

Amplified Spontaneous Emission from Electron–Hole Quantum Droplets in Colloidal CdSe Nanoplatelets

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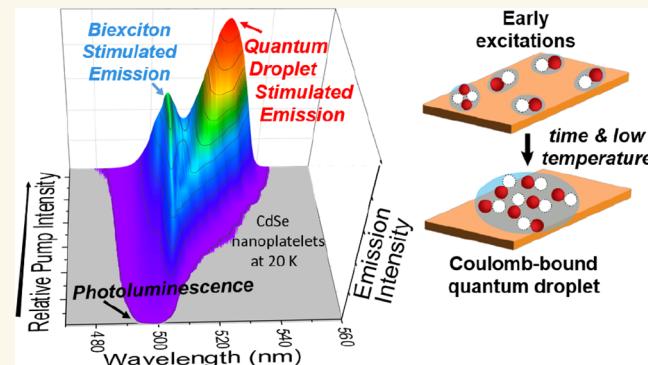
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ABSTRACT: Two-dimensional cadmium selenide nanoplatelets (NPLs) exhibit large absorption cross sections and homogeneously broadened band-edge transitions that offer utility in wide-ranging optoelectronic applications. Here, we examine the temperature-dependence of amplified spontaneous emission (ASE) in 4- and 5-monolayer thick NPLs and show that the threshold for close-packed (neat) films decreases with decreasing temperature by a factor of 2–10 relative to ambient temperature owing to extrinsic (trapping) and intrinsic (phonon-derived line width) factors. Interestingly, for pump intensities that exceed the ASE threshold, we find development of intense emission to lower energy in particular provided that the film temperature is ≤ 200 K. For NPLs diluted in an inert polymer, both biexcitonic ASE and low-energy emission are suppressed, suggesting that described neat-film observables rely upon high chromophore density and rapid, collective processes. Transient emission spectra reveal ultrafast red-shifting with the time of the lower energy emission. Taken together, these findings indicate a previously unreported process of amplified stimulated emission from polyexciton states that is consistent with quantum droplets and constitutes a form of exciton condensate. For studied samples, quantum droplets form provided that roughly 17 meV or less of thermal energy is available, which we hypothesize relates to polyexciton binding energy. Polyexciton ASE can produce pump-fluence-tunable red-shifted ASE even 120 meV lower in energy than biexciton ASE. Our findings convey the importance of biexciton and polyexciton populations in nanoplatelets and show that quantum droplets can exhibit light amplification at significantly lower photon energies than biexcitonic ASE.

KEYWORDS: multiple excitons, optical gain, quantum droplet, excited-state dynamics, stimulated emission, exciton condensation



Colloidal synthesized, two-dimensional CdSe nanoplatelets (NPLs) exhibit thickness-tunable absorption and emission properties that offer potential utility in applications such as high color rendering index light-emitting diodes and solution-processed lasers.^{1–5} Routes to monodisperse control over the monolayer (ML) thickness in colloidal NPL ensembles permit the observation of homogeneous line width-dominated radiative recombination that, combined with large absorption cross-section, yields low-threshold amplified spontaneous emission (ASE), high modal gain, and robust laser action.^{1,4–9} However, band-edge optical gain and ASE compete with fast nonradiative recombination pathways such as Auger recombination^{10–13} and carrier trapping that have motivated continued research efforts.^{14–16} CdSe NPLs, like several other 2D semiconductors,^{17–19} engender large exciton binding energies in the range of 100 to

400 meV,^{20–23} which approach 25 times the bulk semiconductor value and significantly exceed available thermal energy at room temperature. As a result of quantum confinement and reduced dielectric screening, electron–hole pairs in NPLs form excitons at room temperature rather than independent charge carriers. A continuous density of states and typical phonon line width broadening in NPLs ($\Gamma = \Gamma_0 + \Gamma_{\text{phonon}}(T)$) suggests that ASE could exhibit temperature-

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dependent threshold as reduced thermal energy serves to focus excitons into a narrower distribution of states, also apparent, e.g., in temperature-dependent photoluminescence (PL)³ and carrier cooling studies.²⁴ At the same time, introduction of a second electron–hole pair within the same particle can result in either two independent free excitons with an uncorrelated center of mass motion, or one biexciton (which is sometimes termed an exciton molecule),^{25–27} provided that the biexciton Coulomb binding energy exceeds available thermal energy. Under conditions that the biexciton binding energy is comparable to available thermal energy, free excitons and biexcitons experience a quasi-equilibrium population distribution as described recently.^{25,28} Biexcitons exhibit 20–45 meV binding energies relative to free excitons for the particles studied herein, which is an order of magnitude weaker than the exciton binding energy.^{25,29} Both exciton and multiexciton behaviors in 2D NPLs, thus, differ fundamentally from 0D quantum dots, wherein two electron hole pairs necessarily spatially overlap in a 0D particle that is smaller than the Bohr radius, irrespective of the biexciton binding energy.³⁰ Furthermore, as the number of photoexcited electron–hole pairs in a NPL increases above two, polyexciton (PE) many-body states comprising three or more excitons can form with distinct properties, including characteristics such as binding energy, but also correlations such as electron–hole plasma (EHP), electron–hole liquid (EHL), or quantum droplets, each of which impact the energy and rates of available recombination pathways.^{26,27,31–35} EHP comprises a compressible gas of nongeminate electrons and holes that yields increasing red-shifted emission with higher density as screening increases.^{17,26,32} EHL, on the other hand, presents a constant electron–hole density and produces a fixed red-shift of emission with little excitation intensity dependence.^{26,27,34} Quantum droplets^{26,31} describe EHL puddles that importantly feature size-dependent screening and yield progressively red-shifted emission as liquid-like droplet size (and thus, screening) increases upon elevation of pump intensity, where such states can be short-lived in direct gap semiconductors like GaAs.^{31,33}

Under conditions where the spatial separation of excitons becomes comparable to the exciton size,²¹ a blue shift conveying a Mott transition is expected as increased Coulomb screening reduces exciton binding energy and leads to uncorrelated band-edge charge carriers. However, the small size of excitons owing to low dielectric screening has prevented the direct observation of such a transition for CdSe NPLs.^{21,36} Lack of an observable bipolar, free-carrier plasma has led to suggestions that, instead, a biexciton gas may form that could serve to largely maintain optical amplification properties at high excitation intensity.³⁷ Competition between a Mott transition and bandgap renormalization has been described for semiconductors, including bulk CdSe at low temperature³⁸ and GaAs quantum wells,^{28,31} as well as in-transition metal dichalcogenides (TMDs) that in each case afford spectral red-shifting owing to EHP or EHL.^{17,27,31,34,39,40}

This report describes the photophysical response of CdSe NPL films under controlled-intensity optical excitation as a function of the temperature. First, we find that the biexcitonic ASE threshold decreases by anywhere between a factor of 2 to 10 upon cooling from 298 to 5 K for neat 4 or 5 ML CdSe NPL films, depending on the characteristics of the room temperature film ASE threshold. Additionally, for neat films cooled to 200 K or below, we are able to observe strong

emission at progressively redder wavelengths upon pump fluence elevation above the biexciton ASE threshold. To discern the origin of this red-shifted emission, we purposely impede ASE and dilute NPLs into an inert polymer that increases the NPL–NPL average separation to ascertain whether the red-shifted emission arises from independent particles. In these polymer-diluted films, both biexcitonic ASE and the additional red-shifted emission are suppressed for otherwise identical or even more intense pumping conditions. Our findings suggest that the red-shifted emission arises due to stimulated emission where individual particles spontaneously radiate too weakly for distinct, direct observation. In particular, the requirement of reduced temperature to produce red-shifted emission for neat films suggests that quantum droplet states likely form with a Coulomb binding energy less than the meV available at room temperature and closer to ~17 meV, corresponding to the temperature where red-shifted emission is observed. However, the nonlinear nature of the observed signal complicates the analysis of the produced polyexciton population. The red-shifted emission is inconsistent with both bandgap renormalization and EHP formation, each of which should not yield the observed sensitivity to sample temperature. This work offers insights regarding the impacts of temperature-dependent features of NPLs as well as polyexciton photophysics in 2D semiconductor NPL solids.

RESULTS AND DISCUSSION

Temperature Dependence of Biexcitonic Amplified Spontaneous Emission. Previous reports have explored means to reduce the optical gain threshold in NPLs that take advantage of their 2D particle shape (Figure S1) and emergent properties such as a putative giant oscillator strength transition, in addition to the growth of core–shell heterostructures.^{5,41,42} We study the influence of temperature reduction on the ASE threshold for multiple reasons. Fundamentally, reduced phonon population at reduced temperature focuses electronic carrier populations into a narrower range of energies, which manifests as a smaller homogeneous PL line width³ (also apparent in Figure S2). This transition narrowing occurs in addition to an overall blue shift of the band-edge for II–VI semiconductors, with the latter owing to the well-known Varshni relation^{2,43} and is important, especially considering the continuous density of states that is accessible in these structures. Moreover, we recently showed that multiexcitons radiate more rapidly upon temperature reduction in CdSe NPLs,⁴⁴ suggesting the reduced competition with deleterious nonradiative Auger recombination for low temperatures. The spectroscopic appearance of trions at temperatures below ~100 K as a lower energy emission feature^{14–16} may also contribute to gain threshold reduction, as individual charges can block ground state absorption and effectively lower local band-edge state degeneracy.⁴⁵ Because biexciton binding energies for the NPL thicknesses studied herein are comparable to room temperature thermal energy, an increased population of biexcitons is expected at temperatures below ambient that can also reduce threshold.⁴⁰

As shown in Figure 1a for 4 ML CdSe NPLs, the biexcitonic ASE threshold of neat films was first evaluated at 298 K using stripe excitation. At low pump intensity, spontaneous PL appears as a single peak (center at 523 nm = 2.371 eV, fwhm = 10.7 nm = 48.6 meV; we note that line width of the neat film exceeds that observed for a colloidal dispersion in Figure S1d). Upon increasing pump intensity for this film to 180 μ J/cm²,

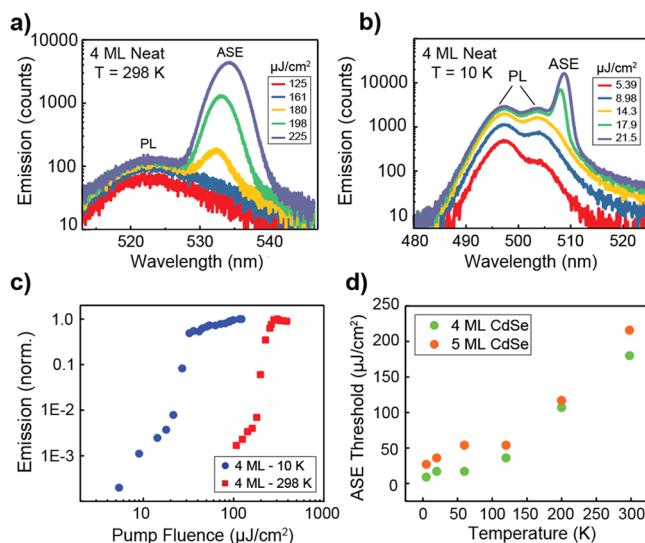


Figure 1. Amplified spontaneous emission threshold as a function of temperature. (a) Emission (PL and ASE) measured from a neat film of 4 monolayer NPLs at 298 K and (b) at 10 K. (c) Comparison of light emission intensity versus pump fluence at 298 and 10 K plotted at 533 and 508 nm, respectively. The ASE threshold values here differ by approximately 1 order of magnitude (~10-fold reduction for lower temperature). A smaller difference of ~2×, but the same general trend, was observed for films with lower room temperature thresholds (see Figure S4). (d) ASE threshold versus temperature for 4- and 5-monolayer neat NPL films derived from data similar to panels (a) and (b).

the emission redshifts (533 nm center, 44.5 meV red-shifted relative to PL), narrows (ASE band fwhm = 24.0 meV; Figure S2), and increases in intensity with a superlinear dependence on pump fluence, consistent with well-reported biexcitonic

ASE.^{1,4,5,33} Biexciton binding energy paired with reabsorption from a small Stokes shift give rise to the observed red-shift compared to PL energy.⁹ When the film is cooled to 10 K (Figure 1b), the onset of ASE for the exact same film region occurs at a significantly lower fluence between 14 and 17.9 $\mu\text{J}/\text{cm}^2$ with an ASE band centered near 508 nm, indicating a 10-fold threshold reduction in comparison to room temperature (Figure 1c), as well as a reduced ASE line width (fwhm = 9.6 meV). Measurements were also carried out for 5 ML NPL samples and similarly exhibited an ~8-fold threshold reduction compared to room temperature (Figure S3). ASE threshold was evaluated across a series of temperatures and showed a rather systematic temperature dependence (Figure 1d), which we attribute to two main factors. Intrinsically, reduced phonon broadening narrows population distribution of the emitting states and radiative rates of biexcitons in CdSe NPLs increase relative to Auger recombination at reduced temperatures⁴⁴ both of which support the ASE threshold reduction. Notably, because biexciton binding energies are comparable to thermal energy at 298 K, some of the threshold reduction upon cooling arises from increased formation of a biexciton population commensurate with reduction of free exciton population, where only the former contribute to ASE.

Importantly, significant variation in biexcitonic ASE threshold is commonly observed at room temperature as previously reported by She et al.⁵ and depends on sample features such as film optical scattering losses and NPL carrier trapping rates. Multiple regions of the same film in regions that appeared similar in optical density yielded a consistent threshold within ~15–20%, but different films and different synthetic batches of NPLs gave rise to variations such as that shown in Figure S4c. Preparation of NPL films with significantly reduced biexcitonic ASE threshold at room temperature (here as low as 12.3 $\mu\text{J}/\text{cm}^2$) also present reduced ASE threshold upon cooling, but by

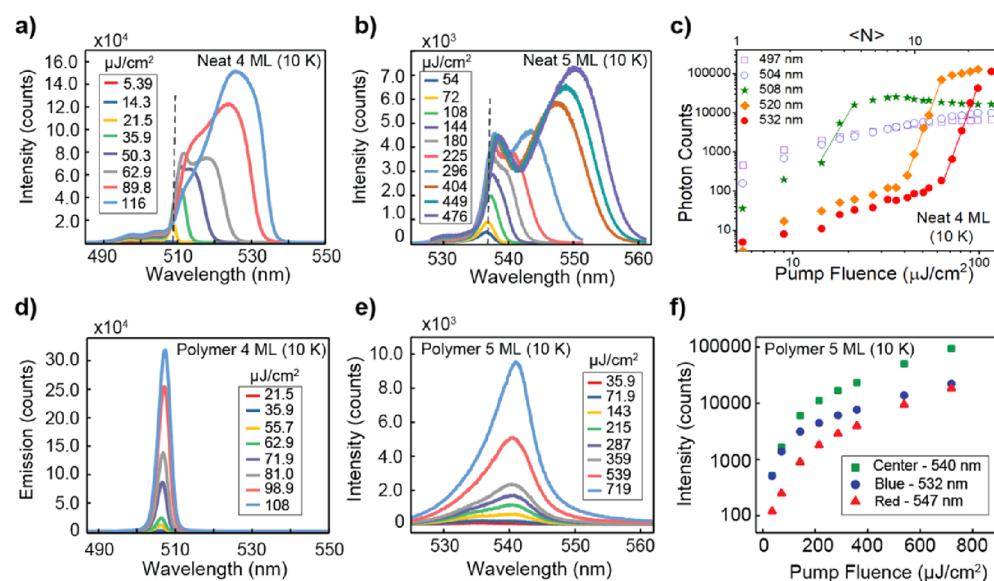


Figure 2. Elevated pump fluence measurements for neat and polymer-diluted films. (a) Emission from neat films of 4 ML NPLs and (b) 5 ML NPLs versus pump intensity at 10 K. Dashed vertical lines in (a) and (b) represent biexciton ASE center wavelengths just above threshold (508.6 and 536.5 nm, respectively). (c) Pump-fluence dependence of wavelength-resolved spontaneous PL, biexciton ASE (508 nm) and “red feature” emission from a 4 ML NPL neat film at 10 K. The average number of photons absorbed per excited nanoparticle, $\langle N \rangle$, was calculated using an absorption coefficient of $4.0 \times 10^{-14} \text{ cm}^{-2}$ for the 400 nm pump wavelength. (d) Emission from polymer-diluted films of 4 ML NPLs and (e) 5 ML NPLs versus pump intensity at 10 K. (f) Fluence-dependent emission at specified wavelengths for a polymer-diluted 5 ML NPL film.

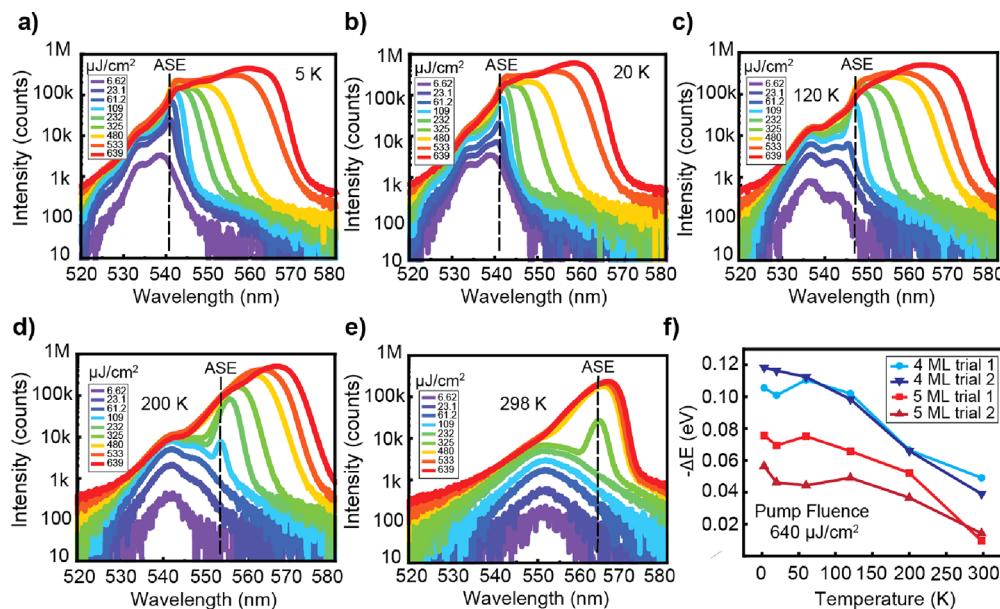


Figure 3. Temperature and fluence dependence of polyexciton emission. (a–e) 5 ML CdSe NPL neat film excited at indicated fluences for 5, 20, 120, 200, and 298 K, respectively. Above ~ 200 K the emission from polyexcitons is no longer prominent and only ASE is distinct (panels e and f). The extent of red-shifting at high pump intensity decreases with temperature elevation and is not appreciably red-shifted at 298 K. (f) Calculated maximum spectral shift obtained when comparing biexcitonic ASE at threshold and highest-investigated pump fluence polyexciton signal (at the center peak wavelength measured for $640 \mu\text{J}/\text{cm}^2$ pump intensity), $\Delta E = E_{\text{ASE}} - E_{\text{PE},639\mu\text{J}/\text{cm}^2}$.

216 a smaller factor of just under 2 (see Figure S4). Because optical
 217 quality of the films likely does not improve with temperature
 218 reduction, reduced carrier trapping in addition to narrowing of
 219 transition line widths and increased biexciton (versus free
 220 exciton) population each reasonably reduce ASE threshold.
 221 Notably, both the low threshold and high threshold films
 222 approach similar biexcitonic ASE thresholds at a cryogenic
 223 temperature in this work.

224 **Red-Shifted, Intense Light Output from Quantum
 225 Droplet Amplified Stimulated Emission.** Excitation
 226 intensities that exceed the biexciton ASE threshold were
 227 initially investigated to characterize the ASE saturation
 228 behavior as a function of temperature. However, rather than
 229 observing simple saturation behavior, as has been previously
 230 reported at room temperature (which also permits the
 231 evaluation of absorption cross section and thus the average
 232 number of excitations per photoexcited particle at a given
 233 excitation fluence, $\langle N \rangle$),^{4,5,36,46,47} at low temperature, elevation
 234 of pump intensity above the biexciton ASE threshold yielded
 235 distinct, progressively red-shifted, emission for both 4 and 5
 236 ML neat films (Figure 2a and b, respectively) here referred to
 237 as polyexciton (PE) emission. The PE assignment naively can
 238 be made on the basis of the calculated average number of
 239 photon absorptions per excited NPL exceeding two, but is
 240 rationalized *vide infra* as ASE from quantum droplet exciton
 241 condensate, specifically. Figure 2c displays pump-intensity-
 242 dependent behavior of light emission at several indicated
 243 wavelengths for the same 4 ML neat film at 10 K. Monitored
 244 wavelengths correspond to spontaneous PL, biexcitonic ASE,
 245 and red-shifted PE emission (shown with logarithmic plotting
 246 in Figure S5). Measurements were also carried out for 5 ML
 247 neat films and yielded similar trends for PL and ASE,
 248 respectively (Figure S5). We consider the sample-derived
 249 light output dependence on pump intensity both in terms of
 250 particular monitored wavelengths as well as total light output
 251 (see Figure S5b,d). Free exciton spontaneous PL intensity

252 increases linearly for low fluences and then begins to saturate 253 as the pump intensity approaches the biexciton ASE onset. 253 Biexcitonic ASE for the neat 4 ML NPL, monitored at 509 nm 254 is observed at $17.9 \mu\text{J}/\text{cm}^2$, saturates with pump intensity 255 elevation near $\sim 32 \mu\text{J}/\text{cm}^2$, and then unexpectedly begins to 256 decrease in intensity for fluences above $\sim 63 \mu\text{J}/\text{cm}^2$. The 257 biexcitonic ASE intensity decrease likely occurs due to 258 competition with further red-shifted PE emission that begins 259 to become discernible above $\sim 40 \mu\text{J}/\text{cm}^2$ at 10 K. Similar 260 trends occur for the 5 ML neat film. Total light output, 261 integrating all emitted photons, shows an approximately linear 262 trend at lower powers, then increases with the square or even 263 cube of pump intensity at the higher fluences studied relating 264 the appreciable influence stimulated emission processes impart 265 on the nanoplatelets. The wavelength-resolved fluence depend- 266 ences relate that the distribution of stimulated emission species 267 evolves despite the more simple trend line of total light output. 268

269 In similarity to highly excited 2D MoS₂,^{17,34} large red shifts 269 at high pump intensity reasonably derive from either 270 polyexciton EHP or polyexciton quantum droplets, both of 271 which would feature dependence of emission wavelength on 272 exciton density.^{26,27,31,33} Conversely, the EHL, with a rather 273 constant exciton density, would lack continuous wavelength 274 shifting with pump fluence. PE species might be expected to 275 spontaneously radiate for collections of isolated NPLs 276 irrespective of NPL density in a film, whereas a high 277 chromophore density is required for development of 278 stimulated emission, given the typical tens-of-picosecond 279 lifetimes of multiexciton states in simple nanostructures.²⁸⁰

281 Other possible sources of transiently red-shifted emission we 281 considered include Auger-heating of particles, wherein 282 expanded NPL crystal lattices or even transiently disordered 283 lattices might spontaneously radiate at lower energy.³⁶ To 284 investigate such possible origins, we diluted NPLs into an inert 285 polymer host, poly(butyl methacrylate-*co*-isobutyl-methacry- 286 late) (see **Methods**), and examined the resultant films. Optical 287

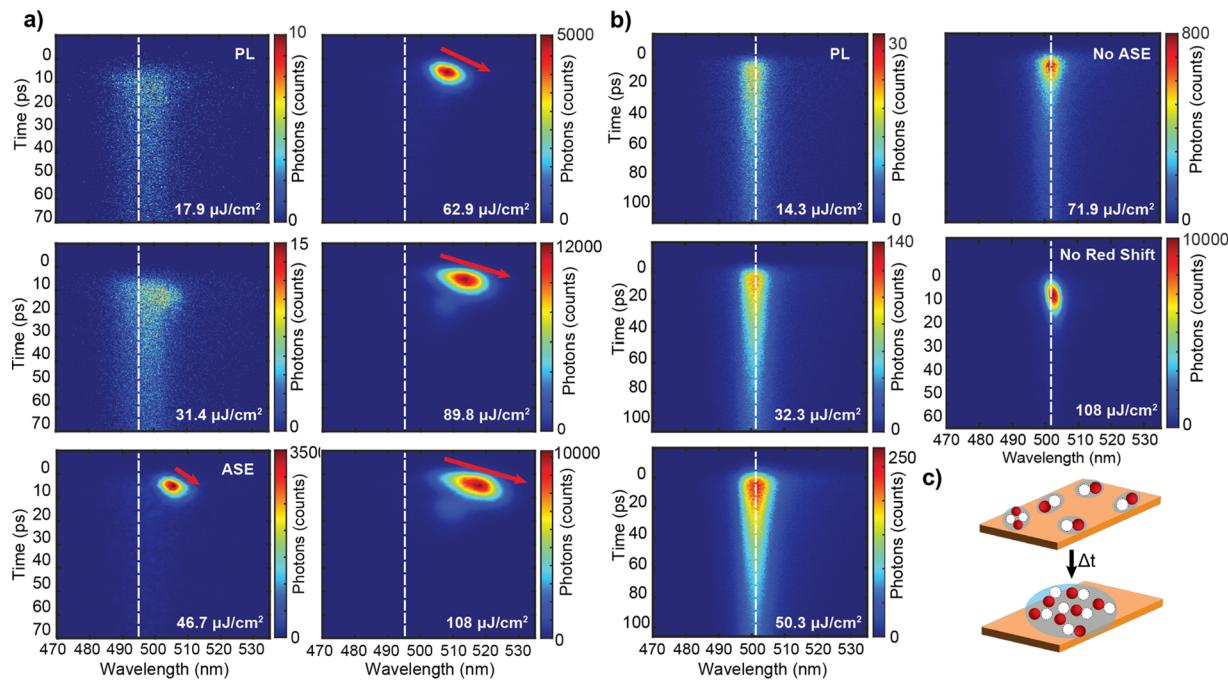


Figure 4. Time-resolved spectral dynamics at 10 K for neat and polymer-diluted 4 ML NPL films. (a, b) Streak camera dynamics recorded for a series of excitation fluences at 10 K both for (a) neat and (b) polymer-diluted 4-ML CdSe NPL films. Both films showed a decrease in emission lifetime when pump fluence is increased, however, only emission from the neat film shows emergence of a red-shifted feature, which appears to continue to red shift with delay time after the pump before it is depleted. Note that photon count scales differ with investigated pump fluence. (c) Within an intensely excited nanoplatelet, excitons form polyexciton quantum droplets owing to a binding energy in addition to that of the biexciton. Once formed, these can undergo amplified stimulated emission.

288 pumping of the polymer-diluted NPL films under identical or
 289 even more-intensely pumped conditions as above for neat films
 290 produced neither distinct biexcitonic ASE nor a detectable,
 291 red-shifted PE feature (Figure 2d,e). Emission intensity at
 292 three wavelengths that correspond to the center, blue, or red
 293 shoulder of the diluted NPL film emission appear in Figure 2f.
 294 Suppression of biexcitonic ASE is expected with NPL dilution
 295 because emitted photons experience a lower probability of
 296 encountering a population-inverted NPL which then impedes
 297 stimulated emission.⁴⁸ Absence of detectable red-shifted
 298 emission at high pump intensity in polymer-diluted NPL
 299 films, however, is perhaps surprising since one might expect
 300 such emission arises from spontaneous radiative recombination
 301 within each individual NPL conceivably upon Auger heating or
 302 from defect states such as surface traps. Rather, this
 303 suppression of red-shifted emission in diluted films points to
 304 an NPL-density dependent origin such as stimulated emission
 305 from PE states. Time-resolved spectroscopic investigation
 306 further bolsters this interpretation (*vide infra*).

307 **Temperature Dependence of Polyexciton Emission**
 308 **and Fluence-Dependent Red-Shifting.** For neat films, red-
 309 shifted PE emission is only observable at temperatures below
 310 200 K for the pump fluence range explored (Figure 3a–e).
 311 This observation is suggestive of a characteristic binding
 312 energy that, if exceeded thermally, reduces the population of
 313 the lower energy PE species. Such a picture is analogous to the
 314 equilibrium of free excitons and biexcitons,^{25,37} or similar to
 315 equilibrium of free carriers and excitons in bulk semi-
 316 conductors.⁴⁹ However, quantification of PE population such
 317 as with a Boltzmann distribution is challenging since
 318 partitioning into a bound PE population versus free exciton
 319 + biexciton is complicated by detection of PE states only thru
 320 amplified stimulated emission with unknown gain cross

321 sections. The stimulated emission detection itself is, of course,
 322 nonlinear with regard to population with competition between
 323 gain and loss channels. A polyexciton forms upon association
 324 of a biexciton and at least one other exciton, which we suggest
 325 can be crudely described by an attractive binding energy of
 326 around 17 meV based upon the ~200 K activation of the red-
 327 shifted stimulated emission, and such PE states are not
 328 observed at 298 K (where the latter corresponds to 25 meV of
 329 thermal energy). Polyexcitons appear to only weakly radiate
 330 spontaneously (because they are not observed in polymer-
 331 diluted NPL films) but apparently can undergo strongly
 332 stimulated emission processes provided that photons at this
 333 energy rapidly interact with other excited NPLs. Because the
 334 PE feature exhibits a binding energy and a continuous red shift
 335 with increasing pump fluence, attribution of the lower-energy
 336 ASE feature seems consistent with the characteristics of
 337 quantum droplets rather than an incompressible EHL.³³⁷ Furthermore,
 338 bandgap renormalization effects would not be
 339 expected to present such temperature sensitivity^{50,51} and trap
 340 state populations would not be expected to produce light
 341 amplification owing to large energy distributions combined
 342 with small oscillator strengths.³⁴²

We next evaluate the PE emission maximum at 640 μJ/cm²
 343 (not entirely arbitrarily but because it is the highest fluence
 344 measured that affords repeatable measurement and avoids
 345 sample damage) relative to the energy of biexciton ASE
 346 measured just above the threshold to quantify the difference
 347 output photon energy between ASE and PE emission. We
 348 examine this for both 4 and 5 ML CdSe neat films at a series of
 349 temperatures (Figure 3f, see also Figure S5 for studies of a 4
 350 ML neat film). The largest PE red-shifts relative to biexcitonic
 351 ASE measured at 5 K for the 640 μJ/cm² excitation fluence
 352 were 118 and 75.7 meV for 4 and 5 ML NPLs, respectively.
 353

354 Note that here we do not expressly compare the 4 and 5 ML
 355 NPL sample properties, but aim to convey that the observables
 356 are distinctly present in both NPL thicknesses.

357 **Light-Emission Dynamics and Transient Spectral**
 358 **Shifting.** Time- and wavelength-resolved emission for CdSe
 359 NPL samples at $T = 5$ K were investigated for both neat and
 360 polymer-diluted films. When detected within the plane of the
 361 film (in-plane = 90° excitation to detection angle), emission
 362 from neat films first emerges at redder wavelengths and then
 363 becomes progressively higher in energy over the course of 30
 364 to 40 ps (Figure S7). However, we note that the waveguided
 365 emission evaluated in this detection configuration propagates
 366 in a dispersive medium with a strong optical transition at
 367 higher energy (the 1S heavy hole exciton absorption). In
 368 particular, the wavelength-dependent refractive index of a neat
 369 CdSe film is higher at 540 nm (1.875) than at 555 nm
 370 (1.85).⁵² For the same excitation fluence conditions, but
 371 instead detected in the surface-normal direction relative to the
 372 film (180° relative to the pump beam, Figure 4a), bluer
 373 emission was found to precede the redder emission by about 8
 374 ps. This measurement configuration reduces the influence of
 375 optical dispersion within the film and suggests that initially
 376 produced free excitons subsequently give rise to lower energy
 377 species of biexcitons and polyexcitons as denoted by reduced
 378 emission energy.

379 The time scale required to observe decreasing emission
 380 energy after excitation conveys two processes. First, quantum
 381 droplets coalesce provided that the sample temperature is
 382 similar to or less than the polyexciton binding energy.
 383 Quantum droplets next become detectable owing to stimulated
 384 emission that decreases in energy as droplets continue to
 385 become larger until they abruptly depopulate. Just ~ 12 ps after
 386 arrival of the excitation pulse, no detectable red-shifted
 387 emission is detected as directly evaluated with a streak camera.
 388 Absence of longer-lived red-shifted emission is consistent with
 389 an amplified spontaneous emission process whereas, e.g.,
 390 spontaneous recombination from trap states would be
 391 expected to yield long-lived recombination dynamics that are
 392 not observed. Figure 4b shows that the same NPLs diluted in
 393 polymer for progressively higher excitation intensity decay
 394 increasingly rapidly (Tables 1 and 2) as multiple electron–hole

Table 1. Fitted Streak Camera Dynamics for 4 ML CdSe NPL Neat and Polymer Films at 10 K for a Series of Excitation Intensities

4 ML NPL neat film		4 ML NPL polymer film	
pump fluence ($\mu\text{J}/\text{cm}^2$)	decay constant (ps)	pump fluence ($\mu\text{J}/\text{cm}^2$)	decay constant (ps)
5.39	28.4 ± 2.1	5.39	74.3 ± 6.3
17.9	31.8 ± 1.0	16.1	60.9 ± 2.4
32.3	23.1 ± 0.6	32.3	54.8 ± 0.8
48.5	4.1 ± 0.04	48.5	44.0 ± 0.3
62.9	3.85 ± 0.04	71.9	21.6 ± 0.3
89.8	4.49 ± 0.03	89.8	31.0 ± 0.4
107.8	5.7 ± 0.04	107.8	6.53 ± 0.08

395 pairs are injected into individual particles but exhibit
 396 comparatively minor red-shifting associated with biexciton
 397 recombination and absence of detectable PE radiative
 398 recombination. Five ML NPL neat and diluted films respond
 399 similarly to the 4 ML films (Figure S9). Polyexcitons, thus,

Table 2. Fitted Streak Camera Dynamics for 5 ML CdSe NPL Neat and Polymer Films at 10 K for a Series of Excitation Intensities

5 ML NPL neat film		5 ML NPL polymer film	
pump fluence ($\mu\text{J}/\text{cm}^2$)	decay constant (ps)	pump fluence ($\mu\text{J}/\text{cm}^2$)	decay constant (ps)
180	40.7 ± 1.3	11	104 ± 2.2
270	4.87 ± 0.1	30	108 ± 1.6
360	3.6 ± 0.05	90	116 ± 1
500	4.5 ± 0.05	180	110 ± 0.8
700	6.1 ± 0.07	360	92.8 ± 0.6
		600	84.8 ± 0.5

400 seem to exhibit spontaneous recombination rates that are
 401 lower than biexcitons.

CONCLUSION

403 We have shown that the biexciton ASE threshold decreases
 404 appreciably with reduced temperature in 2D CdSe NPLs.
 405 Elevated pump fluence at reduced sample temperature for neat
 406 NPL films gives rise to significantly red-shifted emission that is
 407 consistent with stimulated emission from polyexcitons, which
 408 we further note is consistent with quantum droplet formation
 409 and a binding energy near ~ 17 meV. Light output in the form
 410 of both biexciton ASE and PE emissions is suppressed upon
 411 dilution in a polymer, which highlights NPL-density depend-
 412 ence for both processes. Time- and wavelength-dependent
 413 probing indicates that the scattered emission normal to the
 414 film initially occurs at higher energy and then rapidly red-shifts,
 415 provided the sample temperature is low enough, as quantum
 416 droplets form. These studies reveal stimulated emission
 417 processes originating from quantum droplet collective
 418 and permit pump-fluence-dependent tuning of optical
 419 amplifiers as well as a potential stepping stone in pursuit of
 420 excitonic Bose–Einstein condensates.

METHODS

422 **NPL Synthesis, Characterization, and Film Preparation.** Colloidal CdSe NPLs were synthesized using methods reported by Ithurria et al. and She et al. with minor modifications.^{2–4} Transmission electron microscopy was performed on studied NPLs and provide the average lateral dimensions of the particles (see Figure S1). NPLs were centrifuged into a pellet, redispersed in methyl-cyclohexane (optical density ~ 1.0 in a 1 mm path cell), and drop-casted onto a clean substrate. Polymer-diluted NPL films, where the polymer was poly(butyl methacrylate-*co*-isobutyl methacrylate), were produced by adding neat solution to 100 μL of polymer solution (5% weight in toluene), stirred for 10 min, and then cast as a film.

423 **Optical Experiments.** Films were mounted in a sample-in- vacuum helium cryostat and photoexcited using 400 nm, 35 fs pulses at a 100 Hz repetition rate that, for ASE measurements, were focused via a cylindrical lens to generate a ~ 2 mm wide by 0.27 mm tall stripe. Absorption cross sections of the samples at the pump wavelength of 3.1 eV were taken from the literature based upon particle dimensions. The product of the wavelength-specific absorption cross-section of a nanoparticle (σ , in cm^{-2} ; typically $\sim 1 \times 10^{-13} \text{ cm}^{-2}$ for a CdSe NPL⁴⁷) and the pump intensity (j , in photons/ cm^2/pulse) yield the average number of photons absorbed per nanoparticle ($\langle N \rangle = \sigma j$) corresponding to the number of initially generated excitons per particle. Except where noted, emission was collected within the plane of the film (90° to the pump) and directed either to a CCD or to a streak camera. Detection geometry instances that are noted was altered to examine emission at 180° relative to the pump beam with

449 reduced influence of temporal chirp within the dispersive medium of
450 the film.

451 ASSOCIATED CONTENT

452 Supporting Information

453 The Supporting Information is available free of charge at
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455 Nanocrystal synthesis and film preparation, static and
456 time-resolved photoluminescence method, transmission
457 electron microscopy, and static and time-resolved pump-
458 power-dependent emission measurements ([PDF](#))

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492 C.L.G. and film preparation was performed by N.E.W. and
493 R.D.S. Electron microscopy was performed by N.E.W. and Y.L.
494 Optical measurements and data analysis were performed by
495 N.E.W., M.R.W., and R.D.S. All authors contributed to the
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497 Notes

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