

# **Constrained Nuclear-Electronic Orbital QM/MM Approach for Simulating Complex Systems with Quantum Nuclear Delocalization Effects Incorporated**

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## **Abstract**

The hybrid quantum mechanics/molecular mechanics (QM/MM) approach, which combines the accuracy of quantum mechanical (QM) methods with the efficiency of molecular mechanics (MM) methods, is widely used in the study of complex systems. However, past QM/MM implementations often neglect or face challenges in addressing nuclear quantum effects, despite their crucial role in many key chemical and biological processes. Recently, our group developed the constrained nuclear-electronic orbital (CNEO) theory, a cost-efficient approach that accurately addresses nuclear quantum effects, especially quantum nuclear delocalization effects. In this work, we integrate CNEO with the QM/MM approach through the electrostatic embedding scheme and apply the resulting CNEO QM/MM to two hydrogen-bonded complexes. We find that both solvation effects and nuclear quantum effects significantly impact hydrogen bond structures and dynamics. Notably, in the glutamic acid - glutamate complex, which mimics a common low barrier hydrogen bond in biological systems, CNEO QM/MM accurately predicts nearly equal proton sharing between the two residues. With an accurate description of both quantum nuclear delocalization effects and environmental effects, CNEO QM/MM is a promising new approach for simulating complex chemical and biological systems.

# 1 Introduction

Hybrid quantum mechanics/molecular mechanics (QM/MM) is a powerful tool in computational chemistry.<sup>1–4</sup> It enables the investigation of intricate chemical properties and processes within complex systems and has been widely used in the study of biological problems, including enzymatic processes<sup>4–6</sup> and drug design.<sup>7–9</sup> Additionally, it has been used in various other fields such as heterogeneous catalysis<sup>10,11</sup> and nanochemistry.<sup>12,13</sup>

QM/MM is unique in its multiscale nature, where higher-level accurate QM methods are applied to regions of primary interest while lower-level cost-effective MM methods are used for the surrounding environment, thereby minimizing the total computational expense. Although QM/MM is less accurate than pure QM methods and presents challenges such as the proper partitioning of QM and MM regions,<sup>14,15</sup> managing QM/MM boundary treatments,<sup>16–20</sup> and addressing overpolarization issues of QM electron densities near the MM region,<sup>21–24</sup> it remains a preferred method for studying complex systems due to its balanced accuracy and computational efficiency.

Despite the remarkable achievements of QM/MM in practical applications,<sup>12,25–28</sup> the majority of current approaches still treat nuclei in the key QM region classically, resulting in the neglect of nuclear quantum effects. This neglect is particularly problematic in systems where hydrogen, the lightest element, plays a significant role, as seen in many enzymatic reactions involving proton transfer, hydrogen atom transfer, and/or hydride transfer processes.<sup>29–33</sup>

To address this challenge, several theories have been developed to conduct QM/MM calculations with nuclear quantum effects included. One such successful approach is path-integral-based methods, which represent quantum systems using ensembles of replicas connected by harmonic springs.<sup>34–40</sup> Path-integral-based QM/MM methods have been successfully applied to study proton transfer,<sup>41</sup> hydride transfer,<sup>42</sup> and RNA cleavage reactions.<sup>43</sup> Although a major limitation of path-integral based methods is the high computational cost, especially if *ab initio* potential energy surfaces for the QM part are to be used, recent

developments have been able to accelerate the calculations and reduce their computational costs.<sup>44–48</sup>

Another promising approach is the nuclear-electronic orbital (NEO) method, which employs multicomponent wave functions to simultaneously describe the quantum behavior of both nuclei and electrons.<sup>49–57</sup> When integrated with QM/MM, NEO has provided insights into the impact of nuclear quantum effects on molecular geometries in condensed phases.<sup>58–60</sup> Although static NEO calculations are limited by the assumption of instantaneous quantum nuclear response to the motion of classical nuclei,<sup>58,61,62</sup> the recently-developed real-time NEO QM/MM can address this limitation and incorporate nonadiabaticity between nuclei and electrons, thus offering insights into short-time vibronic dynamics.<sup>59,63,64</sup>

Additionally, semi-classical trajectory methods have been integrated with QM/MM calculations with nuclear quantum effects incorporated.<sup>65</sup> They have been utilized to simulate the vibrational spectra of small biological molecules in condensed phases.<sup>65</sup>

Recently, our group developed the constrained nuclear-electronic orbital (CNEO)<sup>66,67</sup> theory to incorporate nuclear quantum effects, particularly quantum nuclear delocalization effects, into classical molecular simulations through a quantum-corrected effective potential energy surface.<sup>68,69</sup> CNEO shows great potential to be a widely-used method for its simple physical picture, high computational efficiency, and accuracy for describing quantum nuclear delocalization effects.<sup>70–76</sup> Due to its similarity to conventional electronic structure methods, with the addition of a more physically accurate quantum delocalized nuclear picture, CNEO is naturally capable of being integrated with the QM/MM framework.

In this work, we develop such an integration using the QM/MM electrostatic embedding scheme. By studying two bimolecular complex systems, one of which is of strong biological relevance, we show that CNEO QM/MM outperforms conventional QM/MM in describing hydrogen bonds and hydrogen-bond dynamics

in the condensed phase, aligning well with experimental evidence.

## 2 Methods

### 2.1 Conventional Electrostatic QM/MM Embedding Scheme

In QM/MM calculations, a key aspect is the effective description of the interactions between the QM and MM regions. Two major embedding schemes are commonly used: mechanical embedding and electrostatic embedding.<sup>1–4,77</sup> In general, the electrostatic embedding scheme offers greater accuracy and is more widely used in computations.<sup>1,2,78,79</sup> In this scheme, the QM system is influenced by the electrostatic potential provided by the MM environment, and the MM portion interacts with the charge obtained from the quantum mechanical calculations of the QM system. Additionally, building upon the electrostatic scheme, polarization of the MM system may be considered through polarized embedding using polarizable force fields.<sup>1,80,81</sup>

In the conventional QM/MM electrostatic embedding scheme, the total energy of the whole system can be decomposed into three parts

$$E_{\text{system}} = E_{\text{QM}} + E_{\text{MM}} + E_{\text{QM-MM}} , \quad (1)$$

where  $E_{\text{QM}}$  and  $E_{\text{MM}}$  are the energies of the QM and MM regions, respectively, and  $E_{\text{QM-MM}}$  represents the QM-MM interaction energy. When QM and MM atoms interact only through non-bonded interactions,  $E_{\text{QM-MM}}$  mainly includes two terms: the electrostatic interactions  $E_{\text{QM-MM}}^{\text{electrostatic}}$  and the van der Waals interactions  $E_{\text{QM-MM}}^{\text{vdW}}$ . However, when there are covalent bonds connecting QM and MM atoms, special considerations on the boundary are needed.<sup>4,17,16,82,18,83,21,84,85</sup> In this development, we will focus our discussion on cases where there are no such covalent bonds.

The van der Waals term  $E_{\text{QM-MM}}^{\text{vdW}}$  is easier to deal with. It describes both the short-range repulsion and dispersion interactions between QM and MM atoms, and

it is often modelled with the Lennard-Jones (L-J) potential

$$E_{\text{QM-MM}}^{\text{vdW}} = \sum_A^{N_{\text{QM}}} \sum_M^{N_{\text{MM}}} \varepsilon_{AM} \left[ \left( \frac{\sigma_{AM}}{|\mathbf{R}_A - \mathbf{R}_M|} \right)^{12} - \left( \frac{\sigma_{AM}}{|\mathbf{R}_A - \mathbf{R}_M|} \right)^6 \right] \quad (2)$$

Here  $\varepsilon$  and  $\sigma$  are pairwise L-J parameters,  $\mathbf{R}$  is the position of nuclei,  $N_{\text{QM}}$  is the number of classical nuclei in the QM region, and  $N_{\text{MM}}$  is the number of atoms in the MM region.

The electrostatic interaction  $E_{\text{QM-MM}}^{\text{electrostatic}}$  describes the Coulombic interactions between the QM system and MM charges. Specifically, it usually includes the Coulombic interactions of electron density and classical nuclear point charges in the QM region with MM charges, denoted by  $E_{\text{e-MM}}^{\text{electrostatic}}$  and  $E_{\text{nuc-MM}}^{\text{electrostatic}}$ , respectively:

$$E_{\text{QM-MM}}^{\text{electrostatic}} = E_{\text{e-MM}}^{\text{electrostatic}} + E_{\text{nuc-MM}}^{\text{electrostatic}} = -\int d\mathbf{r} V_{\text{MM}}^{\text{ext}}(\mathbf{r}) \rho^{\text{e}}(\mathbf{r}) + \sum_A^{N_{\text{QM}}} V_{\text{MM}}^{\text{ext}}(\mathbf{R}_A) Z_A. \quad (3)$$

Here  $\rho^{\text{e}}(\mathbf{r})$  is the electron density,  $Z_A$  is the nuclear charge of the  $A$ -th nucleus, and  $V_{\text{MM}}^{\text{ext}}(\mathbf{r})$  is the external potential produced by MM charges. Usually, the MM charges are represented by point charges and the MM potential can be expressed as

$$V_{\text{MM}}^{\text{ext}}(\mathbf{r}) = \sum_M^{N_{\text{MM}}} \frac{q_M}{|\mathbf{r} - \mathbf{R}_M|}, \quad (4)$$

in which  $q_M$  is the effective charge of the  $M$ -th MM atom. Note that instead of point charges, Gaussian charges can also be used, which have been shown to be able to avoid overpolarization of the QM electron density.<sup>17,21,84,22</sup>

Because the QM/MM electrostatic interaction energy depends on the electron density, the solution to the electron density must come from the variational

optimization of  $E_{\text{QM}} + E_{\text{QM-MM}}^{\text{electrostatic}}$ . In practical calculations, if Kohn-Sham density functional theory (DFT) is used, the Kohn-Sham equation will incorporate the MM electrostatic potential  $V_{\text{MM}}^{\text{ext}}(\mathbf{r})$  in addition to the external potential generated by classical nuclei in the QM region:

$$\left[ -\frac{1}{2}\nabla^2 + \int d\mathbf{r}' \frac{\rho^e(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} - V_{\text{MM}}^{\text{ext}}(\mathbf{r}) - \sum_A^{N_c} \frac{Z_A}{|\mathbf{r} - \mathbf{r}_N|} + V_{\text{xc}}^e(\mathbf{r}) \right] \psi_i^e(\mathbf{r}) = \varepsilon_i^e \psi_i^e(\mathbf{r}) \quad (5)$$

Upon convergence of self-consistent field (SCF) calculations for  $E_{\text{QM}} + E_{\text{QM-MM}}^{\text{electrostatic}}$ , the total energy  $E_{\text{system}}$  can be calculated by adding the MM energy, as well as the van der Waals term  $E_{\text{QM-MM}}^{\text{vdW}}$ . Afterwards, the forces on QM and MM atoms can be calculated through analytic gradient expressions of the total energy with respect to QM and MM coordinates.

## 2.2 Past Development of CNEO-DFT

In the past few years, our group developed the CNEO framework to incorporate nuclear quantum effects, especially quantum nuclear delocalization effects, into quantum chemical calculations and molecular dynamics (MD) simulations.<sup>66,67,70–73</sup> This is achieved within the multicomponent quantum chemistry framework by imposing positional constraints on quantum nuclei

$$\langle \psi_I^n | \hat{\mathbf{r}}_I | \psi_I^n \rangle = \mathbf{R}_I, \quad (6)$$

where  $\psi_I^n$  is the nuclear orbital of the  $I$ -th quantum nucleus, and  $\hat{\mathbf{r}}_I$  and  $\mathbf{R}_I$ , respectively, are its associated quantum position operator and classical position specified by the molecular geometry. In this way, CNEO treats nuclei quantum mechanically but also retains the intuitive classical molecular picture.

With the introduction of constraints on the expectation value of quantum nuclear position operators, the multicomponent electronic Kohn-Sham equation remains the same as conventional NEO theory

$$\left[ -\frac{1}{2}\nabla^2 + \int d\mathbf{r}' \frac{\rho^e(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} - \sum_A \frac{Z_A}{|\mathbf{r}-\mathbf{r}_A|} - \sum_I Z_I \int d\mathbf{r}' \frac{\rho_I^n(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} + V_{xc}^e(\mathbf{r}) \right] \psi_i^e(\mathbf{r}) = \varepsilon_i^e \psi_i^e(\mathbf{r}) \quad , \quad (7)$$

where  $\rho_I^n$  denotes the density of the  $I$ -th quantum nucleus, and  $Z_I$  denotes its charge.  $N_c$  and  $N_q$  are the total numbers of classical and quantum nuclei, respectively. The terms in the bracket represent in order the electronic kinetic energy term, Hartree potential, external potential due to classical nuclei, external potential due to quantum nuclei, and exchange-correlation potential for electrons.

In contrast, the nuclear Kohn-Sham equation is modified with an extra term  $(\mathbf{f}_I \cdot \mathbf{r})$  associated with the constraint on the expectation position<sup>66</sup>

$$\left[ -\frac{1}{2m_I}\nabla^2 - Z_I \int d\mathbf{r}' \frac{\rho^e(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} + Z_I \sum_A \frac{Z_A}{|\mathbf{r}-\mathbf{r}_A|} + Z_I \sum_{J \neq I} Z_J \int d\mathbf{r}' \frac{\rho_J^n(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} + V_{c,I}^n(\mathbf{r}) + \mathbf{f}_I \cdot \mathbf{r} \right] \psi_I^n(\mathbf{r}) = \varepsilon_I^n \psi_I^n(\mathbf{r}) \quad .(8)$$

Here the first four terms corresponds to those in Equation (7) but are now for nuclei.

$V_{c,I}^n(\mathbf{r})$  is the correlation potential for the  $I$ -th quantum nucleus. Note that there is no nuclear exchange within CNEO because of the distinguishable nucleus assumption and nuclear self-Coulomb is explicitly excluded.<sup>66</sup> The Lagrange multiplier  $\mathbf{f}_I$  needs to be solved iteratively together with electronic and nuclear orbitals, subject to the geometric constraints on quantum nuclear expectation positions via Equation (6). The converged orbitals can be subsequently used to evaluate the multicomponent energies as a function of both classical and quantum nuclear positions, leading to quantum-corrected effective potential energy surfaces.

Analytic gradients<sup>67</sup> and Hessians<sup>70</sup> with respect to both classical and quantum nuclear positions have also been developed.

### 2.3 Development of CNEO-DFT QM/MM

For the current CNEO-DFT QM/MM development, because some or all nuclei in the QM region are now described quantum mechanically, additional terms in the QM-MM interaction energy  $E_{\text{QM-MM}}$  will arise due to the interactions between the quantum nuclei and the MM environment. Specifically, these terms include both the electrostatic interactions and the van der Waals interactions between quantum nuclei and MM atoms.

For the simpler van der Waals interactions, the additional quantum nuclei-MM (q-MM) term can be calculated with

$$E_{\text{q-MM}}^{\text{vdW}} = \sum_I^{N_q} \sum_M^{N_{\text{MM}}} \varepsilon_{IM} \left[ \left( \frac{\sigma_{IM}}{|\mathbf{R}_I - \mathbf{R}_M|} \right)^{12} - \left( \frac{\sigma_{IM}}{|\mathbf{R}_I - \mathbf{R}_M|} \right)^6 \right]. \quad (9)$$

Then the total QM-MM van der Waals interaction energy becomes

$$E_{\text{QM-MM}}^{\text{vdW}} = E_{\text{c-MM}}^{\text{vdW}} + E_{\text{q-MM}}^{\text{vdW}}. \quad (10)$$

where we now use c-MM to denote the interactions between the classical nuclei in the QM region and MM atoms.

For electrostatic interactions, the additional term can be calculated with

$$E_{\text{q-MM}}^{\text{electrostatic}} = \sum_I^{N_q} Z_I \int d\mathbf{r} V_{\text{MM}}^{\text{ext}}(\mathbf{r}) \rho_I^n(\mathbf{r}), \quad (11)$$

and the total electrostatic QM-MM interaction energy becomes

$$E_{\text{QM-MM}}^{\text{electrostatic}} = E_{\text{c-MM}}^{\text{electrostatic}} + E_{\text{q-MM}}^{\text{electrostatic}} + E_{\text{c-MM}}^{\text{electrostatic}}. \quad (12)$$

Similar to the conventional QM/MM approach, the variational energy minimization of  $E_{\text{QM}} + E_{\text{QM-MM}}^{\text{electrostatic}}$  with respect to QM densities leads to Kohn-Sham equations for quantum particles in the QM region. The resulting electronic and nuclear Kohn-Sham equations are highly similar to those in CNEO-DFT, except that the MM potential now enters both the electronic equation (Equation 7) and the nuclear equation (Equation 8) as an additional external potential term.



In CNEO-DFT QM/MM, analytic gradients with respect to the displacement of classical nuclei in the QM region, the displacement of the expectation positions of quantum nuclei in the QM region, and the displacement of MM atom positions can be derived in a similar way to what has been done for conventional DFT QM/MM. These details are provided in the Supporting Information.

## 2.4 Computational Details

We implemented the CNEO-DFT QM/MM in our locally-modified version of PySCF<sup>86–88</sup>, which is available through our group GitHub page.<sup>89</sup> Molecular dynamics simulations were carried out with GROMACS.<sup>90–92</sup> In all the following calculations, the aug-cc-pVDZ electronic basis set<sup>93</sup> was used for both CNEO-DFT and conventional DFT. For the glutamic acid-glutamate complex, density fitting with the aug-cc-pVDZ-RI auxiliary basis set was used for electronic integrals.<sup>94,95</sup> With CNEO-DFT, all hydrogen atoms in the QM region were treated as quantum nuclei with the PB4D protonic basis set.<sup>96</sup> The B3LYP<sup>97–99</sup> electronic exchange-correlation functional was used and no electron-proton correlation (epc) functional was used. Note that our preliminary tests found that the currently developed epc functionals<sup>100–103</sup> tend to make negligible difference to molecular geometries and vibrational frequencies in the CNEO framework. Therefore, we chose to present results without epc functionals here and leave the detailed investigation of epc effects for future work. For MM-related calculations, we utilized a modified OPLS all-atom force field for the hydrogen-bonded complexes<sup>104–106</sup> and a modified TIP3P water.<sup>107</sup> The polar hydrogens (hydrogen in N-H and O-H) of the hydrogen-bonded molecules were assigned Lennard-Jones coefficients from Ref. 108. Additional computational details can be found in the Section 1 of Supporting Information. Regarding computational cost, we observed that incorporating nuclear quantum effects in CNEO-DFT QM/MM results in only a minor increase in computational cost (typically 10% to 20% longer wall time) compared to conventional DFT-based QM/MM. This comparison is summarized in Section 2 of the Supporting Information.

## 3 Results and Discussion

We first considered a phenol-water complex (Figure 1), which is a hydrogen

bonded system that has been studied in the past during the development NEO-DFT QM/MM.<sup>58</sup> In this system, the hydrogen bond to be investigated is the one between the hydrogen atom in the phenol hydroxyl group and the oxygen atom in the water. Therefore, the QM region constitutes the phenol molecule and the hydrogen-bonded water molecule.

### 3.1 Phenol-water complex

Following the procedure in Ref. 58, we investigated four key geometric properties for the optimized geometries of the complex in both gas phase and in a water droplet: the OH bond length of the phenol hydroxyl group (O-H), the hydrogen bond distance ( $\text{O}\cdots\text{H}$ ), the distance between the two oxygen atoms ( $\text{O}\cdots\text{O}$ ), and the  $\angle\text{OHO}$  bond angle. The results from methods based on pure MM, DFT, and CNEO-DFT are presented in Table 1.

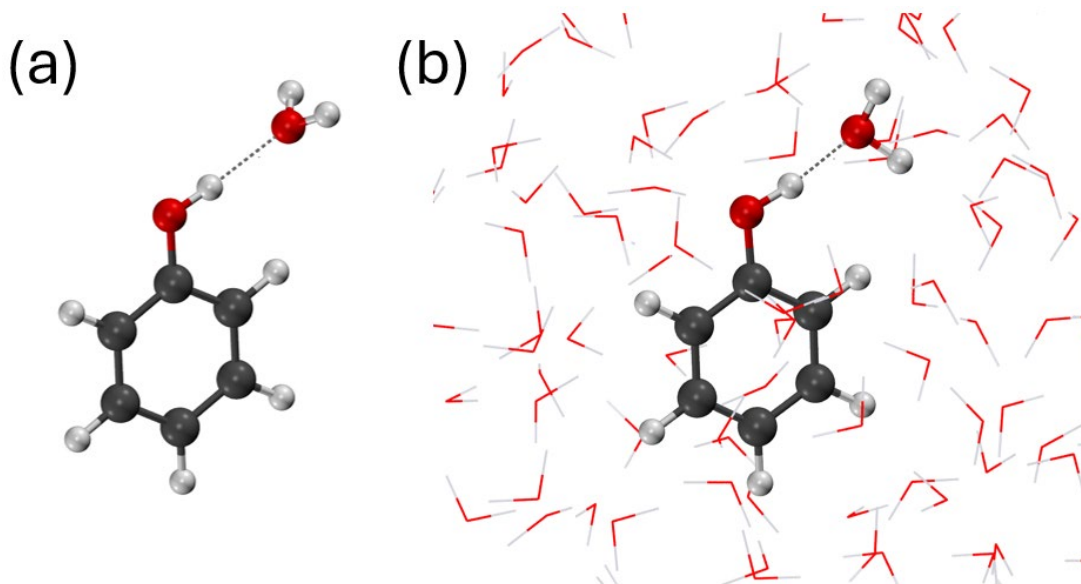


Figure 1. Phenol-water complex in the (a) gas phase and (b) aqueous phase

For all three methods, the hydroxyl O-H bond length is consistently very close to 1 Å. Additionally, switching from gas phase to aqueous phase has little impact on the distance. These results indicate that all three methods can describe the equilibrium bond length well. In contrast, the hydrogen bond  $\text{O}\cdots\text{H}$  distance

varies dramatically with the underlying method. Specifically, pure MM predicts the largest distance with 1.93 Å in the gas phase and 1.91 Å in the aqueous phase, whereas CNEO predicts the smallest distance with 1.82 Å in the gas phase and 1.59 Å in the aqueous phase. Interestingly, switching from the gas phase to the aqueous phase barely changes the pure MM results ( $\Delta = -0.02$  Å) but it leads to a large distance decrease for both DFT QM/MM ( $\Delta = -0.15$  Å) and CNEO-DFT QM/MM ( $\Delta = -0.23$  Å). As to the O $\cdots$ O distance, because the  $\angle$  OHO bond angle is almost linear and thus the O $\cdots$ O distance is roughly the sum of O-H and O $\cdots$ H distances, the behavior of the O $\cdots$ O distance is similar to that of the O $\cdots$ H distance.

Table 1 Geometric Properties of Phenol-Water Complex

| Environment                              | Method         | Distance (Å)    |                 |                 | $\angle$ OHO<br>(degree) |
|--|----------------|-----------------|-----------------|-----------------|--------------------------|
|  |                | O-H             | O $\cdots$ H    | O $\cdots$ O    |                          |
| Geometry Optimization<br>(Gas phase)     | MM             | 0.96            | 1.93            | 2.88            | 177                      |
|  | DFT            | 0.97            | 1.88            | 2.85            | 173                      |
|  | CNEO-DFT       | 1.01            | 1.82            | 2.82            | 172                      |
| Geometry Optimization<br>(Aqueous phase) | Full MM        | 0.96            | 1.91            | 2.85            | 166                      |
|  | DFT QM/MM      | 0.99            | 1.73            | 2.71            | 169                      |
|  | CNEO-DFT QM/MM | 1.03            | 1.59            | 2.61            | 171                      |
| Molecular Dynamics<br>(Aqueous phase)    | Full MM        | $0.95 \pm 0.04$ | $3.33 \pm 0.59$ | $3.92 \pm 0.56$ | $124 \pm 17$             |
|  | DFT QM/MM      | $0.98 \pm 0.02$ | $1.87 \pm 0.20$ | $2.81 \pm 0.18$ | $161 \pm 9$              |
|  | CNEO-DFT QM/MM | $1.03 \pm 0.03$ | $1.67 \pm 0.15$ | $2.70 \pm 0.15$ | $166 \pm 7$              |

The long hydrogen bond distance by pure MM and its insensitivity to environmental change is a manifestation of its failure in describing hydrogen bonds. This is because using only Coulombic and van der Waals interaction terms in pure

MM tends to inadequately capture the intricate nature of hydrogen bonds.<sup>109,110</sup> In contrast, both DFT QM/MM and CNEO-DFT QM/MM can qualitatively describe the significant environmental effect, although CNEO-DFT QM/MM predicts shorter O $\cdots$ H and O $\cdots$ O distances than DFT QM/MM by 0.14 Å and 0.10 Å, respectively. Additionally, in CNEO-DFT QM/MM, the hydrogen atom is located closer to the center of the two oxygen atoms. These results are qualitatively consistent with previous computational studies that also found neutral hydrogen bond complexes contract when solvated by water.<sup>111</sup>

One notable point is that for this type of static QM/MM geometry optimization, theoretically, CNEO QM/MM and NEO QM/MM should yield the same equilibrium geometry results. This can be confirmed by comparing with the data in Ref. 58, which shows that our CNEO QM/MM results match well the optimized geometric parameters obtained from NEO QM/MM, with negligible differences attributed to different basis sets and MM water environment. This consistency in results is a strong indicator that both developments have correctly implemented their respective theories.

Next we performed MD simulations on the phenol-water complex system starting from optimized geometries obtained from the respective methods. Within the *NVT* ensemble at 270 K, all MD simulations are performed for 10 ps, with the first 2 ps used for equilibration and the remaining 8 ps for data collection. The geometric properties as well as their standard deviation during the later 8 ps MD simulations are also shown in Table 1. Note that we only performed the simulation in the aqueous phase because in the gas phase, the phenol-water easily dissociates at the picosecond time scale.

Compared to the geometry optimization results, MD simulations barely change the hydroxyl O-H bond distance on the phenol group and the bond distance standard deviations remain small. This is because the simulation temperature is low compared to the bond strength and thus show negligible thermal fluctuation effects. In contrast, the hydrogen bonded O $\cdots$ H distance becomes larger with MD simulations as a result of the significant thermal fluctuation, which also makes its

standard deviation significantly larger than that of the O-H bond distance. Note that with pure MM, the average O $\cdots$ H distance increased by about 1.4 Å and the average  $\angle$ OHO reduces to about 125 degrees. This large change is due to the inadequately weak hydrogen bond being broken and re-formed many times during the 8 ps sampling time. Please note that all *NVT* simulations for this complex were conducted at a relatively low temperature of 270 K. We anticipate that at room temperature, hydrogen bonds would break and form more frequently, potentially altering the water molecule to which phenol is hydrogen-bonded. In contrast, the hydrogen bond predicted by both DFT QM/MM and CNEO-DFT QM/MM remains unbroken and is much less affected by thermal fluctuation. Specifically, for the O $\cdots$ H distance, a increase of 0.14 Å and 0.08 Å is observed for DFT QM/MM and CNEO-DFT QM/MM, respectively, and for the bond angle, DFT QM/MM observes a change of about 8 degrees, which is slightly larger than the 5-degree change observed by CNEO-DFT QM/MM. Compared to conventional DFT results, the reduced susceptibility to thermal fluctuations in CNEO-DFT suggests a stronger hydrogen bond, attributed to its quantum treatment of hydrogen nuclei. Given the great performance of CNEO-DFT in describing hydrogen-bonded systems from the past studies,<sup>70,72,73,76</sup> this stronger hydrogen bond is likely to be physically correct, although the absence of experimental data on the position of the hydrogen atom makes it challenging to reach a definitive conclusion.

We note that for MD simulations, CNEO-DFT QM/MM and NEO-DFT QM/MM will be significantly different. CNEO-DFT QM/MM does not assume the instantaneous response of the quantum nuclei to the motion of classical nuclei.<sup>66,70</sup> Therefore, it carries a more physically correct picture and can accurately describe the O-H and O $\cdots$ H vibrational pictures.<sup>71–73</sup> Nonetheless, the recently developed real-time NEO QM/MM dynamics work can mitigate the problem of NEO-DFT QM/MM with the desired capability of describing electron-nuclear nonadiabaticity, although the computational cost will be much higher.<sup>59</sup>

### 3.2 Glutamic acid-glutamate Complex

To further demonstrate the power of CNEO-DFT QM/MM and its potential

in biological studies, we next investigated a glutamic acid-glutamate complex (Figure 2) in both gas phase and aqueous phase. This complex is a typical low-barrier hydrogen bond system<sup>112–115</sup> in which two glutamate anions share a proton, and it is known to play a vital role in some biological systems.<sup>114,116–118</sup> For example, in human transketolase, this complex (between E366' and E160) is believed to participate in a proton wire, which is the structural origin of the enzyme's cooperativity,<sup>114</sup> and in bacteriorhodopsin, a proton pump that uses photon energy to establish transcellular proton gradient, this complex (between E194 and E204) is directly involved in the key pump process by releasing the shared proton to the extracellular environment.<sup>116–118</sup>

Due to the high significance in biological systems, the location of the shared proton in this complex and its real-time dynamics is of particular interest. For human transketolase, high-resolution X-ray crystallography concludes that the proton is almost equally shared by the two carboxylic oxygens of E366' and E160 residues, and the O···O distance is 2.55 Å,<sup>114</sup> which is much shorter than that of a normal hydrogen bond (2.7~3.1 Å). Note that these high-resolution X-ray crystallography studies can obtain hydrogen positions, which are different from the conventional impression that hydrogen positions cannot be obtained by X-ray crystallography. For bacteriorhodopsin, although the location of the proton is not exactly known, the determined O···O distance is 2.48 Å,<sup>116</sup> which is even shorter and may imply a more equally shared proton.

To mimic the real biological environment, we should ideally embed the two amino acids in relatively rigid protein backbones. However, for this proof-of-concept study, we simplified the problem by applying distance constraints to two pairs of carbon atoms according to the experimental X-ray structure of human transketolase.<sup>119</sup> Specifically, the distance between the two  $\alpha$ -carbons is constrained to 7.84 Å and the distance between the two carboxylic carbons is constrained to 9.01 Å. (Figure 2) These constraints serve a role similar to the protein backbones, which preserve the intercarboxylic hydrogen bond and prevent strong conformational changes that would be unnatural in a protein environment.

Additionally, we acknowledge that in a real biological setting, the system would not be fully immersed in an aqueous environment, which is another difference between our current treatment and actual biological conditions.

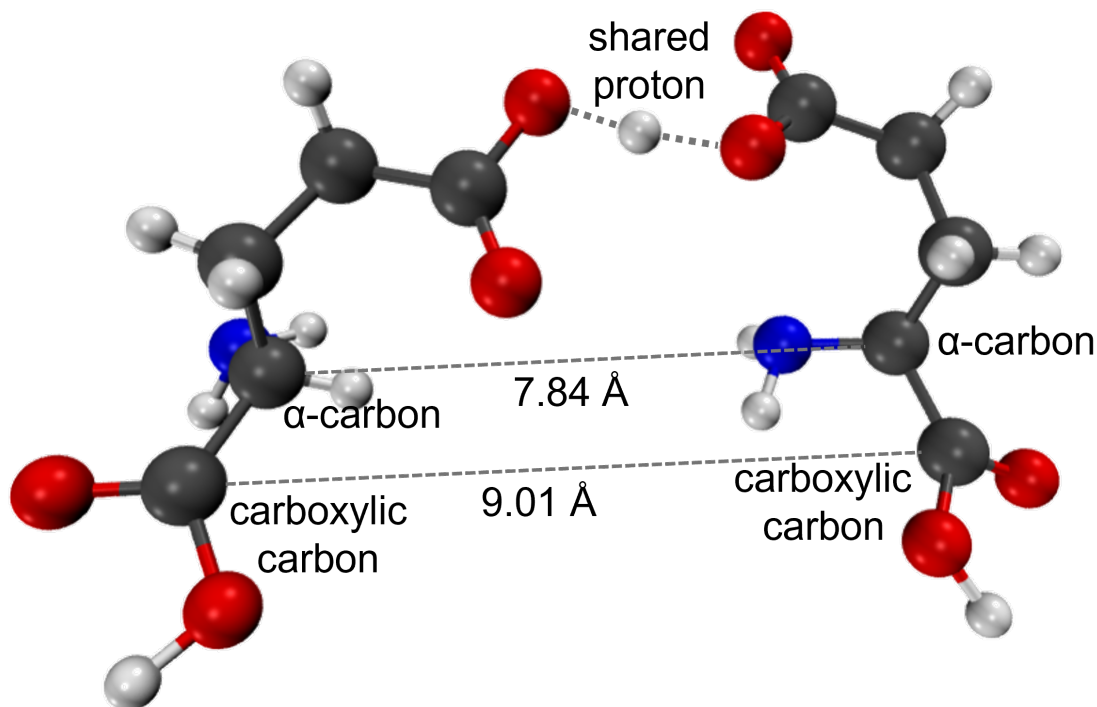


Figure 2 Structure of the glutamic acid-glutamate complex and the applied distance constraints between two  $\alpha$ -carbons and two carboxylic carbons to mimic the real structure in the enzyme environment.

As with the phenol-water complex, we first optimized the geometries of the glutamic acid-glutamate complex in both gas phase and aqueous phase. As shown in Table 2, classical MM again yields the longest  $\text{O}\cdots\text{O}$  distances (around 2.65 Å) and the largest difference between  $\text{O-H}$  and  $\text{O}\cdots\text{H}$  distances (around 0.7 Å), thus incorrectly predicting the proton to be owned by one residue. With DFT, the  $\text{O}\cdots\text{O}$  distance is predicted to be significantly shorter (2.46-2.49 Å) and the length difference between  $\text{O}\cdots\text{H}$  and  $\text{O-H}$  becomes smaller, which is 0.29 Å in the gas phase and 0.40 Å in solution. For CNEO-DFT, the  $\text{O}\cdots\text{O}$  distance is similarly short, and the  $\text{O}\cdots\text{H}$  and  $\text{O-H}$  distance difference further reduces to about 0.12 Å in both phases, which aligns well with the experimental result that the H is equally shared

by the two residues,<sup>114</sup> although as acknowledged above, there are some differences between the current setup and real biological conditions.

There is a major difference between the current glutamic acid-glutamate complex and the previous phenol-water complex: for the phenol-water complex, the hydrogen bond distance and the O $\cdots$ O distance shorten in aqueous phase, whereas for the glutamic acid-glutamate complex, these distances barely change with CNEO-DFT or even becomes slightly longer with DFT. This phenomenon has been observed in the past and it was attributed to the differences between neutral complexes and negatively charged complexes.<sup>111</sup> Heuristically speaking, the attractive interactions between the solvent and solute compress the solute and thereby shorten the hydrogen bonds, as observed in neutral complexes. However, in charged complexes, the dipole-ion interactions are much stronger than the dipole-dipole interactions present in neutral complexes. Consequently, the hydrogen bonds in charged complexes are already much shorter in the gas phase, and placing the charged complex in a polar solvent makes little difference to the hydrogen bond length. However, more rigorously, the bond length changes reflect an interplay between electronic effects, nuclear quantum effects, and solvation effects. The collective impact of these effects leads CNEO-DFT QM/MM to predict that the hydrogen bond barely changes upon solvation for the glutamic acid-glutamate complex, whereas DFT QM/MM predicts slightly elongated O $\cdots$ H and O $\cdots$ O differences (by  $\sim 0.05$  Å).

Table 2 Geometric Properties of Glutamic acid-Glutamate Complex

| Environment                             | Method   | Distance (Å) |              |              | $\angle$ OHO<br>(degree) |
|---|----------|--------------|--------------|--------------|--------------------------|
|   |          | O–H          | O $\cdots$ H | O $\cdots$ O |                          |
| Geometry<br>Optimization<br>(Gas phase) | MM       | 0.97         | 1.69         | 2.65         | 170                      |
|   | DFT      | 1.09         | 1.38         | 2.46         | 171                      |
|   | CNEO-DFT | 1.17         | 1.30         | 2.46         | 170                      |
| Geometry<br>Optimization                | Full MM  | 0.97         | 1.68         | 2.64         | 170                      |



|                                    |                |                 |                 |                 |              |
|------------------------------------|----------------|-----------------|-----------------|-----------------|--------------|
| (Aqueous phase)                    | DFT QM/MM      | 1.05            | 1.45            | 2.49            | 170          |
|                                    | CNEO-DFT QM/MM | 1.17            | 1.29            | 2.45            | 170          |
| Molecular Dynamics (Gas phase)     | MM             | $0.97 \pm 0.03$ | $1.83 \pm 0.21$ | $2.74 \pm 0.19$ | $152 \pm 27$ |
|                                    | DFT            | $1.11 \pm 0.06$ | $1.38 \pm 0.11$ | $2.47 \pm 0.07$ | $168 \pm 6$  |
|                                    | CNEO-DFT       | $1.16 \pm 0.05$ | $1.34 \pm 0.09$ | $2.48 \pm 0.07$ | $168 \pm 5$  |
| Molecular Dynamics (Aqueous phase) | Full MM        | $0.96 \pm 0.02$ | $1.83 \pm 0.17$ | $2.75 \pm 0.16$ | $153 \pm 26$ |
|                                    | DFT QM/MM      | $1.05 \pm 0.04$ | $1.49 \pm 0.13$ | $2.53 \pm 0.09$ | $168 \pm 7$  |
|                                    | CNEO-DFT QM/MM | $1.13 \pm 0.06$ | $1.38 \pm 0.12$ | $2.50 \pm 0.08$ | $170 \pm 5$  |

Next, molecular dynamics simulations were carried out with each method from the corresponding optimized geometries, and the geometric properties are also reported in Table 2. With pure MM, the hydrogen bond becomes considerably longer ( $\sim 0.15$  Å) and inadequately weaker, again indicating the failure of the force field in describing hydrogen bonds. In contrast, the hydrogen bonds treated by both DFT QM/MM and CNEO-DFT QM/MM are stronger with the increase of the hydrogen bond length always within 0.1 Å.

Since the bond lengths statistics within the *NVT* ensemble do not provide dynamical information in this low-barrier hydrogen bonded system, in order to investigate the important proton transfer dynamics, we performed 4 ps *NVE* simulations with each method and plotted the O<sub>1</sub>-H and O<sub>2</sub>-H (O<sub>1</sub> and O<sub>2</sub> are the two carboxylic oxygens sharing the proton) distances as a function of time. The results are shown in Figure 3.

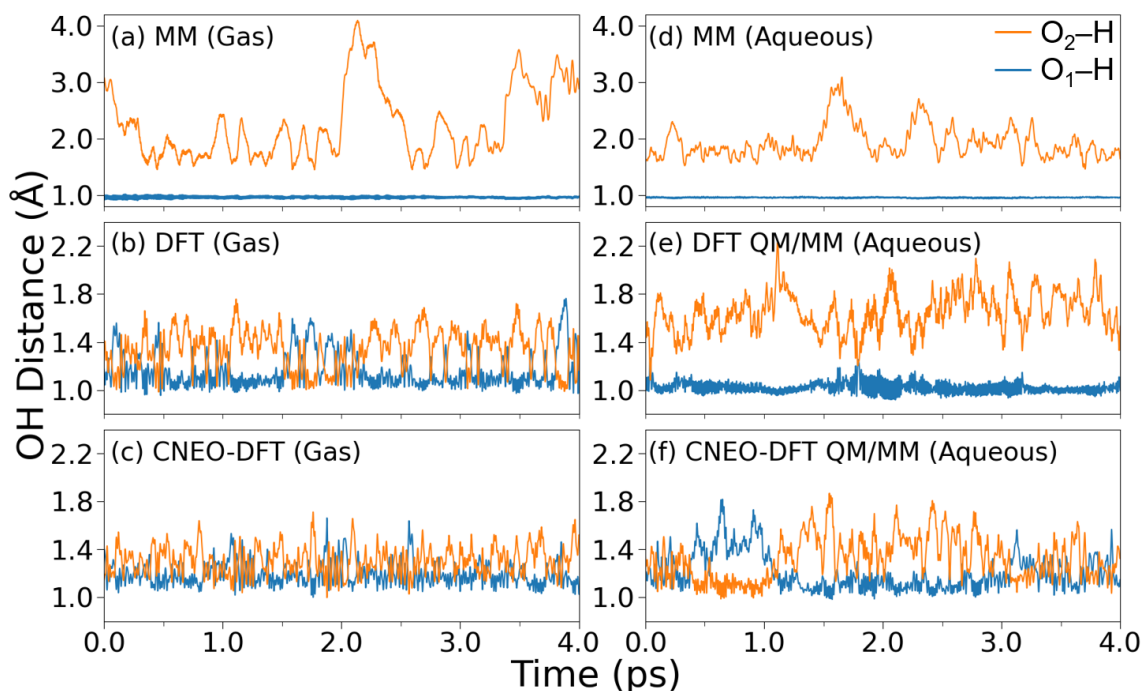


Figure 3 Distances between the shared proton and its two adjacent oxygen atoms during *NVE* simulations of glutamic acid-glutamate complex in the gas and aqueous phases by classical molecular dynamics, DFT-based molecular dynamics, and CNEO-DFT-based molecular dynamics.

Due to the inability to describe bond formation and bond dissociation, proton transfer never occurs in classical MM. The bonded OH always vibrates around its local minimum with a small length variance whereas the hydrogen bonded  $O\cdots H$  distance can fluctuate significantly. This fluctuation becomes smaller in the aqueous phase owing to confinement from environmental molecules. In contrast, proton transfer can be observed with both DFT and CNEO-DFT *ab initio* molecular dynamics with the relative  $O_1-H$  and  $O_2-H$  distances swapped frequently during the gas phase simulation. It is noticeable that proton transfer is more frequent in CNEO-DFT than in DFT. Interestingly, in the aqueous phase, proton transfer is now nearly prohibited in DFT QM/MM simulations but can still occasionally take place with CNEO-DFT QM/MM. Although a possible reason for this difference between DFT and CNEO-DFT is the slightly smaller  $O\cdots O$  distance that facilitates hydrogen sharing and hydrogen transfer by CNEO-DFT, the major reason is that the incorporation of quantum nuclear delocalization effects in the CNEO effective

surface can lower the proton-transfer barrier<sup>72,73,75</sup> and accelerate the proton transfer dynamics. The slower or prohibited proton transfers in aqueous phase compared to the gas phase may be explained by considering solvent fluctuations and their influence on the proton potential. In the gas phase, the absence of solvent leads to a relatively symmetric double well with similar depths on both sides. In contrast, in the aqueous phase, solvent fluctuations tend to create tilted double wells, and consequently, the proton is more likely to remain on one side of the well until significant changes in the solvent configuration cause the double well to tilt toward the other side, thereby facilitating proton transfer.<sup>120</sup>

With this dynamic information, we can now reinvestigate the bond length distributions in the prior *NVT* simulations and better interpret the proton location in the glutamic acid-glutamate complex. Because of the occurrence of proton transfer that weakens the identification of hydrogen bond donor and acceptor, we combined the bond length data of O-H and O $\cdots$ H and plotted them in an overall distribution in Figure 4. In DFT simulations, because there is little to no proton transfer, the hydrogen bond tends to be asymmetric with the proton being more possessed by one oxygen, leading to two overlapping peaks in gas phase and more distinctly separated peaks in the aqueous phase. In contrast, with CNEO-DFT simulations, the overall distribution becomes a single peak in both gas phase and aqueous phase due to the much more frequent proton transfer. The peak positions are both at around 1.2 Å, and the average OH distances are 1.24 Å and 1.25 Å for gas phase and aqueous phase, respectively. This prediction is in great agreement with the experiment X-ray results on human transketolase,<sup>119</sup> in which the proton is shown to be equally shared by the two glutamate residue with the OH distance being 1.28 Å.

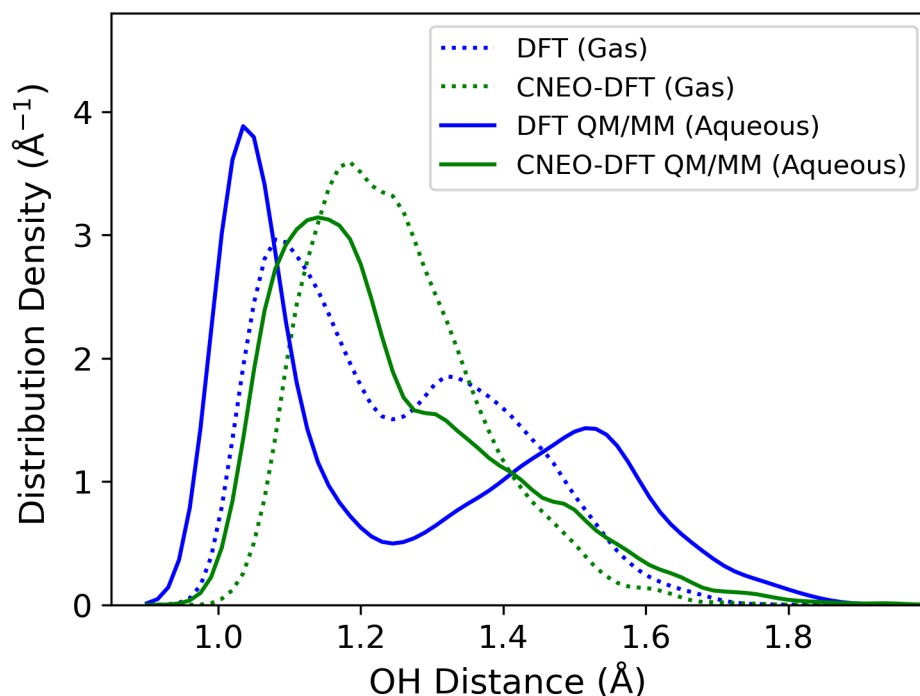


Figure 4 Distance distributions between the shared proton and adjacent oxygen atoms of the glutamic acid-glutamate complex in the gas (dotted line) and aqueous (solid line) phases from DFT-based (blue) and CNEO-DFT-based (green) *NVT* simulations.

We further investigated the correlation between the OH distances and the  $\text{O}\cdots\text{O}$  distance by plotting their joint probability in Figure 5. The lower branch in each panel represents the bonded O-H distance while the higher branch represents the hydrogen bonded  $\text{O}\cdots\text{H}$  distance. It can be observed that the smaller the  $\text{O}\cdots\text{O}$  distance, the more likely that the two branches merge together, facilitating the proton transfer. This observation is consistent with the conventional understanding of proton transfer processes. However, in general, DFT and DFT QM/MM give larger  $\text{O}\cdots\text{O}$  distances and more distinguishable O-H and  $\text{O}\cdots\text{H}$  distributions, whereas CNEO-DFT and CNEO-DFT QM/MM yield smaller  $\text{O}\cdots\text{O}$  distances and more overlapped O-H and  $\text{O}\cdots\text{H}$  branches that allow more proton transfers.

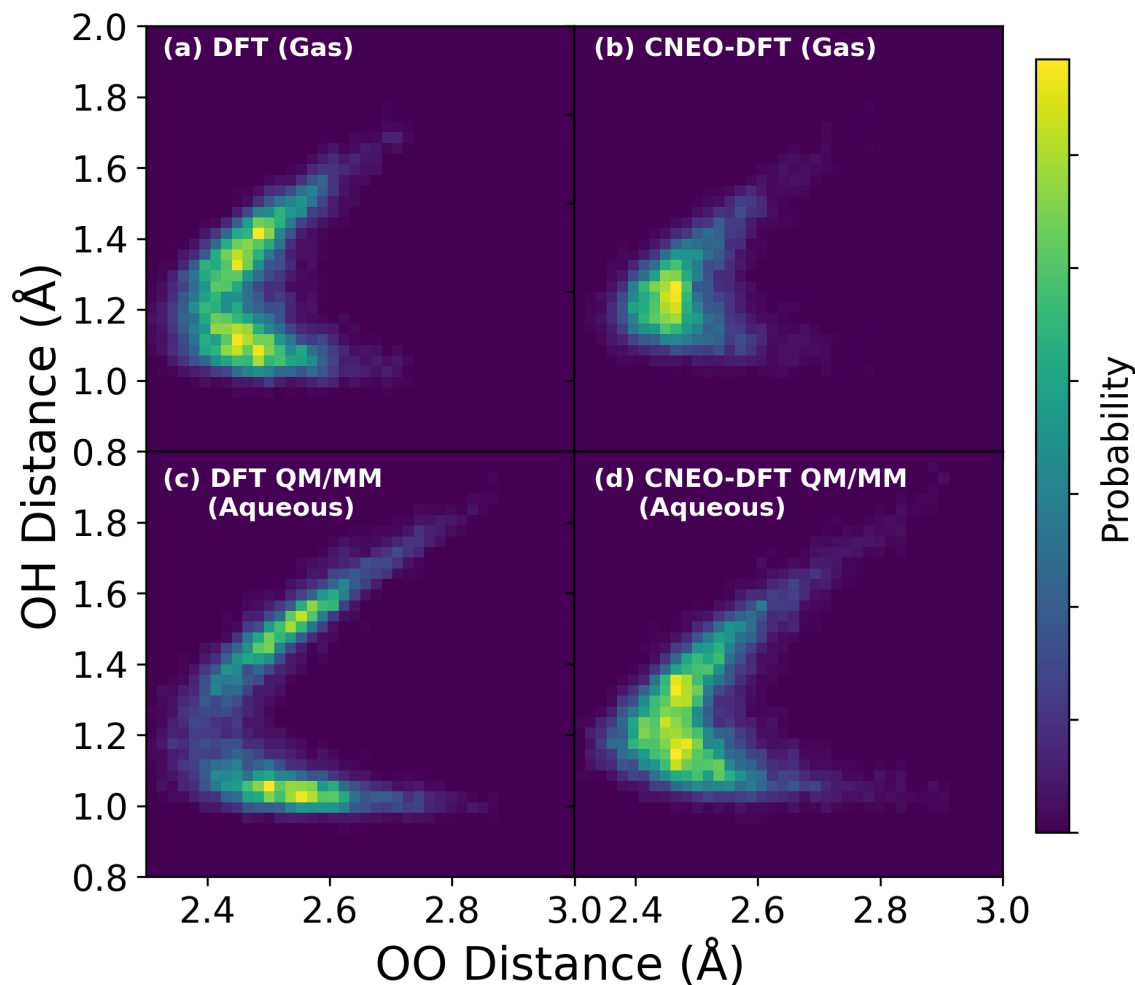


Figure 5 Correlation between oxygen-proton (OH) and oxygen-oxygen (OO) distances in the glutamic acid-glutamate complex in the gas phase and aqueous phases from DFT-based and CNEO-DFT-based *NVT* simulations.

## 4 Conclusions

In conclusion, we integrated CNEO with the QM/MM electrostatic embedding scheme and achieved the accurate and efficient incorporation of nuclear quantum effects, particularly quantum delocalization effects, in the QM region of QM/MM simulations. We applied the resulting CNEO QM/MM theory to the calculation of a phenol-water complex and a glutamic acid-glutamate complex in both gas phase and aqueous phase. We investigated the impact of nuclear quantum effects on both optimized geometries and molecular dynamics. For the neutral phenol-water complex, solvation reduces the hydrogen bond distance and

the incorporation of nuclear quantum effects through CNEO-DFT leads to a shorter hydrogen bond than that of DFT simulations. In contrast, for the negatively charged glutamic acid-glutamate complex, solvation leads to a slight increase for the hydrogen bond distance as predicted by DFT and DFT QM/MM but a negligible change as predicted by CNEO-DFT and CNEO-DFT QM/MM. Through dynamics simulations, we observed much more frequent proton transfer in CNEO-DFT QM/MM simulations than in DFT QM/MM simulations for the glutamic acid-glutamate complex in both gas phase and aqueous phase due to the incorporation of quantum nuclear delocalization effects. Additionally, the location of the shared proton predicted by CNEO QM/MM is in great agreement with the experimental observations. All of these results demonstrate the significant impact of the solvation environment and quantum nuclear delocalization effects, both of which are key features of the CNEO QM/MM approach. As an accurate and efficient method, CNEO QM/MM holds great promise for future investigation of hydrogen-related processes in complex chemical and biological environments.

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## **Supporting Information**

Additional computational details and detailed derivation of CNEO-DFT QM/MM energy, Kohn-Sham equations, and analytic gradients with both point charge and Gaussian charge models.

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## TOC graphics

