicate conditions that do not result in high activation (R_{s,rel} > 2). Regions shaded in red are guides to the eye and represent pO₂ values with R_{s,rel} > 2.

Activation behavior was equivalent during anneals in argon (pO₂ < 2 × 10⁻⁷ bar), confirming that N₂ is not critical. The lower bound on pO₂, set by β-Ga₂O₃ stability, was evident in anneals under UHV (P_{total} < 2 × 10⁻⁹ bar and pO₂ < 10⁻⁹ bar) and forming gas (4% H₂ in N₂, pO₂ < 10⁻¹² bar). UHV anneals of 5 × 10¹⁹ cm⁻³ resulted in R_s of 1–2 kΩ/□ (tenfold increase, indicated as black “x” in Fig. 2), and anneals under forming gas decomposed Ga₂O₃ (Fig. S3 in the supplementary material). Under UHV, it is unlikely that the effect is a result of the change in the total pressure but rather a result of the decreased pO₂. This establishes a lower bound for annealing at 950 °C of pO₂ > 10⁻⁹ bar. While lower Si concentration implants tolerate pO₂ up to 1 bar, there does not appear to be any advantage to higher pO₂ for activation.

While activation was achieved over a wide range of pO₂, anneals were much more sensitive to trace p_{H₂O} contamination. As-implanted samples at 5 × 10¹⁹ cm⁻³ were annealed for 20 min at 950 °C under R N₂ (P_{total} = 1 bar, p_{H₂O} < 1 × 10⁻⁸ bar, pO₂ < 5 × 10⁻⁷ bar) mixed with controlled amounts of H₂O; p_{H₂O} values of < 1 × 10⁻⁸, 2.5 × 10⁻⁷, 2.5 × 10⁻⁶, and 2.5 × 10⁻⁵ bar were tested. Figure 3 shows R_s, mobility, and activation fraction as a function of p_{H₂O} after the initial anneal (blue). Even at 2.5 × 10⁻⁷ bar p_{H₂O} (0.25 ppm), the activation fraction decreased. By 2.5 × 10⁻⁵ bar p_{H₂O}, R_s increased by an order of magnitude as n_s decreased tenfold. Figure 3 indicates that mobility decreased only slightly with the initial H₂O addition but then increased at high p_{H₂O} (likely due to reduced scattering with the lower n_s). Presence of H₂O became more detrimental with the addition of O₂ to the ambient, as discussed in the supplementary material. Subsequent annealing for 20 min (orange) in dry, low pO₂ nitrogen at 950 °C showed partial recovery of properties for p_{H₂O} > 10⁻⁶ bar. For p_{H₂O} < 10⁻⁶ bar (< 1 ppm), however, the additional 20-min dry anneal resulted in “over-annealing” (discussed below) and a slight increase in R_s. These data show that the impact of annealing in a wet ambient is largely recoverable, but for high implant activation p_{H₂O} must be held to < 10⁻⁸ bar. Reducing p_{H₂O} in the system to this level requires an extended gas purge before annealing, as discussed further in the supplementary material.

Based on the findings of the impact of pO₂ and p_{H₂O}, the annealing behavior with time and temperature was measured under N₂ (pO₂ < 10⁻⁶, p_{H₂O} < 10⁻⁸ bar, P_{total} = 1 bar) for 5 × 10¹⁹ cm⁻³ implants over 2.5–30 min at temperatures from 850 to 1050 °C, using sequential anneals of single samples to minimize sample variation errors. After sample loading, the furnace was purged for 20 min. Following each anneal, indium contacts were soldered to the corners of the samples, Hall measurements were obtained, and the indium contacts were stripped with HCl; the sample was then loaded for the next anneal step. It is important to note that the “total anneal time” does not correct for the finite time required to reach the set temperature after transfer into the furnace (approximately 2 min). However, the staged annealing does provide monotonic trends with time. Figure 4 shows these staged time annealing results for temperatures from 850 to 1050 °C. At lower temperatures (850–900 °C), there was a strong annealing time dependence to R_s [Fig. 4(a)], which decreased for times up to 30 min as mobility [Fig. 4(b)] and carrier activation [Fig. 4(c)] increased. Even after 30 min, the mobility did not reach the level observed for higher

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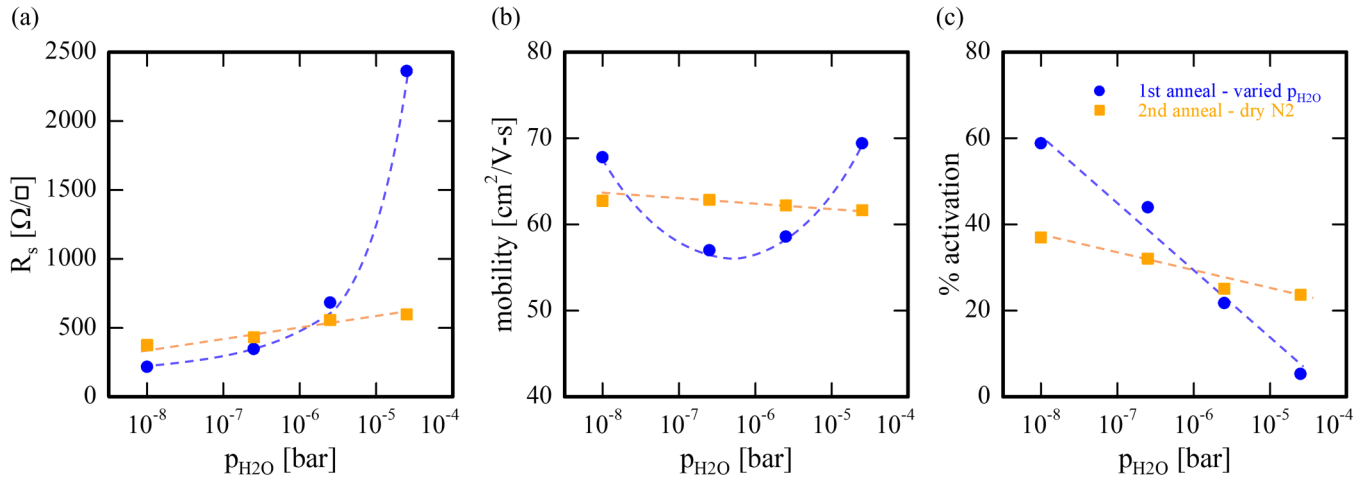


FIG. 3. Plots of R_s (a), μ (b), and % activation (c), as a function of p_{H_2O} added to otherwise high purity (R_s dried to $p_{H_2O} < 10^{-8}$ bar) N_2 , showing first anneal (950 °C, 20 min) with varied H_2O content in blue and after a second anneal (950 °C, 20 min) under dry N_2 in orange, showing the recovery of electrical properties. Dashed lines are added as a guide to the eye.

temperature anneals. At higher temperatures (1000 and 1050 °C), the mobility saturated at the shortest anneals, indicating that the implant damage rapidly recovered. However, Si is known to diffuse at temperatures >950 °C^{15,24,35} limiting useful annealing to lower temperatures. With extended time at higher temperatures, R_s began to increase associated with a decrease in carrier activation; this “over-annealing” behavior is discussed further below. With these considerations, 950 °C emerges as an optimized annealing temperature with a broad anneal time window of 5–30 min; R_s reached a minimum after only 10 min (corresponding with maximized μ and % activation) and held for 30 min before R_s started to slowly increase.

For long anneal times, the activation fraction decreased resulting in “over-annealing.” At $5 \times 10^{19} \text{ cm}^{-3}$, deactivation was observed even at low temperatures, occurring after 40 min at 950 °C but after only 15 min at 1050 °C. Over-annealing in implanted samples manifested as a decrease in active carriers at all anneal temperatures, and with a decrease in mobility at the highest temperatures only. To investigate the dose dependence, samples at 5×10^{18} and $1 \times 10^{20} \text{ cm}^{-3}$ were also time-stage annealed with Hall measurements after each step. Figure 5 shows the properties as a function of anneal time (950 °C, $p_{O_2} < 10^{-6}$, $p_{H_2O} < 10^{-8}$ bar, $P_{\text{total}} = 1$ bar). For $5 \times 10^{18} \text{ cm}^{-3}$ implants, there was minimal

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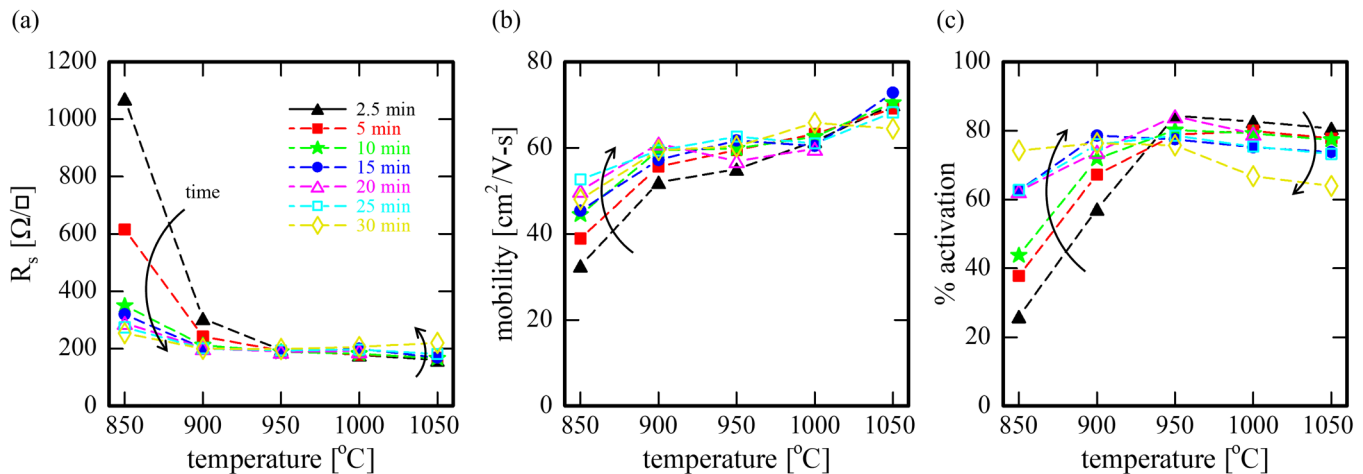


FIG. 4. Plots of R_s (a), μ (b), and % activation (c) vs anneal temperature for different times (indicated by different colors and symbols in the legend), showing trends with time and temperature for anneals under dry N_2 . Arrows indicate trends with increasing time, showing a decrease in R_s (a), increase in μ (b), and an increase in carrier activation (c) with time at lower temperatures and a slight increase in R_s (a) with a decrease in carrier activation (c) with time at higher temperatures.

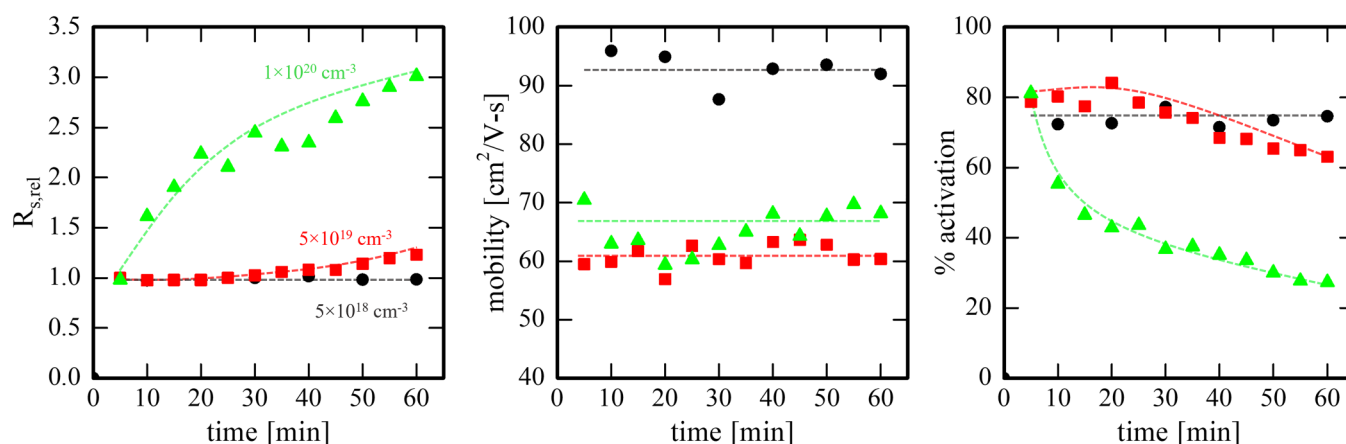


FIG. 5. Plots of $R_{s,rel}$ ($=R_s/R_{s,t=5\text{min}}$) (a), μ (b), and % activation (c) vs time for implant conditions $5 \times 10^{18} \text{ cm}^{-3}$ (black), $5 \times 10^{19} \text{ cm}^{-3}$ (red), and $1 \times 10^{20} \text{ cm}^{-3}$ (green) for anneals under dry N_2 . No evidence of over-annealing was seen in the $5 \times 10^{18} \text{ cm}^{-3}$ sample, minimal over-annealing was observed in the $5 \times 10^{19} \text{ cm}^{-3}$ sample after 20 min, and significant over-annealing in the $1 \times 10^{20} \text{ cm}^{-3}$ sample occurred after the initial 5 min anneal. Lines are added as a guide to the eye.

change in activation up to 60 min with $>70\%$ activation and $\mu > 90 \text{ cm}^2/\text{V}\cdot\text{s}$. For $5 \times 10^{19} \text{ cm}^{-3}$, anneals for up to 20 min showed 80% activation with $\mu \sim 60 \text{ cm}^2/\text{V}\cdot\text{s}$, followed by a decrease in carrier activation and a 25% rise in R_s by 60 min. At the highest implant concentration, $1 \times 10^{20} \text{ cm}^{-3}$, there was a very strong time dependence with significant over-annealing even after 10 min. For a 5 min anneal, 81% of the carriers were activated (estimated concentration of $8.14 \times 10^{19} \text{ cm}^{-3}$) with a mobility of $70.8 \text{ cm}^2/\text{V}\cdot\text{s}$ and R_s of $75.3 \Omega/\square$. All subsequent anneals reduced the carrier activation and after 60 min R_s increased threefold to $228 \Omega/\square$ with only 28% of the implanted carriers activated. Earlier reports in the literature have suggested that an elevated temperature during implantation is required to activate $1 \times 10^{20} \text{ cm}^{-3}$ Si concentration.¹⁷ Our results, however, show that $1 \times 10^{20} \text{ cm}^{-3}$ implants can be almost fully activated with high mobility if p_{O_2} , $p_{\text{H}_2\text{O}}$, and time are carefully controlled. As over-annealing is highly correlated to Si concentration, it is likely related to the formation of sub-nm defect pairs,⁸ or potentially larger scale (5–10 nm) features arising from the clustering of Si_{Ga} defects as has been seen after annealing at 1100°C for 30 min in air.³⁶

To determine if over-annealing is a result of implant-induced damage, an *in situ* doped $6.9 \times 10^{19} \text{ cm}^{-3}$ MOCVD sample was subjected to the same staged anneals at 950°C . R_s increased from 40 (as grown) to $190 \Omega/\square$ after 30 min with the mobility decreasing from 91 to $58 \text{ cm}^2/\text{V}\cdot\text{s}$ and carriers deactivating to $2.3 \times 10^{19} \text{ cm}^{-3}$. These results suggest that the deactivation is not primarily a result of implant damage, but that over-annealing is associated with defects in the film and substrate. Mechanisms may differ between implanted and *in situ* doped samples with the deactivation of the *in situ* doped samples also involving a decrease in mobility, even at 950°C .

Figure 6 compares deactivation as a function of staged time for samples implanted at $5 \times 10^{19} \text{ cm}^{-3}$ from two different epitaxial PAMBE growth runs. Results show that the rate of deactivation is

dependent on the sample position within the $23 \times 25 \text{ mm}$ wafers (likely substrate variations) and is potentially dependent on precise conditions during the epitaxial growth. Samples from the two growths were annealed together to ensure identical thermal

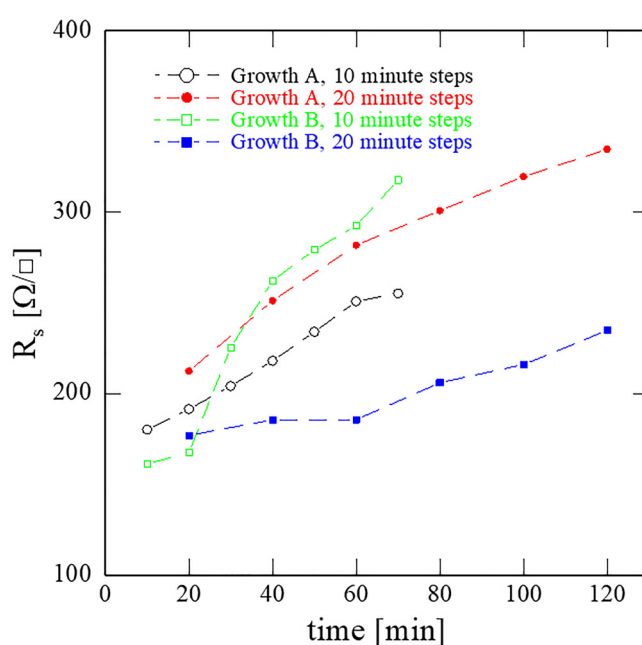


FIG. 6. (a) Plots of R_s vs time for $5 \times 10^{19} \text{ cm}^{-3}$ implanted samples from two PAMBE growths (A and B) and two anneal time steps (10 and 20 min) showing that over-annealing began after 20 min (at 950°C , $p_{\text{O}_2} < 10^{-6}$, $p_{\text{H}_2\text{O}} < 10^{-8}$ bar, $P_{\text{total}} = 1$ bar), but the rate varied depending on specific growth runs and position on the substrate.

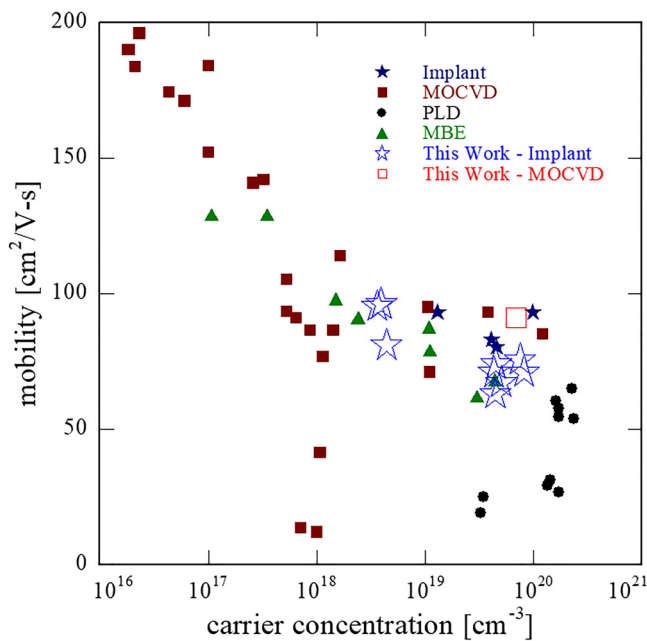


FIG. 7. Blue open stars represent mobility and carrier concentration values for implant samples reported in this study (red open square for *in situ* MOCVD) compared with select literature reports for (010) β -Ga₂O₃ samples doped with Si by implant,^{17,19} MOCVD,^{10,14,37–39} PLD,^{40–42} and MBE.^{12,13}

histories, with one pair annealed in 10-min increments and the second pair in 20-min increments. Both pairs show differences in deactivation rates, but the slower deactivating sample in each run came from different epitaxial growth runs. These results indicate that growth-induced defects, which may vary by substrate position and growth method, are likely important in determining the rate of deactivation. The specific defect contributing to this effect is not known but may be related to the density of various defects from growth or doping methods, such as dislocations or extrinsic point defects formed during growth or screw dislocations formed after implant annealing.²⁴

The optimized anneal conditions for activating Si in β -Ga₂O₃ vary with implant concentrations, becoming more restrictive as the Si concentration increases. The annealing ambient is critical for activation, requiring $p_{\text{H}_2\text{O}} < 10^{-8}$ bar and $10^{-9} < p_{\text{O}_2} < 10^{-6}$ bar. Annealing at 950 °C for 5–20 min is sufficient to fully recover the lattice and mobility while minimizing over-annealing, even for concentrations to $1 \times 10^{20} \text{ cm}^{-3}$. Figure 7 compares these Si mobility and carrier activation results from implant and annealing with other literature results for Si in (010) β -Ga₂O₃, as well as the MOCVD *in situ* doped sample results discussed in this paper. For the three implants studied in this work, we observed 94.0 cm²/V s at $3.95 \times 10^{18} \text{ cm}^{-3}$, 71.6 cm²/V s at $4.22 \times 10^{19} \text{ cm}^{-3}$, and 70.8 cm²/V s at $8.15 \times 10^{19} \text{ cm}^{-3}$. These results confirm that implant and thermal anneals are competitive with *in situ* doping methods. The ability to form good ohmic contacts with an average contact resistance $R_c = 0.29 \pm 0.02 \Omega \text{ mm}$ was demonstrated by TLM

measurements in the $5 \times 10^{19} \text{ cm}^{-3}$ samples annealed at 950 °C (see the [supplementary material](#)).

B. Implant damage and lattice recovery

To investigate the damage and subsequent recovery, XRD, RBS/c, and STEM were used to analyze samples implanted to $5 \times 10^{19} \text{ cm}^{-3}$. Figure 8(a) shows XRD scans for pre-implant (gray), post-implant (blue), and post-anneal (orange) for 20 min at 950 °C. No additional peaks were seen in the full range 2θ scans after implant or after annealing, though the implanted sample does exhibit shoulders around the (020) peak indicating strain and extended defects within the film; this damage is recovered with annealing. Phase transformations that may have been induced by the implant were not detected by XRD for implant concentrations up to $1 \times 10^{20} \text{ cm}^{-3}$ (XRD in Fig. S7 in the [supplementary material](#)), likely due to the low total displacements per atom (DPA) for these implant conditions. Additional XRD scans, including rocking curves, and further discussion of the absence of the γ -phase, are included in the [supplementary material](#).

Damage accumulation and recovery was further investigated with RBS/c, as shown in Fig. 8(b) for an as-implanted and annealed (950 °C, 20 min, dry N₂) $5 \times 10^{19} \text{ cm}^{-3}$ sample. The random spectrum, with slight planar channeling, matches well with RBS simulations^{43,44} of pure Ga₂O₃ (blue). Channeling of the as-implanted sample (red) indicates only partial damage with no fully amorphous layer; the maximum scattering is only 70% of the expected fully amorphous level (scattering expected for a 200 nm Ga₂O₃ film layer is shown in magenta). After annealing, channeling (green) shows full recovery of the crystal lattice with a χ_{min} of 2.8%, consistent with a good single crystal; the de-channeling with depth is also typical for (010) oriented films.³⁶

Figure 9 summarizes high-angle annular dark-field (HAADF)-STEM measurements performed on a sample implanted to $5 \times 10^{19} \text{ cm}^{-3}$ Si. The image shows defects identified as Ga_i interstitials (blue arrows), regions of retained β -phase (green), and regions of both [110] γ -phase and overlapping γ -phase (pink), as has been repeatedly observed in the literature as implant-induced phase transformations.^{22–24} This observed phase transformation supports previous findings that γ -Ga₂O₃ is the kinetically favored structure, often forming in regions of high disorder such as substrate interfaces, free surfaces, and areas with high implant damage.⁴⁵ To highlight the implant damage, the Fast Fourier Transform (FFT) of the damaged lattice [Fig. 9(a)] is shown in Fig. 9(b) with the FFT of the annealed, recovered lattice overlaid in green (HAADF-STEM image shown in Fig. S9 in the [supplementary material](#)). Overlapping FFT peaks appear white, confirming the presence of the retained β -phase in the damaged lattice; additional diffraction spots present only in the damaged FFT are shown in magenta. Figure 9(c) shows the predicted electron diffraction patterns⁴⁶ of both the β -phase along the [010] axis (green) and the γ -phase along the [110] axis (magenta), showing that the overlaid patterns match the FFT of the implanted area, confirming the presence of the γ -phase in the implanted region. Additional images in the [supplementary material](#) show a comparable analysis from 90° rotated from the [010] axis.

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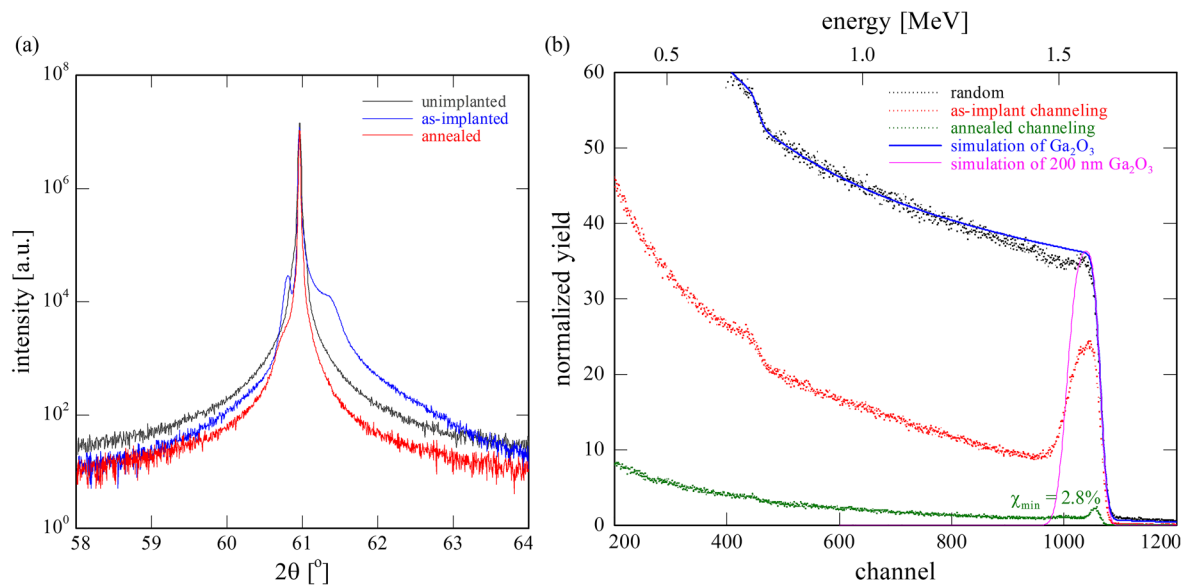


FIG. 8. (a) θ - 2θ XRD patterns of (020) reflection for un-implanted (gray), as-implanted to $5 \times 10^{19} \text{ cm}^{-3}$ (blue, showing shoulders associated with lattice damage), and implanted and annealed (950 $^{\circ}\text{C}$, 20 min, N_2 , red); and (b) RBS/c spectra compared to simulated spectra showing random (black and blue line, respectively); implanted to $5 \times 10^{19} \text{ cm}^{-3}$ channeling in red, showing peak yield in the implanted region not reaching full random signal but matching projected depth of damage (simulated 200 nm in magenta); and after annealing (20 min, 950 $^{\circ}\text{C}$ dry N_2), recovery of the crystal lattice to a near perfect structure shown in green with a χ_{\min} of 2.8%.

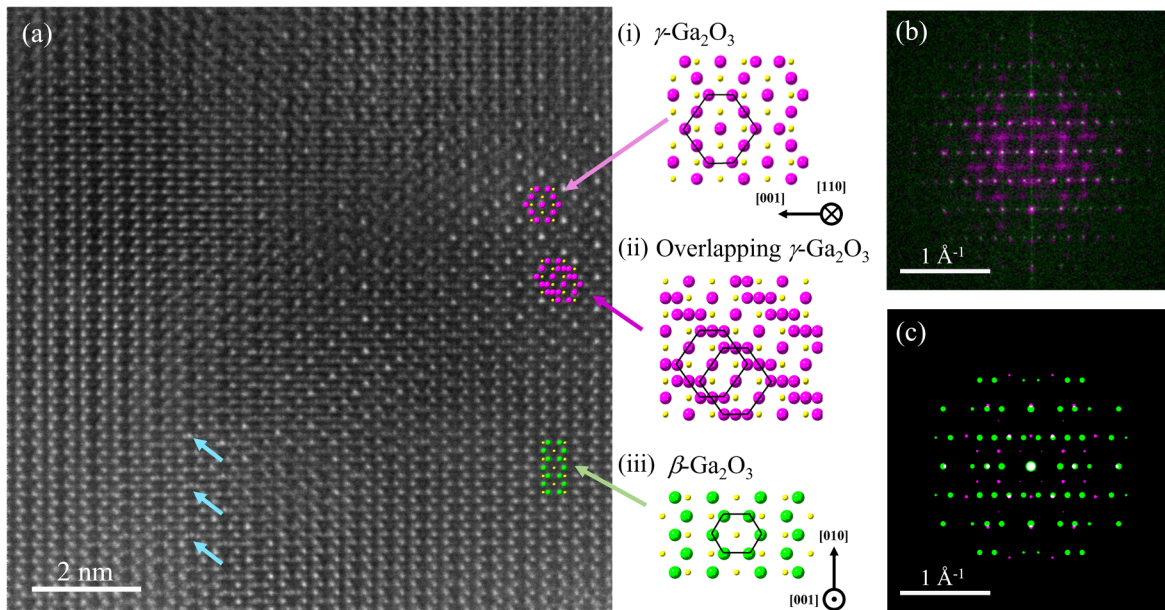


FIG. 9. (a) Atomic resolution HAADF-STEM image of the as-implanted film, highlighting regions of transformed γ -phase (i) and overlapping γ -phase (ii), Ga interstitials (blue arrows), and retained β -crystallinity (iii). Green and magenta represent Ga atoms (in β and γ , respectively) and yellow represents O atoms. (b) FFT of the as-implanted region shown in (a) overlaid with the FFT of the β -phase crystal. The magenta shows the additional damage from the implant and white represents areas with intensity from both FFT patterns. Note no pure green spots are observed in the FFT as the implanted region contains both β - and γ -phases. (c) Simulated single crystal electron diffraction patterns along the [010] zone axis of β -Ga₂O₃ and [110] of γ -Ga₂O₃, showing correlation with the measured pattern in (b).

The combined structural information from XRD, RBS/c, and STEM confirms remnant crystallinity in the as-implanted films for the $5 \times 10^{19} \text{ cm}^{-3}$ Si implant. It is hypothesized that this remnant crystallinity seeds recovery of the lattice upon annealing, without requiring epitaxial regrowth from below the depth of damage or the substrate.

IV. CONCLUSIONS

With careful control of annealing pO_2 , pH_2O , temperature, and time, Si implant concentrations in $\beta\text{-Ga}_2\text{O}_3$ from 5×10^{18} to $1 \times 10^{20} \text{ cm}^{-3}$ can be highly activated (>80%) with full recovery of mobility to $>70 \text{ cm}^2/\text{V s}$. In the ambient, pO_2 must be above 10^{-9} bar to maintain stability of Ga_2O_3 , with the upper bound being dependent on Si concentration (>1 bar for $5 \times 10^{18} \text{ cm}^{-3}$ and 10^{-6} bar for $1 \times 10^{20} \text{ cm}^{-3}$). Water must be minimized during implant annealing with $\text{pH}_2\text{O} < 1 \times 10^{-8}$ bar as even 2.5×10^{-7} bar pH_2O reduces active carriers and increases R_s ; the impact is even stronger when O_2 is also present in the gas ambient ($\text{pO}_2 > 10^{-6}$ bar). 950°C is an optimal temperature for activation of all three implant concentrations, maximizing the recovered mobility with minimal diffusion. Anneal time is also critical, especially for high concentrations, with 5 min in a traditional furnace sufficient to activate implants at 950°C . The upper time limit for annealing is set by the onset of deactivation and depends on Si concentration. At low Si concentrations, deactivation is not observed, after even 60-min anneals, while high Si concentrations begin to deactivate within 10 min. Investigations into the lattice damage and recovery show a high degree of retained $\beta\text{-Ga}_2\text{O}_3$ crystallinity in as-implanted regions, which rapidly seeds lattice recovery and enables annealing at the relatively low temperature of 950°C . For $5 \times 10^{19} \text{ cm}^{-3}$ implants, contact resistances below $0.29 \Omega \text{ mm}$ can readily be achieved, showing promise for selective area doping methods. Mobility as a function of carrier concentration for implants is comparable to the best reports from *in situ* doped methods, showing that ion implantation is a highly competitive doping method in $\beta\text{-Ga}_2\text{O}_3$.

SUPPLEMENTARY INFORMATION

See the supplementary material for additional implant details, a furnace schematic, a discussion of the importance of purge times, results of annealing Ga_2O_3 in forming gas, contact resistance analysis, additional XRD plots, and additional STEM images.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Katie R. Gann: Conceptualization (equal); Data curation (lead); Formal analysis (lead); Investigation (equal); Methodology (equal); Validation (lead); Visualization (equal); Writing – original draft (lead); Writing – review & editing (equal). **Naomi Pieczulewski:** Data curation (equal); Formal analysis (supporting); Investigation (equal); Visualization (equal); Writing – review & editing (equal). **Cameron A. Gorsak:** Investigation (equal); Resources (equal); Writing – review & editing (equal). **Karen Heinselman:** Formal analysis (equal); Investigation (equal); Writing – review & editing (equal). **Thaddeus J. Asel:** Investigation (equal); Resources (equal); Writing – review & editing (supporting). **Brenton A. Noesges:** Investigation (equal); Resources (equal); Writing – review & editing (supporting). **Kathleen T. Smith:** Formal analysis (supporting); Investigation (equal); Visualization (supporting); Writing – review & editing (equal). **Daniel M. Dryden:** Investigation (supporting); Writing – review & editing (equal). **Huili Grace Xing:** Supervision (equal); Writing – review & editing (equal). **Hari P. Nair:** Supervision (equal); Writing – review & editing (equal). **David A. Muller:** Supervision (equal); Writing – review & editing (supporting). **Michael O. Thompson:** Conceptualization (equal); Funding acquisition (lead); Project administration (lead); Software (equal); Supervision (lead); Visualization (equal); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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