



AGe₂O₄Q (A = Ba, Sr; Q = S, Se): A series of heteroanionic oxychalcogenides with large birefringence

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ABSTRACT

Heteroanionic materials are of current research interest owing to their varied structural chemistry and properties. Recently, a number of heteroanionic materials have been synthesized that can be used for water splitting, battery materials, thermoelectrics, and nonlinear optical applications. Birefringent heteroanionic materials are still rarely researched. Herein, we report a series of new oxychalcogenides, AGe₂O₄Q (A = Ba, Sr; Q = S, Se), that are synthesized by solid-state reactions in fused silica tubes with their structures determined by single-crystal X-ray diffraction. Optical property measurements show that AGe₂O₄Q (A = Ba, Sr; Q = S, Se) exhibit large birefringences, 0.13–0.19 @ 1064 nm. These are one-order of magnitude larger than their single-anionic homologue, BaGe₂O₅ - 0.03 @ 1064 nm. This suggests that constructing heteroanions through using chalcogenides to partially substitute O in tetrahedral foundation building units (FBUs) is a viable method for designing new birefringent materials. Furthermore, the crystal structures, UV–vis–NIR diffuse reflectance spectra, infrared and Raman spectra as well as the first-principles calculations for AGe₂O₄Q (A = Ba, Sr; Q = S, Se) are also reported.

1. Introduction

Birefringence originates from the optical anisotropy of materials and plays indispensable important role for the development of advanced technology [1–6]. During the past decades, a number of the oxide-based birefringent crystals, such as YVO₄ [7], TiO₂ [8], LiNbO₃ [9] and CaCO₃ [10], have been discovered and commercialized in ultraviolet (UV) and visible regions. Recently, some borates with large birefringence and short UV cut-off edges ($\lambda_{\text{cut-off}} < 200$ nm), such as Na₃Ba₂(B₃O₆)₂F (0.113@589 nm) [11], Ba₂Ca(B₃O₆)₂ (0.124@589 nm) [12], Ba₂Mg(B₃O₆)₂ (0.110@589 nm) [13], MBaYB₆O₁₂ (M = Rb, Cs) (0.120@589 nm) [14], and Ca(BO₂)₂ (0.134@589 nm) [15] have also been reported. These materials may be potential deep-UV birefringent crystals. However, compared with UV, deep-UV and visible regions, the birefringent crystals in the infrared (IR) regions are rarely reported.

For design of the IR birefringent crystals, chalcogenides may be a good materials class because they can exhibit excellent transmission in wide IR regions [16,17]. Typically, sulfides are transparent to ~11 μm ,

selenides to ~15 μm , and tellurides to beyond 20 μm [18–20]. But for chalcogenide crystals, they generally possess narrow band-gaps, which are unfavorable for materials to exhibit high laser damage thresholds (LDT). That will limit their applications in the high-energy laser systems that are important for environmental monitoring and information communication [21–23]. In recent research, it has been shown that heteroanionic compounds can exhibit superior functional properties than the single-anionic compounds because the former can integrate the properties of the different anion groups [24,25]. Especially in the oxychalcogenides, many interesting functional materials have been found, such as the excellent thermoelectric materials, e.g. BiCuSeO [26], high-capacity battery cathode material, e.g. Ag₂V₂O₆F₂ [27], and the excellent nonlinear optical crystal, e.g. Sr₆Ge₃OSe₁₁ [28].

In the reported research, we believe that the heteroanionic oxychalcogenides will be interesting for the design of IR birefringent crystals. Firstly, the intrinsic difference between M–O and M–Q bonds in the heteroanionic [MO_xQ_y] (Q = S, Se) groups is helpful for enhancing optical anisotropy of materials which can make materials to produce a

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large birefringence. Secondly, in heteroanionic $[\text{MO}_x\text{Q}_y]$ ($\text{Q} = \text{S}, \text{Se}$) groups, the M-Q bonds are helpful to reduce the IR absorptions of materials so that the materials can exhibit wide IR transmission regions [29–32]. Our research in the heteroanionic A-Ge-O-Q ($\text{A} = \text{alkaline earth}; \text{Q} = \text{S}, \text{Se}$) system have resulted in the discovery of four new heteroanionic oxychalcogenides, $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$). They all exhibit large birefringence at 1064 nm, 0.13, 0.16, 0.15, 0.19 for $\text{BaGe}_2\text{O}_4\text{S}$, $\text{BaGe}_2\text{O}_4\text{Se}$, $\text{SrGe}_2\text{O}_4\text{S}$ and $\text{SrGe}_2\text{O}_4\text{Se}$, respectively. These birefringences are one-order magnitude larger than the one of their corresponding single-anionic homologue, BaGe_2O_5 (0.03 at 1064 nm) [33], indicating the effectiveness of heteroanionic groups for the design of the birefringent crystals. In addition, UV-VIS-NIR diffusion spectra and IR spectra also show these compounds also have wide band-gaps and wide IR transmission regions. Therefore, $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) may be potentials as IR birefringent crystals. Herein, we will report their syntheses, crystal structures, optical properties and the first principle calculations.

2. Experimental section

2.1. Reagents

BaF_2 (Aladdin Chemistry Co., Ltd., 99.9 %), Ba (Beijing Hawk Science and Technology Co. Ltd. 99.9 %), GeO_2 (Aladdin Chemistry Co., Ltd., 99.5 %), Ge (Beijing Hawk Science and Technology Co. Ltd. 98 %), SrS (Beijing Hawk Science and Technology Co. Ltd. 98 %), SrSe (Beijing Hawk Science and Technology Co. Ltd. 98 %), S (Aladdin Chemistry Co., Ltd., 99.5 %), and Se (Aladdin Chemistry Co., Ltd., 99.9 %) were used as received from commercial sources without any further purification.

2.2. Synthesis

$\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were all synthesized by the solid-state reactions in the fused silica tube. For $\text{BaGe}_2\text{O}_4\text{S}(\text{Se})$, the starting materials of BaF_2 (0.67 mmol, 0.1175 g), Ba (0.67 mmol, 0.0920 g), GeO_2 (1.00 mmol, 0.1046 g), Ge (0.33 mmol, 0.0240 g), and S/Se (1.33 mmol, 0.0426/0.1050 g) were used. For $\text{SrGe}_2\text{O}_4\text{S}(\text{Se})$, stoichiometric mixture of starting materials SrS/SrSe (1.00 mmol, 0.1197/0.1666 g) and GeO_2 (2.00 mmol, 0.2093 g) were used. These starting materials were put into graphite crucibles and were flame-sealed into 10 mm (inner diameter) fused-silica tubes under vacuum ($\sim 10^{-3}$ Pa), respectively. These tubes were then placed into a temperature controlled muffle furnace, heated from room temperature to 1123 K for $\text{BaGe}_2\text{O}_4\text{S}(\text{Se})$ (1198 K for $\text{SrGe}_2\text{O}_4\text{S}(\text{Se})$) in 40 h, kept at these temperatures for 96 h, and then cooled to room temperature at 2.5 °C/h. Colourless crystals of $\text{Ba}(\text{Sr})\text{Ge}_2\text{O}_4\text{S}$ (~45 % yield based on GeO_2) and light yellow crystals of $\text{Ba}(\text{Sr})\text{Ge}_2\text{O}_4\text{Se}$ (~40 % yield based on GeO_2) were obtained (Fig. S1).

2.3. Single-crystal structure determination

High-quality block single crystals of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were selected for single-crystal X-ray diffraction (XRD). Diffraction data were collected by using Mo $K\alpha$ radiation ($\lambda = 0.71073 \text{ \AA}$) on a Bruker SMART APEX II diffractometer equipped with a 4K CCD detector at room temperature [34]. Their structures were solved by direct methods and refined by full-matrix least-squares method on F^2 with anisotropic thermal parameters for all atoms using SHELXTL program package [35]. Besides, the PLATON program was used to check the symmetry, and no other missed or higher symmetry element was found [36]. Crystal data and structure refinement information were showed in Table 1. The atomic coordinates, equivalent isotropic displacement parameters and selected interatomic distances and angles of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were listed in Table S1 and Table S2 in the Supporting Information, respectively.

Table 1

Crystal data and structure refinement for $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$).

Empirical formula	$\text{BaGe}_2\text{O}_4\text{S}$	$\text{BaGe}_2\text{O}_4\text{Se}$	$\text{SrGe}_2\text{O}_4\text{S}$	$\text{SrGe}_2\text{O}_4\text{Se}$
Formula weight	378.58	425.48	328.86	375.76
Space group	$P2_1/c$			
a (Å)	a = 6.9990 (12)	a = 7.179(7)	a = 6.6983 (11)	a = 6.7928 (6)
b (Å)	b = 9.4705 (18)	b = 9.592(9)	b = 9.4824 (14)	b = 9.5694 (8)
β (°)	$\beta = 94.6110$ (6)	$\beta = 96.160$ (3)	$\beta = 94.355$ (5)	$\beta = 95.357$ (5)
c (Å)	c = 8.2181 (14)	c = 8.491(8)	c = 8.1342 (13)	c = 8.2785 (9)
Volume(Å ³)	542.97(17)	581.3(10)	515.16(14)	535.78(13)
Z	4			
ρ_{Calcd} (g/cm ³)	4.631	4.862	4.240	4.662
Completeness	99.90 %	99.30 %	99.60 %	100.0 %
Data/parameters	1254/73	1336/73	1185/73	1233/74
Goodness-of-fit on F^2	1.091	1.070	1.046	1.051
Final R indexes [$F_o^2 > 2s(F_o^2)$] ^a	$R_1 = 0.0425$, $wR_2 = 0.1005$	$R_1 = 0.0574$, $wR_2 = 0.1552$	$R_1 = 0.0279$, $wR_2 = 0.0545$	$R_1 = 0.0225$, $wR_2 = 0.0376$
Largest diff. peak and hole (e.Å ⁻³)	1.778 and -3.604	2.001 and -4.555	0.818 and -0.787	0.669 and -0.634

$$^a R_1 = \sum |F_o| - |F_c| / \sum |F_o|, wR_2 = \{\sum [w(F_o^2 - F_c^2)^2] / \sum [w(F_o^2)^2]\}^{1/2}.$$

2.4. Powder X-ray diffraction

Powder X-ray diffraction (PXRD) of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) compounds were measured on the SmartLab9KW X-ray diffractometer analyzer with Cu- $K\alpha$ radiation ($\lambda = 1.5418 \text{ \AA}$) in reflection mode at room temperature with a step size of 0.02° in the range of $2\theta = 10\text{--}70^\circ$. The measured PXRD patterns exhibit a good consistency with the simulated ones except for a small amount of BaSe was detected in $\text{BaGe}_2\text{O}_4\text{Se}$ (Fig. 1).

2.5. UV-vis-IR diffuse reflectance spectroscopy and IR spectroscopy

Optical diffuse reflectance spectra were performed at room temperature with A Shimadzu SolidSpec-3700DUV spectrophotometer. Data were collected in the wavelength range 200–2400 nm. The IR spectra were recorded at room temperature by a Nicolet iS50 FT-IR spectrometer transform IR spectrometer in the 400–4000 cm^{-1} range. Polycrystalline powder of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were directly put on the test platform to obtain IR spectral vibration peaks.

2.6. Raman spectroscopy

The Raman spectra were collected with small bulk crystals on a confocal microscope-laser Raman spectrometer (WITec) equipped with a CCD detector using 532 nm radiation from a diode laser. Crystals were selected and loaded on a SiO_2 slide; then, a 50× objective lens was used to choose the area to be measured on the crystal. The spectrum data was collected using an integration time of 10 s.

2.7. Birefringence measurement

The birefringence of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were measured by using a cross-polarizing microscope. According to the equation $R = \Delta n \times d$, Δn can be obtained, where R , Δn , and d are retardation, birefringence, and thickness, respectively.

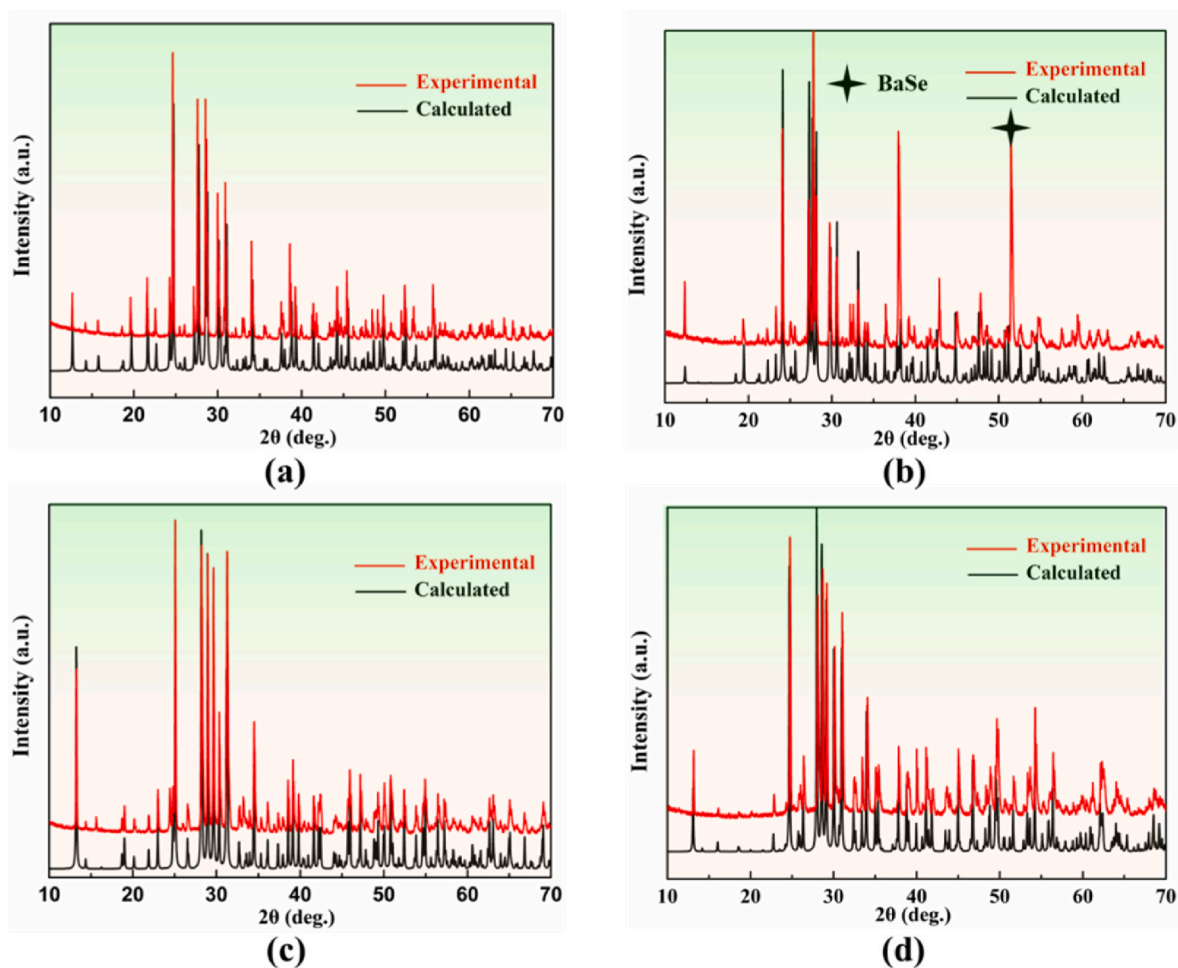


Fig. 1. Powder XRD of (a) $\text{BaGe}_2\text{O}_4\text{S}$, (b) $\text{BaGe}_2\text{O}_4\text{Se}$, (c) $\text{SrGe}_2\text{O}_4\text{S}$, and (d) $\text{SrGe}_2\text{O}_4\text{Se}$.

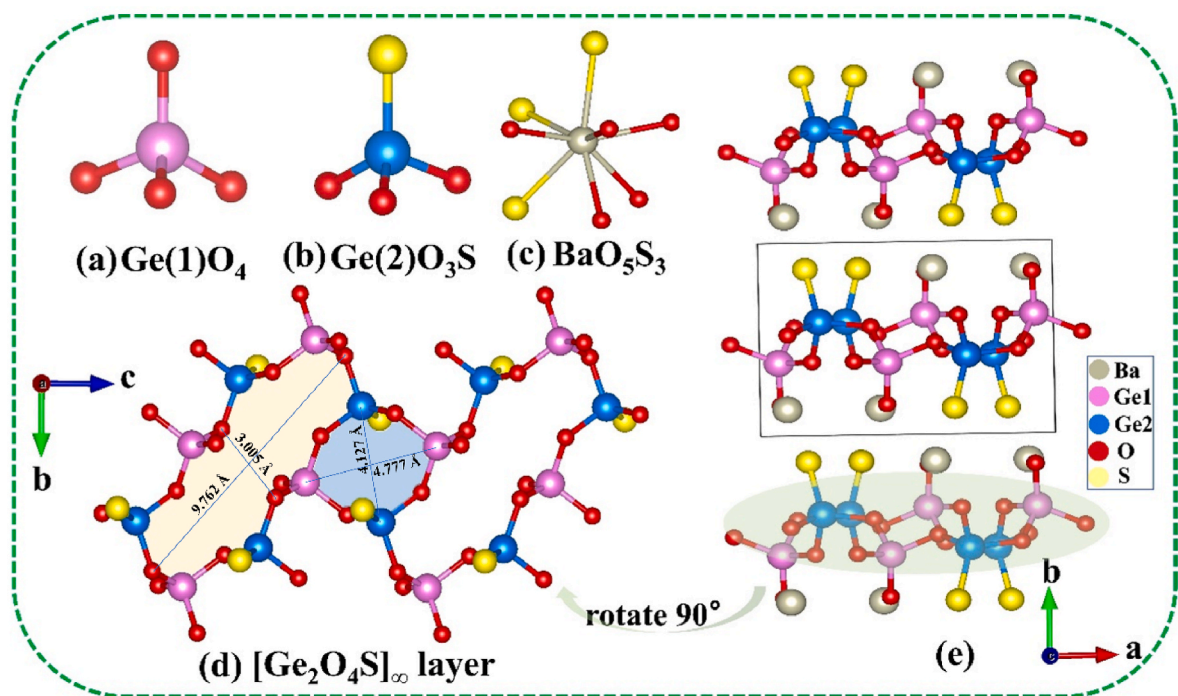


Fig. 2. The structure of $\text{BaGe}_2\text{O}_4\text{S}$: (a) $[\text{Ge}(1)\text{O}_4]$ unit; (b) $[\text{Ge}(2)\text{O}_3\text{S}]$ unit; (c) $[\text{BaO}_5\text{S}_3]$ unit; (d) 2D $[\text{Ge}_2\text{O}_4\text{S}]_\infty$ layered structure formed by the 16-membered rings and 8-membered rings; (e) the arrangement of 2D layered structures of anion units along b -direction.

2.8. Theoretical calculations

First-principles calculations of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were performed by a plane-wave pseudopotential density functional theory (DFT) method implemented on CASTEP software [37,38]. For embodying correlation, core–electron interactions were characterized by norm-conserving pseudopotentials (NCP) [39]. Meanwhile, the generalized gradient approximation (GGA) of Perdew-Buker-Ernzerhof (PBE) was exerted [40]. The valence states are as follows: Ba $5p^6 6s^2$, Sr $4p^6 5s^2$, Ge $4s^2 4p^2$, S $3s^2 3p^4$, Se $4s^2 4p^4$, and O $2s^2 2p^4$. To achieve energy convergence, the plane-wave energy cutoff was set at 810 eV for $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$). The Brillouin zone involved $5 \times 4 \times 4$ for $\text{AGe}_2\text{O}_4\text{S}$ ($\text{A} = \text{Ba}, \text{Sr}$), and $5 \times 3 \times 4$ for $\text{AGe}_2\text{O}_4\text{Se}$ ($\text{A} = \text{Ba}, \text{Sr}$).

3. Results and discussion

3.1. Crystal structures

$\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) crystallize in monoclinic space group $P2_1/c$. As $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$), are iso-structural, only $\text{BaGe}_2\text{O}_4\text{S}$ is illustrated in detail as a representative. The asymmetric unit of $\text{BaGe}_2\text{O}_4\text{S}$ contains one Ba atom, two Ge atoms, four O atoms and one S atom, which all occupy the Wyckoff positions of 4e. For Ge atoms, they are all coordinated by O or O/S atoms to form tetrahedral single-anionic $[\text{GeO}_4]$ and heteroanionic $[\text{GeO}_3\text{S}]$ units (Fig. 2a and b), with the Ge–O bond distances ranging from 1.683(9) to 1.794(8) Å, and Ge–S bond distance is 2.103(4) Å. All of these Ge–O or Ge–S bonds have the consistent distances with the ones in other germinates or Ge-containing sulfides [41,42]. In the structure, the $[\text{GeO}_4]$ and $[\text{GeO}_3\text{S}]$ tetrahedra alternatively connect with each other to form the 16-membered rings and 8-membered rings, and then these 16-membered rings and 8-membered rings are further linked to form the two-dimensional (2D) $[\text{Ge}_2\text{O}_4\text{S}]_\infty$ layers by sharing O atoms (Fig. 2d). In connectivity terms,

the structure may be written as $\{[\text{Ge}(1)\text{O}_{3/2}\text{O}_{1/1}][\text{Ge}(2)\text{O}_{3/2}\text{S}_{1/1}]\}^{2-}$ with Ba^{2+} cations filled between adjacent two layers to maintain the charges balanced (Fig. 2c, e). Remarkably, $\text{Ge}(2)\text{O}_3\text{S}$ and $\text{Ge}(1)\text{O}_4$ are staggered and antiparallel arranged with each other in the same layers, which cancels the macro-polarity and results in their centrosymmetric structures. The bond valence sum (BVS) calculations for Ba: 1.92; Ge: 4.20–4.25; S: 2.02 and O: 1.93–2.18 are agreement with their normal oxidation states, assuring the consistency of the crystal structures [43].

3.2. Structural comparison

From the viewpoint of structure, the heteroanionic $\text{BaGe}_2\text{O}_4\text{S}$ can be seen as the derivative of BaGe_2O_5 with one O atom is substituted by S atom (Fig. 3). But remarkably, BaGe_2O_5 and $\text{BaGe}_2\text{O}_4\text{S}$ are not iso-structural. BaGe_2O_5 features a 2D $[\text{Ge}_2\text{O}_5]_\infty$ layer that is composed of the $[\text{GeO}_4]$ and $[\text{GeO}_6]$ octahedra (Fig. 3a, c). For $\text{BaGe}_2\text{O}_4\text{S}$, although it also features a 2D $[\text{Ge}_2\text{O}_4\text{S}]_\infty$ layer, the layer is constructed of the tetrahedral $[\text{GeO}_4]$ and $[\text{GeO}_3\text{S}]$ units (Fig. 3d, f). That is, from BaGe_2O_5 to $\text{BaGe}_2\text{O}_4\text{S}$, the $[\text{GeO}_6]$ octahedra change to the $[\text{GeO}_3\text{S}]$ tetrahedra. The structural transformation can be understood based on the difference of ionic radius of O and S atoms and the valence matching principle [44]. In BaGe_2O_5 , all Ba^{2+} cations are only coordinated by the O^{2-} anions. Because of the large difference of ionic radius of Ba^{2+} and O^{2-} anions, Ba^{2+} cations tend to be coordinated by more O^{2-} anions (twelve O^{2-} ions in BaGe_2O_5) (Fig. 3b). That makes Ba^{2+} cations have the low Lewis acid strength ($2/12 = 0.17$). As such, the coordinated O atoms of Ba^{2+} cations should be the bridged O atoms between GeO_4 and GeO_6 units because these bridged O atoms will have little residual negative charges and low Lewis base strengths. In addition, these bridged O atoms cannot be the bridged O atoms between GeO_4 and GeO_6 units because these bridged O atoms will have no more residual negative charges (Fig. 3g). In BaGe_2O_5 , two different coordination environments of Ge atoms, the $[\text{GeO}_4]$ tetrahedra and the $[\text{GeO}_6]$ octahedra, are

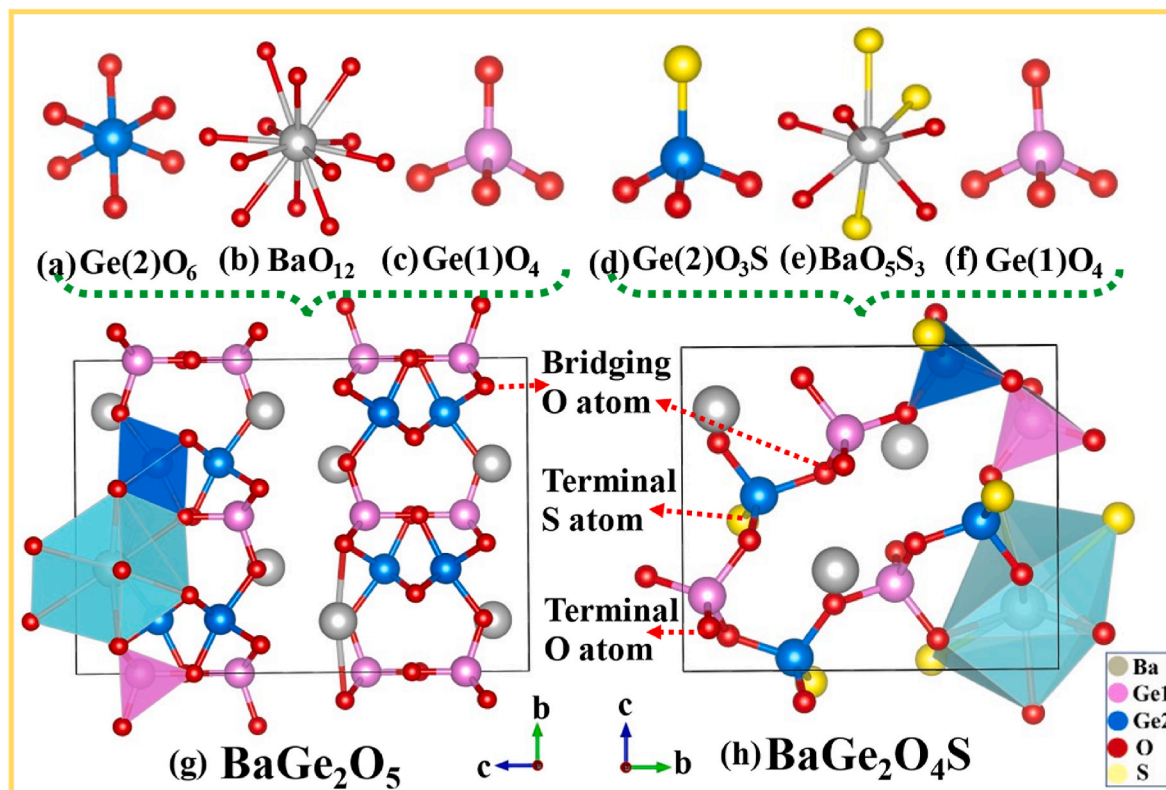


Fig. 3. (a) $\text{Ge}(2)\text{O}_6$ unit of BaGe_2O_5 ; (b) BaO_{12} unit of BaGe_2O_5 ; (c) $\text{Ge}(1)\text{O}_4$ unit of BaGe_2O_5 ; (d) $\text{Ge}(2)\text{O}_3\text{S}$ unit of $\text{BaGe}_2\text{O}_4\text{S}$; (e) BaO_5S_3 unit of $\text{BaGe}_2\text{O}_4\text{S}$; (f) $\text{Ge}(1)\text{O}_4$ unit of $\text{BaGe}_2\text{O}_4\text{S}$; (g) the structure of BaGe_2O_5 ; (h) the structure of $\text{BaGe}_2\text{O}_4\text{S}$.

observed. In $\text{BaGe}_2\text{O}_4\text{S}$, however, S^{2-} anions have closer ionic radius with Ba^{2+} cations. So, the coordination numbers of Ba^{2+} cations is less (eight in $\text{BaGe}_2\text{O}_4\text{S}$) and hence the Ba^{2+} cations have the relatively higher Lewis acid strength ($2/8 = 0.25$) (Fig. 3e). Thus, the coordinated O/S atoms of Ba^{2+} cations can be the terminal O/S atoms. But as the Lewis acid strength of Ba^{2+} cations is not high enough, the corresponding Ge–O/S bonds for the terminal O/S ions are shorten so that they have the relatively little negative charges left to match the Lewis acid strength of Ba^{2+} cations (Table S2). So, the basic building units (BBUs) in $\text{BaGe}_2\text{O}_4\text{S}$ must be tetrahedral $[\text{GeO}_4]$ and the $[\text{GeO}_3\text{S}]$ units (Fig. 3h). But the $[\text{GeO}_6]$ octahedra are impossible for $\text{BaGe}_2\text{O}_4\text{S}$ because the residual negative charges of terminal O atoms for octahedral $[\text{GeO}_6]$ would be too high, which cannot match with the Lewis acid strength of Ba^{2+} cations. Based on the above discussion, we can see that the heteroanionic $\text{BaGe}_2\text{O}_4\text{S}$ can exhibit larger structural anisotropy because of the intrinsic differences between Ge–O and Ge–S as well as the shorter terminal Ge–O/S distances (perpendicular to $[\text{Ge}_2\text{O}_4\text{S}]_\infty$ layer) than the bridged Ge–O distances (in the $[\text{Ge}_2\text{O}_4\text{S}]_\infty$ layer). The large structural anisotropy may be helpful to generate a large birefringence.

3.3. Birefringence measurements

The birefringence of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) was measured

by a cross-polarizing microscope in the visible region. The observed interference colors in cross-polarized light were second-order blue for $\text{BaGe}_2\text{O}_4\text{S}$ and $\text{SrGe}_2\text{O}_4\text{S}$. And, the interference color observed is second-order green under cross-polarized for $\text{BaGe}_2\text{O}_4\text{Se}$ and $\text{SrGe}_2\text{O}_4\text{Se}$ (Fig. 4). Matching with the Michal–Levy chart, the retardations (R values) were found to be 790 nm for second-order blue and 810 nm for second-order green. And their crystal thicknesses were found to be 9.3, 6.0, 9.5 and 6.8 μm , respectively. Following the equation $R = \Delta n \times d$, we can obtain that the birefringence of $\text{BaGe}_2\text{O}_4\text{S}$, $\text{BaGe}_2\text{O}_4\text{Se}$, $\text{SrGe}_2\text{O}_4\text{S}$ and $\text{SrGe}_2\text{O}_4\text{Se}$ are 0.09, 0.14, 0.08 and 0.12 in the visible region. Remarkably, as the cross-polarizing microscope can only measure the birefringence in the crystal wafers, the measured value may be smaller than the largest birefringence of materials. That means the birefringence of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) may be larger than the measured values. The large birefringence might be favorable for their potential application as birefringent crystals.

3.4. UV–vis–NIR diffuse reflectance spectroscopy and IR spectroscopy

Furthermore, the optical band-gaps of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) were also measured by the UV–vis–NIR diffuse reflectance spectra and they were converted into the absorption based on Kubelka–Munk Equation: $F(R) = K/S = (1 - R)^2/2R$ [45]. As shown in Fig. 5, the optical band gaps of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) are 4.32 eV, 3.68 eV, 4.20

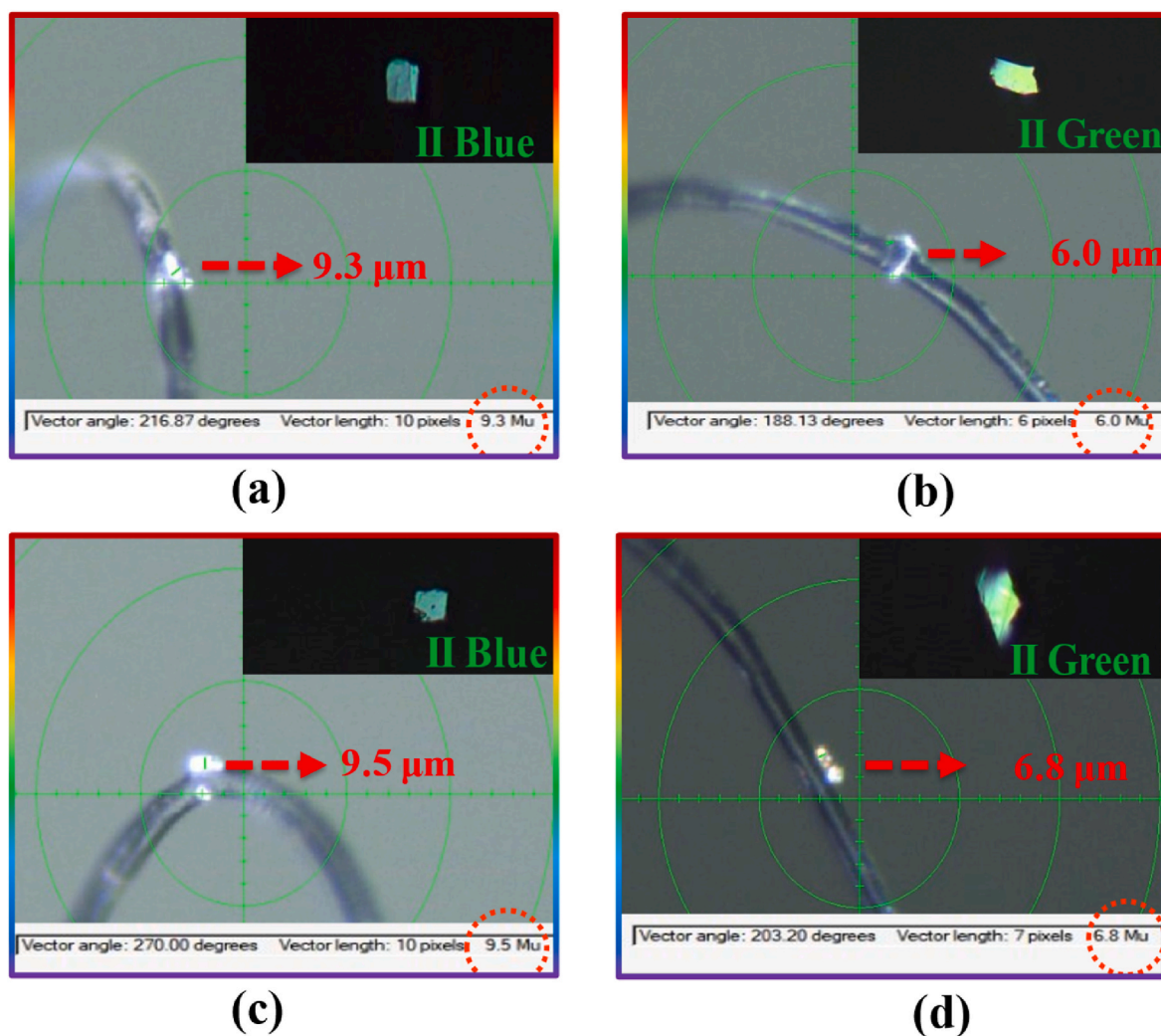


Fig. 4. The photographs of crystal size and their interference colors observed in the cross-polarized light for (a) $\text{BaGe}_2\text{O}_4\text{S}$ (b) $\text{BaGe}_2\text{O}_4\text{Se}$ (c) $\text{SrGe}_2\text{O}_4\text{S}$ and (d) $\text{SrGe}_2\text{O}_4\text{Se}$.

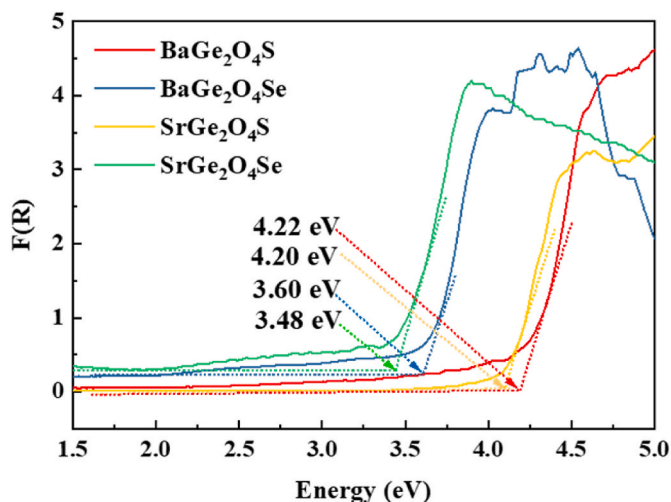


Fig. 5. UV-vis-NIR optical absorption spectra of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$).

eV and 3.48 eV, respectively, which are larger than single-anionic classical chalcogenide compounds, such as AgGaS_2 (2.56 eV) [46], AgGaSe_2 (1.83 eV) [47], and can be comparable to some oxide-based crystals, such as $\text{Sr}_2\text{CdGe}_2\text{O}_7$ (2.89 eV) [48], $\text{NaCa}_4\text{V}_5\text{O}_{17}$ (2.74 eV) [49], $\text{Li}_2\text{K}_4\text{TiOGe}_4\text{O}_{12}$ (4.43 eV) [50], etc. Meanwhile, in order to evaluate the IR transmission of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$), their IR spectra were also measured (Fig. S2). That shows that there are no distinct absorption

peaks existing in the range from 4000 to 1050 cm^{-1} , corresponding to wide transmission range from 2.5 μm to 9.5 μm . Therefore, $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$) would be potential as mid-IR optical materials. Then, there are three absorption peaks ($\approx 1050, 700$ and 500 cm^{-1}) observed in their respective IR spectra, which can be attributed to the Ge-O and Ge-S/Se stretching mode [51,52]. All of these assignments are consistent with those of other compounds containing Ge-S/Se and Ge-O groups, such as GeO_2 [53], GeS_2 [54], $\text{Ae}_3\text{Q}[\text{GeOQ}_3]$ ($\text{Ae} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$) [51], etc.

3.5. Raman spectroscopy

To deeply analyze the specific absorption spectra of different units, the Raman spectra of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$) were measured using the micron-sized crystals. As shown in Fig. S3, the strong absorption peaks in the range of 874–472 cm^{-1} can be attributed to the characteristic vibrations of the Ge-O-Ge bonds, while the peaks in the range of 377–260 cm^{-1} are for the Ge-S/Se bonds. The appearance of these vibrational peaks also shows that there are Ge-O or Ge-S/Se bonds in the compounds of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$). Besides, these absorption peaks below 200 cm^{-1} might be related to the vibrations of Ba/Sr-S or Ba/Sr-Se bonds, respectively [55–57].

3.6. Theoretical calculations

The electronic band structures of $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$) were calculated by the DFT as shown in Fig. S4. For $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}$; $\text{Q} = \text{S}, \text{Se}$), the top of the valence band (VB) and the bottom of the conduction band (CB) are located at the same G-point, describing the

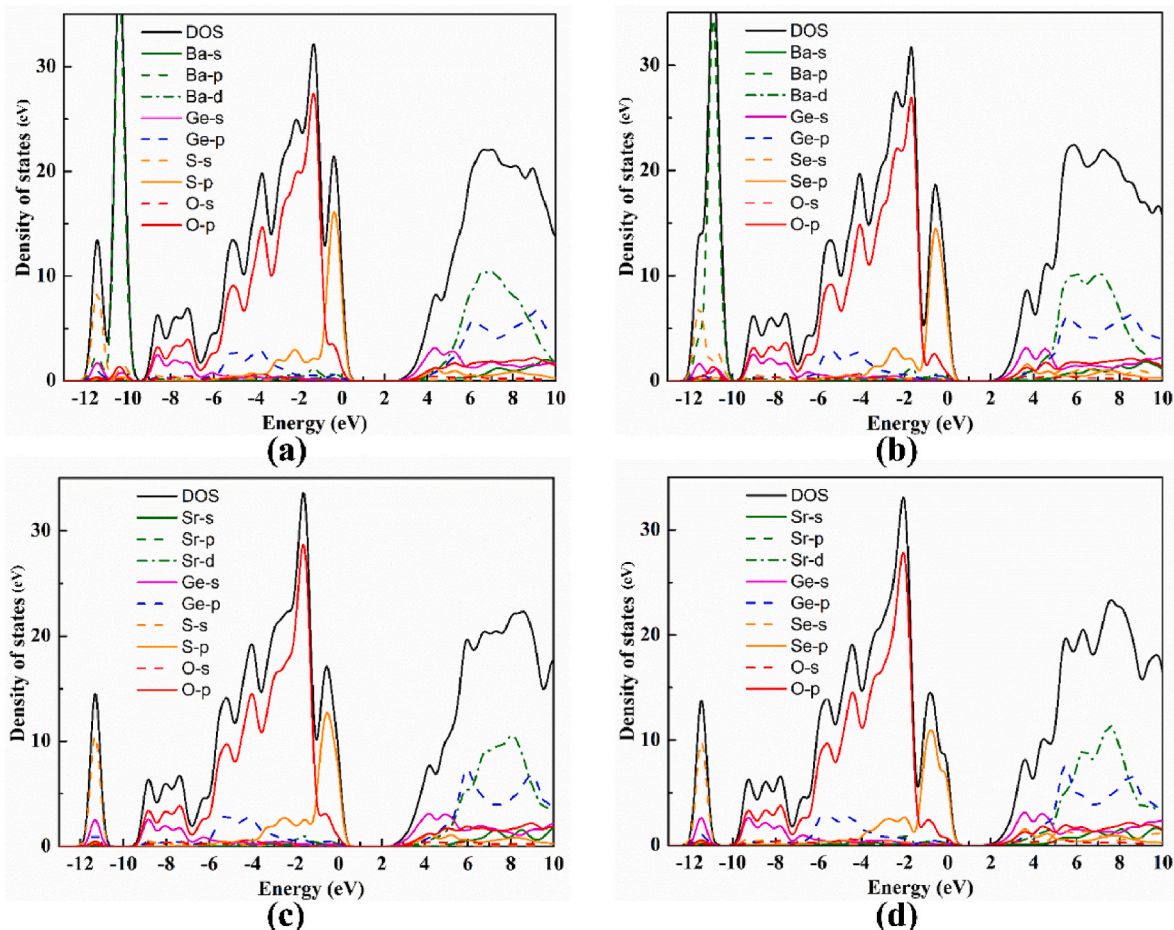


Fig. 6. Calculated total and partial DOS for (a) $\text{BaGe}_2\text{O}_4\text{S}$, (b) $\text{BaGe}_2\text{O}_4\text{Se}$, (c) $\text{SrGe}_2\text{O}_4\text{S}$, and (d) $\text{SrGe}_2\text{O}_4\text{Se}$.

indirect bandgaps of 2.83 eV for BaGe₂O₄S, 2.33 eV for BaGe₂O₄Se, 2.60 eV for SrGe₂O₄S and 2.13 eV for SrGe₂O₄Se, respectively. Clearly, these band-gaps are underestimated by the GGA as the exchange–correlation functional [40]. Four compounds also exhibit the similar density of states (DOS) and partial density of states (PDOS) (Fig. 6). The Ge 4s, 4p, S/Se 3p, and O 2p orbitals construct the top region of valence states from −9.6 to 0 eV. Their wide hybridization in this area indicates that Ge–O and Ge–S/Se bonds make the main contribution of the upper side of the valence band. The bottom region of conduction states mainly is composed of 4s, 4p states of Ge, 3p state of S/Se, and 2p state of O. Thus, [GeO₃S/Se] and [GeO₄] tetrahedra have the significant effect on its optical properties, which determine the birefringent of AGe₂O₄Q (A = Ba, Sr; Q = S, Se).

The refractive indices of AGe₂O₄Q (A = Ba, Sr; Q = S, Se) and BaGe₂O₅ were also calculated by DFT. As shown in Fig. 7, the calculated birefringence values for BaGe₂O₄S, BaGe₂O₄Se, SrGe₂O₄S and SrGe₂O₄Se at 1064 nm are 0.13, 0.16, 0.15 and 0.19, respectively, while the birefringence of BaGe₂O₅ is only 0.03 at 1064 nm. Therefore, it is clear that the birefringence of compounds is indeed largely enhanced from single-anionic compounds to heteroanionic compounds. The birefringence values of AGe₂O₄Q (A = Ba, Sr; Q = S, Se) are comparable to those of the commercialized birefringent crystals, such as α-BaB₂O₄ (Δ*n* = 0.116 at 1064 nm) [58], YVO₄ (Δ*n* = 0.225 at 1064 nm) [7] and CaCO₃ (Δ*n* = 0.171 at 633 nm) [10]. So, they are potentials as IR birefringent crystals.

3.7. The dipole moment calculations

As is well known, the anisotropic polarization of the structure is the main cause of material birefringence [59]. Due to the fact that alkaline cations typically exhibit spherically symmetric coordination, their contribution to birefringence can be negligible. The birefringence is mainly determined by the highly asymmetric anion groups [60]. In order to further understand the relationship between the structure and birefringence, the anisotropy of anion groups can be quantified by calculating their dipole moments. As described above, the dipole moments of the anion groups, the [GeO₆] polyhedra and [GeO₄] tetrahedra in BaGe₂O₅, and the [GeO₄] and [GeO₃Q] tetrahedra in BaGe₂O₄Q, are calculated according to the bond valences method [42]. As shown in Table 2, the dipole moments from the [GeO₆] polyhedra and [GeO₄] tetrahedra in BaGe₂O₅ are very small (μ = 2.99 and 0.44 Debye (D), respectively). However, in BaGe₂O₄Q, the heteroanions [GeO₃Q] (Q = S,

Table 2

Comparison of dipole moments for GeO₃S/Se mixed-anion units and GeO₄ and GeO₆ single-anionic units.

Compounds	Polyhedra	Magnitude (D)	Δ <i>n</i> (at 1064 nm)
BaGe ₂ O ₅	GeO ₆	2.99	0.03
	GeO ₄	0.44	
BaGe ₂ O ₄ S	GeO ₃ S	7.25	0.13
	GeO ₄	4.16	
BaGe ₂ O ₄ Se	GeO ₃ Se	14.11	0.16
	GeO ₄	4.64	
SrGe ₂ O ₄ S	GeO ₃ S	5.50	0.15
	GeO ₄	4.58	
SrGe ₂ O ₄ Se	GeO ₃ Se	11.32	0.19
	GeO ₄	4.76	

Se) and [GeO₄] units have larger dipole moments, 5.5–14.11 D and 4.16–4.76 D, respectively. Generally, the larger dipole moments can generate the larger birefringence [61–63]. Therefore, the calculations of dipole moments are also consistent with their birefringence magnitudes.

4. Conclusion

In summary, four new heteroanionic oxychalcogenides, AGe₂O₄Q (A = Ba, Sr; Q = S, Se), have been synthesized by the solid-state reaction. They all contain 2D heteroanionic [Ge₂O₄Q] layers. Compared with the single-anionic BaGe₂O₅, the octahedral [GeO₆] units are changed to tetrahedral [GeO₃Q] units. And owing to the larger polarization anisotropy of [GeO₄] and [GeO₃Q] units, AGe₂O₄Q (A = Ba, Sr; Q = S, Se) all exhibit relatively large birefringence, 0.13, 0.16, 0.15 and 0.19 at 1064 nm, for BaGe₂O₄S, BaGe₂O₄Se, SrGe₂O₄S and SrGe₂O₄Se respectively. These birefringence values are one-order magnitude larger than their single-anionic germanate, BaGe₂O₅ (0.03 @ 1064 nm). It indicates that constructing heteroanionic oxychalcogenides is a feasible strategy for enhancing the birefringence of materials. In addition, AGe₂O₄Q (A = Ba, Sr; Q = S, Se) all exhibit large *E_g* (3.48–4.32 eV) and wide the IR transparent region (2.5–9.5 μm). Therefore, AGe₂O₄Q (A = Ba, Sr; Q = S, Se) may be potential as IR birefringent crystals.

Accession codes

CCDC 2279313–2279316 contain the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +44 1223 336033.

CRediT authorship contribution statement

Dong Gao: Conceptualization, Methodology, Writing - original draft, preparation. **Fuqiang Chen:** Data curation, Investigation. **Hongping Wu:** Formal analysis. **Zhanggui Hu:** Project administration. **Jiyang Wang:** Validation. **Yicheng Wu:** Funding acquisition. **Hongwei Yu:** Supervision. **P Shiv Halasyamani:** Writing - review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

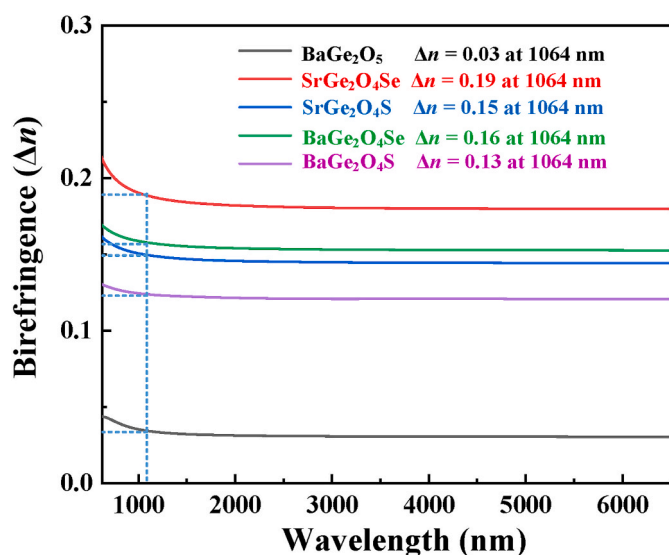


Fig. 7. Dispersion of birefringence (Δ*n*) of BaGe₂O₄S, BaGe₂O₄Se, SrGe₂O₄S, SrGe₂O₄Se and BaGe₂O₅.

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Supporting information

Atomic coordinates, equivalent isotropic displacement parameters, bond valence sum, table of bond lengths and angles, the IR and Raman spectra for $\text{AGe}_2\text{O}_4\text{Q}$ ($\text{A} = \text{Ba}, \text{Sr}; \text{Q} = \text{S}, \text{Se}$) and calculated band structures.

Appendix A. Supplementary data

Supplementary data to this article can be found online at.

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