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Alive but Barely Kicking: News from 3+yr of Swift and XMM-Newton X-Ray Monitoring of Quasiperiodic Eruptions from eRO-QPE1

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Abstract

Quasiperiodic eruptions (QPEs) represent a novel class of extragalactic X-ray transients that are known to repeat at roughly regular intervals of a few hours to days. Their underlying physical mechanism is a topic of heated debate, with most models proposing that they originate either from instabilities within the inner accretion flow or from orbiting objects. At present, our knowledge of how QPEs evolve over an extended timescale of multiple years is limited, except for the unique QPE source GSN 069. In this study, we present results from strategically designed Swift observing programs spanning the past 3 yr, aimed at tracking eruptions from eRO-QPE1. Our main results are as follows: (1) the recurrence time of eruptions can vary from flare to flare and is in the range of 0.6–1.2 days; (2) there is no detectable secular trend in evolution of the recurrence times; (3) consistent with prior studies, their eruption profiles can have complex shapes; and (4) the peak flux of the eruptions has been declining over the past 3 yr, with the eruptions barely detected in the most recent Swift data set taken in 2023 June. This trend of weakening eruptions has been reported recently in GSN 069. However, because the background luminosity of eRO-QPE1 is below our detection limit, we cannot verify whether the weakening is correlated with the background luminosity (as is claimed to be the case for GSN 069). We discuss these findings within the context of various proposed QPE models.

Unified Astronomy Thesaurus concepts: Tidal disruption (1696); Black hole physics (159); High energy astrophysics (739); Supermassive black holes (1663); Astronomy data analysis (1858); X-ray astronomy (1810); X-ray sources (1822)

1. Introduction

Quasiperiodic eruptions (QPEs) are intense, repeating bursts of soft X-rays originating from nuclei of nearby galaxies (Miniutti et al. 2019; Giustini et al. 2020; Arcodia et al. 2021). Their central black holes have masses in the range of 10^5 – $10^7\,M_\odot$ as derived from host galaxy stellar velocity dispersion scaling relations (Wevers et al. 2022). There are currently four QPE systems known with recurrence periods (i.e., the time between subsequent flares) varying from a few hours to 0.8 days (Miniutti et al. 2019; Arcodia et al. 2021). Two additional nuclear transients with one and a half eruptions (Chakraborty et al. 2021) and a half eruption (Quintin et al. 2023) have been suggested as potential QPE systems. While the first two (GSN 069 and RX J1301.9+2747) were discovered

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in archival XMM-Newton data sets, two systems (eRO-QPE1 and eRO-QPE2 as named in Arcodia et al. 2021) were found through follow-up of candidates from a systematic search in sky survey data from the eROSITA instrument on board the Spectrum-Roentgen-Gamma (SRG) space observatory (Predehl et al. 2021). The latter findings provide the exciting prospect of identifying more QPE sources with future all-sky X-ray surveys.

Broadly speaking, QPEs have the following observational properties. They all have soft/thermal spectra with best-fit blackbody temperatures of a few tens to a few hundreds of eV (Miniutti et al. 2019; Arcodia et al. 2021). There is no commonality in their burst profiles. For example, GSN 069, RX J1301.9+2747, and eRO-QPE2 have more or less symmetric bursts, while eRO-QPE1 has a complex behavior where some eruptions show a fast-rise, slow-decay behavior while others are more or less symmetric and can sometimes be broad (Arcodia et al. 2022). In general, their X-ray temperature is correlated with luminosity (Miniutti et al. 2019; Giustini et al. 2020; Arcodia et al. 2021). The recurrence time is

Table 1
Summary of eRO-QPE1's Swift/XRT Data and Spectral Modeling of Its Eruptions

Epoch	MJD _{start} (days)	MJD _{end} (days)	Count Rate (counts s ⁻¹)	Counts	Average kT (keV)	Average Flux	Peak Flux	Quiescence Flux
Swift#1	59373.074	59376.986	0.0244 ± 0.0016	223	0.135 ± 0.016	8.0 ± 0.7	20.6 ± 3.1	< 0.3
Swift#2	59502.022	59505.948	0.0126 ± 0.0012	124	0.135 ± 0.016	3.9 ± 0.4	11.5 ± 2.2	< 0.4
Swift#3	59635.025	59638.941	0.0099 ± 0.0011	94	0.099 ± 0.015	3.1 ± 0.6	9.7 ± 2.8	< 0.3
Swift#4	59867.057	59871.634	0.0058 ± 0.0016	15	0.099 ± 0.015	1.7 ± 0.6	6.5 ± 3.9	< 0.4
Swift#5	60009.023	60013.651	0.0096 ± 0.0012	64	0.124 ± 0.020	2.3 ± 1.1	7.1 ± 3.8	< 0.2
Swift#6	60110.017	60114.723	0.0043 ± 0.0008	33	0.124 ± 0.020	1.1 ± 0.4	3.2 ± 1.7	< 0.3

Note. Here 0.3-1.2 keV Swift/XRT spectra were fit with the tbabs*ztbabs*zashift(diskbb) model using XSPEC (Arnaud 1996). MJD_{start} and MJD_{end} represent the start and end times (in units of MJD days) of the Swift monitoring campaign. Count Rate and Counts represent background-subtracted values in 0.3-1.2 keV. The column density at the host, ztbabs, was constrained to be within $(0.049-0.089) \times 10^{22}$ cm⁻², the best-fit XMM-Newton value. Temperatures of Swift #1 and Swift #2, Swift #3 and Swift #4, and Swift #5 and Swift #6 were tied. All the error bars represent 1σ uncertainties except for the 3σ quiescence level upper limits. The Average Flux, Peak Flux, and Quiescence Flux values correspond to 0.3-1.2 keV and have units of 10^{-13} erg s⁻¹ cm⁻². The total C-stat/degrees of freedom was 32.2/35.

not strictly periodic with GSN 069, RX J1301.9+2747, eRO-QPE1, and eRO-QPE2, showing variations on the order of $\approx 30\%$ (Giustini et al. 2020; Miniutti et al. 2023a).

The underlying physical mechanism producing QPEs is currently unknown but an increased interest in this subject has led to several theoretical models being proposed in the past few years. These models can be put into two broad categories: ones that invoke inner accretion disk instabilities (Raj & Nixon 2021; Pan et al. 2022; Śniegowska et al. 2023; Kaur et al. 2023), perhaps similar to those occurring in stellar-mass black hole X-ray binaries GRS 1915+105 (Neilsen et al. 2011) and IGR J17091-3624 (Altamirano et al. 2011), and those involving one or more orbiting stellar objects (King 2020; Metzger et al. 2022; Suková et al. 2021; Xian et al. 2021; Krolik & Linial 2022; Zhao et al. 2022; Franchini et al. 2023; Linial & Metzger 2023; Linial & Sari 2023). It has also been proposed that self-lensing binary supermassive black holes (SMBHs) can, in principle, produce quasiperiodic flares, but this scenario appears to be inconsistent with data from GSN 069 and RX J1301.9+2747 (Ingram et al. 2021). As evident in the extensive list of theoretical models referenced above, the models with an orbiting object around a massive black hole have increased the excitement in the field, as QPEs could potentially represent extreme mass ratio inspirals (EMRIs) of a secondary orbiter gradually sinking down to the central SMBH. If that is the case, some studies have suggested that some QPE sources could be detectable by future space-based gravitationalwave missions like LISA and Tiangin (Zhao et al. 2022). But Chen et al. (2022) have argued that the signals from the currently known OPE sources may be too weak to be detectable by future gravitational-wave detectors. Irrespective of the underlying mechanism, QPEs have opened up a unique new window into the inner accretion flows of massive black holes.

To pin down the mechanism driving QPEs, observations constraining their long-term evolution are necessary. Such information is available in the published literature only for GSN 069 (Miniutti et al. 2023b, 2023a). Here we present results from a monitoring campaign over an extended temporal baseline of 3 yr using Neil Gehrels Swift (Swift hereafter) and archival XMM-Newton observations of eRO-QPE1/2MASS 02314715–1020112, which exhibited QPEs separated by \approx 0.8 days during the first monitoring data set (Arcodia et al. 2021). We performed additional

high-cadence observations on multiple epochs, and our main observational findings are discussed in Section 2. We discuss the implications of our findings within the context of several proposed theoretical models in Section 3, and we compare with GSN 069 and discuss future prospects of tracking eRO-QPE1 in Section 4. We summarize our findings in Section 5.

2. Data and Observational Findings

Swift's X-Ray Telescope (XRT; Burrows et al. 2005) performed six sets (Swift #1...6; Table 1) of high-cadence monitoring observations of eRO-QPE1. See the Appendix for a detailed discussion of data reduction and spectral analyses. Here we highlight the main observational findings.

Eruptions were detected in all these campaigns but with decreasing strength over time. This is evident even by eye in Figure 1, where the brightness at peaks is gradually decreasing with time. The same is quantified in the top panel of Figure 2, which shows that the peak and average fluxes of the eruptions have decreased by approximately a factor of 10 and 4, respectively, over 3 yr. The quiescent level was detected in the first XMM-Newton observation, but only upper limits were available during the Swift observations (Figure 2, bottom panel).

Another key observational finding is that the recurrence time varies from one monitoring campaign to the next. Surprisingly, the three eruptions seen in the first Swift campaign (Swift #1) were separated by ~ 1.1 days (left panel of Figure 3), i.e., $\sim 40\%$ longer than the previously published recurrence time of 0.8 days (Arcodia et al. 2021). However, this recurrence time returned to a mean value of 0.8 days roughly 6 months later in 2021 October (Swift #2; right panel of Figure 3). This is also quantified in the Lomb–Scargle periodograms (LSPs) shown in Figure 4. Over the course of all six monitoring campaigns, the recurrence time varied between 0.6 and 1.2 days (see Appendix A.1 and Figure 4).

While several eruptions reported here are consistent with the fast-rise, smooth-decay profile reported in Arcodia et al. (2021), there are numerous examples of more complex profile shapes. For example, the second eruption in Swift #2 has an extended decay. The fourth and fifth eruptions (around days 2.3 and 3.3) in Swift #3 have a dip near their peaks. The eruption around day 1.5 in Swift #6 and the last two eruptions in Swift #2 appear symmetric in shape. In summary, contrary to previous reports, we find that the eruption profiles have

 $[\]overline{^{15}}$ We follow the naming convention of Arcodia et al. (2021).

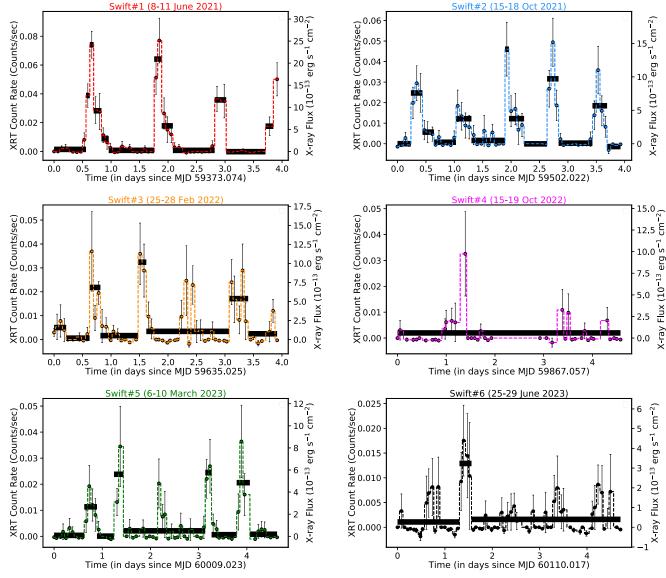


Figure 1. 0.3–1.2 keV X-ray light curves of eRO-QPE1. Each light curve is from a high-cadence monitoring program with Swift. The observation dates are indicated at the top of each panel. Both the X-ray count rate and the observed flux were measured in the 0.3–1.2 keV band. The decrease in strength of eruptions over time is evident. Note that the y-scale is different in each panel. The thick black horizontal lines are the optimal time bins derived from the Bayesian blocks algorithm of Scargle et al. (2013).

different shapes. This is an important aspect to stress, as Arcodia et al. (2021) used the fast-rise, slow-decay profile as an argument against a certain type of radiation pressure instability.

3. Implications for Various Theoretical Models

We now discuss the observations presented above within the context of various models proposed for QPEs.

3.1. QPEs Models with Orbiting Objects

3.1.1. Repeating Partial Tidal Disruption Event

First, we explore three flavors of repeating partial tidal disruption event (rpTDE) scenarios: (1) eRO-QPE1's central black hole is repeatedly disrupting a star on a timescale of several years, and the QPEs are produced as a result of inner disk-related physics; (2) QPEs are a direct result of a white dwarf that is in a $\sim\!1\text{-day}$ orbit around an SMBH; and (3) rpTDE of a main-sequence star by an SMBH.

Miniutti et al. (2023a) noted that GSN 069's long-term behavior appears to be consistent with the tidal disruption of a star, and the QPEs only appeared once the flux fell below a critical value. It may therefore be the case that the QPE phenomenon is intricately tied to, and in fact requires, a prior TDE, with the production mechanism related to the ensuing disk physics (and any potential instabilities associated therewith) or a change in the morphology of the returning debris stream (Coughlin & Nixon 2020; Guolo et al. 2023). Unfortunately, the quiescent X-ray flux from eRO-QPE1 is below the Swift/XRT detectability threshold (see Figure 2), and we are not currently able to test this hypothesis. However, future XMM-Newton monitoring observations can address the nature of the long-term evolution of quiescence emission (see Section 4.2).

A second scenario has been suggested in which the X-ray eruptions are produced owing to accretion following the repeated partial tidal stripping of a white dwarf by the black hole in the nucleus of the galaxy (King 2020; see also Zalamea et al. 2010

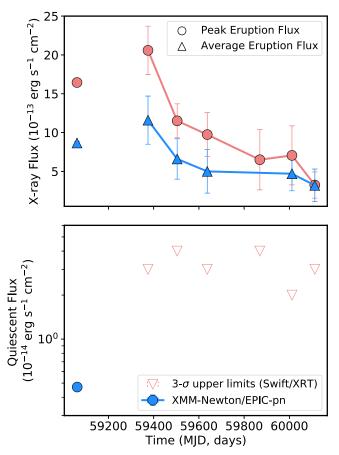


Figure 2. Long-term evolution of the average peak luminosity of the eruptions (top) and the quiescent level (bottom). The fluxes are observed values in the 0.3–1.2 keV band. The error bars represent 1σ uncertainties. They include both measurement and model fitting uncertainties (see Appendix A.1). Swift/XRT data were not sensitive enough to detect the quiescent level, but 3σ upper limits are shown. XMM-Newton's observed 0.3–1.2 keV quiescent flux was derived from combining data from obsIDs 0861910201 and 0861910301 (blue circle in the bottom panel).

in the context of EMRIs). If the energy generated as a result of accretion is $E_{\rm acc} = \eta Mc^2$ with $\eta = 0.1$, then using a luminosity distance of 233 Mpc alongside the mean observed eruption flux of 3.4×10^{-13} erg s⁻¹ cm⁻² (see Figure 2) implies an X-ray (0.3–1 keV) energy release per outburst of $E \simeq 7 \times 10^{46}$ erg (average flux \times 4 \times π (luminosity distance)² \times (1 + z = $0.0505) \times (average eruption duration of 8 hr from Arcodia$ et al. 2021), and hence an accreted mass of $M_{\rm acc} = E_{\rm acc}/(0.1c^2) \simeq 4 \times 10^{-7}~M_{\odot}$. For a white dwarf with mass \sim few \times 0.1 M_{\odot} , this amounts to a very small fraction of the total mass of the star, implying that the pericenter distance of the white dwarf is extremely fine-tuned to coincide with its partial tidal disruption radius (i.e., where material is just barely able to be removed from the surface of the star). How the star achieved precisely this distance is not clear, as neither gravitational-wave emission nor tidal interactions can dramatically change the pericenter distance. However, because the amount of mass stripped from the star is a very sensitive function of distance (see Guillochon & Ramirez-Ruiz 2013), we might expect variation in the mass accreted—and hence the luminosity (according to this model)—even for small changes to the pericenter due to, e.g., the exchange of angular momentum between the star and the orbit. These secular changes are consistent with eRO-QPE1's trend in Figure 2.

Additionally, eRO-QPE1's black hole is estimated to be $\sim 10^6~M_{\odot}$ (Wevers et al. 2023), which implies that the pericenter distance of the star must be highly relativistic—at most on the order of a few gravitational radii. Adopting a white dwarf mass of 0.6 M_{\odot} and a corresponding radius of $R_{\star} = 0.011 \ R_{\odot}$ (Nauenberg 1972) yields a tidal disruption radius of $0.6GM_{\rm BH}\,c^{-2}$, i.e., the partial tidal disruption radius is about twice that value (Guillochon & Ramirez-Ruiz 2013) at \sim 1.2 GMc^{-2} . If we set the pericenter distance of the star to 1.2 GMc^{-2} (which requires a rapidly spinning black hole and a prograde orbit for the star to not be directly captured), and the semimajor axis is determined from the recurrence period of $T = 1 \text{ day to be } a = (T\sqrt{GM}/(2\pi))^{2/3} \simeq 200GM c^{-2} \text{ for }$ $M = 10^6 M_{\odot}$, then this corresponds to an eccentricity of $e \simeq 0.994$. For these parameters, the gravitational-wave inspiral time can be estimated from Equations (5.6) and (5.7) from Peters (1964) and is $\sim 3.2 \, \text{yr}$, i.e., the source would have declined substantially in recurrence time during the 3 yr over which it has been observed. This is in obvious disagreement with the behavior exhibited by eRO-QPE1, which has a recurrence time that is relatively stable (see Figure 4).

More generally, we can calculate the time-dependent evolution of the orbital parameters (i.e., the semimajor axis and the eccentricity) by integrating Equations (5.6) and (5.7) of Peters (1964) for different black hole and stellar masses. Figure 5 shows the orbital period of the white dwarf as a function of time in years for four different black hole masses; the left panel uses a white dwarf mass of $M_{\star} = 0.6~M_{\odot}$ (also used by King 2020, and where the mass distribution of white dwarfs peaks), while the right panel adopts $M_{\star} = 0.4 \ M_{\odot}$. Here we assumed an initial orbital period of 1 day, a pericenter distance equal to twice the tidal radius $r_t = R_{\star} (M_{\bullet}/M_{\star})^{1/3}$, and the mass-radius relationship $R_{\star} = 0.011 (M_{\star}/(0.6M_{\odot})^{-1/3}R_{\odot})$ which is valid for a nonrelativistic (i.e., for a lower-mass white dwarf) fully degenerate gas. We use the leading-order Newtonian estimates for the tides, gravitational radiation, and orbital dynamics. Since the orbit is highly relativistic, there will be substantial corrections beyond the lowest-order solution given in Peters (1964) (see, e.g., Blanchet 2014; Tucker & Will 2021). These higher-order terms generally lead to accelerated decay of the eccentricity and period shortening, especially for the case of heavier central SMBHs, even though the qualitative picture stays the same. Thus, the results shown in Figure 5 should be considered upper limits to the orbital period as a function of time, i.e., higher-order terms will only result in an acceleration in the decay rate of the period.

This figure shows that for a white dwarf mass of $M_{\star} = 0.6 \, M_{\odot}$ the orbital period decays substantially—by at least a factor of 2—until the black hole mass is well below the value inferred from the M- σ relation and into the intermediatemass black hole regime. For $M_{\star} = 0.4 \, M_{\odot}$ the period decays by at least $\sim 15\%$ for $M_{\bullet} = 10^5 \, M_{\odot}$, and only for $M_{\bullet} = 10^4 \, M_{\odot}$ and $M_{\bullet} = 10^3 \, M_{\odot}$, i.e., intermediate-mass black holes, is the period change sufficiently small that it would remain undetected over the 3 yr observational period of eRO-QPE1. This figure shows that if eRO-QPE1's eruptions are produced from the repeated tidal stripping of a white dwarf, the black hole mass must be substantially smaller than the one inferred from M- σ , or the white dwarf mass must be very small (making the star rare).

We also note that, for partial disruptions in which $\gtrsim 10\%$ of the mass of the star is removed, which corresponds to pericenter distances smaller than $\sim r_t/(0.65)$ for a 5/3-polytropic star

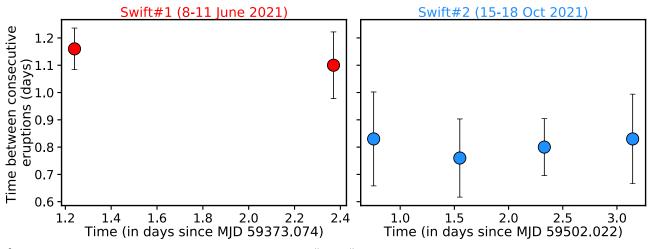


Figure 3. Evolution of time between consecutive eruptions with time for Swift #1 and #2 data sets. The peaks of eruptions were determined in a model-independent manner using the Bayesian blocks algorithm of Scargle et al. (2013). These values are consistent with the Lomb-Scargle peaks shown in Figure 4.

(Guillochon & Ramirez-Ruiz 2013; Mainetti et al. 2017; Miles et al. 2020), higher-order moments (i.e., beyond the quadrupole) of the gravitational field of the black hole induce a positiveenergy kick to the surviving star (and this has been verified across a wide range of black hole masses and stellar/planetary types; e.g., Faber et al. 2005; Manukian et al. 2013; Gafton et al. 2015; Kremer et al. 2022). This effect could conceivably stabilize the orbital decay that is induced by the gravitationalwave emission. However, for the extremely small amount of mass lost by the star necessary to power QPEs, the stellar pericenter distance is such that the tidal excitation of modes in the star removes energy from the orbit (i.e., the star is in the classic tidal dissipation regime; Fabian et al. 1975; Press & Teukolsky 1977). Specifically, it was recently shown by Cufari et al. (2023) that, for a pericenter distance of $r_t/(0.55)$ —very close to the distance from the black hole at which almost no mass is lost from the star—the change in the specific energy of the orbit is $\Delta \epsilon \simeq -0.025 GM_{\star}/R_{\star}$ and is roughly the maximum amount by which tides reduce the energy of the orbit (i.e., larger pericenter distances yield less tidal excitation, but smaller pericenter distances lead to a positive-energy kick; see Figure 1 in Cufari et al. 2023). In this case, the fractional change in the energy of the orbit is $\Delta \epsilon / \epsilon = 0.025 M_{\star} a / (M_{\bullet} R_{\star}) \sim$ 0.1% for $M_{\star} = 0.6 M_{\odot}$, $R_{\star} = 0.011 R_{\odot}$, $M_{\bullet} = 10^{6} M_{\odot}$, and $a = 200GM_{\bullet}c^{-2}$, which is comparable in magnitude to the perorbit change in energy induced by gravitational-wave emission. Thus, in this case we would only expect tides to accelerate the inspiral.

In the third scenario of repeated partial disruption of a main-sequence star, it is also difficult to reconcile the observed timescales and energetics of QPEs. This model has been invoked to explain the repeating nuclear transients ASASSN-14ko (Payne et al. 2021), AT2018fyk (Wevers et al. 2023), eRASSt-J0456 (Liu et al. 2023), and Swift J0230 (Evans et al. 2023; Guolo et al. 2023). Specifically, we would expect the return time of the tidally stripped debris to be comparable to the dynamical time at the surface of the star, multiplied by the square root of the mass ratio of the black hole to the star (Lacy et al. 1982; Rees 1988). For a white dwarf, this timescale is of the order of a kilosecond—in rough agreement with the flare duration of QPEs—while for main-sequence stars it is ~few × 10 days (see, e.g., the simulations in Guillochon & Ramirez-Ruiz 2013; Golightly et al. 2019; Law-Smith et al. 2020; Nixon et al. 2021), which is

orders of magnitude longer than the flare duration in QPEs, in general. Similar to the white dwarf model, the extremely small amount of mass accreted per burst is also problematic, and it requires fine-tuning to achieve a pericenter distance that is very closely aligned with the partial disruption radius of a star.

3.1.2. QPEs from Interactions of an Orbiting Perturber with the Accretion Disk

Suková et al. (2021) proposed that QPEs could be produced from repeated interaction of an object with the accretion disk of an SMBH (see also Xian et al. 2021; Franchini et al. 2023; Linial & Metzger 2023). In their model, at each interaction, the perturbation causes (1) the modulation of the accretion rate onto the black hole, depending on the ratio of the influence radius of the object to its distance, and (2) ejection of matter clumps toward the magnetic poles, which can drive a quasiperiodic ultrafast outflow. Assuming that the perturber period is equal to twice the eruption period (two eruptions per orbit, i.e., $P_{\rm orb} \sim 2 \times 0.9$ days), the semimajor axis is given by $a \sim 399.3(P_{\rm orb}/1.8~{\rm days})^{2/3}(M_{\bullet}/10^{5.8}M_{\odot})^{-2/3}R_g$, where $R_g = GM_{\bullet}c^{-2}$ is a gravitational radius of the SMBH. Hence, it would vary between $\sim 1003R_g$ for $M_{\bullet} = 10^{5.2}~M_{\odot}$ and $\sim 159R_g$ for $M_{\bullet} = 10^{6.4}~M_{\odot}$.

The varying recurrence time in Figures 3 and 4 can be addressed well by the Schwarzschild precession of the orbit, which can modulate the recurrence timescale, especially for mildly eccentric orbits. Using the formula for the periapse (Schwarzschild) precession, the timescale for the apsidal rotation by 90° can be expressed as follows:

$$\tau_{\frac{\pi}{2}} \sim 80.3 \left(\frac{P_{\text{orb}}}{2.2 \text{ days}}\right)^{\frac{5}{3}} \left(\frac{M.}{10^{5.8} M_{\odot}}\right)^{-\frac{2}{3}} \left(\frac{1 - e^2}{0.96}\right) \text{days}, \quad (1)$$

where e is the orbital eccentricity, which is set to e=0.2. This implies that the orbital orientation with respect to the accretion disk changes on a timescale of 100 days owing to the periapse precession, and this can thus partially address the changing eruption recurrence. For instance, initially, for a highly inclined perturbing body, the orbital orientation when the perturber intersects the disk at the apoapse and the periapse has an eruption periodicity of ~ 1.1 days, or half of the orbital period. In $\tau_{\frac{\pi}{2}} \sim 80$ days, both intersections are close to the periapse,

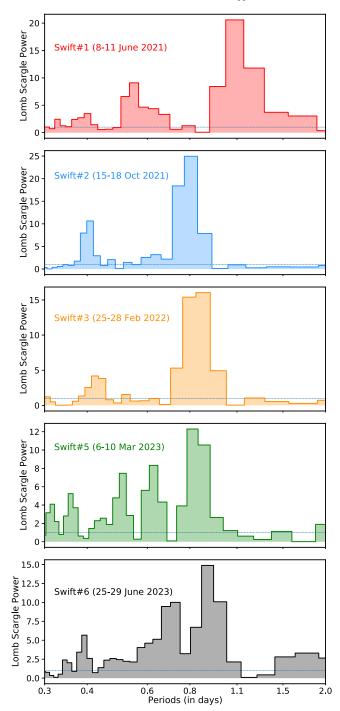


Figure 4. Lomb–Scargle periodograms of the light curves shown in Figure 1. Here we zoom in on the 0.3-to-2.0-day timescale. The highest peaks (corresponding FWHM) for Swift #1, Swift #2, Swift #3, Swift #5, and Swift #6 are $1.09^{+0.23}_{-0.08}$ days, $0.81^{+0.09}_{-0.00}$ days, $0.83^{+0.09}_{-0.07}$ days, $0.82^{+0.10}_{-0.04}$ days, and $0.91^{+0.12}_{-0.25}$ days, respectively. We do not show the LSP from Swift #4, as it was affected by a large data gap. The blue/dashed horizontal line at a power value of 1 represents the LSP's nominal white-noise level. While the main purpose of these plots is to show the evolution of the main LSP peak and not to delve into the details of the LSP, it is interesting that a harmonic is also present in all cases at roughly 1/2 the period of the main peak.

specifically the eruption recurrence timescale is 0.82 days for e=0.2. This is comparable to the change in the recurrence timescale between the Swift #1 and #2 data sets; see Figure 3. Since the Swift monitoring was separated by a few months and lasted always only a few days, for each monitoring session we

effectively capture the system in a specific orbit-disk orientation, and hence the recurrence timescale would vary accordingly.

Further variations can be caused by the disk precession (see also Franchini et al. 2023), which can take place on various timescales depending on the outer radius of the misaligned disk and the black hole spin when the disk precession is rigid-like and driven by the Lense-Thirring effect. The Lense-Thirring precession also leads to the rotation of the line of nodes for the orbiting body, which also affects the timing between the eruptions, especially for perturbers close to the rotating SMBH.

The disk precession can also be driven by the torques from the misaligned object, and the precession period in that case is longer than the orbital period. The disk precession due to the torques from the orbiting secondary has a timescale of a few hundred days to days for massive perturbers of at least $\sim 10^4 M_{\odot}$ for the total mass (primary+secondary) of 10^6 M_{\odot} . More specifically, for the secondary-to-primary mass ratio of $M_s/M_p = 10^{-2}$ the precession period is 214 days, and for $M_s/M_p = 10^{-1}$ the precession period is 22 days, assuming an inclination of $\Omega = 10^{\circ}$ between the secondary and the accretion disk around the primary. In Figure 6, we plot the expected precession period as a function of the mass ratio adopting the model of Papaloizou & Terquem (1995), Larwood (1997), and Britzen et al. (2018). We consider three inclinations (10°, 45°, and 80°), a polytropic index for the nonrelativistic gas (n = 3/2), the semimajor axis of ~ 0.014 mpc (corresponding to an orbital period of \sim 1.8 days), and the outer radius of the precessing disk corresponding approximately to the semimajor axis of the binary. We see that the precession period of a few days is only possible for nearly equal-mass components.

Another reason for changes in periodicity could be the time lag between the perturber-disk interaction and the time when the perturbation reaches the SMBH. The thermal front propagation is given by the sound-crossing timescale as $t_{\rm front} \approx R/(\alpha c_{\rm s}) \sim (H/R)^{-1}t_{\rm th}$, where the thermal timescale can be estimated as $t_{\rm th} \sim \alpha^{-1} \left[R^3/(GM.)\right]^{1/2} \sim 0.36 \, (\alpha/0.1)^{-1} (R/100R_g)^{3/2} \, (M_{\bullet}/10^{5.8})$ days. For the ratio of scale height to radius of $H/R \sim 0.1$, the front propagation timescale is $t_{\rm front} \sim 3.6 \left[(H/R)/0.1\right]^{-1} (\alpha/0.1)^{-1} (R/100R_g)^{3/2} (M_{\bullet}/10^{5.8})$ days. Therefore, the eruption recurrence timescale can be modulated by the propagation timescale, which is further affected by the disk thickness and hence the current accretion state.

While in the perturber-disk interaction model presented by Suková et al. (2021) the eruptions are produced by quasiperiodic enhancements in the accretion rate, in the analogous models presented by Linial & Metzger (2023) and Franchini et al. (2023), the X-ray emission flare is produced in shocked, optically thick expanding clouds of disk material ejected above and below the disk (see, e.g., discussion in Linial & Metzger 2023). In principle, both emission mechanisms accretion based and shock based—could be at work. The decreasing amplitude of eruptions in Figure 2 is consistent with the models of Suková et al. (2021), Franchini et al. (2023), and Linial & Metzger (2023). It can be attributed to diminishing inclination between the perturber's orbit and the accretion disk, which decreases the relative velocity of the perturber with respect to the disk material and hence the energy generated in density waves and shocks. Such an alignment process can take place owing to the ongoing Bardeen-Petterson effect if the accretion disk is initially misaligned with respect to the equatorial plane. Alternatively, it could also be the result of the disk surface density becoming lower owing to an ongoing

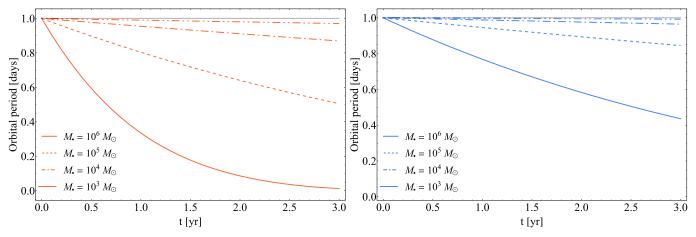


Figure 5. The Keplerian orbital period of a white dwarf orbiting a massive black hole, with black hole mass indicated in the legend, as a function of time in years, where the left (right) panel adopts a white dwarf mass of $M_{\star}=0.6~M_{\odot}~(0.4~M_{\odot})$. The pericenter distance is equal to twice the canonical tidal radius, while the orbital period is initially equal to the recurrence time of 1 day. Over the course of the observations of eRO-QPE1, being roughly 3 yr, there would be a substantial and noticeable decline in the recurrence time of the flares owing to gravitational-wave emission, unless the black hole mass is significantly below the value inferred from the $M-\sigma$ relation (being $\sim 10^6~M_{\odot}$), or the white dwarf mass is significantly smaller than the mean value of $\sim 0.6~M_{\odot}$.

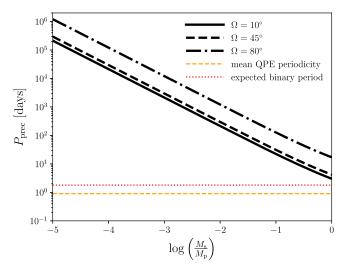


Figure 6. Accretion disk's precession period due to the torques by the secondary (expressed in days) as a function of the logarithm of the component mass ratio ($\log(M_s/M_p)$). We depict three cases corresponding to the low inclination of the secondary with respect to the accretion disk ($\Omega=10^\circ$; solid line), intermediate inclination ($\Omega=45^\circ$; dashed line), and high inclination of $\Omega=80^\circ$ (dotted–dashed line). The mean QPE periodicity and the expected binary period are represented by dashed orange and red dotted lines, respectively.

decrease in the accretion rate. This follows from the eruption luminosity being proportional to the disk surface density, $L_{\rm QPE} \propto \Sigma$ (Linial & Metzger 2023; Tagawa & Haiman 2023), and for the standard disk there is a power-law dependency of the surface density on the accretion rate, $\Sigma \propto \dot{m}^{7/10}$ (Frank et al. 2002). The accretion rate can be decreasing over the course of several months to years following a TDE (see, e.g., Linial & Metzger 2023, and further discussion) with a power-law time dependency, in particular $\dot{m} \propto t^{-5/3}$ for the canonical TDE, and hence $L_{\rm QPE} \propto t^{-7/6}$. One of the key differences between models proposed by Suková et al. (2021) and those by Franchini et al. (2023) and Linial & Metzger (2023) is that the former predicts the presence of repeated outflows. However, the search for such outflows is beyond the scope of this letter.

As discussed in Linial & Metzger (2023), the emission properties of QPEs may secularly evolve owing to changes in

the accretion flow, and specifically the disk's scale height and accretion rate, as well as changes to the secondary object's physical radius. If the secondary is a star, its outer layers are repeatedly ablated by shocks at every disk passage, consequently changing the star's cross section and its interaction with the disk. Linial & Metzger (2023) further proposed that the origin of the accretion disk is bound debris of a previously tidally disrupted star around the same SMBH. The long-term evolution of the TDE disk naturally results in evolution timescales of order years to a decade (e.g., their Equations (34) and (35)), in agreement with the trends observed in the data. Another outcome of star-disk interaction is the orbital decay induced by hydrodynamical drag at disk passages. However, this should lead to a rather slow, gradual decrease in the recurrence timescale unlike a rather abrupt change of the recurrence timescale from 1.1 days in 2021 June to 0.8 days in 2021 October, i.e., over the course of 4 months. The stellar orbit can only be abruptly changed by a massive mass loss from the system, for example, when a distorted stellar body would split like in a Hills mechanism.

The star-disk interaction model was also presented by Tagawa & Haiman (2023), where the QPE luminosity is dominated by the breakout emission of the bow shock of the star as it emerges from the active galactic nucleus disk. They argue that for eRO-QPE1 both the breakout emission and the cooling emission of the expanding shocked bubble could contribute. This could partially address multiple peaks in Lomb-Scargle periodograms since the breakout emission should contribute once per orbit (when we see the emerging bow shock as the star ascends above the accretion disk), while we detect the cooling emission twice owing to the expansion of the shocked gas both above and below the accretion disk. On the other hand, their model requires massive stars ($\sim 10~M_{\odot}$) on retrograde, low-inclination orbits, which appears to be rather restrictive.

Finally, it is important to note that the shape of the eccentric orbits with a smaller pericenter distance near a fast-spinning black hole can be very different from Keplerian-like ellipses (e.g., Chandrasekhar 1998, chap. 7). In fact, the disk-crossing radius can fluctuate in a rather wide range, thus giving the possibility to explain changes of the outburst properties (Karas & Vokrouhlický 1994; Xian et al. 2021; King 2023).

3.1.3. OPE from Roche Lobe Overflow from a Star Orbiting an SMBH

Roche lobe overflow from an orbiting star was suggested to explain several OPE properties, such as their peak luminosities, their temperatures, and the flare durations (Krolik & Linial 2022; Linial & Sari 2023). In that case a small fraction of the stellar envelope is tidally stripped close to the pericenter of the stellar orbit. Therefore, the eruption recurrence timescale is given by the orbital period, which sets the semimajor axis to $a \sim$ $251.6(P_{\text{orb}}/0.9 \text{ days})^{2/3} (M_{\bullet}/10^{5.8} M_{\odot})^{-2/3} R_g$. The X-ray eruptions could be produced via the oblique stream-stream shocks close to the innermost stable circular orbit, which can address the soft X-ray thermal emission corresponding to \sim 110 eV. The stellar orbit is expected to be only mildly eccentric ($e \le 0.5$). In that case, for the soft X-ray eruptions to be produced close to the innermost stable circular orbit, the detached stellar stream needs to lose its specific angular momentum, which is initially comparable to the orbital angular momentum of the star at the pericenter crossing. This can be achieved by several processes, such as induced magnetic stresses (Krolik & Linial 2022) and/or magnetohydrodynamic drag due to ambient hot plasma (Zajaček et al. 2014), especially when the stellar orbit is more compact on the scale of a few \times 10 r_g , i.e., the model can thus work better for eRO-QPE1 when the SMBH is heavier with $\sim 10^{6.4} M_{\odot}$. Assuming that most of the energy is dissipated at $R_{\rm dis} \sim 10R_g$ owing to oblique stream-stream shocks driven by apsidal precession, the mean stellar mass loss per eruption can be estimated as $\Delta M \sim 7 \times 10^{-7} (L_{\rm erupt}/2.2 \times 10^{42} {\rm erg \, s^{-1}}) (\tau_{\rm erupt}/8 \, {\rm h}) (R_{\rm dis}/10 R_g) \, M_{\odot}$, where $L_{\rm erupt}$ is the mean eruption luminosity and $\tau_{\rm erupt}$ is the mean eruption duration. The system SMBH-star is relatively long-lived since the stellar body is depleted in $\tau_{\star} = (M_{\star}/\Delta M)P_{\rm orb} \sim 3500 \text{ yr.}$ The merger timescale for the orbital period of $P_{\rm orb} \sim 0.9$ days and a nearly circular orbit is $\tau_{\rm merge} \sim 4.85~(P_{\rm orb}/0.9~{\rm days})^{8/3}~(M_{\bullet}/10^{5.8}M_{\odot})^{-2/3}~(M_{\star}/1M_{\odot})^{-1}~{\rm Myr},$ hence about three orders of magnitude longer than τ_{\star} . The irregularity of the eruption recurrence can be caused by the intense X-ray irradiation of the upper stellar atmosphere. This stems from the comparison of the X-ray and stellar flux densities at the periapse (Krolik & Linial 2022),

$$F_{\rm X}/F_{\star} \sim 6 \times 10^{3} (1 - e)^{-2} (L_{\rm erupt}/2.2 \times 10^{42} \,{\rm erg \ s^{-1}}) \times (P_{\rm orb}/0.9 \,{\rm days})^{-4/3} (M_{\bullet}/10^{5.8} M_{\odot})^{-2/3} (T_{\star}/T_{\odot})^{4}.$$
 (2)

The maximum unbound mass per orbit escaping the star due to the excess heating by the X-ray eruption can be estimated as follows:

$$\Delta M_{\rm unbound} \sim 3 \times 10^{-8} (1 - e)^{-2} (L_{\rm erupt}/2.2 \times 10^{42} \, {\rm erg \ s^{-1}}) \times (D_{\rm erupt}/0.3) (P_{\rm orb}/0.9 \, {\rm days})^{-1/3} \times (M./10^{5.8} M_{\odot})^{-2/3} (M_{\star}/1 M_{\odot})^{1.64} M_{\odot},$$
(3)

where $D_{\rm erupt}$ is the duty cycle of eruptions. For mildly eccentric orbits ($e \sim 0.5$), $\Delta M_{\rm unbound}$ is comparable to ΔM , and hence the modulation of mass transfer and QPE luminosity via the excess heating is a plausible mechanism.

The stellar mass transfer may thus be initially enhanced and unstable owing to the induced turbulence in the upper atmosphere. In addition, the progressive tidal truncation of the star may lead to its shrinking when the atmosphere layer is depleted via the Roche lobe overflow. The short periodicity of ~ 0.9 days is consistent with a solar-like star whose radius is comparable to the Roche lobe radius at its pericenter. The required stellar

radius has an approximately solar value. Using the relation for the limiting stellar radius for the tidal stripping, $R_\star \sim G^{1/3}/(4\pi^2)^{1/3}(1-e)P_{\rm orb}^{2/3}M_\star^{1/3}$, we obtain the numerical estimate of $R_\star/R_\odot \sim 3.92(1-e)(P_{\rm orb}/0.9~{\rm days})^{2/3}(M_\star/1M_\odot)^{1/3}$. Hence, if the stellar radius slightly shrinks below this value, the flares may be weakened or fall below the detection limit. The stripping of the envelope can also be connected with the inspiral of the star and thus shortening of the QPE period (Bogdanović et al. 2014). However, the precise timing of these processes requires 3D hydrodynamical models involving a realistic stellar model that is subject to tidal forces and radiation heating due to the X-ray flare close to the pericenter.

A modification of the Roche lobe overflow model was presented by Lu & Quataert (2023), where the Roche lobe overflowing star feeds a compact accretion disk. As in Krolik & Linial (2022), the QPE emission is due to circularization shocks, hence not accretion dominated. The steady-state accretion disk should provide a quiescent accretion with the Eddington ratio of ~ 0.08 (their Equation (12)) for $M_{\bullet} = 10^6 M_{\odot}$, which is above the inferred upper limit on the quiescent X-ray luminosity of eRO-QPE1.

3.2. QPE Models Related to Accretion Flow Instabilities

3.2.1. QPEs from Radiation Pressure Instability

Accretion disk instabilities were invoked already in early studies (Lightman & Eardley 1974) and revealed that the innermost regions of viscous disks cannot be stable when reaching a significant fraction of Eddington luminosity. In the unstable mode, the radiation pressure becomes so strong that the local cooling exceeds the heating. When the local temperature increases, the excess of accretion rate leads to the disk depletion and density drops. The disk can rebuild on short timescales and enter a cyclic oscillatory mode, if the advective process is regulating the thermal imbalance. Numerical simulations of such oscillations presented in Janiuk et al. (2002) and the theoretical light curves well matched the observations of Galactic microquasars, GRS 1915+105, and then IGR J17091 (see Janiuk et al. 2015). The extension of the unstable zone and hence the amplitudes and timescales of the observable luminosity flares depend on the mass inflow rate, as well as on the mass of the central black hole. Application of the same global disk instability model to a wide range of black hole masses, from stellar mass to intermediate and SMBH, is quite straightforward. However, in order to produce realistic patterns, certain modifications of disk physics have to be assumed. For instance, Grzedzielski et al. (2017) considered alternative forms of the viscous stress tensor and found that oscillation periods on the order of 1 day are possible for a $4 \times 10^4 M_{\odot}$ intermediate-mass black hole. The ratio of flare width to the recurrence time between flares is another measurable quantity, which may help to verify this model and its parameters. Alternatively, Śniegowska et al. (2023) discussed explicitly the role of magnetic fields in regulating the oscillation pattern and partial stabilization of the disk. For the case of a $10^5 M_{\odot}$ black hole, the intraday oscillation timescales, characteristic of the QPE phenomenon, are possible with a strong magnetic field. An accretion rate of $\dot{m} = 0.5$ and magnetic field of coefficient b = 0.22 decreased the outburst timescale to \sim days. In this case, the pattern is irregular, and few-day flares are accompanied by sequences of 1-day outbursts. In addition, changing the viscosity parameter to $\alpha = 0.1$ shortened the outburst timescale down to 16 hr. We note that the shape of the outbursts obtained from radiation pressure instabilities is asymmetric and

that the dimming phase takes 10% of the duration of the full flare, which appears to be in contradiction with fast-rise, slow-decay or symmetric profiles of most of the flares of eRO-QPE1. In addition, considering the upper limit on the quiescent-level flux of eRO-QPE1, $F_q \lesssim 4 \times 10^{-14}\,\mathrm{erg\,s^{-1}\,cm^2}$, the Eddington ratio can be constained to be $\dot{m} \lesssim (4\pi D_L^2 F_q) \kappa_{\mathrm{bol}}/L_{\mathrm{Edd}} \sim 0.03$ for $M_{\bullet} = 10^{5.8}~M_{\odot}$ and the bolometric correction of $\kappa_{\mathrm{bol}} \sim 10$ (Richards et al. 2006; Netzer 2019). For XMM-Newton's quiescent flux of $F_q^{\mathrm{XMM}} \sim 5 \times 10^{-15}\,\mathrm{erg\,s^{-1}\,cm^{-2}}$, we obtain $\dot{m} \sim 0.004$. Hence, the relative accretion rate is at least one order of magnitude lower than the limiting accretion rate of $\dot{m}_{\mathrm{RPI}} \gtrsim 0.16 \alpha_{0.1}^{41/29} m_{5.8}^{-1/29}$ that is required for the radiation pressure instability to effectively operate (Sniegowska et al. 2020) within the radiation-pressure-dominated standard accretion disk.

3.2.2. QPEs from Shock Front Oscillations

Another possible source of QPEs is oscillations of the shock front in low angular momentum flows. The source of the low angular momentum material accreting onto the SMBH can be strong stellar winds from massive stars orbiting the central black hole on larger distances (~parsec scale) as was estimated for Sgr A* by Mościbrodzka et al. (2006). If the accreting material on the central SMBH has sub-Keplerian angular momentum distribution, for a certain range of the parameter space (energy and angular momentum of the incoming matter) the possibility of the existence of multiple critical points appears (Paczynski & Bisnovatyi-Kogan 1981; Muchotrzeb & Paczynski 1982; Abramowicz & Kato 1989). In such a case, a shock front connected with a sudden drop of the inward velocity from supersonic to subsonic regime and a simultaneous increase of the flow density may emerge. The accretion solution then passes through both the outer and the inner sonic points. The relation of quasi-spherical slowly rotating accretion flows to variability of X-ray sources has been reported already by Jufu & Abramowicz (1988), and the parameter space corresponding to the shock emergence in a different geometrical setup was described by Abramowicz & Chakrabarti (1990).

More recently, numerical simulations have shown that for a subset of parameters the shock front location is unstable and oscillations of the shock bubble develop (Suková & Janiuk 2015), which is accompanied by quasiperiodic flares in the accretion rate. Suková et al. (2017) provided an extended study of the dependence of the oscillations on angular momentum and energy by means of 1D/2D and 3D GRMHD simulations, while Palit et al. (2019) focused on the effect of adiabatic index on the resulting flow.

Considering the mass of the SMBH in the range $M \in (10^{5.2}, 10^{6.4})~M_{\odot}$, the recurrence time of 0.9 days or $(10^5-6\times10^3)GM/c^3$ in geometrized units corresponds to the frequency $f \in (1\times10^{-5}, 2\times10^{-4})c^3/(GM)$. Such values were reported by Suková et al. (2017, see their Table 3 and Figure 18) for shock fronts oscillating at the distance of several tens of gravitational radii from the center.

The model can accommodate the variations in the period taking into account that the oscillations shown by Suková et al. (2017) are quasiperiodic in nature even when the parameters of the incoming gas (energy and angular momentum) are kept strictly constant. Moreover, the mean position of the shock front and the frequency of the oscillations depend quite strongly on those parameters; hence, their relatively small change can lead to a change in the recurrence period or even to

the disappearance/reappearance of the shock front, which is reflected in the accretion rate behavior. The gradual decrease of the peak flux may be attributed to the slow density decline of the incoming gas.

The coherent oscillations of the shock front are expected to appear in a situation where the incoming gas has relatively stable properties falling inside the multicritical parameter space, which may be a short-lived situation depending on the properties of the gas on the larger scale.

3.2.3. QPEs from Disk Tearing Instability

The disk tearing instability can occur in disks that are sufficiently misaligned to a spinning black hole such that a large warp amplitude can develop in the disk (Nixon et al. 2012; Doğan et al. 2018; Raj et al. 2021). When only a modest warp amplitude is reached, the warp propagates through the disk via either waves if the disk is hot and low viscosity or diffusion if the disk is cool and high viscosity (Papaloizou & Pringle 1983). However, for disks that achieve a large warp amplitude it has been shown that they can become unstable, leading to the disk separating into diskrete rings (Doğan et al. 2018; see also Ogilvie 2000). In either the wavelike or diffusive case of warp propagation it is possible for the disk to tear into discrete rings (Drewes & Nixon 2021). In disks that are strongly unstable, the disk emission can exhibit complex variability, as the unstable region can be far from the black hole; this means that a combination of shocks, subsequent accretion, and geometric effects are responsible for determining the emergent light curve. These processes are discussed in detail in Nixon & Salvesen (2014) and Raj & Nixon (2021).

However, for disks that are only weakly unstable, the instability is confined to the very inner regions of the disk. Raj & Nixon (2021) provide an example simulation of such a disk, where the innermost annulus of the disk is repeatedly torn off and accreted in a brief flare-like event. In their Figure 3 they provide the accretion rate onto the central black hole with time, which shows regularly spaced peaks. They suggest that X-rays may be produced when the ring of gas that is torn from the disk precesses and shocks against its neighboring ring before falling into the black hole. For a black hole of mass $4 \times 10^6 M_{\odot}$ the spacing between these peaks is approximately a day and thus could be consistent with the eruptions in eRO-QPE1. The shapes of most of the eruptions observed in eRO-QPE1 (being fast rise and slower decay) are reversed compared to those seen in Figure 3 of Raj & Nixon (2021); while this does not appear consistent, it may be that a more detailed model of the emission from the disk could account for this shape. For example, the shocks may cool more slowly than assumed in the simulation, or they may be optically thick such that some expansion is required before the radiation may escape.

It is also possible that the X-ray flux declines over time in a tearing disk, as observed for eRO-QPE1 (Figure 2), if either the disk accretion rate or inclination is declining with time so that there is less energy generated in the shocks; if the disk was formed from a past TDE, for example, the monotonically declining fallback rate (as $\propto t^{-5/3}$ for complete disruptions) would naturally lead to a weakening X-ray flux with time owing to the diminishing mass supply. This changes the disk conditions, which, in turn, leads to a change in the radius at which the disk tears and hence a change to the recurrence timescale. The most significant change in the time between eruptions for eRO-QPE1 occurred between Swift #1 and Swift

#2, and this drop in recurrence timescale was accompanied by the largest drop in average peak flux. This could be explained by a (small) reduction in the radius at which the disk tears (perhaps caused by the disk becoming slightly thinner) such that less material is involved in the inter-ring shocks. It is difficult to see why the period would then increase again while the flux continues to decline. However, to within the error bars the period is consistent with being constant from Swift #2 to #6, and therefore this might be reasonably explained by the radius of the instability remaining roughly constant while the disk accretion rate drops slightly, reducing the average peak flux accordingly. To confirm whether such details can be adequately reproduced by a disk tearing model requires targeted simulations. Such simulations could be used in the future to constrain the disk and black hole parameters for eRO-OPE1 in the case that disk tearing is driving the eruptions.

3.3. Summary of Models

- 1. The repeated partial stripping of a white dwarf (Zalamea et al. 2010; King 2020) requires such a highly relativistic pericenter that, in spite of the extremely small mass ratio, gravitational-wave emission nontrivially reduces the orbital period over the timescale of 3 yr. The nondetection of gravitational-wave decay, as our data imply (see Figure 4), is only consistent with this model if the white dwarf mass is substantially below the (observationally constrained) most likely mass of 0.6 M_{\odot} , and/or if the black hole mass is $\lesssim 10^4 M_{\odot}$ and in the intermediate-mass black hole regime.
- 2. The interaction of the stellar or the compact-object perturber with a standard accretion disk (Franchini et al. 2023; Linial & Metzger 2023) can address the eruption luminosity, its temperature, the flare recurrence timescale, and its irregularities (due to the various precession mechanisms). The decrease in the amplitude seems to require a previous TDE, which ensures that the accretion rate is progressively getting smaller.
- 3. The Roche lobe overflow from the main-sequence star does not necessarily require the existence of the standard accretion disk (Krolik & Linial 2022; see, however, Lu & Quataert 2023); hence, the model is also suitable for lowluminosity sources such as eRO-QPE1. It can also explain the flare luminosity, recurrence timescale, and temperature when the detached stream can collide with itself close to the innermost stable circular orbit, which results in oblique circularization shocks (Krolik & Linial 2022). The caveats include the angular momentum loss for the matter to reach the innermost stable circular orbit. The recurrence irregularity can be addressed by the additional mass loss due to X-ray heating. The decrease in the flare amplitude and the period could be related to a rapid mass loss from the disturbed stellar body, though this would require a detailed numerical modeling.
- 4. Models involving disk instabilities depend on the accretion rate, the viscosity parameter of the accretion flow, and its magnetic field strength and configuration. For the radiation pressure instability to operate effectively, the relative accretion rate should at least reach $\dot{m} \sim 0.1$ (Sniegowska et al. 2020) so that the inner part of the disk is radiation pressure dominated and thus unstable. Therefore, this model appears problematic for eRO-QPE1, whose upper limit on the Eddington ratio is

 ~ 0.01 . Another model involving the oscillating shock bubble modulating the accretion rate in a quasiperiodic manner (Suková & Janiuk 2015; Suková et al. 2017) depends on the boundary conditions (e.g., a distant windblowing star) supplying low angular momentum material to the inner regions. The model requires the fine-tuning of several parameters to ensure that the period of the QPE and the eruption amplitude decrease as observed. Finally, the disk tearing instability can address the timing and the quasiperiodic manner of the eRO-OPE1 flares by the mechanism of the detachment and the precession of the inner disk ring and its collision with the neighboring ring, resulting in bright flares due to shocks and subsequent accretion (Raj & Nixon 2021). The disk tearing instability requires a sufficiently high misalignment between the accretion disk and the SMBH spin to operate. A targeted simulation is necessary to address the change in the QPE period and the amplitude with time.

4. Discussion

We note that in accreting stellar-mass black holes (StMBHs), quasiperiodic oscillations (QPOs) of the X-ray flux have been known for several decades (Lewin & van der Klis 2006; McClintock & Remillard 2006). There are intriguing similarities and differences compared to QPOs in low-mass X-ray binaries; nonetheless, in the case of accreting neutron stars, properties of QPOs are likely determined by the internal oscillations within the accretion flow and in the boundary layer. In the case of StMBH QPOs, timescales are in the range of a fraction of a second to a few milliseconds (van der Klis 1998; McClintock & Remillard 2006). Thus, a typical power spectrum consisting of a few kiloseconds of exposure samples several tens to hundreds of thousands of cycles of the underlying phenomenon. In the case of eRO-QPE1, using roughly 300 ks of XRT exposure, we sampled about 27 eruptions. Thus, it is possible that we are looking at individual frequencies/timescales making up the broad quasi-periodicity similar to those seen in StMBHs, and it may not be valid to make strong inferences based on time between individual eruptions.

4.1. Comparison to GSN 069 and Repeating TDEs

There are two aspects of eRO-QPE1 that are strikingly similar to GSN 069's behavior. First, the recurrence time varies between 0.6 and 1.2 days (Figure 4). This corresponds to a coherence value, Q, defined as the ratio of dispersion in time between eruptions and the mean duration between eruptions, of 0.9 days/0.3 days \approx 3. This is comparable to GSN 069, where the recurrence time varied between 25 and 35 ks before they disappeared in 2020 (see the bottom right panel of Figure 3 of Miniutti et al. 2023a), i.e., coherence of $30/10 \approx 3$.

Second, GSN 069 showed a decline in QPE intensity over a period of 500 days following the first detection of eruptions (see Figure 2 of Miniutti et al. 2023a). eRO-QPE1 is showing the same trend (Figure 2). More recent follow-up of GSN 069 has shown that QPEs have disappeared for about 2 yr before reappearing with a much shorter recurrence period (Miniutti et al. 2023b). Continued monitoring of eRO-QPE1 will test whether eRO-QPE1 continues to behave the same way.

Two X-ray TDEs, AT2018fyk/ASASSN-18UL (Wevers et al. 2023) and eRASSt J045650.3–203750 (Liu et al. 2023),

are known to repeat on timescales of \sim 1200 and \sim 200 days, respectively. These have been interpreted as rpTDEs (Liu et al. 2023; Wevers et al. 2023). It is worth noting that these two systems show a diminishing luminosity in successive peaks, indicating a progressive reduction in peak amplitude over time, but we note that only two peaks were observed for AT2018fyk and four peaks for eRASSt J045650.3–203750 (obtained in private communication).

4.2. Future Prospects of Tracking eRO-QPE1's Eruptions

Based on the mean duration of eRO-QPE1 eruptions of 7.6 hr (Arcodia et al. 2021) and the capabilities of current X-ray facilities, i.e., XMM-Newton, NICER, and Swift, we estimate a sensitivity limit beyond which detecting eRO-QPE1's eruptions would be challenging. For instance, Swift has an orbital period of roughly 96 minutes (5.6 ks) around Earth and can typically observe a target for a few kiloseconds per orbit (see, e.g., https://swift.gsfc.nasa. gov/proposals/cy20_faq.html#monitor). Assuming 2 ks exposure every 5.6 ks, on average, Swift can accumulate about 10 ks over a 7.6 hr duration of a typical eruption. In order to detect an eruption robustly and roughly constrain its temperature, one would need at least 25 counts, i.e., a 5σ threshold. This translates to an average count rate during an eruption of $25/10 \,\mathrm{ks} = 0.0025 \,\mathrm{count \, s}^{-1}$. Using HEASARC WebPIMMS (https://heasarc.gsfc.nasa.gov/ cgi-bin/Tools/w3pimms/w3pimms.pl) and assuming a blackbody temperature of 0.11 keV, this translates to an observed 0.3-1.2 keV flux of 6×10^{-14} erg s⁻¹ cm⁻². In other words, if the average eruption flux is below this value, Swift/XRT would find it difficult to clearly identify an eruption. Similarly for NICER, assuming a minimum count rate of 2x the nominal threshold value of 0.2 counts s $^{-1}$ (Remillard et al. 2022) implies that if the average eruption flux is below 3 \times 10 $^{-14}$ erg s $^{-1}$ cm $^{-2}$, NICER will find it difficult to identify the eruptions. Thus, detecting eruptions with NICER should already be challenging in the present state (see the bottom right panel of Figure 1 and top panel of Figure 2). For XMM-Newton, the prospects are better. For example, if we require detecting at least 50 counts within 7.6 hr, the corresponding count rate is ~ 0.002 counts s⁻¹, which translates to a flux of 2 \times 10⁻¹⁵ erg s⁻¹ cm⁻². Thus, 1.2 days or 125 ks of continuous exposure with XMM-Newton can guarantee detecting an eruption. We do not consider Chandra owing to its deteriorating soft X-ray response. In summary, if the decaying trend in eruption peak luminosity shown in Figure 2 continues, they can be traced for the next several years with both Swift and XMM-Newton.

5. Summary

eRO-QPE1 is the second QPE source showing a gradual decay in strength of eruptions over time. In the case of GSN 069, Miniutti et al. (2023b) have recently reported that the QPEs decayed and eventually disappeared for about 2 yr and reappeared with a much shorter recurrence time. In addition, in the case of GSN 069, along with the eruption strength, the quiescent level was also declining over time. The Swift/XRT observations presented here were not sensitive enough to detect the quiescent level. Only XMM-Newton has the effective area and the sensitivity to detect and track the quiescent level over the coming years. It is unknown whether eRO-QPE1's quiescence and eruptions exhibit the same behavior. Further monitoring observations with Swift and XMM-Newton over the next few years will certainly be able to address this question

and may enable a unifying picture for long-term evolution of QPE sources.

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Facilities: Swift (XRT), XMM-Newton/EPIC

Appendix Supplementary Material: Data Reduction and Analysis

Details of Swift/XRT and XMM-Newton/EPIC data reduction, time series, and energy spectral analysis are described here.

We used data from Swift/XRT and XMM-Newton's European Photon Counting Camera (EPIC) pn in this work. The details of our data reduction procedures are discussed below.

A.1. Swift/XRT

Between 2021 June and 2023 June Swift's XRT (Gehrels et al. 2004; Burrows et al. 2005) performed six sets of high-cadence observations of eRO-QPE1. These were part of Swift's approved guest observer programs: 1720147 (cycle 17), 1821153 (cycle 18), and 1922142 (cycle 19) (PI: Pasham). In each of these six campaigns, eRO-QPE1 was observed for 12–16 times per day for 4–5 days. Each visit was between 100 and 500 s long, with a cumulative exposure of about 50 ks per campaign.

We started our analysis by downloading the raw data from the publicly available HEASARC archive: https://heasarc.gsfc.nasa.gov/cgi-bin/W3Browse/w3browse.pl. Using the xrtpipeline tool from HEASoftv6.29 c, we reduced these 353 data sets as per the standard data reduction guidelines as described on Swift webpages: https://www.swift.ac.uk/analysis/xrt/xrtpipeline.php. A few of the obsIDs had exposures of just a few tens of seconds, and those were excluded from further analysis. From each of the remaining obsIDs, we extracted source counts from a circular region with a radius of 30" centered on coordinates (02:31:47.26, – 10:20:10.31) (J2000.0 epoch). Background events were extracted from an annulus centered on the same coordinates

with an inner and outer radius of 70" and 220", respectively. We only used events with grades 0–12. We combined data on a per-obsID basis and extracted the resulting background-subtracted count rates (Figure 1).

To track the strength of the eruptions over the past 3 yr, we employ two different methods. First, for each Swift data set (Swift #1,..., #6), we assign a data point as belonging to an eruption if the count rate is more than 10 times the mean background rate, which is roughly 0.0003 counts s⁻¹ in all cases. Then, we compute the mean of the top 20% of all count rates assigned to eruptions. This value is a proxy for the peak X-ray flux. These estimates are shown as filled circles in Figure 2.

Independently, we also compute the average X-ray flux of eruptions per Swift data set as follows. First, we use the Bayesian blocks algorithm of Scargle et al. (2013) to identify the start and end times of each eruption in each data set. For this, we use the Astropy (Astropy Collaboration et al. 2013) implementation of this algorithm (https://docs.astropy.org/ en/stable/api/astropy.stats.bayesian blocks.html), which also takes the measurement errors into account. As evident by eye, the eruptions are especially weak in the later epochs. Thus, following the description in Section 4.3 of Scargle et al. (2013), we use a lenient false-alarm probability of 50% to improve sensitivity to identify eruptions. The corresponding bin edges are shown as black dashes in Figure 1. Then, we estimate the average strength of the eruptions as the mean of all count rates belonging to eruptions in a given epoch. The resulting curve is shown as filled triangles in Figure 2 and is consistent with analysis based on peak rates derived from the simple count rate cut described above.

The Bayesian blocks algorithm also allows us to identify the peak time of each eruption. For Swift #1, these values are 0.66 ± 0.03 days, 1.82 ± 0.07 days, and 2.92 ± 0.10 days for the three eruptions identified by the algorithm. The times are measured with reference to the first observation, i.e., MJD 59373.074. For Swift #2, the peak times of eruptions (with reference to MJD 59502.022) are 0.34 ± 0.10 days, 1.17 ± 0.14 days, 1.93 ± 0.03 days, 2.73 ± 0.10 days, and 3.56 ± 0.13 days. For Swift #3, these values are 0.11 ± 0.11 days, 0.72 ± 0.09 days, 1.54 ± 0.07 days, and 3.24 ± 0.17 days. The algorithm did not identify any eruptions during Swift #4. During Swift #5, the eruption peaks occurred at 0.76 ± 0.13 days, 1.34 ± 0.10 days, 3.20 ± 0.03 days, and 3.93 ± 0.02 days. It is evident from these values that the recurrence time between eruptions can vary between 0.6 and 1.2 days. This is consistent with the locations of the broad peaks (0.6-1.2 days) in the Lomb-Scargle periodograms shown in Figure 4.

To convert from observed $0.3-1.2\,\mathrm{keV}$ count rate to flux/luminosity, we extracted a combined X-ray spectrum using data from all eruptions in each campaign, modeled it with a thermal component (tbabs*ztbabs*zashift(diskbb)), and obtained a conversion factor (see Table 1). Similarly, we constrained the quiescent flux level by combining obsIDs between eruptions in each campaign. The 3σ count rate/flux upper limits were obtained using ximage's sosta tool.

A.2. XMM-Newton/EPIC

XMM-Newton's EPIC observed eRO-QPE1 on two occasions, 2020 July 27 (obsID: 0861910201) and 2020 August 4 (0861910301), for about 90 ks each. We downloaded the raw

data from the HEASARC archive and reduced them using the standard procedures: https://www.cosmos.esa.int/web/xmmnewton/sas-threads. We extracted source events from a circular aperture of 25" centered on coordinates mentioned above, and background events were extracted from a nearby circular region of 50" radius. We ensured that the background aperture was free from point sources. Flaring windows were removed by filtering on the 10–12 keV light curve of the entire field of view. ObsID 0861910201 had two clear eruptions, while one eruption was present in obsID 0861910301.

We extracted the EPIC-pn X-ray spectra of the three peaks of the eruptions and binned them using XMM-Newton analysis tool specgroup to have a minimum of 1 count per spectral bin with oversample = 3. Then, we fit them separately with the same model used for modeling Swift/XRT eruptions, i.e., tbabs*ztbabs*zashift(diskbb). While the temperature and the normalization of diskbb were left free, the neutral column density of the host was tied across all three spectra. The fit resulted in C-stat/dof of 83.3/65. The best-fit column density was $(0.069 \pm 0.020) \times 10^{22}$ cm⁻². The best-fit temperature values (in chronological order) were $0.125 \pm 0.006 \,\mathrm{keV}$, $0.192 \pm 0.010 \, \text{keV}$, and $0.121 \pm 0.005 \, \text{keV}$. The corresponding 0.3–1.2 keV observed fluxes were $(8.4\pm0.3)\times10^{-13}\,\mathrm{erg\,s^{-1}\,cm^{-2}},\,(33.8\pm0.8)\times10^{-13}\,\mathrm{erg\,s^{-1}\,cm^{-2}},\,\mathrm{and}\,(7.6\pm0.3)\times10^{-13}\,\mathrm{erg\,s^{-1}\,cm^{-2}},\,\mathrm{respectively}.$ Because these observations were closely spaced in time, and we are interested in the evolution-over-years timescale, we report the average values in Figure 2. Similarly, we computed the average flux of the eruptions.

We then extracted two quiescence spectra, one from each of the obsIDs, and fit them again with $tbabs^*ztbabs^*zashift$ (diskbb). We fixed the host galaxy neutral column density at $0.069\times10^{22}~{\rm cm}^{-2}$ and tied the diskbb's temperature and normalization, which resulted in a C-stat/dof of 35.5/33. The best-fit temperature was $0.082\pm0.025~{\rm keV}$. The observed $0.3-1.2~{\rm keV}$ flux could not be constrained independently. However, if we freeze the disk temperature at the best-fit value of $0.082~{\rm keV}$, the resulting flux is $(4.7\pm0.7)\times10^{-15}~{\rm erg~s}^{-1}~{\rm cm}^{-2}$.

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References

Abramowicz, M. A., & Chakrabarti, S. K. 1990, ApJ, 350, 281 Abramowicz, M. A., & Kato, S. 1989, ApJ, 336, 304 Altamirano, D., Belloni, T., Linares, M., et al. 2011, ApJL, 742, L17 Arcodia, R., Merloni, A., Nandra, K., et al. 2021, Natur, 592, 704 Arcodia, R., Miniutti, G., Ponti, G., et al. 2022, A&A, 662, A49

```
Amaud, K. A. 1996, in AIP Conf. Ser. 101, Astronomical Data Analysis Software
   and Systems V, ed. G. H. Jacoby & J. Barnes (Melville, NY: AIP), 17
Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A,
  558, A33
Blanchet, L. 2014, LRR, 17, 2
Bogdanović, T., Cheng, R. M., & Amaro-Seoane, P. 2014, ApJ, 788, 99
Britzen, S., Fendt, C., Witzel, G., et al. 2018, MNRAS, 478, 3199
Burrows, D. N., Hill, J. E., Nousek, J. A., et al. 2005, SSRv, 120, 165
Chakraborty, J., Kara, E., Masterson, M., et al. 2021, ApJL, 921, L40
Chandrasekhar, S. 1998, The Mathematical Theory of Black Holes (Oxford:
   Oxford Univ. Press)
Chen, X., Qiu, Y., Li, S., & Liu, F. K. 2022, ApJ, 930, 122
Coughlin, E. R., & Nixon, C. J. 2020, ApJS, 247, 51
Cufari, M., Nixon, C. J., & Coughlin, E. R. 2023, MNRAS, 520, L38
Doğan, S., Nixon, C. J., King, A. R., & Pringle, J. E. 2018, MNRAS,
   476, 1519
Drewes, N. C., & Nixon, C. J. 2021, ApJ, 922, 243
Evans, P. A., Nixon, C. J., Campana, S., et al. 2023, NatAs, 7, 1368
Faber, J. A., Rasio, F. A., & Willems, B. 2005, Icar, 175, 248
Fabian, A. C., Pringle, J. E., & Rees, M. J. 1975, MNRAS, 172, 15
Franchini, A., Bonetti, M., Lupi, A., et al. 2023, A&A, 675, A100
Frank, J., King, A., & Raine, D. J. 2002, Accretion Power in Astrophysics
   (Cambridge: Cambridge Univ. Press), 398
Gafton, E., Tejeda, E., Guillochon, J., Korobkin, O., & Rosswog, S. 2015,
          $ 449 771
Gehrels, N., Chincarini, G., Giommi, P., et al. 2004, ApJ, 611, 1005
Giustini, M., Miniutti, G., & Saxton, R. D. 2020, A&A, 636, L2
Golightly, E. C. A., Nixon, C. J., & Coughlin, E. R. 2019, ApJL, 882, L26
Grzedzielski, M., Janiuk, A., Czerny, B., & Wu, Q. 2017, A&A, 603, A110
Guillochon, J., & Ramirez-Ruiz, E. 2013, ApJ, 767, 25
Guolo, M., Pasham, D. R., Zajaček, M., et al. 2023, arXiv:2309.03011
Ingram, A., Motta, S. E., Aigrain, S., & Karastergiou, A. 2021, MNRAS,
   503, 1703
Janiuk, A., Czerny, B., & Siemiginowska, A. 2002, ApJ, 576, 908
Janiuk, A., Grzedzielski, M., Capitanio, F., & Bianchi, S. 2015, A&A,
   574, A92
Jufu, L., & Abramowicz, M. A. 1988, ChA&A, 12, 119
Karas, V., & Vokrouhlický, D. 1994, ApJ, 422, 208
Kaur, K., Stone, N. C., & Gilbaum, S. 2023, MNRAS, 524, 1269
King, A. 2020, MNRAS, 493, L120
King, A. 2023, MNRAS, 526, L31
Kremer, K., Lombardi, J. C., Lu, W., Piro, A. L., & Rasio, F. A. 2022, ApJ,
   933, 203
Krolik, J. H., & Linial, I. 2022, ApJ, 941, 24
Lacy, J. H., Townes, C. H., & Hollenbach, D. J. 1982, ApJ, 262, 120
Larwood, J. D. 1997, MNRAS, 290, 490
Law-Smith, J. A. P., Coulter, D. A., Guillochon, J., Mockler, B., &
   Ramirez-Ruiz, E. 2020, ApJ, 905, 141
Lewin, W. H. G., & van der Klis, M. 2006, in Compact Stellar X-ray Sources,
   ed. W. Lewin & M. van der Klis (Cambridge: Cambridge Univ. Press), 39
Lightman, A. P., & Eardley, D. M. 1974, ApJL, 187, L1
Linial, I., & Metzger, B. D. 2023, ApJ, 957, 34
```

Linial, I., & Sari, R. 2023, ApJ, 945, 86

Liu, Z., Malyali, A., Krumpe, M., et al. 2023, A&A, 669, A75

```
Lu, W., & Quataert, E. 2023, MNRAS, 524, 6247
Mainetti, D., Lupi, A., Campana, S., et al. 2017, A&A, 600, A124
Manukian, H., Guillochon, J., Ramirez-Ruiz, E., & O'Leary, R. M. 2013,
    pJL, 771, L28
McClintock, J. E., & Remillard, R. A. 2006, in Compact stellar X-ray sources,
   ed. W. Lewin & M. van der Klis, Vol. 39 (Cambridge: Cambridge Univ.
   Press), 157
Metzger, B. D., Stone, N. C., & Gilbaum, S. 2022, ApJ, 926, 101
Miles, P. R., Coughlin, E. R., & Nixon, C. J. 2020, ApJ, 899, 36
Miniutti, G., Giustini, M., Arcodia, R., et al. 2023a, A&A, 670, A93
Miniutti, G., Giustini, M., Arcodia, R., et al. 2023b, A&A, 674, L1
Miniutti, G., Saxton, R. D., Giustini, M., et al. 2019, Natur, 573, 381
Mościbrodzka, M., Das, T. K., & Czerny, B. 2006, MNRAS, 370, 219
Muchotrzeb, B., & Paczynski, B. 1982, AcA, 32, 1
Nauenberg, M. 1972, ApJ, 175, 417
Neilsen, J., Remillard, R. A., & Lee, J. C. 2011, ApJ, 737, 69
Netzer, H. 2019, MNRAS, 488, 5185
Nixon, C., King, A., Price, D., & Frank, J. 2012, ApJL, 757, L24
Nixon, C., & Salvesen, G. 2014, MNRAS, 437, 3994
Nixon, C. J., Coughlin, E. R., & Miles, P. R. 2021, ApJ, 922, 168
Ogilvie, G. I. 2000, MNRAS, 317, 607
Paczynski, B., & Bisnovatyi-Kogan, G. 1981, AcA, 31, 283
Palit, I., Janiuk, A., & Suková, P. 2019, MNRAS, 487, 755
Pan, X., Li, S.-L., Cao, X., Miniutti, G., & Gu, M. 2022, ApJL, 928, L18
Papaloizou, J. C. B., & Pringle, J. E. 1983, MNRAS, 202, 1181
Papaloizou, J. C. B., & Terquem, C. 1995, MNRAS, 274, 987
Payne, A. V., Shappee, B. J., Hinkle, J. T., et al. 2021, ApJ, 910, 125
Peters, P. C. 1964, PhRv, 136, 1224
Predehl, P., Andritschke, R., Arefiev, V., et al. 2021, A&A, 647, A1
Press, W. H., & Teukolsky, S. A. 1977, ApJ, 213, 183
Quintin, E., Webb, N. A., Guillot, S., et al. 2023, A&A, 675, A152
Raj, A., & Nixon, C. J. 2021, ApJ, 909, 82
Raj, A., Nixon, C. J., & Doğan, S. 2021, ApJ, 909, 81
Rees, M. J. 1988, Natur, 333, 523
Remillard, R. A., Loewenstein, M., Steiner, J. F., et al. 2022, AJ, 163, 130
Richards, G. T., Lacy, M., Storrie-Lombardi, L. J., et al. 2006, ApJS, 166, 470
Scargle, J. D., Norris, J. P., Jackson, B., & Chiang, J. 2013, ApJ, 764, 167
Sniegowska, M., Czerny, B., Bon, E., & Bon, N. 2020, A&A, 641, A167
Śniegowska, M., Grzędzielski, M., Czerny, B., & Janiuk, A. 2023, A&A,
   672. A19
Suková, P., Charzyński, S., & Janiuk, A. 2017, MNRAS, 472, 4327
Suková, P., & Janiuk, A. 2015, MNRAS, 447, 1565
Suková, P., Zajaček, M., Witzany, V., & Karas, V. 2021, ApJ, 917, 43
Tagawa, H., & Haiman, Z. 2023, MNRAS, 526, 69
Tucker, A., & Will, C. M. 2021, PhRvD, 104, 104023
van der Klis, M. 1998, AdSpR, 22, 925
Wevers, T., Coughlin, E. R., Pasham, D. R., et al. 2023, ApJL, 942, L33
Wevers, T., Pasham, D. R., Jalan, P., Rakshit, S., & Arcodia, R. 2022, A&A,
   659, L2
Xian, J., Zhang, F., Dou, L., He, J., & Shu, X. 2021, ApJL, 921, L32
Zajaček, M., Karas, V., & Eckart, A. 2014, A&A, 565, A17
Zalamea, I., Menou, K., & Beloborodov, A. M. 2010, MNRAS, 409, L25
Zhao, Z. Y., Wang, Y. Y., Zou, Y. C., Wang, F. Y., & Dai, Z. G. 2022, A&A,
   661, A55
```