

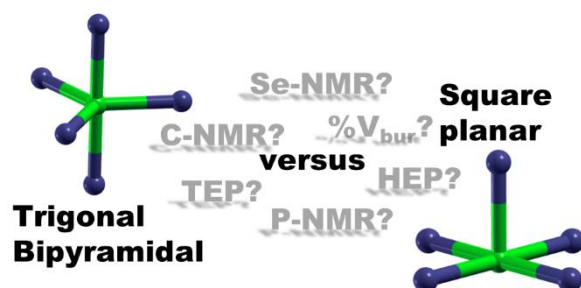
ARTICLE

Trigonal Bipyramidal or Square Planar? Density Functional Theory calculations of iron bis(dithiolene) N-heterocyclic carbene complexes

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Density functional theory (DFT) calculations of 57 iron bis(dithiolene)-N-heterocyclic carbene adducts were conducted to determine what parameters predict, and possibly influence, the coordination of these aforementioned adducts. The parameters considered herein include three different types of nuclear magnetic resonance (C-NMR, Se-NMR, and P-NMR) isotropic chemical shifts, the Tolman Electronic Parameter (TEP), the Huynh Electronic Parameter (HEP), and the percent buried volume (%V_{bur}) of the different N-heterocyclic carbenes (NHCs) calculated from DFT. These parameters were selected based upon prior literature connection to σ -donor ability, π -acidity, and steric effects. The computed values of the properties were compared via multivariable linear regression models to see which properties best predict the Addison τ parameter—a measure of whether the complex would assume the square pyramidal or trigonal bipyramidal geometry. It was determined that a combination of TEP and %V_{bur} are the best predictors of the τ value, for the parameters considered herein. The inclusion of additional parameters yields mild improvement to the statistical models for the prediction of the τ value.

Introduction

N-heterocyclic carbenes (NHCs) are a class of molecules with interesting electronic properties that have application in many areas of chemistry—most dominantly in organometallic chemistry, materials chemistry, and catalysis.^{1–3} These ligands have many applications because they are highly modular, meaning they are extremely diverse in terms of both structure and stereo-electronic diversity.^{1,4} This modular behavior is enhanced by the large libraries of NHCs that have been prepared.^{2,4–6}

Though there are many different structures of NHCs, this work will focus on the simple, imidazole-2-ylidenes (shown below in Figure 1).^{2,7} All imidazole-2-ylidenes NHCs contain a pentagonal carbon/nitrogen structure, including a lone pair of electrons on the head carbon. The nucleophilic carbene is stabilized by the donation of π -electron density from the two adjacent nitrogen heteroatoms to the carbon and by the σ -withdrawing nature of the nitrogen atoms.^{2,5,8}

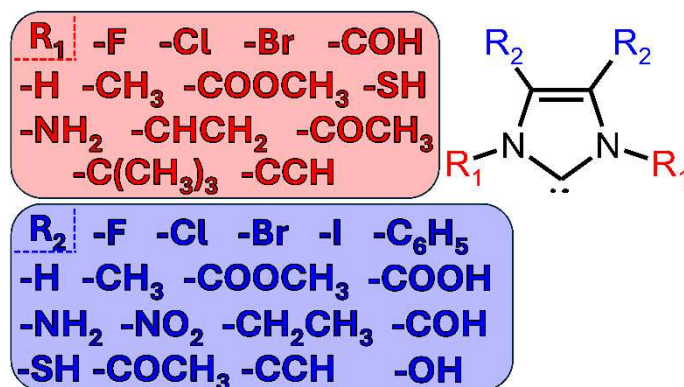


Figure 1: Skeletal structures of the N-heterocyclic carbenes (NHCs) considered in this study.

In an experimental sense, NHCs are fairly easy to prepare when paired with a transition metal, and contain a strong bond between the metal and the NHCs. NHCs play an important role in transition metal complexes because of their ability to act as strong σ -donor ligands while behaving as π -acceptors, making the interaction tunable.^{2,6,8–10} The NHC will donate electron density from an occupied orbital to the metal while simultaneously accepting electron density from the metal into an unoccupied molecular orbital. This bonding mechanism results in a strong bond between the metal center and the NHC ligand.⁸ Examples of different techniques/parameters that have been considered to deconvolute the NHC-metal center bond can be found in Figure 2.

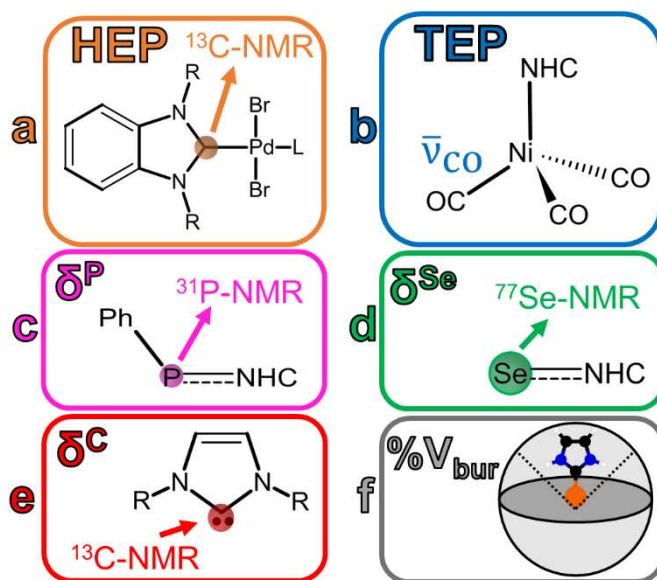


Figure 2: Schematic representations of (a/orange) the Huynh Electronic Parameter (HEP), (b/blue) the Tolman electronic parameter (TEP), (c/pink) phosphorous isotropic chemical shift (δ^{P}), (d/green) selenium isotropic chemical shift (δ^{Se}), (e/red) free-carbene carbon isotropic chemical shift (δ^{C}), and (f/grey) percent buried volume ($\%V_{\text{bur}}$).

The Tolman Electronic Parameter (TEP) is determined by measuring the symmetric CO stretch in nickel-containing complexes. Originally this technique was applied to carbonyl complexes with phosphorous ligands¹¹ but has since been applied to NHC complexes.⁵ While the previously mentioned NMR techniques can be utilized to parse out σ/π contributions, TEP has been associated with only net bonding impact and cannot be utilized to determine σ/π donating/accepting character. A stronger net electron donor should increase electron density at the Ni atom, strengthening the metal-carbon bond but weaken the CO bond order, yielding a lower CO frequency value. A stronger net acceptor would do the

opposite—ligands competing for backbonding from the metal center's electron density result in a higher CO stretching frequency.

Previously, the electronic structure of NHCs has been examined on the basis of gauging their π -acidity.¹² This is typically done via Se-NMR and/or P-NMR^{5,13–15}. Additionally, the σ -donating capabilities of these NHCs have also been judged utilizing the Huynh electronic parameter (HEP) which uses ¹³C-NMR to gauge the σ -donor strength of a ligand. The isotropic chemical shift indicates more (upfield) or less (downfield) shielding on the carbene carbon atom of the 1,3-diisopropylbenzimidazolin-2-ylidene ligand, attached to a Pd atom complex. An upfield signal indicates a weaker σ -donor, while a downfield signal represents a stronger σ -donor. Together, HEP and Se-/P-NMR probe techniques can be utilized to understand σ -donor/ π -acceptor trends and net impacts on bonding for NHCs.^{13,14}

The percent buried volume (%V_{bur}) calculation defines the percentage of a coordination sphere around a metal-ligand complex that is occupied by the NHC ligand, thereby relating %V_{bur} to steric hinderance/bulk.^{8,9,16} The center is the metal contained in the complex and the sphere has a defined radius (usually 3.50 Å, but can be user defined).^{9,17} A higher %V_{bur} value should indicate a bulkier ligand and has been connected to steric hinderance. Clavier *et al.* have demonstrated a correlation between the Tolman cone angle (θ) and %V_{bur} for a variety of different phosphine ligands contained in gold(I) chloride complexes.⁹

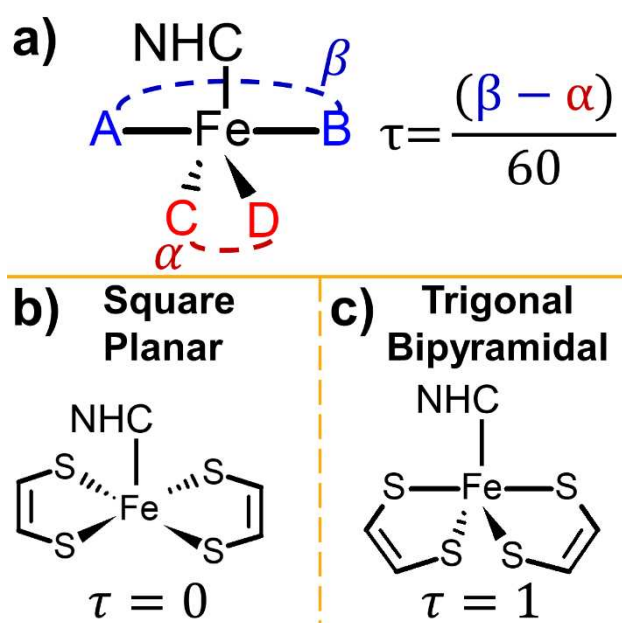


Figure 3: a) A visual description of the Addison τ parameter. Examples of square planar geometry (b) and trigonal bipyramidal geometry (c). For the square planar geometry, $\alpha = \beta = 180^\circ$, $\tau = 0$ and for trigonal bipyramidal geometry $\alpha \approx 120^\circ$, $\beta \approx 180^\circ$, $\tau \approx 1$.^{18,20}

In terms of physical structure, the geometry of NHC-metal complexes can be understood utilizing the Addison τ parameter.^{18–20} This parameter reveals information such as the coordination number of complex and is relevant to the catalytic ability of the complex.^{19,21,22} The value of τ is calculated as

$$\tau = (\beta - \alpha) / 60 \quad [1]$$

where β and α are bond angles of adjacent dithiolene ligands, as seen in Figure 3. The Supporting Information contains α and β for each of the considered complexes. The calculation of the τ parameter will yield a value between 0 and 1, indicating the coordination space around the metal center. A value near 0 will indicate the complex is in a square pyramidal shape, while a value closer to 1 will indicate a trigonal bipyramidal geometry.

Understanding the relationship between electronic structure, physical structure, and the effect of different R groups on the τ parameter is imperative to our understanding of how NHCs function and how they might be useful for future applications, especially with regards catalysis or how these molecules interact with surfaces as a possible route to safe hydrogen storage.^{23,24}

Computational Details

With regards to experimental design: Previous studies have outlined the basic structure of many different varieties of these molecules, and the imidazolydene form was selected for investigation. All structures were constructed optimized using the UFF force field in the program Avogadro.²⁵ All density functional theory (DFT) calculations were conducted using TURBOMOLE,²⁶ the BP86 functional,²⁷ and the def2-TZVPD²⁸ basis set. We, and others, have found the BP86 functional to be sufficient for obtaining the correct spin-states for iron bis(dithiolene) complexes.^{19,29}

Nuclear Magnetic Resonance (NMR) shielding constant calculations were completed with the previously described basis functions and functional for all systems other than our Huynh Electronic Parameter (HEP)^{5,30}. In calculations of the HEP, the dhf-TZVP basis was used for each of the lighter elements, and the dhf-ecp was utilized for Pd atoms. HEP and free NHC ¹³C chemical shifts (δ^C) were calculated utilizing equation 2:

$$\delta = \sigma_{reference} - \sigma_{probe} \quad [2]$$

where σ_{probe} is the isotropic chemical shielding of the nuclei of interest, and $\sigma_{reference}$ is the isotropic chemical shielding of a carbon nuclei in tetramethylsilane (TMS). Selenium chemical shifts (δ^{Se}) were calculated in a similar fashion to equation 2 with $\sigma_{reference}$ referenced to the selenium isotropic chemical shielding of dimethylselenide. For phosphorous chemical shifts (δ^P), the method developed by Maryasin et. al³¹ was adopted as the primary reference standard for ³¹P NMR is often a 85% solution of phosphoric acid in water, a difficult system to model.³² Equation 3 was utilized to calculate δ^P :

$$\delta^P = \sigma_{reference} - \sigma_{probe} - \delta_{reference} \quad [3]$$

Where σ_{probe} is the isotropic chemical shielding of the nuclei of interest, and $\sigma_{reference}$ is the isotropic chemical shielding of a phosphorous nucleus in secondary reference compound, and $\delta_{reference}$ is the chemical shift of the reference nucleus with respect to a primary reference. We elect to choose triphenylphosphine (PPh₃) as our secondary reference. In the gas phase, PPh₃ has a chemical shift of -4.7 ppm.³¹

For Tolman Electronic Parameter (TEP) calculations, nickel containing complexes were analysed via a vibrational frequency calculation that measured the CO stretch. Vibrational frequencies were visualized using the TMoleX19 application.

A comparison of the theoretical spectroscopic values and experimental values for different NHCs considered herein is provided in the supporting information.

For the buried volume calculation (%V_{bur}), the web application SambVca 2.1^{17,33} was utilized which calculated the percent buried volume of the NHC in the NHC-iron bis(dithiolene) complexes.

All statistics and regression models were calculated with the statistics software package R, version 4.3.0.³⁴ Max-min normalization was applied to each variable when constructing regression models, following equation 4:

$$x' = \frac{x - x_{min}}{x_{max} - x_{min}} \quad [4]$$

where x is the calculated property obtained from our DFT calculations, x' is the normalized value, and x_{max}/x_{min} is the maximum/minimum, respectively, value determined for x of all NHCs considered herein. This should result in a value between 0 and 1 for all properties included within the regression model.

Results and Discussion

In order to gain more clarity regarding the impact of the electronic structure of the NHCs on the complexes, the different parameters were calculated (HEP, TEP, δ^P , δ^{Se} , and δ^C). The Addison τ values and %V_{bur} were extracted from the geometry optimizations of the iron bis(dithiolene) adducts. HEP values were extracted from vibrational frequency calculations of optimized HEP complexes. TEP values were extracted from vibrational frequency calculations of optimized TEP-NHC complexes. Se isotropic chemical shifts (δ^{Se}) were calculated from NMR calculations of optimized Se-NHC adducts. P isotropic chemical shifts (δ^P) were calculated from NMR calculations of optimized phosphinidene-NHC adducts. Carbene carbon isotropic chemical shifts (δ^C) were calculated from optimized free NHC geometries. A schematic representation of the aforementioned parameters can be seen in Figure 2. These values were normalized in preparation for the regression analysis.

A pairwise plot (also often referred to as a scatter plot matrix) and heatmap of the previously mentioned parameters can be found in Figure 4. Figure 4a illustrates relationship between two variables within the considered parameters while Figure 4b provides the associated Pearson correlation coefficient between each variable. A value of +1 signifies a total positive correlation, a value of zero indicates no correlation, and a value of -1 signifies a negative linear correlation. Selenium isotropic chemical shift seems have positive correlations with δ^P , δ^C , & %V_{bur}. This is unsurprising as these previously mentioned chemical shifts are a metric of π -acidity. The most negatively correlated parameters were HEP and %V_{bur}. The most positively correlated parameter with τ was %V_{bur} while TEP was the most negatively correlated.

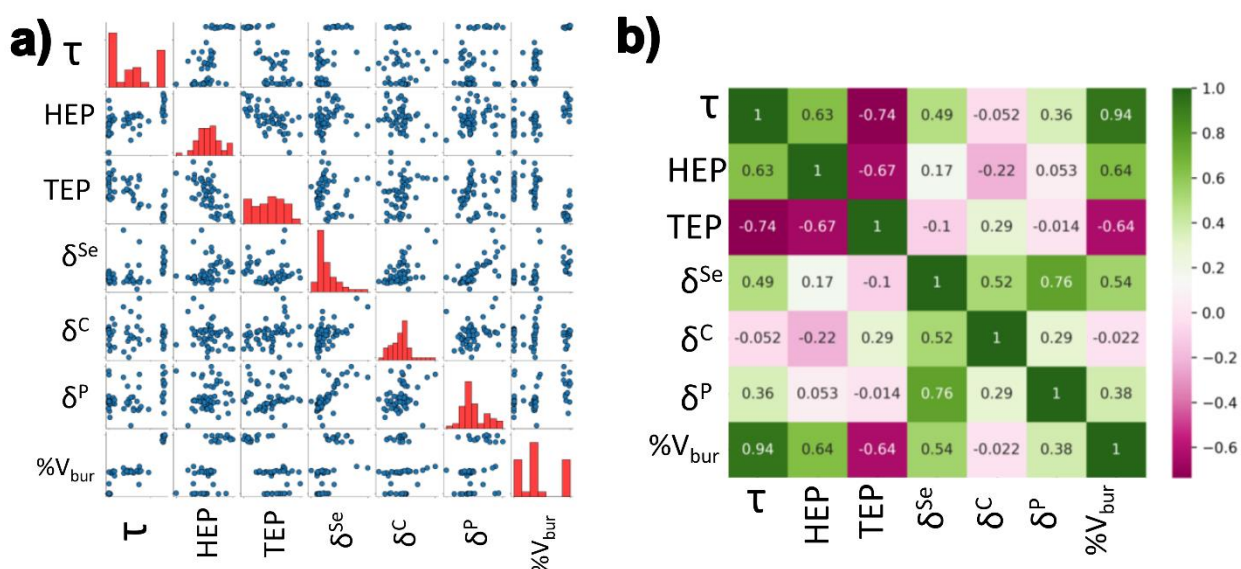


Figure 4: a) A pairwise plot and b) heat map of the Pearson coefficients for the parameters summarized in Figures 2 & 3. For the pairwise plot, the blue circles in a) represent the calculated properties of each individual NHC, while the red bars indicate the distribution of data. For the heatmap in b), green values show a positive Pearson correlation while pink indicates a negative correlation between the different parameters.

Utilizing least-squares-fits, single-/multi-variable regression models were constructed from the normalized aforementioned parameters to predict the τ parameter of 57 iron bis(dithiolene)-NHC adducts. The structure of the considered NHCs can be found in Figure 1. A total of 63 different linear-regression models were created that predicted τ values. These models contained varying degrees of freedom (DOF) ranging from 3 DOF to 8 DOF. Models including only 1 independent variable were found to have poor performance in the predictability of τ values. A full summary of all models can be found in the Supporting Information. In order to determine the optimal model, a series of statistical parameters were considered, including residual standard error (S), adjusted R^2 values, and Akaike Information

Criterion (AIC)³⁵ values, and Bayesian information criterion (BIC)³⁶ values. See S2 in Supporting information for full statistical analysis, but for brevity only the 5 most accurate models, as seen in Table 1, are discussed herein.

Model 1 (see Table 1) had the 2nd largest adjusted R² value (0.9077) of the tested models, indicating a “linear” fit of the data to τ values. This model also has the lowest S, and AIC value, and the 2nd lowest BIC model indicating the model is more suitable to predict τ values compared to the other models. AIC and BIC are utilized to balance model fit with complexity of the model. It is well known that AIC emphasizes prediction accuracy while BIC is better in the identification of the “true” model in smaller sample sizes.

Of the variables studied in this work that most correctly predicted the τ values, it can be seen that there is a trend in which the five best models, which all utilize TEP, and %V_{bur} as independent variables. This indicates that electronic parameters, such as TEP, and steric parameters, such as %V_{bur}, must be considered when predicting the τ value. σ^C also appears in the top 4 models, another electronic parameter. Interestingly, HEP and σ^{Se} , highly regarded and useful metrics to better understand the electronic structure of NHCs, were found to only appear in 2 of the 5 top performing models. What can be inferred from all of these top performing statistical models is that both electronic effects and steric interactions must be taken into account when exploring the impact of modifying the NHC on the geometry of the transition metal complex.^{10,15} Sole consideration of only one or a few of these properties will not provide a wholistic picture of the bonding mechanisms occurring in these systems. Therefore, those looking to make correlations with these aforementioned properties should be cautious to make those correlations with limited data.

Table 1: Top 5 performing models considered in this study along with their adjusted R² value (Adj-R²), standard error (S), AIC values, and BIC values.

Model #	Model Equation	Adj-R ²	S	AIC	BIC
1	$\tau = -1.927 \cdot 10^{-2} (\text{TEP}) - 7.625 \cdot 10^{-4} (\sigma^P) + 6.956 \cdot 10^{-2} (\%V_{\text{bur}}) + 38.019$	0.9077	0.1577	-42.11	-31.98
2	$\tau = -1.732 \cdot 10^{-2} (\text{TEP}) + 7.362 \cdot 10^{-2} (\%V_{\text{bur}}) + 33.716$	0.9091	0.1595	-41.79	-33.68
3	$\tau = -1.925 \cdot 10^{-2} (\text{TEP}) - 1.353 \cdot 10^{-4} (\sigma^{Se}) + 6.876 \cdot 10^{-2} (\%V_{\text{bur}}) + 37.987$	0.9067	0.1586	-41.41	-31.29
4	$\tau = -1.861 \cdot 10^{-2} (\text{TEP}) - 1.116 \cdot 10^{-3} (\sigma^C) + 7.265 \cdot 10^{-2} (\%V_{\text{bur}}) + 36.341$	0.9052	0.1599	-40.58	-30.45
5	$\tau = -2.043 \cdot 10^{-2} (\text{TEP}) - 1.966 \cdot 10^{-2} (\text{HEP}) - 7.127 \cdot 10^{-4} (\sigma^P) + 7.113 \cdot 10^{-2} (\%V_{\text{bur}}) + 40.369$	0.9066	0.1587	-40.58	-28.42

Conclusions

DFT calculations at the BP86/def2-TZVPD level of theory of iron bis(dithiolene)-N-heterocyclic carbene adducts were conducted to investigate what factors influence the coordination in these iron-containing complexes. Several parameters were connected to the coordination based on their documented associations with σ -donor ability, π -acidity, and steric effects. Using multivariable linear regression models, these parameters were compared to determine their correlation with the Addison τ parameter, which indicates whether the complex adopts a square pyramidal or trigonal bipyramidal geometry. The analysis revealed that a combination of TEP and %V_{bur} together are the most effective predictors of the τ value among the parameters considered in this study. Adding more parameters leads to only slight improvements in the statistical models for predicting the τ value.

Author Contributions

K.M.: Investigation, Data curation, Methodology, Project administration, Writing-original draft, Writing-review & editing, Formal analysis, Visualization

A.V.B.S.: Writing-review & editing

S.S.: Conceptualization, Resources, Supervision, Funding acquisition, Investigation, Data curation, Methodology, Project administration, Writing-original draft, Writing-review & editing, Software, Formal analysis, Validation, Visualization

Conflicts of interest

There are no conflicts to declare.

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