

1 **Climatology of Atmospheric Unstable Layers Revisited – A Corrigendum**

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10 ABSTRACT

11 We have published a recent paper on differences between temperature fluctuations of
12 various vertical scales in raw and processed US High-Resolution Radiosonde Data
13 (HVRD). In that paper, we note that the small-scale temperature fluctuations in the raw US
14 HVRD are significantly larger than those in the processed US HVRD and that those
15 small-scale temperature fluctuations are much larger during daytime than during nighttime.
16 We believe that this is due to the varying amount of solar radiation falling on the radiosonde
17 temperature sensor as the radiosonde instrument swings and rotates. In light of these new
18 results, we present revisions to some of our conclusions about the climatology of
19 atmospheric unstable layers. When we repeat our calculations of atmospheric unstable layers
20 using the processed US HVRD, we find the following. 1. The 0000/1200 UTC differences
21 in unstable layer occurrences in the lower stratosphere that were noted in our earlier paper
22 essentially disappear. 2. The “notch” in the deep tropics, where there is a relative deficiency
23 of thin unstable layers and a corresponding excess of thicker layers is still a feature when
24 processed data are analyzed, but the daytime “notch” is less marked when the processed data
25 were used. 3. The discontinuity in unstable layer occurrences, when there was a change in
26 radiosonde instrumentation, is still present when processed data are analyzed, but is
27 diminished from what it was when the raw data were analyzed.

28

29 SIGNIFICANCE STATEMENT

30 In a previous paper deriving the climatology of atmospheric unstable layers, we
31 emphasized several findings. We reexamine three of the main points of that paper when
32 processed US high vertical-resolution radiosonde data are analyzed instead of the raw data
33 used in that previous paper. We find the 0000/1200 UTC differences virtually disappear in
34 the new analysis. We find that the “notch” feature previously noted at Koror still exists, and
35 we find that the discontinuity in unstable layers, when radiosonde instrumentation is
36 changed, is diminished, but is still present in the new analysis.

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39 **1. Introduction**

40 Geller et al. (2021) showed some early results of analyses of atmospheric unstable
41 layers, where such layers are defined by $\frac{\partial \theta}{\partial z} < 0$, where θ is potential temperature, and z is
42 altitude. The data set they analyzed was the US 1-second High Vertical-Resolution
43 Radiosonde Data (HVRD), which had been used previously to derive turbulence
44 information (e. g., Ko et al., 2019), and those data were described in Geller et al. (2021) and
45 Ko et al. (2019). Geller et al. (2021) derived their results using raw data, meteorological
46 parameters derived from the radiosonde measurements while Ko et al. (2019) utilized the
47 processed data, which have been subjected to radiation corrections and smoothing. Radiation
48 corrections have been well documented (e. g., Dirksen et al., 2014), but the details of the
49 smoothing used in deriving the processed data are proprietary to the radiosonde
50 manufacturer and are unavailable to us. This being the case, Wang and Geller (2024)
51 analyzed the temperature fluctuations at various vertical scales in both the raw and
52 processed US HVRD. Some of their findings were the following.

- 53 1. The small-scale temperature fluctuations were larger in the raw HVRD than in
54 the processed HVRD.
- 55 2. The small-scale temperature fluctuations were much larger in daytime soundings
56 compared to those in nighttime soundings, those day/night differences being
57 smaller, but still present, in the processed data. Small-scale temperature
58 fluctuations were larger in the lower stratosphere than in the troposphere in both
59 the raw and processed data.
- 60 3. The discontinuity that was noted in unstable layer occurrences at a radiosonde
61 station when the instrumentation was changed, using raw HVRD, is also
62 present in the occurrences of small-scale temperature fluctuations. This
63 discontinuity in the occurrences of small-scale temperature fluctuations, when
64 raw HVRD were used, was larger in daytime soundings than in nighttime
65 soundings. There was also a similar, but smaller, discontinuity when processed
66 HVRD were used.
- 67 4. For larger vertical scale temperature fluctuations ($> 1,000$ m), the geographical
68 pattern of the root-mean-square (rms) temperature fluctuations very much
69 resemble those that have been previously been reported for gravity waves.

70 This is a corrigendum to Geller et al. (2021) in that, while the computations in this paper
71 are the same as in our earlier paper, our conclusions about atmospheric unstable layers over
72 the US are significantly altered when processed US HVRD are used instead of raw
73 HVRD.

74 The computational methods used in this paper are the same as those used in Geller et al.
75 (2021) except for the fact that processed US HVRD are analyzed instead of raw US
76 HVRD. That is to say, we have used the same algorithm of Wilson et al. (2010) and
77 Wilson et al. (2011) for rejecting spurious overturns existing due to “noise” in the data, and
78 we used the methods of Wilson et al. (2013) to account for the destabilizing effect of
79 moisture.

80 One of the principal conclusions of Geller et al. (2021) was that unstable layer
81 occurrences of vertical scale 10-400 m were greater at 0000 UTC in the western United
82 States and were greater at 1200 UTC in the eastern United States. Geller et al. (2021) also
83 noted the existence of a “notch” in unstable layer occurrences at Koror (7.3°N , 134.5°E) at
84 altitudes near 12 km, where there was a relative deficiency in thin unstable layers and an
85 accompanying excess of thicker unstable layers. Finally, Geller et al. (2021) noted a
86 discontinuity in the occurrences of unstable layers of thicknesses 10-400 m at Jacksonville,
87 FL when the radiosonde instrumentation at that station was changed. In the following we
88 will see how each of these three conclusions are changed when processed US HVRD are
89 used instead of raw US HVRD.

90 **2. 0000/1200 UTC Differences**

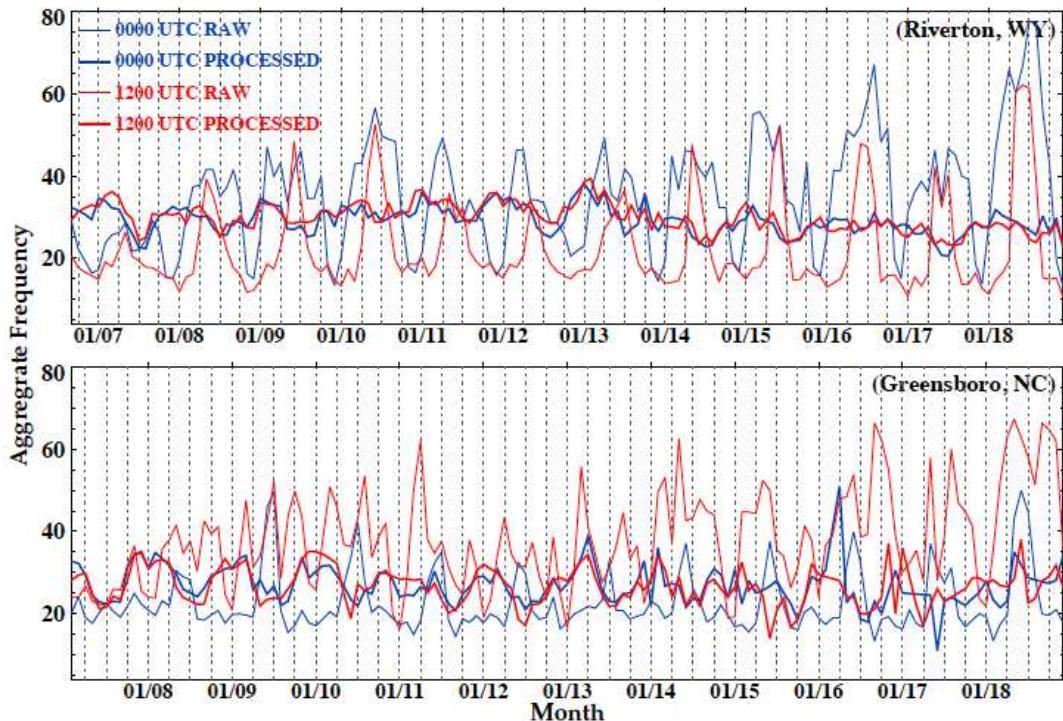
91 The top panel in figure 2 of Geller et al. (2021) showed the aggregate frequencies of
92 occurrence of unstable layers of thickness 10-400 m, occurring at altitudes 15-25 km at 0000
93 and 1200 UTC, at Riverton, Wyoming (43.06°N , 108.47°W), and the top panel of figure 4
94 of Geller et al. (2021) shows the same for Greensboro, North Carolina. Geller et al. (2021)
95 pointed out that those aggregate frequencies were greater at 0000 UTC than at 1200 UTC at
96 Riverton, while the opposite was true for Greensboro. Figure 5 of Geller et al. (2021) showed
97 that, in general, these aggregate frequencies for altitudes 15-25 km were larger at 1200 UTC
98 than at 0000 UTC for radiosonde stations in the eastern United States, while the opposite
99 was true for radiosonde stations in the western United States. The locations of Riverton, WY
100 and Greensboro were shown in that figure 5, so Geller et al. (2021) concluded that the

101 Riverton and Greensboro results shown in their figures 2 and 4 were a manifestation of the
102 general picture shown in their figure 5.

103 Figure 1 shows the aggregate frequencies for the occurrence of unstable layers of
104 thickness 10-400 m for altitudes 15-25 km for Riverton (top panel) and for Greensboro
105 (bottom panel) at 0000 and 1200 UTC when those calculations used raw US HVRD (thin
106 lines) and also when those calculations used the processed US HVRD (thick lines). It is
107 clear that the 0000/1200 UTC differences that were apparent when the raw data were
108 analyzed virtually disappear when the processed data were analyzed. Note that the aggregate
109 frequencies of unstable layers are often larger when the processed data were used than when
110 the raw data were used. We believe that this is due to our applying the methodology of
111 Wilson et al. (2010) and Wilson et al. (2011) to reject spurious unstable layers that arise
112 from noise in the data. Wang and Geller (2024) have shown that, in general, the trend-to-
113 noise ratio (tnr) for small-scale vertical temperature gradients is larger in the processed
114 HVRD than in the raw HVRD. This smaller tnr in the raw data leads to greater rejection
115 of small-scale overturnings when the raw data are used than when the processed data are
116 used. The greater rejections of small-scale overturnings less than 100 m when the raw data
117 are analyzed sometimes result in smaller aggregate frequencies for unstable thicknesses less
118 than 100 m when the raw data are used than when the processed data are used.

119 We show that this is the case in the following two figures. Figure 2 shows that UTC
120 differences are greatly diminished when the processed HVRD are analyzed relative to
121 when the raw HVRD are analyzed, and the number of occurrences are greatly diminished
122 for unstable layer thicknesses 100-400 m relative to the situation for the 10-400 m
123 thicknesses. Two other interesting features are also seen. Contrary to what was seen in figure
124 1, the aggregate frequencies at both 0000 and 1200 UTC are always less when the processed
125 data are used than when the raw data are used. The fact that the aggregate frequencies were
126 sometimes seen to be greater when the processed HVRD were used than when the raw
127 HVRD were used must have been due to a greater aggregate frequency of unstable layers
128 of thickness 10-100 m, and this was due to a greater number of the thin layers being discarded
129 in the raw data when the Wilson et al. (2010) and Wilson et al. (2011) methodology was
130 used. Also, although the 0000/1200 UTC differences are much smaller in figure 2 relative to
131 what is seen in figure 1, the 0000/1200 UTC difference in occurrences are in the same sense
132 regardless of whether the raw or processed HVRD are analyzed; that is to say, the 0000

133 UTC occurrences are systematically greater for Riverton, and the 1200 UTC occurrences are
134 systematically greater for Greensboro.



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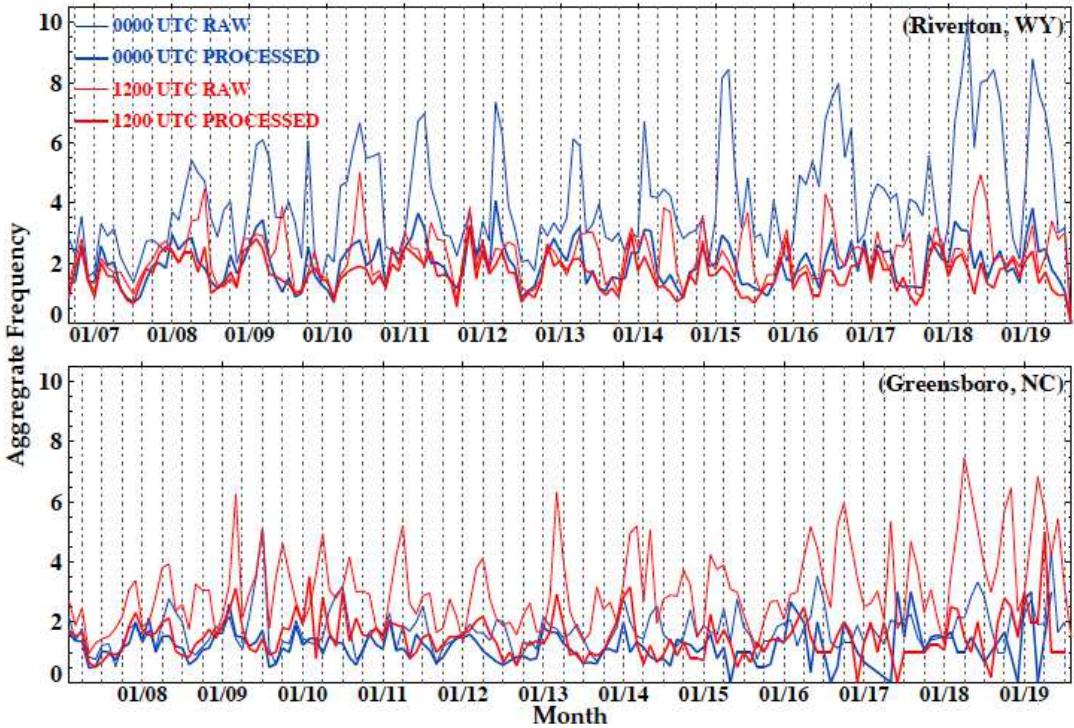
136 Figure 1. Time series for the aggregate frequencies of occurrence of unstable layers of
137 thicknesses 10-400 m at altitudes of 15-25 km at Riverton, WY (43.06 °N, 108.47
138 °W) for months since September, 2006 (top) and Greensboro, NC (36.08 °N, 79.95
139 °W) since February, 2007 (bottom) calculated with raw US HVRD (thin lines)
140 and processed US HVRD (thick lines) at 0000 UTC (blue) and 1200 UTC (red).
141 Vertical dashed lines indicate Januaries (at the year indicators), Aprils, Julys, and
142 Octobers.

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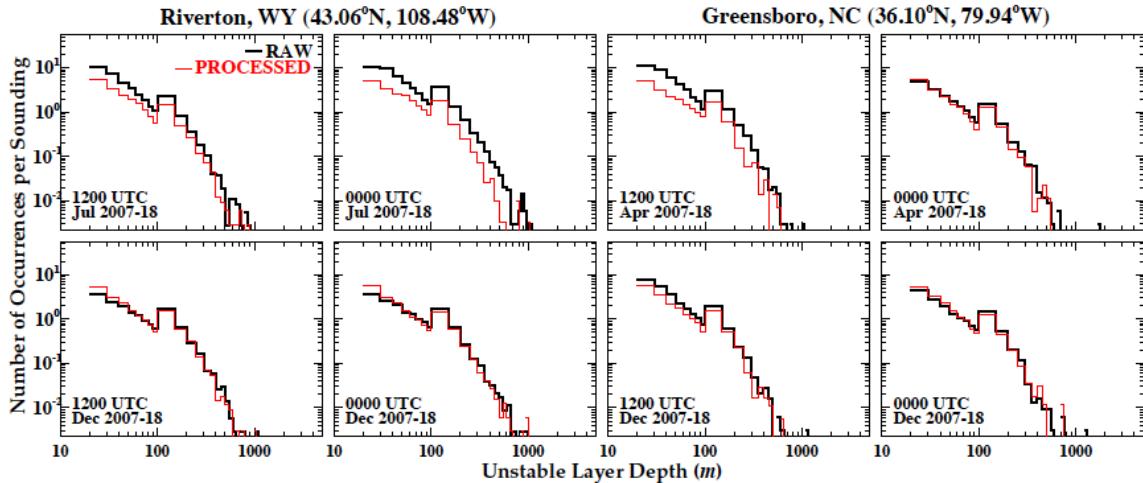
145 A more quantitative way to examine the differences in the occurrences of unstable layers
146 of different thicknesses is to look at the histograms showing the numbers of occurrences per
147 sounding of unstable layers for various vertical layer thicknesses.¹ This is shown in figure 3
148 for July and December at Riverton and April and December at Greensboro for the altitude
149 range 15-25 km for 0000 and 1200 UTC. We show results for this altitude range since Wang
150 and Geller (2024) have shown that the differences between temperature fluctuations in raw
151 and processed HVRRD profiles are largest in the stratosphere. Note that at Riverton the July
152 histograms show larger occurrences of unstable layers of all thicknesses when the raw data
153 were used. This is consistent with the larger aggregate frequencies seen during the summer
154 months in figure 1 at that station. In December at Riverton, however, a different situation is
155 seen. At both 0000 and 1200 UTC, larger occurrences are seen for layers 20-50 m, with
156 similar occurrences seen for larger unstable layer depths. This is consistent with the results
157 of figure 1 where the aggregate frequencies are less for the raw data than for the processed
158 data in the winter months. The July histogram results are also consistent with the results of
159 figure 2 where the aggregate frequencies for thicknesses 100-400 m are much larger in
160 summer when the raw data at 0000 UTC are used than when processed data are used with
161 the 1200 UTC differences being smaller. In winter, the differences in aggregate frequencies
162 when raw versus processed data are used are much smaller for thickness 100-400 m,
163 consistent with what is seen in the histograms. At Greensboro, again the histogram results
164 are consistent with what was seen in the aggregate frequency time series shown in figures 1
165 and 2.

¹ It should be noted that the histogram in figure 3 is plotted differently than in Geller et al. (2021) in that different intervals are used for thicknesses less than and greater than 100 m to emphasize the differences between results using raw and processed data for the thinner layers. This gives rise to a different slope of the histogram results for thicknesses less than and greater than 100 m.



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167 Figure 2. Same as figure 1, but for unstable layers of thicknesses 100-400 m.



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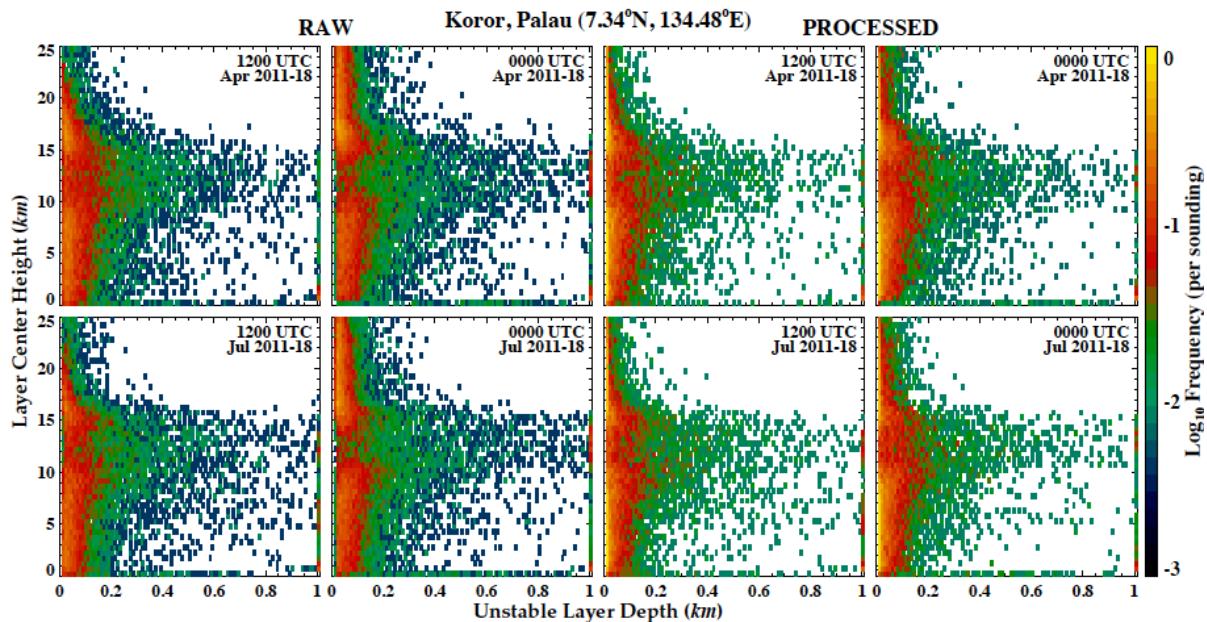
169 Figure 3. Histograms, showing numbers of occurrences per sounding of unstable layers of
170 various depths for July and December at Riverton, WY (left) and April and
171 December at Greensboro, NC (right) using raw data (black) and processed data
172 (red) at 00 and 12 UT. Note that different intervals have been used for unstable
173 layer thicknesses less than 100 m than for thicknesses greater than 100 m.

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175

176 3. The “notch” at Koror

177 Figure 4 shows plots of \log_{10} of the frequency of the occurrences of unstable layers of
 178 various depths as a function of altitude using raw HVRRD (left panels) and processed
 179 HVRRD (right panels) for April and July for 0000 and 1200 UTC at Koror (7.34°N , 134.48°E). Geller et al. (2021) pointed out the existence of a “notch” at altitudes around 12 km at
 180 Koror, where this “notch” was characterized by a deficiency of thin unstable layers and a
 181 corresponding excess of thicker layers at those altitudes. It should be noted that 1200 UTC is
 182 nighttime, and 0000 UTC is daytime at Koror. It is clear that this “notch” is more obvious at
 183 0000 UTC (daytime) when the raw HVRRD were used than when the processed HVRRD
 184 were used, particularly in the relative deficiency of thin layers, while the 1200 UTC
 185 (nighttime) pictures of the notch using raw HVRRD looked relatively more similar to the
 186 results using the processed HVRRD. Interestingly, the excess in thicker unstable layers
 187 concentrated at altitudes near 12 km was more obvious when the processed HVRRD were
 188 used, both at 0000 and 1200 UTC. Thus, this “notch” feature was present when either the
 189 raw or processed HVRRD were used. We believe that two influences on the thicknesses of
 190 unstable layers are seen in figure 4. Grise et al. (2010) have pointed out the existence of a
 191 minimum in atmospheric stability in the deep tropics. Furthermore, Gettelman and Forster
 192 (2002) and Fueglistaler et al. (2009) had earlier associated this stability minimum with
 193

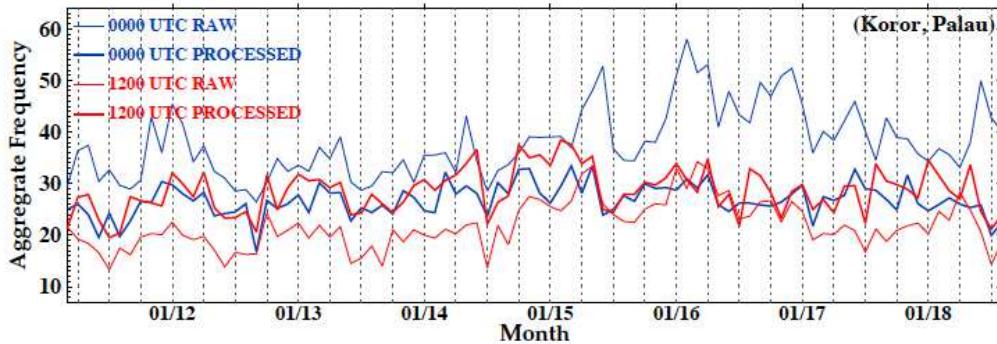


194
 195 Figure 4. Plots showing \log_{10} frequency of occurrence per sounding of the
 196 depth of unstable layers with altitude at Koror (7.3°N , 134.5°E) for April and July
 197 where 1200 UTC is at night and 0000 UTC is daytime. Left – results using raw
 198 HVRRD. Right – results using processed HVRRD.

199 convective cloud outflow. This convective cloud outflow likely advects cloud top
200 turbulence, which accounts for the greater number of thick unstable layers at Koror at
201 altitudes around 12 km. This turbulence may act to entrain the thinner unstable layers at
202 those latitudes, but we believe that another influence is leading to the apparent depletion of
203 thin unstable layers at those altitudes, and that is the application of the Wilson et al. (2010)
204 and Wilson et al. (2011) methodology to discard spurious overturnings that arise from noise
205 in the data. The Wilson et al. (2010) and Wilson et al. (2011) methodology acts to discard
206 more of the thinner unstable layers when there is a smaller tnr. Clearly in the region of the
207 stability minimum, the gradient in potential temperature is smallest, leading to more
208 discarding of thin unstable layers. This is consistent with what is seen in figure 4, Wang and
209 Geller (2024) have shown that spurious small-scale temperature fluctuations are greater in
210 daylight than at night. This is consistent with a less distinct “notch” being seen at Koror at
211 1200 UTC (nighttime) than at 0000 UTC (daytime) when the raw data are used.

212 In figure 4, more frequent thicker unstable layers (thicknesses greater than about 400 m)
213 appear present in the 10-14 km altitude region (i. e., the “notch” region) when the processed
214 HVRD are used, as manifested by the preponderance of green pixels in the processed plots
215 in that altitude region. We note that Wilson et al.’s (2011) figure 7 showed a greater
216 frequency of thicker overturns in low-resolution (6-7 m) standard radiosonde data than in
217 high-resolution (10-20 cm) balloon data. This is likely due to small-scale overturnings
218 disrupting the thicker unstable layers, thereby breaking those thicker overturns into a
219 number of smaller overturns. This is also consistent with the results in Wilson et al. (2010).

220 Geller et al.’s (2021) figure 9 showed time series of the aggregate frequencies of
221 unstable layers of thicknesses 10-400 m occurring between 15-25 km at Koror. They noted
222 that there were more unstable layers of those thicknesses at 0000 UTC than at 1200 UTC
223 and also that there appeared to be a secular increase in layers of those thicknesses after 2014.
224 Figure 5 shows those results both when the raw HVRD were used as in Geller et al. (2021)



225
 226 Figure 5. Time series of monthly aggregate frequencies of unstable layers of thicknesses 10-
 227 400 m at Koror at 0000 UTC and 1200 UTC, where the starting month is March,
 228 2011. As before, 0000 UTC results are in blue, 1200 UTC results are in red, thin
 229 lines show results from raw data, and thick lines are from processed data.

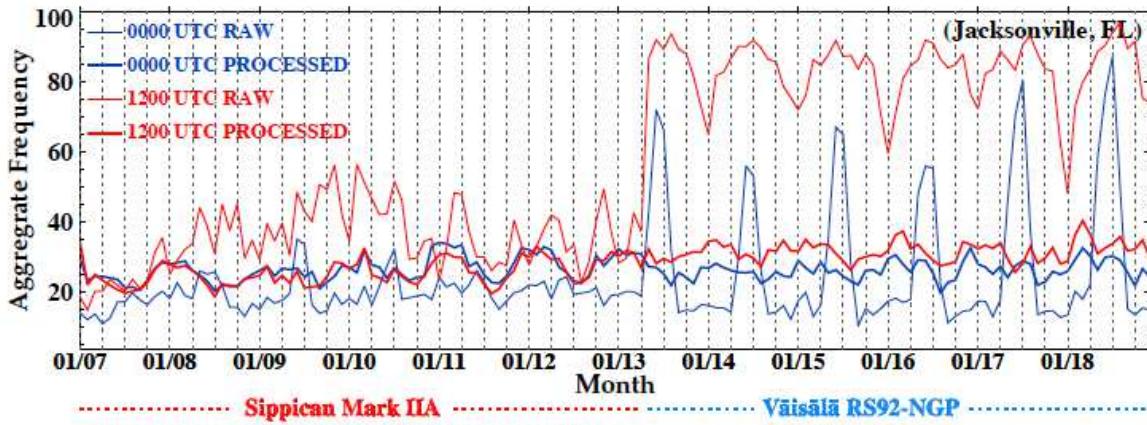
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231 and when the processed HVRD were used. Note that the 0000/1200 UTC differences are
 232 greatly diminished when the processed data were analyzed, and the secular increases in the
 233 occurrences of those layers are no longer present when the processed HVRD are used.
 234 Also, it is interesting to note that the 0000 UTC plots show that while the aggregate
 235 frequencies of unstable layers of thickness 10-400 m in the stratosphere are often larger
 236 when the raw HVRD are used, the calculations with the processed HVRD often show
 237 larger aggregate frequencies of unstable layers of thickness 10-400 m in the stratosphere at
 238 1200 UTC. Histograms for the numbers of unstable layers of various thicknesses per
 239 sounding (not shown) are consistent with this.

240

241 **4. Discontinuity when radiosonde instrumentation was changed**

242 Figure 6 shows the time series for the aggregate frequencies of the occurrences of
 243 unstable layers of thicknesses 10-400 m in the stratosphere (15-25 km) at Jacksonville,
 244 Florida. A clear discontinuity is seen in early 2013 in the raw data results, when there was a



245

246 Figure 6. Time series of monthly aggregate frequencies of unstable layer thicknesses

247 10-400 m in the 15-25 km altitude region at Jacksonville, FL at 0000 UTC and
 248 1200 UTC, where the starting month is January, 2007. Blue lines show results at
 249 0000 UTC, and red lines show results at 1200 UTC. Thin lines show results using
 250 raw data, and thick lines show results using processed data.

251 change in radiosonde instrumentation from the Sippican Mark IIa to the Väisälä RS92-NGP.
 252 Geller et al. (2021), while noting this discontinuity, did not give any explanation for its
 253 cause. In light of the Wang and Geller (2024) paper, we believe that this is a result of the
 254 differing amount of spurious small-scale temperature fluctuations when different radiosonde
 255 instruments are used. These results are consistent with the findings of Wang and Geller
 256 (2024) who showed that small-scale temperature fluctuations are larger in raw HVRD than
 257 in processed HVRD. Wang and Geller (2024) also showed that the day/night differences in
 258 those small-scale temperature fluctuations are smaller when processed HVRD are used
 259 than when raw HVRD are used. Also as mentioned in the previous section, Wilson et al.
 260 (2010) showed that spurious small-scale temperature fluctuations can affect the calculated
 261 statistics for larger-scale unstable overturnings, or unstable layers. Wang and Geller (2024)
 262 hypothesized that the varying sunlight falling on radiosonde temperature sensors are likely
 263 the cause of much of these small-scale temperature fluctuations as the temperature sensors
 264 experience different sunlight exposure as the instrument rotates and swings, so it is
 265 reasonable to assume that the different temperature sensors used by different radiosonde
 266 manufacturers might have different responses to this. This discontinuity is diminished when
 267 the processed HVRD are used, but it is not eliminated. It appears that the data processing
 268 was much more effective during the period when the Sippican Mark IIa instrument was

269 being used in that the 0000/1200 UTC differences are diminished, but not eliminated. Also,
270 note that the number of unstable layers occurrences at 1200 UTC is much less when the
271 processed data were used. Explaining the causes behind the greater differences in the
272 aggregate frequencies of the unstable layers found when the Sippican Mark IIa instrument
273 was used relative to those when the Väisälä RS92-NGP was used instrument was used will
274 likely require understanding both the responses of those temperature sensors to varying
275 radiation and the smoothing used in deriving the processed data.²

276 **5. Summary and Conclusions**

277 Geller et al. (2021) presented several results on atmospheric unstable layers, where
278 their calculations were performed using raw US HVRD. Wang and Geller (2024) have
279 shown that spurious temperature fluctuations at small vertical scales are present in raw US
280 HVRD, particularly during daytime. They argue that much of those spurious small-scale
281 temperature fluctuations are due to the varying solar radiation falling on the radiosonde
282 temperature sensor so they expect that those spurious small-scale vertical temperature
283 fluctuations will be different for different radiosonde instruments. Wang and Geller (2024)
284 show that the small-scale temperature variations are smaller by about a factor of two in the
285 processed HVRD relative to the raw HVRD and that the 0000/1200 UTC differences in
286 those temperature fluctuations are also much smaller in the processed HVRD, but are still
287 present. Therefore, we conclude that the smoothing employed in the processed HVRD
288 diminishes, but does not eliminate the spurious temperature fluctuations. Given this
289 situation, we examine how the conclusions in Geller et al. (2021) are changed when their
290 calculations are done using processed instead of raw HVRD.

291 Our principal findings were the following.

² We note that there was a change in instrumentation from the Sippican Mark IIA to the Lockheed Martin LMS-6 on 05 April 2015 0000 UTC at Koror. This likely accounts for the discontinuity seen in figure 5 around mid-2015.

292 1. The 0000/1200 UTC differences in unstable layer occurrences that were seen
293 over the contiguous United States in Geller et al. (2021) were largely a
294 consequence of the day-night differences in spurious small-scale temperature
295 fluctuations in the raw US HVRD, and those day-night differences largely
296 disappeared when the processed US HVRD were used.

297 2. The “notch” in unstable layer occurrences that was seen at Koror, in the deep
298 tropics, where there are less thin unstable layers and more thicker unstable layers
299 at altitudes around 12 km is less prominent, but still present, when the daytime
300 processed HVRD are analyzed compared to what was seen when the raw data
301 were used. This “notch” feature is similar in nighttime soundings when either the
302 raw or processed US HVRD were used.

303 3. The discontinuity in unstable layer occurrences noted in Geller et al. (2021),
304 accompanying a change in radiosonde instrumentation, when the raw HVRD
305 were analyzed is diminished, but not eliminated, when the processed HVRD
306 were analyzed. One cause of this discontinuity appears to be the different
307 responses to the varying solar radiation experienced when the different
308 temperature sensors swing and/or rotate during radiosonde ascent.

309

310 The results of this paper illustrate some of the cautions that should be exercised when
311 analyzing raw US HVRD, and to a lesser extent processed US HVRD. More specifically,
312 the results of this paper indicate that the spurious temperature fluctuations in HVRD, and
313 their day/night differences can affect determinations of unstable layers, or the turbulent
314 overturnings with which Thorpe analysis of turbulence begins. This is particularly the case
315 when raw HVRD, and to a lesser extent processed HVRD, are used. Thus, caution should
316 be exercised when comparing Thorpe analysis of turbulence from the HVRD obtained with
317 different radiosonde instruments.

318

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323 of the World Climate Research Programme (WCRP) in encouraging this research.

324

325 *Data Availability Statement.*

326 Radiosonde data analyzed in this study were obtained from the U.S. National Oceanic
327 and Atmospheric Administration National Centers for Environmental
328 Information: <ftp://ftp.ncdc.noaa.gov/pub/data/ua/>. Copies of the diagnostic software used for
329 the analysis of this paper can be obtained by contacting Dr. Ling Wang at lwang@gats-
330 inc.com.

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