

## ARTICLE

# Room-temperature in-plane thermoelectric transport in 2H-MoTe<sub>2</sub> with back-gate bias modulation

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On-chip integrated nanoscale coolers are in high demand due to the shrinking device size of modern electronics. Thermoelectric and thermionic coolers made out of 2D layered materials are one attractive solution. 2D transition metal dichalcogenides can have relatively good electrical properties and relatively low thermal conductivities, which indicates their potential to reach a high thermoelectric figure of merit. Here, we report a comprehensive experimental and theoretical study on the thermoelectric transport properties of thin 2H-MoTe<sub>2</sub> flakes prepared in field-effect transistor geometry to enable electrostatic gating. The electrical conductivity and the Seebeck coefficient were measured as a function of the back gate voltage. Applying the back gate voltage was found to enhance the thermoelectric power factor by up to 45 % compared to the zero-bias value. The in-plane thermal conductivity of  $9.8 \pm 3.7 \text{ W m}^{-1} \text{ K}^{-1}$  was measured using the heat diffusion imaging method in a 25 nm thick flake. The electronic band structure and the electrical transport are further studied using first-principles calculations with energy-dependent relaxation times, by considering electron-phonon scattering and ionized impurity scattering. First-principles calculations are also performed to obtain thermal conductivity values using both the relaxation time approximation and the full iterative solution to the phonon Boltzmann equation, as a validation of the experimental measurements. This fundamental study of 2H-MoTe<sub>2</sub> expands our understanding of the 2D thermoelectrics and offers pathways to further enhancements in the device's performance.

## Introduction

In recent years, there has been growing research interest in 2D thermoelectric materials.<sup>1</sup> Thermoelectric modules can convert thermal energy to electricity or use electricity for heat management. The thermoelectric power factor is defined as  $PF = \sigma S^2$ , where  $\sigma$  is the electrical conductivity and  $S$  is the Seebeck coefficient,  $S = -\frac{\Delta V}{\Delta T}$ . Seebeck effect describes how much voltage difference ( $\Delta V$ ) can be generated with a temperature difference ( $\Delta T$ ) and is the basis of thermoelectric power generation. Power factor times temperature ( $PFT$ ) is also often used since it shares the same unit as thermal conductivity,  $k$ . The efficiency of thermoelectric energy conversion is an

increasing function of the thermoelectric figure of merit,  $ZT = \frac{PFT}{k}$ .

With the continued miniaturization of modern electronics, the dissipated power density keeps increasing<sup>2</sup>. 2D materials are great candidates for nanoscale power generation to recycle waste heat and for hot spot cooling due to their nanometer thicknesses. They often possess unique chemical, mechanical, and physical properties compared to their bulk counterparts<sup>3,4</sup>. As a result of the small thickness, the Fermi level and the charge carrier concentrations of 2D materials can be tuned by electrostatic gating using the electric field effect<sup>5</sup>. This is an advantage over bulk materials as it avoids chemical doping processes and allows real-time Fermi-level tuning and optimization of the thermoelectric figure of merit using a single sample. For example, monolayer graphene on hexagonal boron nitride (hBN) has been shown to have a  $PFT$  as high as  $10.35 \text{ W m}^{-1} \text{ K}^{-1}$  at room temperature under the optimal back gate bias<sup>6</sup>, which is one order of magnitude higher than that of commercial thermoelectric material, bulk Bi<sub>2</sub>Te<sub>3</sub>. Graphene also has a high thermal conductivity on the order of  $1000 \text{ W m}^{-1} \text{ K}^{-1}$ . While this makes graphene an excellent candidate for active cooling purposes<sup>7–9</sup>, where passive cooling by phonon transport works together with active cooling by the Peltier effect to conduct heat away from the hot spots, it also means that its  $ZT$  is not as appealing for thermoelectric energy conversion applications.

For conventional energy conversion applications, we turn to 2D transition metal dichalcogenides (TMDs). They possess a

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wide range of tunable electronic properties (from insulating to superconducting) and a relatively low thermal conductivity (much smaller than graphene), which may result in high  $ZT$  values. High  $ZT$  requires a large Seebeck coefficient, high electrical conductivity, and low thermal conductivity. At the same time, the interplay between these transport parameters means that  $ZT$  enhancement is complex: for example, the higher carrier concentration is beneficial for higher electrical conductivity but leads to lower Seebeck coefficient values. The intricate balance usually occurs in highly doped semiconductors<sup>10</sup> or possibly semimetals<sup>11</sup>.

2D semiconductor  $\text{MoS}_2$  has been studied extensively for thermoelectric applications and the best-performing samples showed a  $PFT$  close to  $2.5 \text{ Wm}^{-1}\text{K}^{-1}$  with high mobility of  $60 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$  (bilayer on  $\text{SiO}_2$  at room temperature)<sup>12</sup> and up to  $350 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$  (six layers on hBN at 50 K)<sup>13</sup>. This large  $PFT$  has been achieved following years of continued research effort. In 2014, a large Seebeck coefficient of  $-30 \text{ mV/K}$  was reported for CVD-grown monolayer  $\text{MoS}_2$ ; the power factor, however, was small due to low conductance.<sup>14</sup> Two years after this, bilayer  $\text{MoS}_2$  was shown to have a Seebeck coefficient of  $-450 \text{ } \mu\text{V/K}$  and a power factor of  $1.5 \text{ Wm}^{-1}\text{K}^{-1}$ .<sup>15</sup> Characterization of the in-plane thermal conductivity of many 2D materials is challenging due to their small sample dimensions. In the case of  $\text{MoS}_2$ , there have been large discrepancies depending on the sample qualities and the experimental techniques. Even with the same Raman spectroscopy-based technique, reported values were between  $35$  and  $85 \text{ Wm}^{-1}\text{K}^{-1}$  for monolayer  $\text{MoS}_2$ <sup>16–19</sup>, where the sample absorption coefficient and the sample quality were expected to play a significant role. The thermal bridge method had a thermal conductivity of few-layer  $\text{MoS}_2$  at about  $45 \text{ Wm}^{-1}\text{K}^{-1}$ <sup>20</sup> and monolayer  $\text{MoS}_2$  at  $24 \text{ Wm}^{-1}\text{K}^{-1}$ <sup>21</sup>. Molecular dynamics calculations revealed thermal conductivity of  $117 \text{ Wm}^{-1}\text{K}^{-1}$  for suspended monolayers and  $31 \text{ Wm}^{-1}\text{K}^{-1}$  for supported samples.<sup>22</sup> As sample quality also affects carrier mobility and transport performance, these large uncertainties make it less plausible to estimate  $ZT$  by combining  $PFT$  and  $k$  across different studies.

2H- $\text{MoTe}_2$  is another semiconducting molybdenum-based TMD material with an indirect gap of  $0.83 \text{ eV}$  in the bulk form and a direct gap of  $1.1 \text{ eV}$  in the monolayer limit.<sup>23,24</sup> Most of the research on  $\text{MoTe}_2$  has been focused on electronic<sup>25–28</sup> and optoelectronic<sup>26,29</sup> applications whereas the studies of its thermoelectric properties are limited. Seebeck coefficient of n-type single crystal bulk  $\text{MoTe}_2$  was measured to be around  $-400 \text{ } \mu\text{V/K}$  from  $77 \text{ K}$  to  $300 \text{ K}$ <sup>30</sup>. At room temperature, its electrical conductivity was about  $750 \text{ S/m}$  and its  $PFT$  was  $0.036 \text{ Wm}^{-1}\text{K}^{-1}$ .<sup>30</sup> A  $330 \text{ nm}$  thick 2H- $\text{MoTe}_2$  thin film prepared by magnetron co-sputtering showed a p-n type transition with increasing temperature, giving a maximum  $PFT$  of  $0.15 \text{ Wm}^{-1}\text{K}^{-1}$  at  $460 \text{ K}$  for p-type conduction and  $0.55 \text{ Wm}^{-1}\text{K}^{-1}$  at  $670 \text{ K}$  for n-type conduction<sup>31</sup>. At room temperatures, the sample was p-type with  $\sigma = 1.5 \times 10^4 \text{ S/m}$ ,  $S = 25 \text{ } \mu\text{V/K}$  and a  $PFT$  of  $0.0028 \text{ Wm}^{-1}\text{K}^{-1}$ .<sup>31</sup> The enhancement in  $PFT$  at higher temperature was a result of increased Seebeck coefficient values with increasing conductivity, which was unusual and was attributed to improved mobility. Investigations of the thermal conductivity

of  $\text{MoTe}_2$  are also very limited. Yan et al. determined the c-axis thermal conductivity of  $\text{MoTe}_2$  as  $1.5 \text{ Wm}^{-1}\text{K}^{-1}$  at  $300 \text{ K}$  using time-domain thermoreflectance (TDTR) method.<sup>32</sup> DFT calculations estimated the in-plane lattice thermal conductivity of monolayer  $\text{MoTe}_2$  to be around  $60 \text{ Wm}^{-1}\text{K}^{-1}$  at room temperature.<sup>33</sup> These studies indicate that 2H- $\text{MoTe}_2$  can be a potential candidate for thermoelectrics, especially in the few-layer limit when the band structure changes due to quantum confinement and the chemical potential can be tuned by the gate voltage.

In this manuscript, we report a comprehensive experimental and theoretical study of room-temperature in-plane thermoelectric transport in thin 2H- $\text{MoTe}_2$  flakes. Electrical conductivity and Seebeck coefficient are measured as a function of the back gate bias. Further understanding of the electrical transport data is provided by first-principles calculations with energy-dependent relaxation times, by considering electron-phonon scattering and ionized impurity scattering. Thermal conductivity is also reported, which, to the best of our knowledge, is the first in-plane thermal transport characterization of thin  $\text{MoTe}_2$ . Due to the difficulty in measuring the thermal conductivity of thin 2D films, most of the literature reports only the power factor. The thermal conductivity measurements enable us to estimate  $ZT$  as well as to provide a more complete evaluation of the  $\text{MoTe}_2$  material in terms of thermoelectric applications. In-plane thermal conductivity of bulk  $\text{MoTe}_2$  is also calculated within both the relaxation time approximation and the full iterative solution to the phonon Boltzmann equation, and compared to the experimental data.

## Materials and Methods

$\text{MoTe}_2$  crystals were grown by the Chemical Vapor Transport (CVT) method using polycrystalline  $\text{MoTe}_2$  charge and iodine transport agent. The growth was conducted in a vacuum-sealed quartz ampoule at  $970 \text{ }^\circ\text{C}$  for 7 d followed by a 3 d annealing at  $800 \text{ }^\circ\text{C}$  to stabilize the hexagonal 2H phase. Phase purity was confirmed by powder X-ray diffraction measurements.

### Device fabrication

Thin 2H- $\text{MoTe}_2$  flakes were exfoliated onto  $300 \text{ nm SiO}_2/\text{p}^+-\text{Si}$  substrates by the Scotch tape method. The substrates were pre-cleaned by acetone and isopropanol sonication, followed by annealing at  $400 \text{ }^\circ\text{C}$  in forming gas (5%  $\text{H}_2/95\% \text{ Ar}$ ) to remove chemical residues. Flakes with a uniform thickness were chosen under an optical microscope. The thickness of the exfoliated flakes was characterized by a Bruker Dimension Icon atomic force microscope (AFM) and was around  $25 \text{ nm}$  for the two devices presented below. The standard thermoelectric electrode patterns were prepared using laser lithography ( $385 \text{ nm}$ ), which includes one heater, two thermometers, and two side contacts, see inset in Fig. 1 for the geometry of the device.  $5 \text{ nm Ti}$  and  $100 \text{ nm Au}$  were evaporated as contact metals (base pressure  $< 10^{-5} \text{ Torr}$ ,  $1 \text{ } \text{\AA}/\text{s}$ ). The shape of each flake was identified under a microscope and subsequently etched to a rectangular shape by opening etch windows with

laser lithography and then reactive ion etching (RIE) with SF<sub>6</sub> (30 W) for up to 1 min. Exposure to air during the fabrication process might cause some surface oxidation, but the oxidation is known only to occur in the top two or three layers near the surface and the bulk of the flake remains intact<sup>34</sup>. The samples were kept inside an argon-filled glovebox and annealed in a high vacuum ( $\sim 10^{-6}$  Torr) at 325 °C for 30 min in the cryostat immediately before measurements to minimize effects from environmental contamination.

#### Measurement setup

The electrical transport measurements were performed in a JANIS cryostat system customized for transport measurements in a high vacuum ( $\sim 10^{-6}$  Torr). A Keithley 2401 SourceMeter was used to measure the four-probe resistance under 1  $\mu$ A current. Back gate voltage,  $V_g$ , was applied to the highly doped Si substrate using a Keithley 2400 SourceMeter. The leakage current from the back gate was limited to a few nA for  $V_g$  up to 100 V. Up to 30 mA current was passed through the heater during Seebeck coefficient measurements and the generated Seebeck voltage was recorded by a Keithley 2182A nanovoltmeter.

The thermal conductivity was measured following the heat diffusion imaging method.<sup>35</sup> This thermoreflectance-based approach captures the temperature decay along the sample after heat flow injection and extracts the thermal conductivity using the heat spreader model. The thermoreflectance imaging system from Microsanj LLC used a 532 nm green LED as the light source. Electrical pulses (5 V, 5 ms) were sent to the heater.

#### First-principles calculations

First-principles calculations were performed using the density functional theory (DFT) and density functional perturbation theory (DFPT) as implemented in the QUANTUM ESPRESSO package.<sup>36</sup> We used ultrasoft pseudopotential<sup>37</sup> with modified Perdew-Burke-Ernzerhof generalized gradient approximation (PBEsol)<sup>38</sup>. A kinetic energy cutoff of 70 Ry and Monkhorst-Pack k-point mesh of  $10 \times 10 \times 4$  was employed in the electronic structure calculation. The convergence threshold of energy was set to  $10^{-7}$  in the self-consistent calculation. The lattice parameters of hexagonal MoTe<sub>2</sub> were chosen based on experimental results.<sup>39</sup> The dynamical matrix was computed on a  $4 \times 4 \times 2$  q-point mesh in the phonon calculations and later interpolated by Fourier transform to compute the phonon modes and frequencies at other general k-points. To accurately describe the thermoelectric properties, we considered the energy-dependent relaxation times including electron-phonon and ionized impurity scattering in transport calculations. The electron-phonon lifetime ( $\tau_{e-ph}$ ) were calculated using the PERTURBO package<sup>40</sup> and the ionized impurity scattering rates were computed using a modified Brooks-Herring approach for strongly screened potential<sup>41</sup>. PERTURBO utilizes the Wannier interpolation scheme<sup>42,43</sup> and interpolates the electron-phonon coupling matrix from a coarse grid to a fine grid ( $60 \times 60 \times 60$ ). Wannierization of a total of 24 bands was performed using projections of  $d_{xy}$ ,  $d_{xz}$ ,  $d_{yz}$ ,  $d_{z2}$ ,  $d_{x2-y2}$  orbitals on each Mo atom and  $p_x$ ,  $p_y$ ,  $p_z$  orbitals on each Se atom. Later, the ionized impurity scattering was calculated using the following equation

<sup>41</sup> and added with the electron-phonon scattering to get the total relaxation time:

$$\frac{1}{\tau_{ion}} = \frac{\pi(N_I/Z)}{\hbar} \left( \frac{q^2 L_D}{\epsilon_0 \epsilon_r} \right)^2 g(E), \quad (1)$$

where  $g(E)$  is the density of states,  $\hbar$  is the reduced Plank constant,  $\epsilon_r$  is the relative permittivity,  $\epsilon_0$  is the permittivity of free space,  $N_I$  is the impurity carrier concentration,  $q$  is the electronic charge, and  $Z$  is the charge of the vacancy/impurity atoms. Here, n-type behavior in MoTe<sub>2</sub> is attributed to tellurium (Te) vacancies<sup>44</sup>. Tellurium vacancy results in the average of 2 conduction electrons per vacancy and therefore,  $Z = 2$  is used for the calculation of ionized impurity scattering rates of undoped MoTe<sub>2</sub> sample.  $L_D$  is the screening length and is given by:

$$\frac{1}{L_D^2} = \frac{q^2}{\epsilon} \int g(E) \frac{\partial f}{\partial E} dE, \quad (2)$$

where  $f$  is the Fermi-Dirac distribution function.

Finally, electronic transport calculation was performed in PERTURBO based on the semi-classical Boltzmann transport method with energy-dependent total relaxation times. For comparison, the transport properties were also evaluated using BoltzTraP package<sup>45</sup> with constant relaxation time approximation (CRTA)<sup>46</sup>. The transport calculations were performed in the in-plane directions and so, van der Waals interactions were not considered in the DFT and DFPT calculations. Using a similar approach, recently we have reproduced thermoelectric transport properties of MoSe<sub>2</sub><sup>47</sup> and SnSe<sub>2</sub>.<sup>48</sup>

In the case of phonons, we performed first-principles calculations by using the Vienna ab initio simulation (VASP), SCAN-rVV10 XC potential to calculate the harmonic and anharmonic interatomic force constants using a  $4 \times 4 \times 2$  supercell. The thermal conductivity of naturally occurring isotopic and hypothetical isotopically pure MoTe<sub>2</sub> bulk were then calculated on a converged q-space grid  $16 \times 16 \times 4$  by iteratively solving the phonon Boltzmann transport equation as implemented in the Sheng-BTE package.

## Results and Discussion

### Electrical transport characterization

The electrical conductivity of the thin MoTe<sub>2</sub> sample is plotted in Fig. 1(a) as a function of  $V_g$ . Without the application of the back gate voltage, the value was around 1350 S/m. The conductivity of MoTe<sub>2</sub> reported in the literature varies depending on the sample preparation. The observed electrical conductivity is within the reported literature values.<sup>30,31</sup> In comparison to the samples from the two references, the electrical conductivity of our sample doubles that of the bulk MoTe<sub>2</sub> crystal<sup>30</sup> while it is one order of magnitude smaller than that of the sputtered thin film sample<sup>31</sup>. As  $V_g$  is swept from -80 V to 80 V, its electrical conductivity varies by one order of magnitude, from 250 S/m to 2550 S/m. The conductivity goes up with increasing gate voltages. Since  $V_g$  is connected to the highly doped Si, increasing  $V_g$  means increasing electron density in the sample and thus the sample exhibits n-type behavior.

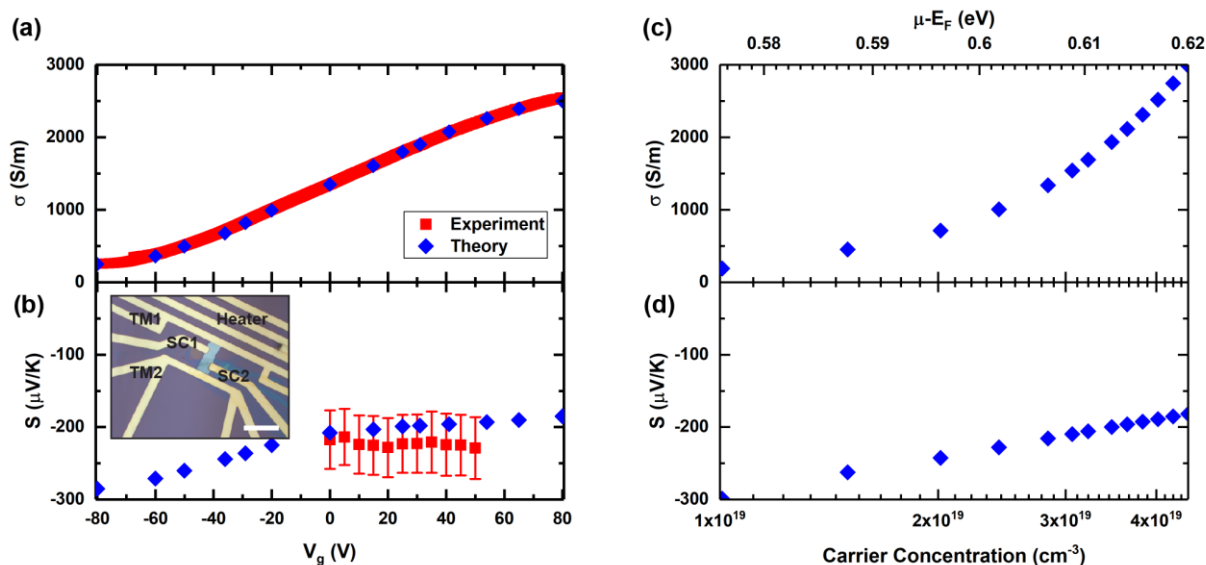


Fig. 1 Experimental (a) electrical conductivity and (b) Seebeck coefficient of the exfoliated thin MoTe<sub>2</sub> sample as a function of the gate voltage, compared with theoretically obtained values. Calculated (c) electrical conductivity and (d) Seebeck coefficients as a function of the carrier concentration (bottom axis) and the chemical potential with respect to the intrinsic Fermi level,  $\mu-E_F$  (top axis). The inset in (c) shows an optical image of the device, with the heater, the thermometers (TMs) and the side contacts (SC) noted. The scale bar is 20  $\mu\text{m}$ .

Another thicker sample of 100 nm was also measured and exhibited similar conductivity values and similar trends as a function of  $V_g$ . The results were included in ESI. The Seebeck coefficient was measured at different  $V_g$  as shown in Fig. 1(b). The negative  $S$  value confirms the n-type conduction of the sample. At  $V_g = 0$  V, the sample shows a Seebeck coefficient of  $-210 \mu\text{V/K}$ . This room temperature value is about half of that of the bulk single crystal<sup>30</sup> but one order of magnitude larger than that of the sputtered thin film<sup>31</sup>. The Seebeck voltage detection was noisy in the entire measurement range that prevented reliable measurements at negative  $V_g$ . Moreover, at large negative  $V_g$  values, an offset open voltage was detected even when the heater was turned off, which should have been close to zero. Similar behavior has been observed and explained for MoS<sub>2</sub>: when the semiconductor channel resistance becomes

too high, resistive coupling from the back gate to the channel causes the offset voltage.<sup>15</sup> The input bias current up to 120 pA from the nanovoltmeter also contributes to the offset voltage and the noise, which was observed for MoS<sub>2</sub><sup>15</sup> and for Si metal-oxide-semiconductor FETs with high resistance<sup>49</sup>. Presumably due to the noisy signals, no significant change in the Seebeck coefficient was observed within the  $V_g = 0$ –50 V range, although one could expect a lower Seebeck coefficient with higher electrical conductivity. The expected change in  $S$  value against  $V_g$  was calculated theoretically in the following section and is shown to be within our experimental error bars. The theoretical Seebeck coefficient reduces to  $-185 \mu\text{V/K}$  at  $V_g = 80$  V and grows to  $-285 \mu\text{V/K}$  at  $V_g = -80$  V (Fig. 1(b)).

#### Electronic Transport calculations

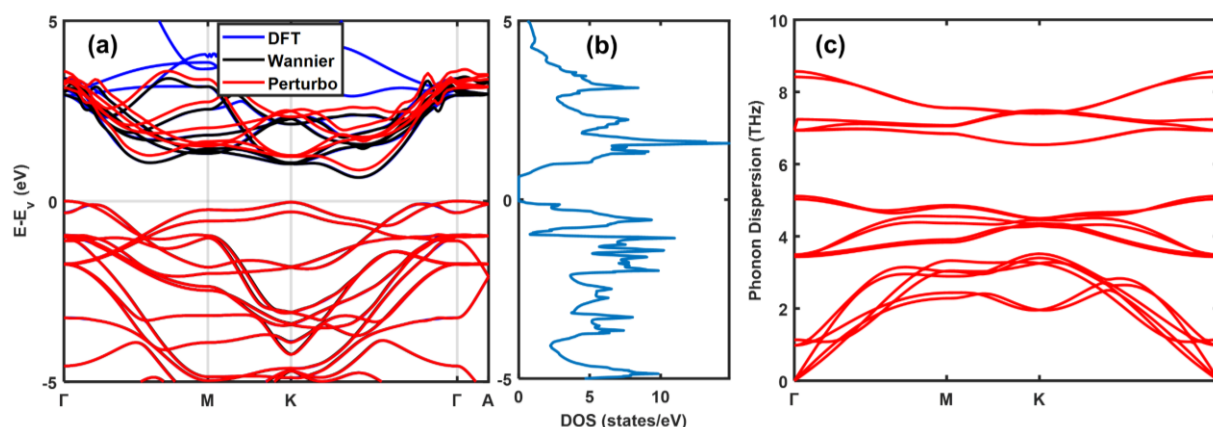


Fig. 2 (a) Electronic band structure, (b) electronic DOS from DFT, and (c) phonon dispersion of bulk MoTe<sub>2</sub>.

Since the devices are over 10 layers thick, they are considered bulk in the band structure calculations. Electronic band structure, electronic density of states (DOS), and phonon-dispersion of bulk MoTe<sub>2</sub> are shown in Fig. 2. The obtained DFT band structure is in good agreement with previous calculations<sup>50,51</sup> and Wannier interpolated band structure. The top of the valence band is at  $\Gamma$ , and the bottom of the conduction band is halfway between  $\Gamma$ -K, resulting in an indirect gap of 0.66 eV. It is well known that PBE functionals underestimate the bandgap for most insulators and semiconductors. So, we shifted the conduction bands during Wannier to PERTURBO interpolation and obtained a band gap of 0.87 eV which closely matches the experimental gap of 0.83 eV<sup>26,27,52</sup>.

The phonon dispersion of MoTe<sub>2</sub> is shown in Fig. 2(c). As the unit cell of hexagonal MoTe<sub>2</sub> has 6 atoms, there are 18 phonon modes at each k-point. Our results are in agreement with other DFPT calculations<sup>53</sup>.

The Seebeck coefficient and electrical conductivity at room temperature are evaluated using semi-classical BTE including electron-phonon scattering and ionized impurity scattering in PERTURBO. The ionized impurity scattering rates are calculated using a modified Brooks-Herring approach and added with electron-phonon scattering using the Matthiessen rule. Both scattering rates are shown in Fig. 3 along with the electronic DOS. It is evident that total scattering times are dominated by the ionized impurity scattering. Finally, transport calculations are performed considering energy-dependent total scattering times. At first, we used carrier concentration as a fitting parameter to match the experimental electrical conductivities at different gate voltages and reported the corresponding Seebeck coefficients. We found that the obtained Seebeck coefficients are within the error bar of the experimentally reported values in Fig. 1(b). Figure 1 (c, d) also show the raw theoretical calculations with no fitting of conductivity and Seebeck coefficient as a function of chemical potential and carrier concentration ( $1 \times 10^{19} \text{ cm}^{-3}$  to  $4 \times 10^{19} \text{ cm}^{-3}$ ), respectively. At zero gate voltage, experimental electrical conductivity and Seebeck are around 1350 S/m and -210  $\mu\text{V/K}$ , respectively, which are corresponding to the carrier concentration of  $2.9 \times 10^{19} \text{ cm}^{-3}$  and chemical potential of 0.6 eV above the intrinsic Fermi level ( $E_F$ ) as shown in Fig. 1(c, d). With increasing gate voltages, electrical conductivity and Seebeck coefficient follow opposite trends: as the carrier concentration increases with the increasing gate voltage, the Seebeck coefficient decreases and the electrical conductivity increases. The Seebeck coefficient changes from -300  $\mu\text{V/K}$  at  $1 \times 10^{19} \text{ cm}^{-3}$  to -189  $\mu\text{V/K}$  at  $4 \times 10^{19} \text{ cm}^{-3}$ . It can be seen that the experimental values are within the range of predicted theoretical values.

We have also analyzed the effects of electron-phonon and ionized impurity scattering on transport properties. The inclusion of ionized impurity scattering does not have any significant effect on the Seebeck coefficient, because the Seebeck coefficient is not sensitive to the details of relaxation times as shown in first principles-based calculations. However, with the ionized impurity scattering included, the electrical

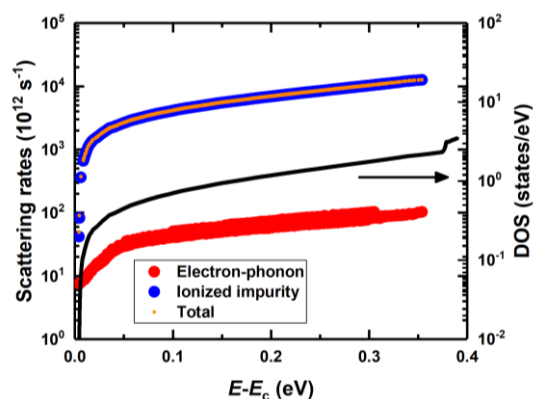


Fig. 3 Scattering rates and DOS as a function of the energy relative to the conduction band minimum ( $E_c$ ).

conductivity closely matches the experimental results. After successfully modeling the experimental Seebeck coefficient and electrical conductivity within energy-dependent relaxation time, we compared the results obtained from energy-dependent relaxation time and CRTA<sup>54</sup> as shown in Table 1. The details of the Seebeck coefficient and electrical conductivity obtained from BoltzTraP<sup>45</sup> are discussed in ESI Fig. S2. Within CRTA, relaxation times are assumed to be energy and momentum independent and the same constant for all electrons. As implemented in BoltzTraP, the constant relaxation time is not calculated. Hence, we take the average electron-phonon and ionized impurity scattering rates weighted by  $df/dE$  calculated within the Fermi-window ( $\mu \pm 20k_B T$ ) as the constant and use it in the CRTA calculations. This relaxation time at room temperature and at zero gate is 0.94 fs. Using this value, the obtained electrical conductivity is 2018 S/m and the Seebeck coefficient is -255  $\mu\text{V/K}$ . The discrepancies in the results between PERTURBO and BoltzTraP come from the use of different relaxation times. To accurately describe the transport properties of a material, energy or momentum dependent scattering times need to be considered.

Table 1. Comparison between experimental data at  $V_g = 0$  and theoretical calculations under different conditions

Parameters		$S$ ( $\mu\text{V/K}$ )	$\sigma$ (S/m)
Experiment		-210	1350
BoltzTrap- CRTA		-255	2018
PERTURBO	$\tau_{e-ph}$	-216	54096
	$(\tau_{e-ph}^{-1} + \tau_{ion}^{-1})^{-1}$	-207	1400

#### In-plane thermal transport

Heat diffusion imaging was applied to a second sample of the same 25 nm thickness to extract the in-plane thermal conductivity. An optical image of the sample as well as a thermoreflectance map is provided in Fig. 4(a) and (b). The sample surface temperature drops exponentially as a function



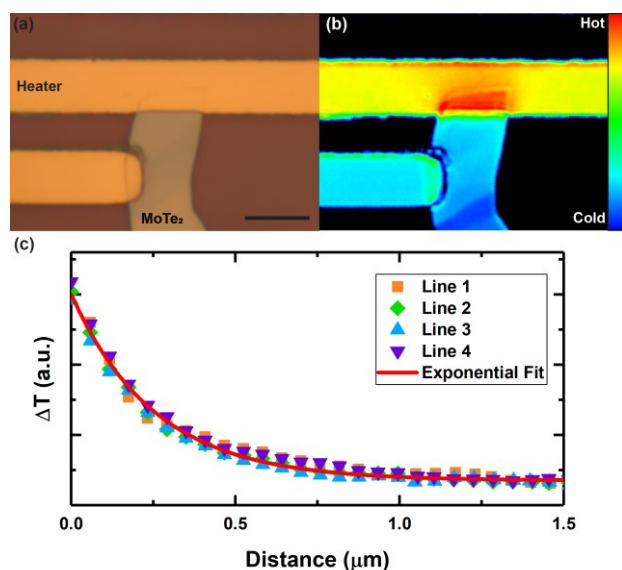


Fig. 4 (a) Optical image of the MoTe<sub>2</sub> device for thermal transport measurement. The scale bar is 5 μm. (b) Thermoreflectance map of the sample surface with 5 V supplied to the heater. Temperature decay curves were taken along the sample perpendicular to the heater. (c) Temperature decay curves and their corresponding exponential fit for thermal conductivity extraction.

of the distance away from the heater and can be fitted into a model for thermal conductivity extraction. Several example temperature decay curves along with an exponential fit are shown in Fig. 4(c). An in-plane thermal conductivity of  $9.8 \pm 3.7 \text{ W m}^{-1} \text{ K}^{-1}$  was obtained for MoTe<sub>2</sub> at room temperature. The error accounts for the variations from the multiple extracted temperature decay profiles for averaging. To the best of our knowledge, this thermal conductivity value is the first reported in multilayer MoTe<sub>2</sub> flakes. According to the Wiedemann-Franz law, the electronic contribution to the thermal conductivity is only on the order of  $0.01 \text{ W m}^{-1} \text{ K}^{-1}$ , which is negligible even with back gate modulation added. Therefore, we assume gating does not change the thermal conductivity.

Figure 5 shows the temperature dependence of the calculated thermal conductivity of MoTe<sub>2</sub> bulk along the in-plane direction from 200 K to 1000 K. The lattice thermal conductivity of MoTe<sub>2</sub> is calculated within both the relaxation time approximation (RTA) considering 3-phonon processes and the full iterative solution to the phonon Boltzmann equation for an isotopically pure sample. While the RTA results are closer to the experimentally measured value, it is known that the RTA solution gives a poor approximation to the lattice thermal conductivity compared to the full iterative method. These results are obtained by considering the interaction cutoff for cubic interatomic force constants calculations up to the seventh nearest neighbor. At room temperature, the calculated thermal conductivity of the isotopically pure bulk MoTe<sub>2</sub> is  $24 \text{ W m}^{-1} \text{ K}^{-1}$  which is on the same order of magnitude but larger than our experimentally measured value of  $9.8 \pm 3.7 \text{ W m}^{-1} \text{ K}^{-1}$ . The

addition of the naturally occurring isotope scattering lowers the thermal conductivity by 10% to  $22 \text{ W m}^{-1} \text{ K}^{-1}$ . The measured sample is a flake with the thickness of 25 nm. The addition of size effect in the simplest approximation can be done by adding a  $v/L$  term, where  $v$  is the group velocity and  $L$  is the thickness, to the scattering rates to serve as the boundary scattering. The addition of this boundary scattering term lowers the thermal conductivity further by 22% and is shown in the plot by the green dashed line. This is still larger than the experimentally measured value. The difference can be attributed to defects inside the experimental sample as well as phonon-electron scattering rates.

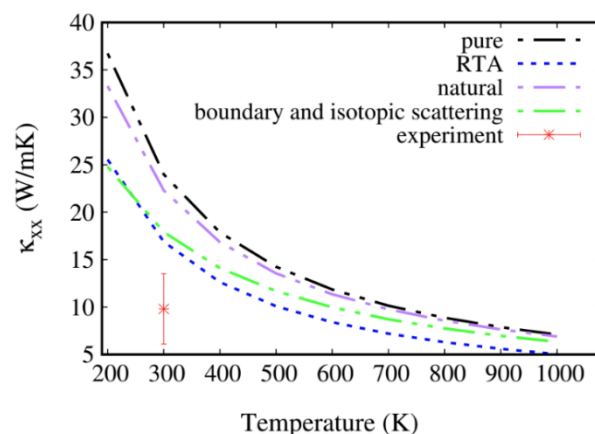


Fig. 5 Calculated thermal conductivity versus temperature of natural and pure MoTe<sub>2</sub> bulk along in-plane direction, and compared with experimental value.

#### Power factor and ZT

The peak power factor of thin MoTe<sub>2</sub> is expected to occur at the highest positive gate voltage since the improvement from the increasing electrical conductivity exceeds the impact from the decreasing Seebeck coefficient. By combining the experimental electrical conductivity and the theoretically predicted Seebeck coefficient, the peak  $PFT$  reaches  $0.027 \text{ W m}^{-1} \text{ K}^{-1}$  at  $V_g = 80 \text{ V}$ . Although our sample does not possess the highest electrical conductivity or the largest Seebeck coefficient value in comparison to the other two literature samples, by reaching a good balance between the two interrelated parameters, our peak  $PFT$  is comparable to the bulk single crystal MoTe<sub>2</sub> value<sup>30</sup> and is one order of magnitude larger than that of sputtered thin film MoTe<sub>2</sub><sup>31</sup>. Compared to the value of  $0.018 \text{ W m}^{-1} \text{ K}^{-1}$  at  $V_g = 0 \text{ V}$ , the back gate modulation is able to enhance the  $PFT$  by 45%.

The peak  $ZT$  at room temperature is about 0.003. We expect the figure of merit to improve at higher temperatures, as was seen in the case of MoTe<sub>2</sub> thin films<sup>31</sup>. Its performance might be further improved via a few routes. For example, previous research has shown that hBN substrate is flatter and has fewer charge puddles compared to SiO<sub>2</sub>, which can greatly improve the transport properties of 2D samples<sup>6,13</sup>. Estimation based on experimental conductivity and carrier concentration indicates

that the mobility of the sample was only  $3 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$ . Optimization of the fabrication process might produce samples with higher mobility.

## Conclusions

In summary, we have exfoliated and fabricated 2H-MoTe<sub>2</sub> samples for in-plane thermoelectric transport characterization. Back gate bias was applied to tune the Fermi level of the device and thus the electrical properties. The electrical conductivity increased with increasing gate voltages while the Seebeck coefficient values remained constant within the experimental error bar. The peak *PFT* of  $0.027 \text{ Wm}^{-1}\text{K}^{-1}$  was obtained at the largest positive bias of +80 V, which was a 45% increase compared to the zero-bias value. These experimental results were supported by first-principles calculations which accounted for electron-phonon scattering and ionized impurity scattering. With an in-plane thermal conductivity of  $9.8 \pm 3.7 \text{ Wm}^{-1}\text{K}^{-1}$ , the *ZT* of 2H-MoTe<sub>2</sub> was estimated to be 0.003. The power factor and the *ZT* values will be larger at higher temperatures. The thermal conductivity can be manipulated and increased by  $3.9 \text{ W/mK}$  under a 1 K temperature difference, by applying an optimum electrical current and using the active cooling method. Further enhancement of the device performance might be achieved by increasing the temperature, using hBN as a substrate, and optimizing fabrication processes to increase carrier mobility. This study adds to the 2D thermoelectric database and is a solid first step in utilizing 2D 2H-MoTe<sub>2</sub> as a thermoelectric material.

## Author Contributions

M.Z. supervised the project. T.Z. fabricated the devices and performed experimental characterizations. S.S.D. performed the electronic first-principles calculations. S.N. and K.E. performed the thermal conductivity calculations. S.K. and A.V.D. grew MoTe<sub>2</sub> single crystals. C.C. helped with AFM measurements. T.Z., S.S.D., and M.Z. drafted the manuscript. All authors reviewed the manuscript prior to submission.

## Conflicts of interest

There are no conflicts to declare.

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intended to imply that the materials or equipment identified are necessarily the best available for the purpose.

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