

# PAH101: A *GW*+BSE Dataset of 101 Polycyclic Aromatic Hydrocarbon (PAH) Molecular Crystals

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## ABSTRACT

The excited-state properties of molecular crystals are important for applications in organic electronic devices. The *GW* approximation and Bethe-Salpeter equation (*GW*+BSE) is the state-of-the-art method for calculating the excited-state properties of crystalline solids with periodic boundary conditions. We present the PAH101 dataset of *GW*+BSE calculations for 101 molecular crystals of polycyclic aromatic hydrocarbons (PAHs) with up to  $\sim$ 500 atoms in the unit cell. The data records include the *GW* quasiparticle band structure, the fundamental band gap, the static dielectric constant, the first singlet exciton energy (optical gap), the first triplet exciton energy, the dielectric function, and optical absorption spectra for light polarized along the three lattice vectors. We envision the dataset being used to (i) identify correlations between DFT and *GW*+BSE quantities, (ii) discover materials with desired electronic/ optical properties in the dataset itself, and (iii) train machine learned models to help in materials discovery efforts. We provide examples to illustrate these three use cases.

## Background & Summary

Computational materials design and discovery requires exploring the infinitely vast chemical space using quantum mechanical methods that can reliably predict the electronic and optical properties of candidate materials. The computational cost of quantum mechanical simulations increases rapidly with the method accuracy and system size. This limits the scope of simulations that can be performed within a reasonable time in terms of the number of systems explored, their size, the accuracy of the predicted properties, and the types of phenomena that can be investigated.<sup>1–7</sup>

Density functional theory (DFT) is the workhorse of first-principles simulations.<sup>8</sup> DFT relies on approximate exchange-correlation functionals to describe the many-body quantum mechanical interactions between electrons. Computationally efficient semi-local functionals have been used extensively for high-throughput materials screening.<sup>9–18</sup> However, DFT is a ground-state theory, therefore it is inherently unable to describe excited-state properties of interest, such as fundamental band gaps, singlet and triplet excitation energies, optical gaps (*i.e.*, the first singlet excitation energy), and optical absorption spectra. The excited states of isolated molecules may be calculated relatively efficiently with time dependent DFT (TDDFT).<sup>19–23</sup> The excited states of crystalline systems may be calculated using Green's function based many-body perturbation theory (MBPT) within the *GW* approximation and Bethe-Salpeter equation (BSE)<sup>24–28</sup>, which lends itself more easily than TDDFT to periodic implementations. Unfortunately, the high computational cost of *GW*+BSE simulations makes it unfeasible to use these methods for large scale materials exploration.

Machine learning (ML) may accelerate computational materials discovery by bypassing the need to perform expensive first-principles simulations.<sup>29–39</sup> To this end, statistical models are constructed based on training data to make predictions for new data points. Training ML models, especially deep neural networks (DNN), typically requires huge datasets. Therefore, data acquisition is often the bottleneck of applying ML to computational materials discovery. With the supercomputing resources available nowadays, acquiring DFT training data with semi-local functionals is relatively fast. This has led to the proliferation of DFT datasets.<sup>39,40–47</sup> As a result, ML models have been trained predominantly on semi-local DFT data, which limits their applicability to structural and ground state properties. Owing to the high computational cost of *GW*+BSE, such datasets are scarce and the amount of data they contain is relatively small compared to DFT datasets.<sup>46,48,49</sup> We note that the *GW* datasets

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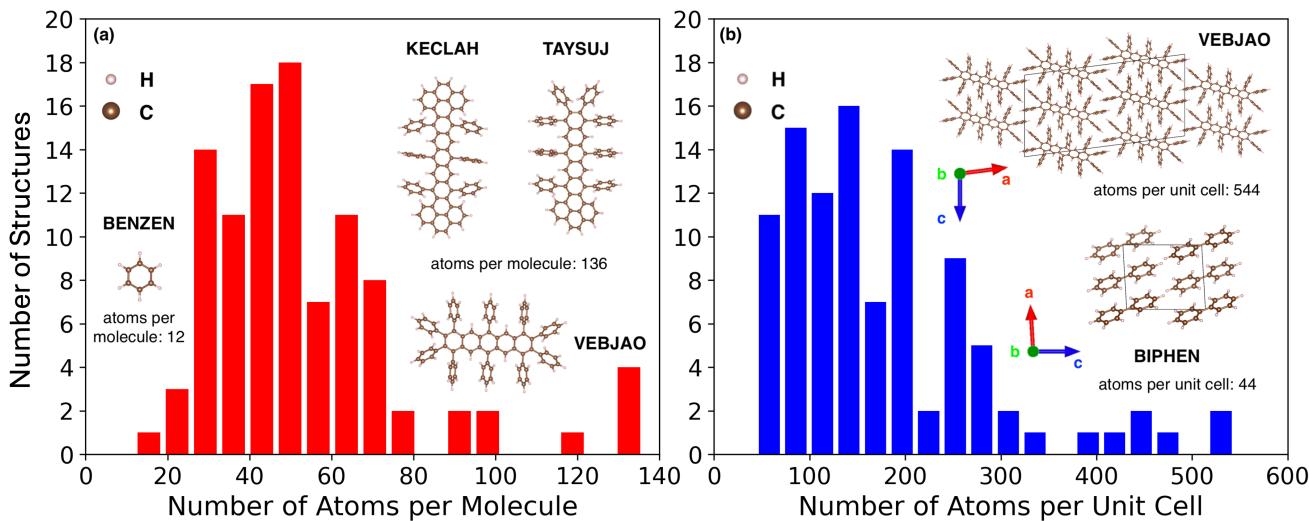
38 cited here comprise small isolated molecules, which are considerably faster to calculate than periodic molecular crystals with  
39 hundreds of atoms in the unit cell. Recently, ML has been applied to predict the  $GW$  quasiparticle energies of small molecules.<sup>50</sup>

40 It is challenging to construct transferable ML models based on “small data”. This has limited the applicability of ML to  
41 excited state properties of molecular crystals. Emerging approaches to ML with small data include multi-fidelity approaches.  
42 These methods combine a small amount of high-fidelity data with a large amount of low-fidelity data, which, although not as  
43 accurate, is sufficiently correlated with the high-fidelity data for statistical inference.<sup>51–60</sup> Recently, high-quality results have  
44 been achieved by fine-tuning a pre-trained DNN model with small datasets or combining feature selection with DNN.<sup>61,62</sup>  
45 Other approaches involve using low-fidelity features, selected based on physical/chemical knowledge, to construct surrogate  
46 models that are predictive of high-fidelity data. One such approach is the sure-independence-screening-and-sparsifying-operator  
47 (SISSO)<sup>63,64</sup> ML algorithm. The input of SISSO is a set of primary features, which are physical descriptors that could be  
48 correlated with the target property. SISSO generates a huge feature space by iteratively combining the primary features using  
49 linear and nonlinear algebraic operations. Subsequently, linear regression is performed to identify the most predictive models.  
50 Physical and chemical knowledge is leveraged in the choice of primary features and in the rules for combining them. SISSO  
51 has been demonstrated to work well with a relatively small amount of data for several different types of materials systems and  
52 properties.<sup>13,65–83</sup>

53 One application that requires predicting the excited-state properties of molecular crystals is singlet fission (SF), the  
54 conversion of one singlet exciton into two triplet excitons.<sup>84–87</sup> The efficiency of solar cells can be boosted by augmenting  
55 traditional absorbers with SF materials.<sup>88–90</sup> The SF material can convert photons with energies high above the traditional  
56 absorber’s band gap into two charge carriers instead of losing their excess energy to heat. Currently, few classes of materials  
57 are known to undergo intermolecular SF in the solid state, and insufficient stability under operating conditions precludes their  
58 utilization in commercial modules.<sup>84,85,91,92</sup> Therefore, there is a need for computational discovery of new SF materials. The  
59 primary criterion for a material to undergo SF is the thermodynamic driving force, *i.e.*, the difference between the singlet  
60 exciton energy and twice the triplet exciton energy,  $E_S - 2E_T$ , which can be calculated using  $GW+BSE$ .<sup>93–97</sup>

61 Recently, we have used SISSO to find models based on low-cost DFT properties that can reliably predict the  $GW+BSE$  SF  
62 driving force.<sup>98</sup> SISSO generated several models that predicted the  $GW+BSE$  SF driving force with errors below 0.2 eV. Based  
63 on considerations of accuracy and computational cost, two SISSO models were selected to build a two-step hierarchical classifier  
64 for screening promising candidates for SF. To train SISSO, we generated a dataset of  $GW+BSE$  calculations of the SF driving  
65 force of 101 molecular crystals of polycyclic aromatic hydrocarbons (PAHs). PAHs are compounds comprising carbon and hydro-  
66 gen atoms and containing multiple aromatic rings. Most SF materials are PAHs. In addition to SF, PAHs and their functionalized  
67 derivatives have versatile applications in organic electronic devices.<sup>99–109</sup> To form the PAH101 set, crystal structures of unsubsti-  
68 tuted PAHs (containing only C and H atoms) were extracted from the Cambridge Structural Database (CSD)<sup>110</sup>. The PAH101 set  
69 contains several sub-classes including acenes, rylene, zethrenes, as well as various compounds that do not belong to any particu-  
70 lar family. As shown in Figure 1, the PAH101 set contains molecules ranging in size from 12 atoms in benzene (CSD Reference:  
71 BENZEN) to 136 atoms in two pyrene-stabilized acenes 9,11,13,22,24,26-Hexaphenyltetrabenz[*de,rs,wx,k<sub>1</sub>l<sub>1</sub>*]nonacene  
72 (CSD Reference: KECLAH), 9,11,13,14,15,16,18,20-Octaphenyldibenzo[*de,c<sub>1</sub>d<sub>1</sub>*]heptacene (CSD Reference: TAYSUJ), and a  
73 phenylated pentacene 1,2,3,4,6,8,9,10,11,13-Decaphenylpentacene (CSD Reference: VEBJAO). The crystal size in the PAH101  
74 set ranges from 44 atoms in the unit cell for biphenyl (CSD Reference: BIPHEN) to 544 atoms in 1,2,3,4,6,8,9,10,11,13-  
75 Decaphenylpentacene (CSD Reference: VEBJAO).

76 The PAH101 dataset contains  $GW+BSE$  results for the electronic and optical properties of molecular crystals, as well as  
77 the DFT-level SISSO primary features used in Ref.<sup>98</sup>. We envision this dataset being used for computational discovery of  
78 crystalline organic semiconductors and chromophores with desired properties for applications in various organic electronic  
79 devices. For example, the dataset contains information on optical gaps and absorption spectra, which could be used to search  
80 for chromophores that absorb light in a certain energy range. In addition, the dataset contains singlet and triplet excitation  
81 energies, which can be used to evaluate candidate chromophores for triplet-triplet annihilation (TTA) and thermally activated  
82 delayed fluorescence (TADF). TTA chromophores can be used for harvesting photons with energies below the absorption  
83 threshold of a solar cell by up-conversion of two low-energy triplet excitons into one singlet exciton that can be absorbed.<sup>111,112</sup>  
84 TADF chromophores can be used to enhance the efficiency of OLEDs by converting electrically generated non-radiative triplet  
85 excitons into radiative singlet excitons.<sup>23,113,114</sup> The dataset also contains  $GW$  band structures. The band dispersion is related to  
86 transport in crystalline organic semiconductors, which affects the performance of organic electronic devices such as field effect  
87 transistors (OFETs).<sup>115</sup> Furthermore, this dataset can be used as a resource for comparing and benchmarking the performance  
88 of various electronic structure methods for calculating the electronic and optical properties of molecular crystals. Finally,  
89 this dataset can be used to augment other datasets, *e.g.*, DFT datasets for molecular crystals or TDDFT datasets for isolated  
90 molecules to train multi-fidelity ML models for predicting various electronic and optical properties of molecular crystals. In  
91 summary, because the PAH101 is a unique set of  $GW+BSE$  data for molecular crystals, we expect it to be a resource of great  
92 usefulness to the computational community.



**Figure 1.** Histograms of the number of atoms (a) in a single molecule and (b) in a crystal unit cell for the materials in the PAH101 set. Also shown are illustrations of the molecular structures of benzene (BENZEN), 9,11,13,22,24,26-Hexaphenyltetrabenzo[*de,rs,wx,k<sub>1</sub>l<sub>1</sub>*]nonacene (KECLAH), 9,11,13,14,15,16,18,20-Octaphenylbenzo[*de,c<sub>1</sub>d<sub>1</sub>*]heptacene (TAYSUJ), 1,2,3,4,6,8,9,10,11,13-Decaphenylpentacene (VEBJAO), and the crystal structures of 1,2,3,4,6,8,9,10,11,13-Decaphenylpentacene (VEBJAO) and Biphenyl (BIPHEN).

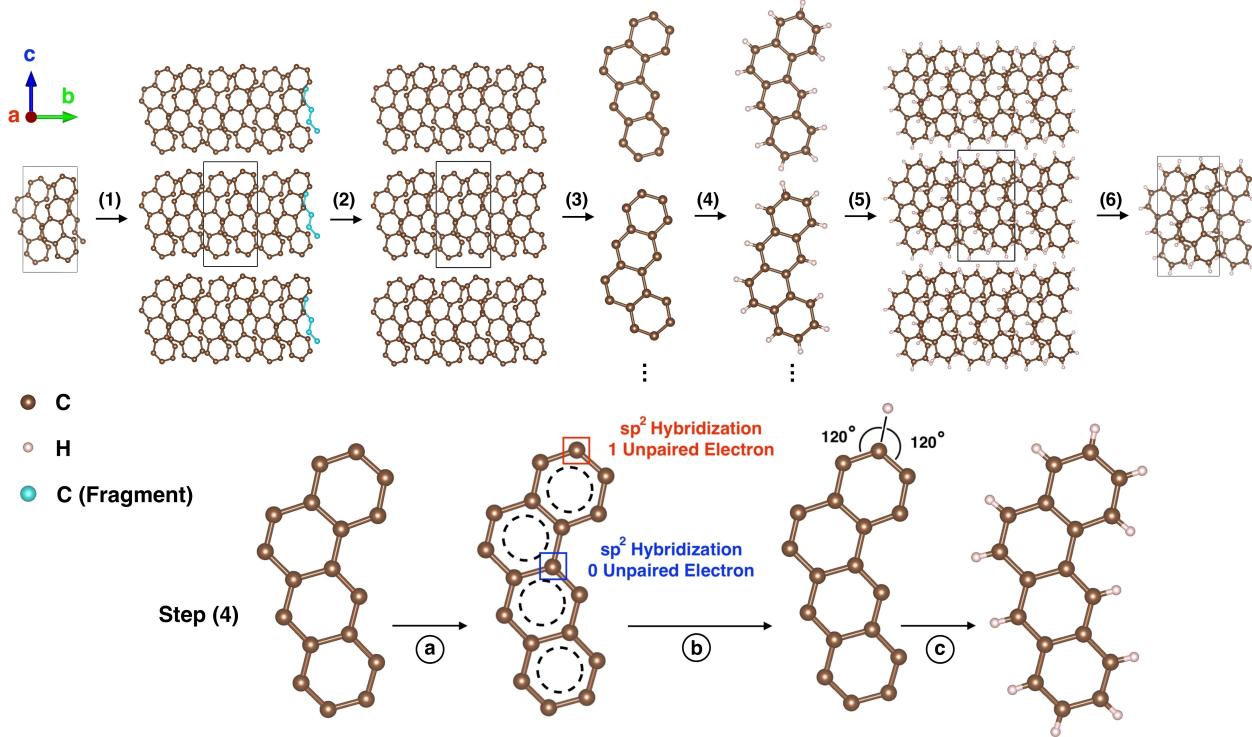
## 93 Methods

### 94 Hydrogen Addition

95 The starting geometries of the 101 molecular crystals were extracted from the Cambridge Structural Database (CSD).<sup>110</sup>  
 96 The CSD reference codes for each material are available in the data records. Some of the CIF files in the CSD are  
 97 missing the hydrogen atom positions, which cannot be determined by X-ray diffraction. To provide an approximate position  
 98 for each missing H atom, we have developed the Hydrogen Append (HAppend) code, available in the GitHub repo:  
 99 <https://github.com/BLABABA/HAppend>. HAppend is written in Python and uses RDKit<sup>116</sup> and Pymatgen<sup>117</sup>. The workflow  
 100 of HAppend is illustrated in Figure 2 using BEANTR as an example. All H atoms were removed from the CIF file for the  
 101 purpose of demonstration. HAppend does not use the symmetry information provided in the CIF file. In step (1) the unit cell is  
 102 replicated to build a super-cell so that any molecular fragments inside the unit cell can be completed. In step (2) all the complete  
 103 molecules and molecular fragments are identified. Subsequently, any broken fragments at the supercell boundary (colored in  
 104 blue in Figure 2) are removed. In step (3) all the complete molecules are extracted. Only two molecules are shown in Figure  
 105 2 for demonstration purposes. Step (4) is identifying the missing hydrogen sites and appending H atoms to each molecule.  
 106 A detailed schematic of step (4) is shown in the bottom row of Figure 2. In step 4a the missing hydrogen sites are identified  
 107 by checking the type of hybridization of each carbon atom against the number of valence electrons participating in covalent  
 108 bonds. In this example, all C atoms in the aromatic rings have  $sp^2$  hybridization. In step 4b H atoms are attached to atoms with  
 109 unpaired valence electrons. The bond length and angle are determined based on the bonded neighbors and hybridization type.  
 110 In this example, given that the C atom is  $sp^2$  hybridized, the two H-C-C angles should be about  $120^\circ$ . This process is performed  
 111 for all atoms in the BEANTR molecule and the completed molecule is obtained after step 4c. Step (5) reconstructs the complete  
 112 super-cell with appended H atoms. Step (6) reduces the super-cell back to the original unit cell with all the coordinates for  
 113 the missing H atoms now known. Finally, sanity checks are performed to verify that the structure is correct. The structure is  
 114 checked against the expected chemical formula (if provided in the CIF file from the CSD). In addition, RDKit is used to repeat  
 115 step 4b and confirm that the explicit valence matches with the type of hybridization for each atom. If the sanity check fails, the  
 116 user may have to attach H atoms manually. HAppend is not limited to PAHs and may be used to add missing H atoms to other  
 117 types of organic molecules.

### 118 Structural Relaxation

119 Full unit cell relaxation was performed with either CASTEP<sup>118</sup> or FHI-aims<sup>119,120</sup> (which code was used is reported in the data  
 120 records). The Perdew, Burke, and Ernzerhof (PBE) exchange-correlation functional<sup>121</sup> was used with the Tkatchenko-Scheffler  
 121 (TS) pairwise dispersion method<sup>122</sup>. For relaxations performed with CASTEP, norm-conserving pseudopotentials were utilized



**Figure 2.** Schematic illustration of the workflow of adding missing H atoms with HAppend, demonstrated for the BEANTR crystal. The top row shows the steps of (1) super-cell construction, (2) removal of broken molecular fragments (colored in blue), (3) extraction of molecules, (4) addition of H atoms to all molecules, (5) reconstruction of the supercell with the H atoms attached to all molecules, and (6) reduction of the supercell to a single unit cell. For Steps (3) and (4) only two molecules are shown for clarity. The bottom row presents a detailed view of the hydrogen addition step: (a) identification of missing H sites, (b) calculation of approximate H atom positions, and (c) attachment of H atoms to the molecule.

for carbon and hydrogen. The plane-wave basis set cutoff was 750 eV. A Monkhorst-Pack k-grid with a spacing of  $0.07 \text{ \AA}^{-1}$  was adopted. The convergence thresholds for total energy, maximum force, maximum stress, and maximum displacement were  $5 \times 10^{-6} \text{ eV/atom}$ ,  $0.01 \text{ eV/\AA}$ ,  $0.02 \text{ GPa}$ , and  $5 \times 10^{-4} \text{ \AA}^{-1}$ , respectively. For structures relaxed with FHI-aims, the tight numerical settings and tier-2 basis sets were used. The fully relaxed crystal structures and the molecular geometries extracted from them are provided in the data records. The GW+BSE calculations were performed for the fully relaxed crystal structures.

## 127 DFT Features

128 The data records include the DFT primary features used for SISSO in Ref.<sup>98</sup>. The DFT features of molecules and crystals were  
 129 calculated using FHI-aims<sup>119,120</sup>. From considerations of computational efficiency, the DFT primary features were calculated  
 130 with locally-optimized geometries. The crystal structures were relaxed with the lattice vectors fixed at the experimental values  
 131 and the single molecule properties were calculated using molecules extracted from these locally-optimized crystal structures.  
 132 All primary features were calculated with the PBE functional.<sup>121</sup> using the tight numerical setting and tier-2 basis sets of  
 133 FHI-aims.<sup>119</sup>

## 134 Mean-Field Wave Function Calculation

135 The Quantum ESPRESSO package<sup>123</sup> was used to compute the DFT eigenvectors and eigenvalues, which served as the starting  
 136 point for non-self-consistent GW+BSE calculations, using the PBE functional. Norm-conserving pseudopotentials were  
 137 chosen in order to take advantage of the simplification of matrix elements in GW+BSE calculations.<sup>124</sup> Troullier-Martins  
 138 norm-conserving pseudopotentials were generated using FHI98PP-converted with fhi2upf.x v.5.0.2 from [Abinit Project](#). The  
 139 kinetic energy cutoff was 50 Ry. The k-point grids used for each material are reported in the data records.

## 140 GW+BSE Calculations

141 The BerkeleyGW package<sup>124</sup> was used to perform GW+BSE calculations. From considerations of computational cost, non-  
 142 self-consistent  $G_0W_0$  calculation were performed. 550 unoccupied states were included in the dielectric function and the

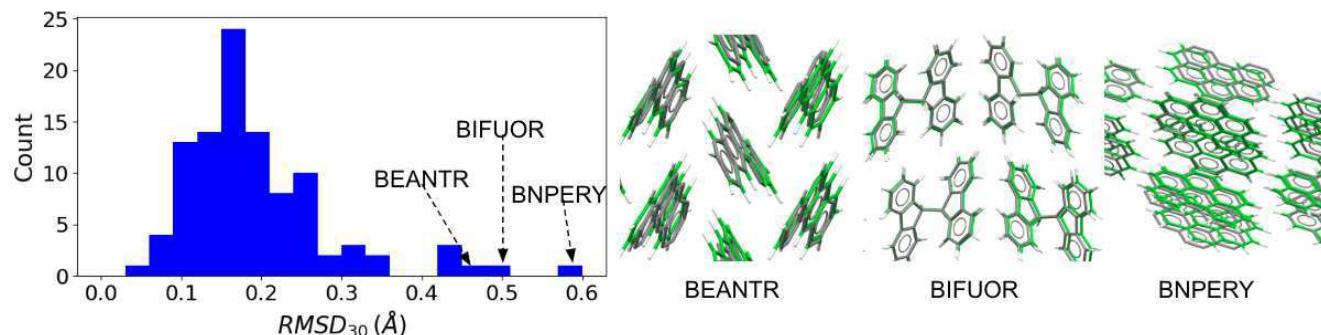
143 self-energy operator evaluations. The static remainder correction was applied to accelerate the convergence. The screened  
 144 and bare Coulomb interaction cutoffs were 10 Ry and 40, respectively. The Bethe-Salpeter equation was solved within  
 145 the Tamm-Dancoff approximation (TDA) with 24 valence bands and 24 conduction bands included. The fine k-point grid  
 146 wave-functions were generated using a fine k-point grid twice as dense as the coarse k-point grid. The coarse and fine k-point  
 147 grid settings for each material are reported in the data records.

## 148 Data Records

149 The PAH101 dataset is available via the NOvel MAterials Discovery (NOMAD) repository<sup>125</sup> and can be accessed at  
 150 DOI: [10.17172/NOMAD/2024.12.05-1](https://doi.org/10.17172/NOMAD/2024.12.05-1). The data are provided in YAML (.yaml) format. Each file is named as *CSD-REFERENCE.archive.yaml*, where *CSD-REFERENCE* is the CSD reference code for each structure. The data structure for  
 151 each material record is described in Table 1. The top level sections are *struct\_id*, *geometry*, *dft*, and *gwbse*. The *struct\_id*  
 152 section contains the CSD reference code. The *geometry* section provides the fully relaxed crystal structure and the single  
 153 molecule geometry extracted from it. The *dft* section contains all the SISSO primary features used in Ref.<sup>98</sup>. The *gwbse* section  
 154 provides quasi-particle (QP) and excitonic properties for the PAH101 crystals, including the fundamental gap, quasiparticle  
 155 band structure, the static dielectric constant, the first singlet exciton energy (optical gap), the first triplet exciton energy, the full  
 156 dielectric function, and optical absorption spectra for light polarized along the three lattice vectors. The GW static dielectric  
 157 constant is not available for some of the materials in the dataset because some data that was not needed for Ref.<sup>98</sup> was not  
 158 preserved.

## 160 Technical Validation

### 161 Crystal Structures



**Figure 3.** Histogram of the  $RMSD_{30}$  of crystal structures relaxed with PBE+TS compared to the experimental structures from the CSD for the PAH101 set. The similarity overlay plots generated by Mercury are shown for BNPERY, BIFUOR, and BEANTR with the experimental structures colored in gray, and the relaxed structures colored in green.

162 To verify the results of full unit cell relaxation with PBE+TS, the root-mean square distance (RMSD) between the relaxed  
 163 structures and the experimental structures was calculated. We used the COMPACK<sup>129</sup> molecular overlay method, implemented  
 164 as the Crystal Packing Similarity tool, in Mercury 2023.2.0<sup>130</sup>. COMPACK overlays clusters of molecules taken from each  
 165 crystal, within given distance and angle tolerances, and minimizes the RMSD between atoms, typically excluding hydrogen.  
 166 The output of COMPACK is the number of molecules that could be overlaid and the RMSD. COMPACK comparisons were  
 167 performed with a cluster of 30 molecules and distance and angle tolerances of 35% and 35°. H atoms were not included.  
 168 These were the settings used for structure comparison in the 7<sup>th</sup> crystal structure prediction blind test<sup>131,132</sup>. Figure 3 shows a  
 169 histogram of the RMSD obtained for the PAH101 set. For the majority of the structures in the dataset the RMSD is below 0.3  
 170 Å. The three structures with the largest RMSDs are BNPERY, BIFUOR, and BEANTR. All three are monoclinic structures  
 171 with larger than average deviations in their *b* lattice parameter and  $\beta$  angle. For instance, the relaxed *b* parameter of BEANTR  
 172 is 6.00 Å, compared to 6.50 Å in the experimental structure, a deviation of 7.7 %. The relaxed structure of BNPERY has a  $\beta$   
 173 angle of 92.2°, compared to 98.5° in the experimental structure. Some differences between structures relaxed by DFT at 0K and  
 174 structures experimentally characterized at room temperature are to be expected.<sup>133</sup> Overall, the performance of PBE+TS is  
 175 within the community accepted standards of agreement with experiment, as established in the crystal structure prediction blind  
 176 tests.<sup>131,132</sup> It is possible that performing relaxations with the more accurate many-body dispersion (MBD)<sup>128</sup> method would  
 177 reduce the RMSD.

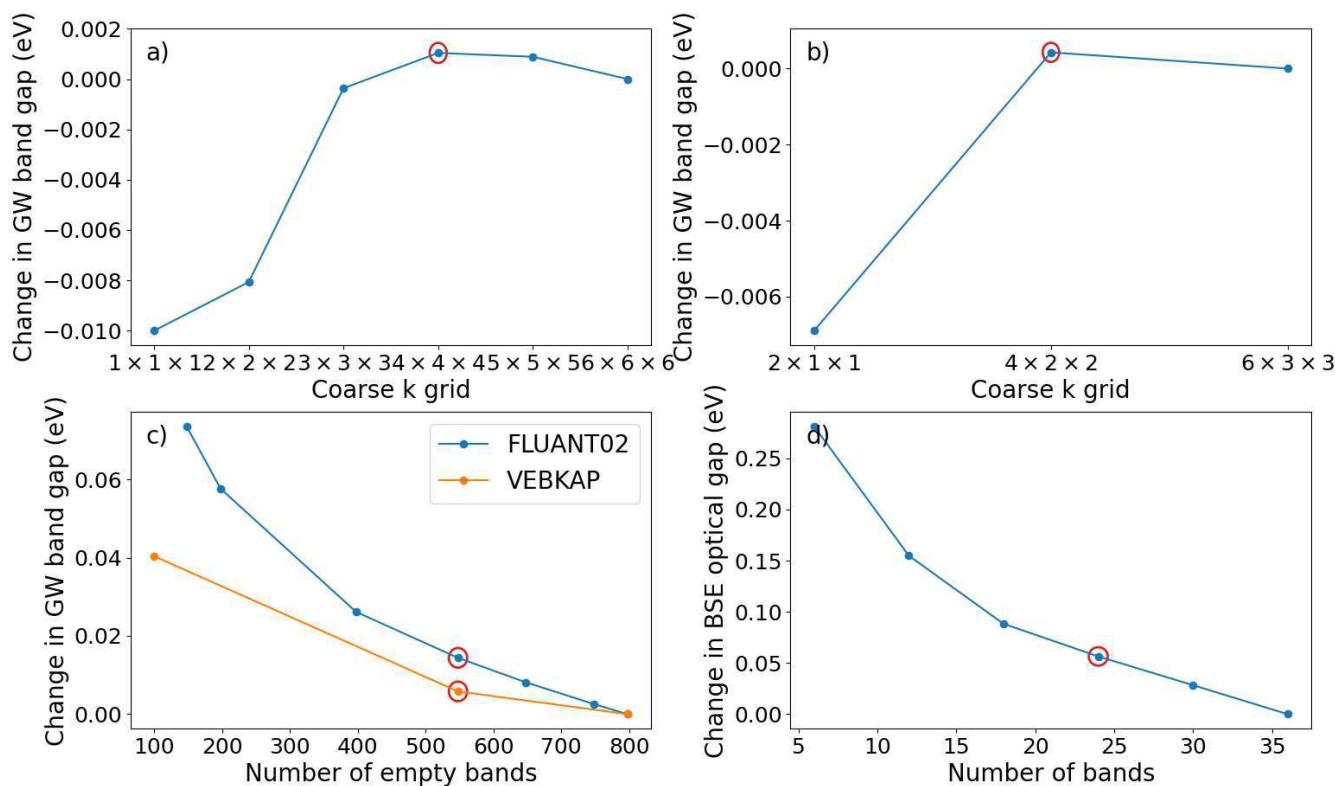
<i>struct_id</i>	the CSD reference code for this structure		
<i>geometry</i>	<i>relaxed_crystal</i>	the DFT-relaxed crystal structure saved in Pymatgen Structure format	
	<i>molecule</i>	the single molecule geometry extracted from <i>relaxed_crystal</i> , saved in Pymatgen Molecule format	
	<i>chemical_formula</i>	chemical formula of the single molecule	
	<i>relax_code</i>	code used to perform crystal structure relaxation	
<i>dft</i>	<i>gap_s</i>	the single molecule gap, calculated based on the energy difference between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO)	
	<i>Et_s</i>	the single molecule triplet formation energy, calculated based on the total energy difference between the ground-state and triplet-state molecule	
	<i>DF_s</i>	the single molecule DFT estimate for the SF driving force, calculated by taking the difference between <i>gap_s</i> and twice <i>Et_s</i>	
	<i>IP_s</i>	the single molecule ionization potential (IP), calculated based on the total energy difference between a cation and neutral molecule	
	<i>EA_s</i>	the single molecule electron affinity (EA), calculated based on the total energy difference between an anion and neutral molecule	
	<i>bandgap</i>	the crystal band gap	
	<i>Et</i>	the crystal triplet formation energy, calculated based on the total energy difference between the ground-state and triplet-state crystal	
	<i>DF</i>	the crystal DFT estimate for the SF driving force, calculated by taking the difference between <i>bandgap</i> and twice <i>Et</i>	
	<i>VBindisp</i>	the valence band dispersion, <i>i.e.</i> , the energy range of the HOMO-derived band	
	<i>CBdisp</i>	the conduction band dispersion, <i>i.e.</i> , the energy range of the LUMO-derived band	
	<i>h<sub>ab</sub></i>	the transfer integral, calculated with fragment orbital DFT <sup>126</sup>	
	<i>polarization</i>	the trace of the polarization tensor for a single molecule, calculated with DFT using the PBE functional and the range-separated self-consistently screened version of many-body dispersion (MBD@rsSCS) method <sup>127, 128</sup>	
	<i>epsilon_mbd</i>	the dielectric constant calculated with PBE+MBD@rsSCS	
	<i>weight_s</i>	the molecular weight in atomic mass units (amu)	
	<i>density</i>	the crystal density in amu Å <sup>-3</sup>	
<i>gwbse</i>	<i>absorption</i>	<i>a</i>	Optical absorption spectrum for light polarized along the a, b, and c crystal axes. Each absorption data record contains four columns: energy (eV), the imaginary and real parts of the dielectric function $\epsilon_2$ and $\epsilon_1$ , and the normalized joint density of states.
		<i>b</i>	
		<i>c</i>	
	<i>bandstructure</i>	<i>kpoints</i>	the high-symmetry <i>k</i> -point path used to calculate the <i>GW</i> band structure
		<i>val</i>	the values of band structure, saved as $n \times 8$ matrix, whose columns are: spin, band index, <i>k</i> -point coordinate x, <i>k</i> -point coordinate y, <i>k</i> -point coordinate z, mean-field energy, quasi-particle energy, difference between mean-field and quasi-particle energy
	<i>bse_Es</i>	the singlet exciton energy (optical gap) calculated with BSE	
	<i>bse_Et</i>	the triplet exciton energy calculated with BSE	
	<i>bse_DF</i>	the SF driving force for a crystal, <i>bse_Es</i> - 2 × <i>bse_Et</i>	
	<i>kgrid_coarse</i>	the <i>k</i> -grid used for coarse grid wave-function calculation	
	<i>kgrid_fine</i>	the <i>k</i> -grid used for fine grid wave-function calculation	
	<i>fundamental_gap</i>	the fundamental gap calculated with <i>GW</i>	
	<i>bse_Es_bind</i>	the singlet-state exciton binding energy	
	<i>bse_Et_bind</i>	the triplet-state exciton binding energy	
	<i>epsilon_gw</i>	the dielectric constant calculated with <i>GW</i> ; N.A. entered if not available	

**Table 1.** Data records: Description of the data structure of the PAH101 set with explanations of all entries.

178 **GW+BSE Convergence**

179 The results of GW+BSE calculations with the BerkeleyGW code are sensitive to the convergence of several parameters<sup>49, 134, 135</sup>.  
 180 Because of the large number of calculations performed for the PAH101 set, we have chosen parameters that provide a balance  
 181 between accuracy and computational cost. The convergence of the settings used for the PAH101 dataset has been demonstrated  
 182 previously for selected systems<sup>93, 98</sup>. Figure 4 shows the convergence with respect to coarse *k*-point grid and the number of  
 183 empty bands used in the *GW* step for representative materials. The number of *k*-points is inversely proportional to the unit cell

size. Benzene has the smallest unit cell in the PAH101 set and therefore requires a relatively large number of k-points. 9,9'-bifluorenyl (CSD reference code BIFUOR) represents a system of intermediate size. For both materials, increasing the number of k-points beyond the chosen settings leads to a change of less than 0.001 eV in the GW band gap. For the representative materials fluoranthene (CSD reference code FLUANT02) and 6-phenylpentacene (CSD reference code VEBKAP), increasing the number of empty bands beyond 550 leads to a change of less than 0.02 eV in the GW band gap. For fluoranthene, increasing the number of valence and conduction bands used for the BSE step beyond 24 leads to a change of less than 0.06 eV in the optical gap. The settings used for the PAH101 set are sufficiently robust for "production" calculations. Notably, in the time that passed since the PAH101 set was generated, there have been advances in streamlining the convergence of MBPT calculations.<sup>136-139</sup> These have focused primarily on inorganic crystals with a few atoms in the unit cell. A workflow that converges the settings for each system individually would be too expensive for systems of the size of the PAH101 set. If a certain material is of particular interest, then more detailed calculations may be pursued with ultra-converged settings and/or more accurate methods than  $G_0W_0$ @PBE.



**Figure 4.** Convergence of GW+BSE calculations for representative materials. Change in the GW band gap as a function of the coarse k-point grid for (a) benzene and (b) 9,9'-bifluorenyl (CSD reference code BIFUOR). (c) Change in the GW band gap as a function of the number of empty bands for fluoranthene (CSD reference code FLUANT02) and 6-phenylpentacene (CSD reference code VEBKAP). (d) Change in the BSE optical gap as a function of the number of fine bands for fluoranthene. The chosen settings are circled in red.

## 196 Optical Absorption

197 The GW+BSE approach has been benchmarked extensively for isolated molecules, for which high-level quantum chemistry  
 198 reference data can be calculated.<sup>49, 140-144</sup> For molecular crystals no benchmark studies are available, owing to the difficulty  
 199 of obtaining reference data for large systems with periodic boundary conditions. Therefore, we are only able to validate the  
 200 results of GW+BSE by comparison to experiments. Table 2 shows a comparison of the GW+BSE optical gaps (singlet exciton  
 201 energies) to experimental values and GW+BSE values reported by others, where available. The GW+BSE values reported  
 202 here are within 0.2 eV or less of the values reported by others. The results of GW+BSE calculations can differ because of  
 203 differences in the implementation and convergence settings, as discussed extensively in Ref.<sup>49</sup> Because the absorption edge  
 204 is not abrupt, Tauc plots are typically used to extract the optical gap from absorption spectra.<sup>145-148</sup> This can lead to some  
 205 uncertainty in the experimental values. Here, if multiple experimental values are found for the same material, they are within

0.1 eV or less of each other in most cases. For the entries marked with \*, we used the Tauc method to extract the optical gap from the experimental data because no value for the optical gap was reported in the paper. For the entries marked with \*\*, there is a larger uncertainty in the optical gaps extracted using the Tauc method because the absorption edge does not decay to zero. In most cases, the GW+BSE optical gaps are within 0.2 eV or less from experimental values.

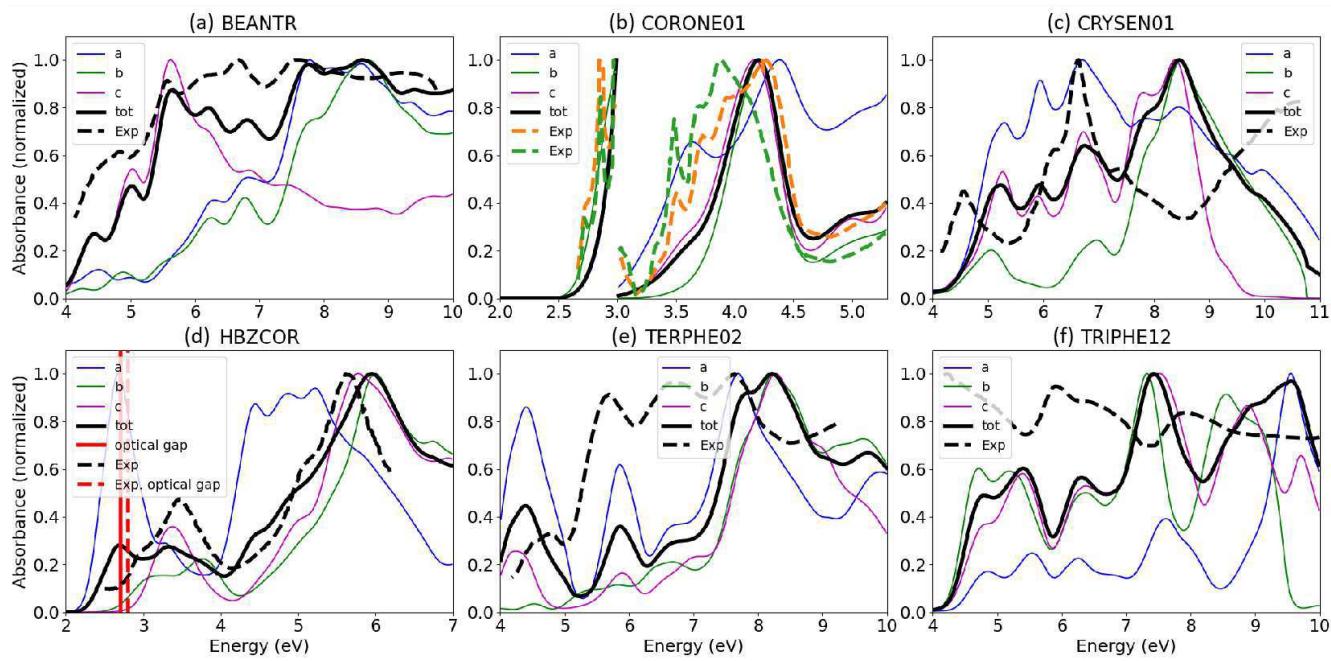
**Table 2.** Optical gaps obtained using  $GW+BSE$  ( $E_g^{GW+BSE}$ ) compared with experimental values ( $E_g^{Exp}$ ) and  $GW+BSE$  values reported by others ( $E_g^{GW+BSE}$  in Ref), where available. Entries marked with \* were extracted by us from absorption spectra using the Tauc method. Entries marked with \*\* have an absorption spectrum that is non-zero in the low-energy region, leading to a larger uncertainty in the optical gaps extracted using the Tauc method.

CSD Ref. Code	Compound Name	$E_g^{GW+BSE}$ (eV)	$E_g^{Exp}$ (eV)	$E_g^{GW+BSE}$ in Ref (eV)
BENZEN	Benzene	4.83	4.69-4.8 <sup>149</sup>	5.0 <sup>150</sup>
ANTCEN	Anthracene	3.22	3.16 <sup>151</sup>	3.3 <sup>150</sup>
TETCEN01	Tetracene	2.24	2.38 <sup>152, 153</sup>	2.4 <sup>150</sup>
PENCEN	Pentacene	1.72	1.8-1.85 <sup>154-156</sup>	1.7-1.8 <sup>150, 157, 158</sup>
ZZZDKE01	Hexacene	1.17	1.37*-1.4 <sup>159-161</sup>	1.0 <sup>150</sup>
QQQCIG04	Rubrene (Orthorhombic)	2.28	2.32 <sup>162</sup>	
QQQCIG13	Rubrene (Monoclinic)	2.62	2.36 <sup>163</sup>	
QQQCIG14	Rubrene (Triclinic)	2.30	2.31 <sup>163</sup>	
PERLEN05	Perylene (SHB)	2.61	2.58* <sup>164, 165</sup>	
PERLEN07	Perylene (HB)	2.45	2.49* <sup>164, 165</sup>	
POBPIG	Diindeno[1,2,3-cd:1',2',3'-lm]perylene	2.21	2.25 <sup>166</sup>	
QUATER10	Quaterrylene	1.33	1.48-1.60 <sup>167-169</sup>	
CORONE01	Coronene	2.96	2.9-2.92* <sup>170, 171</sup>	
HBZCOR	Hexabzeno(bc,ef,hi,kl,no,qr)coronene	2.70	2.80 <sup>172, 173</sup>	
BEANTR	1,2-Benzanthracene	3.27	3.14 <sup>174</sup>	
BIPHEN	Biphenyl	3.41	4.1-4.18 <sup>175-178</sup>	
CRYSEN01	Chrysene	3.66	3.6** <sup>179</sup>	
TERPHE02	p-Terphenyl	4.17	3.9** <sup>179</sup>	
BNPERY	1,12-Benzoperylene	2.80	2.4-2.5* <sup>180</sup>	
KUBVUY	10,10'-Diphenyl-9,9'-bianthryl	3.23	2.9* <sup>181</sup>	
KUBWAF01	9,9'-Bianthracenyl	3.05	2.7-2.8* <sup>182</sup>	

The  $GW+BSE$  absorption spectra are validated by comparison to thin film experimental data for representative materials.<sup>172, 179, 183</sup> For an anisotropic crystal the absorbance depends on the polarization direction of the incident light. Most absorption experiments are performed on polycrystalline samples and even in experiments performed on single crystals the crystallographic orientation of the sample with respect to the polarization of the incident light is often unknown. This introduces some uncertainties in the comparison with experiments. We calculate the absorbance for light polarized along the  $a$ ,  $b$ , and  $c$  lattice vectors and normalize the maximum of the total absorbance to one. The results are shown in Figure 5. For 1,2-benzanthracene (BEANTR), coronene (CORONE01), and hexabzeno(bc,ef,hi,kl,no,qr)coronene (HBZCOR) the agreement of the  $GW+BSE$  spectra with experiment is very good. For chrysene (CRYSEN01), p-terphenyl (TERPHE02), and triphenylene (TRIPHE12) the agreement is more qualitative.

In addition to the unknown direction of the polarization with respect to the crystal axes, there are other factors, both on the experimental side and on the theoretical side that can contribute to discrepancies. In ref.<sup>179</sup> the crystal structure of the films is not reported. The crystal structures used in our calculations are the common forms of p-terphenyl and chrysene, but both materials have other polymorphs reported in the CSD (for triphenylene all CSD entries appear to be the same structure but we cannot rule out the appearance of a different thin film polymorph). In polycrystals there can be contributions from grain boundaries (in samples comprising very small crystallites, which is not the case here, there can be surface contributions as well). Furthermore, we do not consider vibrational contributions in our simulations. Sources of errors in  $GW+BSE$  calculations include the DFT exchange-correlation functional used for the mean-field starting point, numerical convergence of various settings (k-point grids, number of empty states used in the GW step, the number of bands used in the BSE step), the non-self-consistency in the GW step, the plasmon pole approximation used in the GW step,<sup>49</sup> the Tamm–Dancoff approximation used in the BSE step,<sup>25, 150, 184-188</sup> and the static approximation for  $W$  used in the BSE step.<sup>184, 189</sup> See also Ref.<sup>190</sup> for additional discussion. The significance of different sources of errors can be material dependent. In the future, it would be desirable to rigorously

231 assess the contributions of different sources of errors in  $GW+BSE$  by comparison to high-level theories or well-controlled  
 232 experiments (performed on single crystals with well-defined polarization) for a diverse benchmark set of molecular crystals.



**Figure 5.** Absorption spectra calculated using  $GW+BSE$  compared with thin film experiments<sup>172, 179, 183</sup> for (a) 1,2-benzanthracene (BEANTR), (b) coronene (CORONE01) with the region around the absorption edge magnified for clarity, (c) chrysene (CRYSEN01), (d) hexabenzo(bc,ef,hi,kl,no,qr)coronene (HBZCOR), (e) p-terphenyl (TERPHE02), and (f) triphenylene (TRIPHE12).

## 233 Usage Notes

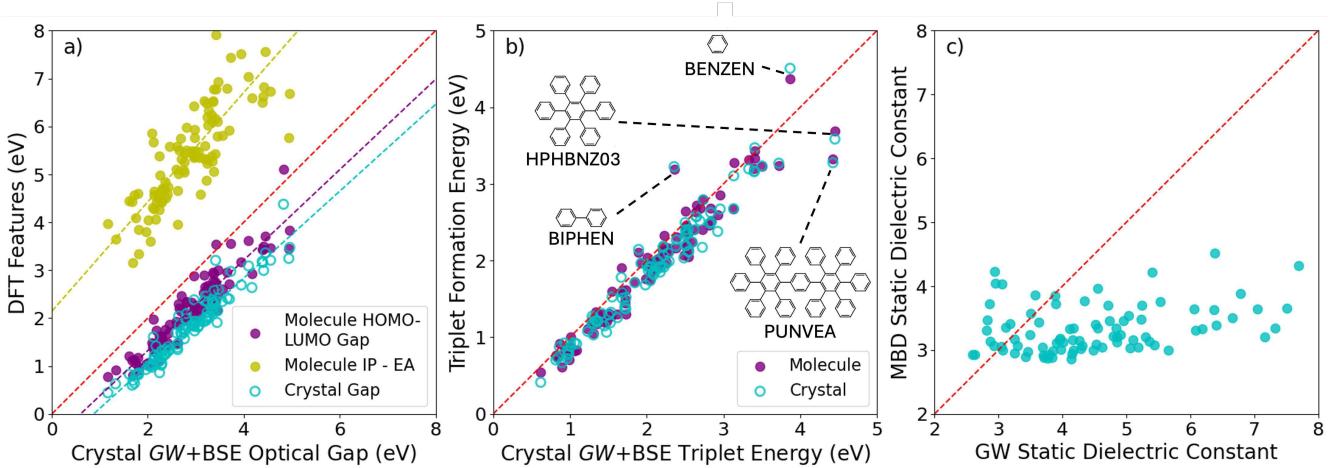
234 The PAH101 set is the currently the largest trove available of  $GW+BSE$  data for molecular crystals. As such, it offers unique  
 235 opportunities to (i) learn about correlations between DFT and  $GW+BSE$  values of various properties, (ii) discover materials  
 236 with desired electronic/ optical properties in the dataset itself, and (iii) train machine learning models to help in materials  
 237 discovery efforts. Here, we provide examples for these three use cases.

## 238 Reliability of DFT Models

239 In materials discovery workflows it is desirable to use models that are fast to evaluate for preliminary screening of a large  
 240 number of candidates. Semi-local DFT has been used extensively for this purpose. However, such models must be sufficiently  
 241 reliable to at least capture the correct trends. Here, we perform statistical analysis across our dataset to examine whether  
 242 selected DFT models are sufficiently predictive of  $GW+BSE$  quantities. The PAH101 dataset may similarly serve as a resource  
 243 for researchers interested in comparing the results of other DFT and TDDFT models to  $GW+BSE$ .

244 Figure 6 shows correlation plots between selected properties calculated by DFT with the PBE functional and  $GW+BSE@PBE$ .  
 245 In Panel (a) single-molecule and crystal DFT quantities are compared to the  $GW+BSE$  crystal optical gap. The fundamental  
 246 gap of a molecule corresponds to the difference between the ionization potential (IP) and electron affinity (EA). The fundamental  
 247 gap of a molecular crystal (calculated by  $GW$ ) is typically significantly narrower than the single molecule fundamental  
 248 gap because of screening and band dispersion in the crystal.<sup>97</sup> The optical gap of a molecular crystal is narrower than the  
 249 fundamental gap because of the exciton binding energy.<sup>191</sup> The IP and EA calculated based on on DFT total energy differences  
 250 are better estimates than the Kohn-Sham eigenvalues of the HOMO and LUMO. However, it has been shown that the molecular  
 251 fundamental gaps obtained from PBE IP-EA have errors of 0.89 eV on average compared to reference data.<sup>192</sup> As expected,  
 252 the molecular PBE IP-EA values significantly overestimate the  $GW+BSE$  optical gaps of the corresponding molecular crystal.  
 253 Although there is correlation with the overall trend of the  $GW+BSE$  optical gaps, the spread of the PBE IP-EA values is too  
 254 large to be considered as a reliable predictor.

255 It is well known that molecular HOMO-LUMO gaps and crystal band gaps are significantly underestimated by (semi-)local  
 256 functionals such as PBE, owing to the self-interaction error (SIE).<sup>193</sup> For the PAH101 set, both the PBE single molecule



**Figure 6.** Correlations between DFT and *GW*+BSE across the PAH101 set for selected properties: (a) DFT molecular IP-EA, molecular HOMO-LUMO gaps, and crystal band gaps compared to *GW*+BSE optical gaps. (b) DFT triplet formation energy of the molecule and crystal compared to the *GW*+BSE triplet exciton energy. Molecular structures of some outliers are also shown. (c) DFT dielectric constant calculated by using the MBD polarizability in the Clausius-Mossotti equation compared with the *GW* static dielectric constant.

257 HOMO-LUMO gap and crystal gap systematically underestimate but correlate well with the *GW*+PBE optical gaps. Based  
 258 on this, these values may be sufficiently reliable for rough preliminary screening based on relative trends among materials.  
 259 The single molecule PBE HOMO-LUMO gap is particularly attractive for this purpose because it is very fast to evaluate.  
 260 Furthermore, there are large datasets of single molecule<sup>46</sup> and crystal PBE gap<sup>47</sup> that can be mined. We note, however, the  
 261 effect of SIE is material-dependent.<sup>143, 194</sup> Compounds whose HOMO and/or LUMO are highly localized may be affected more  
 262 severely than PAHs, whose frontier molecular orbitals are typically delocalized over the aromatic system. Therefore, it would  
 263 be prudent to reevaluate the reliability of DFT-PBE molecular and crystal gaps for more diverse data sets.

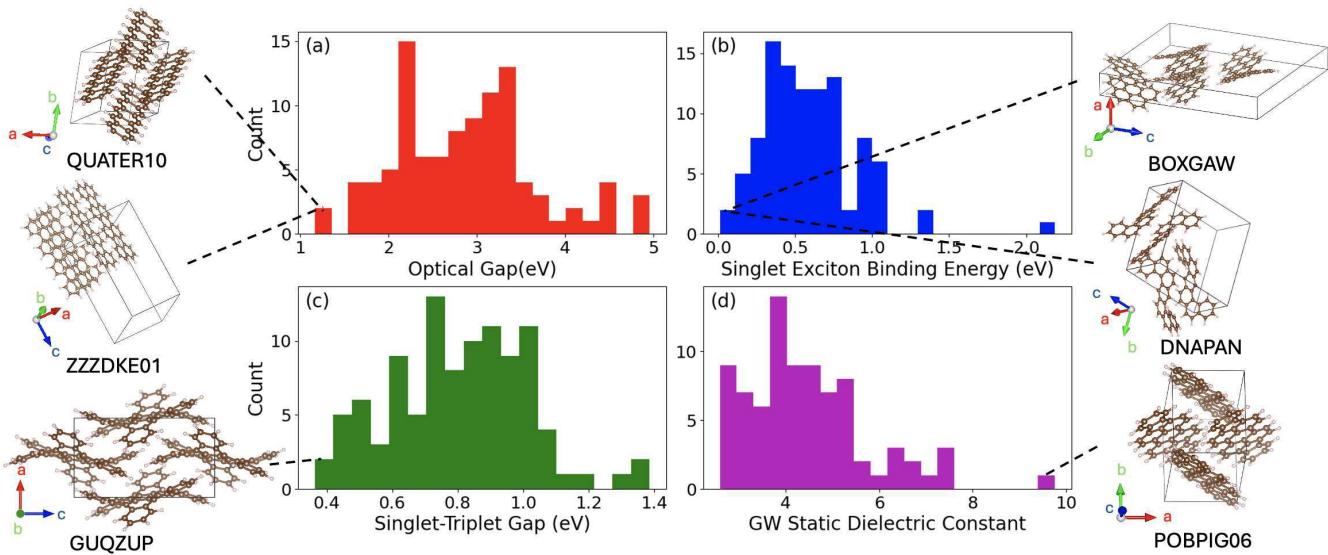
264 In Panel (b) the single molecule and crystal DFT triplet formation energies are compared to the *GW*+BSE triplet excitation  
 265 energies. Overall, the single molecule and crystal DFT values are quite close to each other and to the *GW*+BSE triplet exciton  
 266 energies, with MAEs of 0.20 eV and 0.23 eV, respectively and  $R^2$  values of 0.89 and 0.86, respectively. The reasons for this  
 267 agreement need to be investigated further (we are not aware of any benchmark studies of DFT triplet formation energies).  
 268 The four most significant outliers, whose molecular structures are shown, are: biphenyl (BIPHEN), benzene (BENZEN),  
 269 2',2'',3',3'',5',5'',6',6''-octaphenyl-p-quinquephenyl (PUNVEA), and hexaphenylbenzene (HPHBNZ03). These compounds  
 270 are characterized by phenyl rings connected by single C-C bonds, whereas the majority of compounds in the PAH101 set are  
 271 characterized by extended aromatic systems. Our results indicate that DFT triplet formation energies are fairly reliable as  
 272 lower-cost descriptors for preliminary screening. However, based on the nature of the outliers, it would be prudent to validate  
 273 these findings for more diverse materials.

274 Panel (c) shows a comparison between the static dielectric constant calculated by PBE+MBD and by *GW*. The *GW* value  
 275 corresponds to the dielectric function value at 0 frequency and 0 wave-vector,  $\epsilon(\omega = 0, q = 0)$ . The DFT value is obtained  
 276 by using the MBD polarizability in the Clausius-Mossotti relation, as described in Ref.<sup>97</sup>. The comparison reveals that the  
 277 DFT values are narrowly distributed around 3 and, in general, do not correlate with the *GW* values. For some materials the  
 278 values obtained from PBE+MBD may fortuitously agree with experimental and/or *GW* values,<sup>195</sup> however, even with the  
 279 self-consistent screening approach used in the MBD method,<sup>127, 128</sup> DFT does not capture the many-body physics contained in  
 280 the *GW* dielectric function. This demonstrates that it is important to consider larger sets of materials to assess the reliability of  
 281 methods.

## 282 Materials Discovery

283 The electronic and optical properties of most of the materials in the PAH101 set have not been thoroughly investigated  
 284 experimentally. Some of the quantities calculated here, such as triplet excitation energies, are difficult to probe experimentally  
 285 and require highly specialized techniques and facilities. Therefore, although the PAH101 set is relatively small, it is possible  
 286 that some useful materials would be found in it. Here, we provide examples for some of the electronic and optical properties  
 287 relevant for organic electronic devices that can be extracted from the dataset. The dataset can be searched for materials with a

particular property or combination of properties. As demonstrated below, the dataset may provide insights on structure-property relations and expose gaps in our understanding of the properties of molecular crystals that call for further investigation.



**Figure 7.** Distributions of (a) the singlet exciton energies, which correspond to the optical gaps, (b) the singlet exciton binding energies, (c) the singlet-triplet gaps, and (d) the *GW* static dielectric constant across the PAH101 dataset. Some crystal structures are also shown.

One of the key properties for device applications is the optical gap, whose distribution in the dataset is shown in Figure 7a. The PAH101 set contains materials with a wide range of optical gaps. Crystalline quaterrylene (QUATER10) and hexacene (ZZZDKE01) have the smallest optical gaps of 1.33 eV and 1.17 eV, respectively. If a material is sought with an optical gap of up to about 5 eV it may be found in the dataset. Absorption spectra for light polarized along the three crystal axes are also provided in the dataset (see Table 1), such that materials can be sought with broad absorption and/or absorption peaks in certain energy ranges.

The singlet exciton binding energy, whose distribution is shown in Figure 7b, corresponds to the difference between the *GW* fundamental gap and the optical gap. This is the energy required to split photogenerated excitons into free charge carriers in organic solar cells. In most organic materials the exciton binding energy is significant compared to inorganic materials because the dielectric screening of charges is not as strong. However, some materials in the PAH101 set have low exciton binding energies (in parentheses), including: anthra(2,1,9,8-hijkl)benzo(de)naphtho(2,1,8,7-stuv)pentacene (BOXGAW; 0.013 eV), dinaphtho(1,2-a:1',2'-h)anthracene (DNAPAN; 0.071 eV), tetrabenzo(de,no,st,cl1d1)heptacene (TBZHCE; 0.130 eV), benzo[Im]chryseno[1,12,11,10-opqrab]perylene (YUNYAJ; 0.165 eV), and hexabenzo(bc,ef,hi,kl,no,qr)coronene (HBZCOP; 0.169 eV). All of these compounds are characterized by very extended and/or elongated  $\pi$  systems, which likely lead to an already low molecular exciton binding energy (not calculated here), further reduced by dielectric screening in the solid form. Triplet exciton binding energies are also provided in the dataset (see Table 1). They are typically significantly higher than singlet exciton binding energies.

Another property of interest for device applications is the singlet-triplet gap, *i.e.*, the energy difference between the lowest singlet excited state and the lowest triplet excited state, both of which are included in the PAH101 dataset (see Table 1). The singlet-triplet gap is a key property for organic light emitting diodes (OLEDs). Most of the electrically generated excitons in OLEDs are triplet excitons, which cannot decay radiatively to the ground state. In thermally activated delayed fluorescence (TADF) chromophores, a small singlet-triplet gap enables reverse intersystem crossing (RISC) from the lowest triplet excited state to the lowest singlet excited state, which subsequently decays to the ground state, emitting a photon.<sup>196-198</sup> Figure 7c shows the distribution of singlet-triplet gaps in the PAH101 dataset. Small singlet-triplet gaps are rare among this class of materials. The materials with lowest singlet-triplet gaps (in parentheses) are: trinaphtho[1,2,3,4-fgh:1',2',3',4'-pqr:1",2",3",4"-za\_1\_b\_1]trinaphthylene (GUQZUP; 0.36 eV), 9,18-diphenyltetrabenzo(a,c,h,j)anthracene (FACPEE; 0.38 eV), acenaphtho[3,2,1,8-fghij]tetrabenzo[a,c,m,o]picene (VUFHUA; 0.435 eV), benzo(1,2,3-bc:4,5,6-b',c')dicoronene (YOFCUR; 0.44 eV), and 2-(naphthalen-2-yl)azulene (PUJQIV; 0.45 eV). Even the lowest singlet-triplet gaps in the PAH101 set would be considered marginal or too high for TADF. However, examining these materials may reveal new classes of chromophores that could be interesting for further investigation and fine-tuning by chemical modification. Charge transfer (CT) excitations

320 between spatially separated HOMO and LUMO states are considered key to achieving small singlet-triplet gaps in TADF  
321 chromophores.<sup>113,197</sup> With the exception of PUJQIV, the materials with the smallest singlet-triplet gaps in the PAH101 set  
322 bear no resemblance to the donor-acceptor compounds typically used for TADF. Rather, they are large PAHs with extended  $\pi$   
323 systems. FACPEE, VUFHUA, and YOFCUR have segments that could lead to CT-like intramolecular excitations. GUQZUP  
324 (shown in Figure 7c) can be described as a graphene flake with no obvious segments. The twisted conformation it adopts in the  
325 crystal structure may contribute to orbital localization and CT-like excitations. The effect of crystal packing and intermolecular  
326 vs. intramolecular CT excitations on singlet-triplet gaps is also not well-understood and should be further investigated in  
327 relation to TADF in crystalline materials.<sup>199,200</sup>

328 Figure 7d shows the distribution of the  $GW$  static dielectric constant in the PAH101 dataset. There is a prevalent perception  
329 in the organic electronic community that all organic solids have a similar dielectric constant of about 3 (we have not been able  
330 to trace the origin of this perception to a particular paper). The DFT values obtained for the PAH101 set (see Figure 6c) may  
331 confirm this perception, but the  $GW$  values tell a different story. Several materials in the dataset have  $GW$  static dielectric  
332 constants (in parentheses) that are significantly higher than 3, including: diindeno[1,2,3-cd:1',2',3'-lm]perylene (POBPIG06;  
333 9.75), benzo[lm]chrysene[1,12,11,10-opqrab]perylene (YUNYAJ; 7.51), hexacene (ZZZDKE01; 7.41), indeno(7,7a,1,2,3-  
334 lmno)-1,12-ethenochrysene (SURTAA; 7.33), and tetrabenz[a,d,j,m]coronene (SETTES; 7.05). These are compounds with  
335 extended and/or elongated  $\pi$  systems, which are probably highly polarizable (the molecular polarizability is not calculated here).  
336 The crystal packing probably also contributes significantly to the dielectric screening. Most of the research on organic materials  
337 with high dielectric constants has been on polymers for applications in bulk heterojunction organic solar cells (e.g.,<sup>201</sup>), which  
338 are very different for the materials in the PAH101 set. This calls for further investigation of the dielectric behavior of molecular  
339 crystals. We note that the full dielectric function, which contains information on the frequency dependence and anisotropy, is  
340 available in the dataset (in the absorption entry, see Table 1).

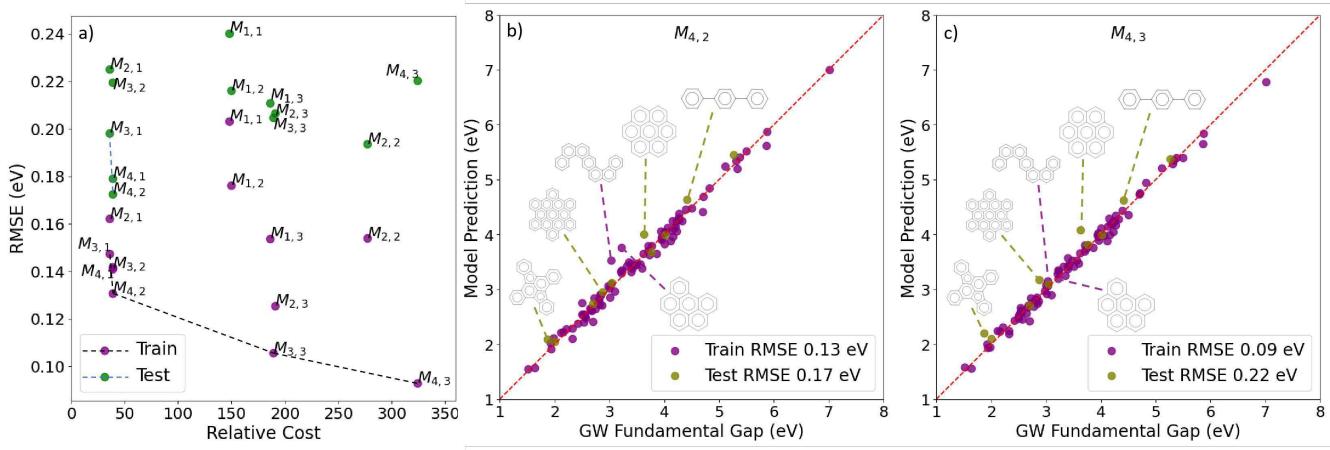
## 341 Machine Learning

342 To demonstrate how the PAH101 dataset can be reused to train ML models for other purposes than SF, we use SISSO to find  
343 predictive models for the  $GW$  fundamental band gap, whose values are also provided in the dataset. The dataset can be used in  
344 a similar manner to train ML models other than SISSO to predict any of the quantities included in the dataset. In addition, it  
345 can be used to supplement larger lower-fidelity datasets to train multi-fidelity models.

346 SISSO models were trained following the same procedure used in Ref.<sup>98</sup>. The same primary features were used (also  
347 provided in the PAH101 dataset), with the exception of  $DF_s$  and  $DF_c$ , because the DFT estimate for the SF driving force  
348 is not a physically meaningful descriptor in relation to the fundamental band gap. The same 10 structures as in Ref.<sup>98</sup> were  
349 withheld as an unseen test set and the remaining 91 structures were used for model training. Features were constructed with a  
350 maximum rung (the number of times primary features are combined) of 3 and a maximum dimension (Dim) of 4. Features  
351 were combined using the operator set  $H = \{+, -, \times, \div, \exp, \log, ()^{-1}, ()^2, ()^3, \sqrt{ }, \sqrt[3]{ }, |\cdot| \}$ . The maximum complexity, i.e., the  
352 maximum number of operators in one combined feature, was set to 10. A total of  $5 \times 10^2$ ,  $4 \times 10^5$ , and  $6 \times 10^{10}$  features were  
353 generated by SISSO with a rung of 1, 2, and 3, respectively.

354 After feature generation, SISSO performs linear regression to yield the model prediction, where each model is the scalar  
355 product of the SISSO-generated feature with a vector of fitted coefficients. Then, the models are ranked according to their  
356 prediction performance. Sure independence screening (SIS) is used to select optimal subspaces from the huge feature space.  
357 The number of features saved after SIS was set to 20. SISSO then uses  $\ell_0$ -norm minimization as a sparsifying operator (SO) to  
358 determine the sparse solution for each such subspace. For each combination of dimension and rung, 40 rounds of leave-10-out  
359 cross validation (LCV) were performed. In each round, 10 data points (out of the 91 points used for model training) were  
360 randomly selected and held out as an unseen validation set. The model with the lowest RMSE for the validation set was selected  
361 in each round. Finally, the model with the lowest root mean square error (RMSE) for the combined LCV training and validation  
362 data was selected out of the 40 models. This model is denoted as  $M_{\text{Dim}, \text{Rung}}$ . A full account of the SISSO models is provided in  
363 the SI.

364 The computational cost of SISSO-generated models varies depending on the number and type of primary features they  
365 contain. The cost of each model was evaluated by summing over the costs of all the primary features included in it. The cost of  
366 features that appear in the model more than once was counted only once. The computer time required to calculate the single  
367 molecule PBE gap,  $Gap^S$ , was assigned a value of 1 cost unit and the cost of other features is tabulated in the SI as multiples of  
368 that unit. The cost of all the primary features has been updated from the values given in Ref.<sup>98</sup> to account for new developments  
369 in the latest version of FHI-aims. In particular, the MBD calculation has become significantly more efficient than in older  
370 versions of the code. The cost was averaged over the 10 structures in the validation set, rather than picking one system of  
371 average size, as in Ref.<sup>98</sup>. Figure 8a shows a Pareto chart of the accuracy vs. the computational cost of the SISSO models  
372 considered here. The “train” RMSE is calculated for the training set of 91 structures. The “test” RMSE is calculated for the 10



**Figure 8.** Performance of SISSO-generated models for predicting the *GW* fundamental band gaps of molecular crystals: (a) Pareto chart of the accuracy vs. the computational cost of SISSO-generated models. The “train” accuracy corresponds to the RMSE obtained for the LCV validation set during training and the “test” accuracy corresponds to the withheld set of 10 materials not included in the training. The dashed lines indicate the Pareto front. Model prediction as a function of the *GW* fundamental band gap for (b)  $M_{4,2}$  and (c)  $M_{4,3}$ . Molecular structures of some of the outliers are also shown.

373 withheld materials, which were excluded from the LCV. The best balance of cost and accuracy is provided by the  $M_{4,2}$  model:

$$M_{4,2} = 0.90 \times \frac{E_T^S \times \text{Gap}^C}{\text{Gap}^S \times \rho^C} - 0.063 \times \frac{\ln(\text{CB}_{\text{disp}}^C) \times \text{AtomNum}^C}{\text{MolWt}^S} + 197 \times \frac{(\text{CB}_{\text{disp}}^C)^3}{\text{EA}^S \times \text{MolWt}^S} + 0.035 \times \frac{\text{EA}^S}{\text{Gap}^S \times \ln(\rho^C)} + 1.67 \quad (1)$$

374 The  $M_{3,3}$  and  $M_{4,3}$  models, whose computational cost is considerably higher, have a better accuracy for the training set. However,  
 375 their RMSE increases significantly for the unseen test set, which is indicative of over-fitting. This is also seen in the correlation  
 376 plots in Figure 8b,c. Interestingly, SISSO does not produce any models that can predict the crystal fundamental gap based only  
 377 on single molecule features (the equations of all models are provided in the SI).

### 378 Code availability

- 379 The *HAppend* code for adding missing hydrogen atoms to molecular crystal structures is available in the GitHub  
 380 Repository [HAppend](#), together with scripts for making band structure and absorption plots.
- 381 Scripts for calculating the SISSO primary features and for processing SISSO results are available in the GitHub repository  
 382 [MLfeat\\_FHI-aims](#).
- 383 The BerkeleyGW code for performing *GW*+BSE calculations<sup>124</sup> is available at the [BerkeleyGW website](#).
- 384 The FHI-aims code,<sup>119</sup> used to perform some relaxations and calculate DFT features, is available at the [FHI-aims website](#).
- 385 The Quantum ESPRESSO code,<sup>123</sup> used to calculate the mean-field wave functions for subsequent *GW*+BSE calculations,  
 386 is available at the [Quantum ESPRESSO website](#).
- 387 The SISSO code,<sup>63</sup> used to perform sure independent screening and sparsifying operator model training, is available at  
 388 the GitHub Repository [SISSO](#)

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## 801 Author contributions statement

802 S. G., X. L., Y. L., X. W., K. Z., and V. C. performed the calculations and curated the data. S. G. and Y. L. performed additional  
803 analysis and validation. B.S. provided the structures relaxed with CASTEP. N. M., S. G., X. L., Y. L., and X. W. wrote the  
804 manuscript. S. G. and X. L. contributed equally to this work. N. M. conceived and led the project.

## 805 Competing interests

806 The authors declare no competing interests.