

Absolute Dimensions of the Interferometric Binary HD 174881: A Test of Stellar Evolution Models for Evolved Stars

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Abstract

We report high-resolution spectroscopic monitoring and long-baseline interferometric observations with the Palomar Testbed Interferometer (PTI) of the 215 day binary system HD 174881 (K1 II-III), composed of two giant stars. The system is spatially resolved with the PTI, as well as in archival measurements with the CHARA Array. Our analysis of these observations, along with an analysis of the spectral energy distribution, have allowed us to infer accurate values for the absolute masses ($3.367^{+0.045}_{-0.041}$ and $3.476^{+0.043}_{-0.043} M_{\odot}$), radii (34.0 ± 1.3 and $22.7 \pm 1.8 R_{\odot}$), effective temperatures (4620 ± 100 and 4880 ± 150 K), and bolometric luminosities of both components, as well as other properties including the orbital parallax (distance). These provide valuable tests of stellar evolution models for evolved stars, which are still relatively uncommon compared to the situation for main-sequence stars. We find generally good agreement of all of these properties of HD 174881 with two sets of recent models (MIST and PARSEC) at compositions near solar, for ages of 255–273 Myr. We also find evidence of an infrared excess, based largely on the flux measurements from IRAS at 60 and 100 μ m.

Unified Astronomy Thesaurus concepts: Interferometric binary stars (806); Spectroscopic binary stars (1557); Stellar evolutionary models (2046); Giant stars (655); Stellar evolution (1599)

Materials only available in the *online version of record*: machine-readable tables

1. Introduction

Stellar evolution theory has had remarkable success in reproducing the observed properties of stars over much of the hydrogen-burning main sequence (see, e.g., J. Andersen 1991a; G. Torres et al. 2010). This has been made possible by significant advances in our knowledge of stellar physics, aided by the ever-growing observational constraints on models provided by binary systems. Those objects allow direct and precise determinations of their component masses (the most fundamental stellar property), as well as their radii, temperatures, chemical compositions, and other important properties. Traditionally, the best measurements have been made in double-lined eclipsing systems, although many spectroscopic-astrometric binaries have provided valuable information as well.

Models for post-main-sequence stars, on the other hand, are somewhat less secure, due in part to the fewer empirical constraints currently available. Binaries with well-detached giant or subgiant components, as needed for meaningful tests of theory, are much less common compared to their main-sequence counterparts. To accommodate the larger stars, the orbits necessarily have longer periods, which makes eclipses less likely. In favorable cases, the stars can be spatially resolved by astrometric techniques, such as speckle interferometry or long-baseline interferometry. When complemented by spectroscopy, if needed, this also provides a way to

determine the component masses, along with the orbital parallax.

Examples of binaries with post-main-sequence components that have provided valuable constraints on stellar evolution theory include, among others, the eclipsing systems TZ For (J. Andersen et al. 1991b; A. Gallenne et al. 2016) and HD 187669 (K. G. Helminiak et al. 2015), the astrometric-spectroscopic binary Capella (α Aur; G. Torres et al. 2009; M. Weber & K. G. Strassmeier 2011; G. Torres et al. 2015), and nearly two dozen other eclipsing systems in the Milky Way and in the Magellanic Clouds (e.g., D. Graczyk et al. 2014, 2018, 2020; D. M. Rowan et al. 2024).

In this paper, we report an analysis of the astrometric-spectroscopic binary HD 174881 (HR 7112; K1 II–III, $V=6.18$), a well-detached system in which both components are giants. It was discovered spectroscopically by P. N. Appleton et al. (1995), who presented a double-lined orbit with a period of 215 days and a small eccentricity of $e=0.141$. For this study, we have obtained additional, higher-resolution spectroscopic observations at the Center for Astrophysics (CfA), which have allowed us to improve the orbit significantly. We also pursued the object with the Palomar Testbed Interferometer (PTI), and have successfully spatially resolved the binary for the first time. The combination of these measurements has allowed us to infer many properties of the system that we use below, to provide stringent constraints on models for the giant phase.

The layout of our paper is as follows. In Section 2 we report our new spectroscopic observations of HD 174881, and report also other radial-velocity measurements from the literature that we incorporate into our analysis. Section 3 describes our interferometric observations with the PTI, as well as additional archival interferometric observations from the Center for High



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Angular Resolution Astronomy (CHARA) Array that also resolve the binary. Section 4 then presents our analysis of the spectral energy distribution of the system, from which we infer the individual absolute luminosities of the components and other properties. In Section 5 we combine the spectroscopic and astrometric measurements to derive the 3D orbit. A comparison of the system properties against models of stellar evolution is given in Section 6. Our conclusions are drawn in Section 7.

2. Spectroscopic Observations and Reductions

Our observations of HD 174881 at the CfA were conducted with an echelle spectrograph on the 1.5 m Wyeth reflector at the (now closed) Oak Ridge Observatory (Massachusetts, USA), and occasionally also with a nearly identical instrument on the 1.5 m Tillinghast reflector at the F. L. Whipple Observatory (Arizona, USA). A single echelle order spanning 45 Å was recorded with intensified photon-counting Reticon detectors at a central wavelength of 5187 Å, which includes the Mg I b triplet. The resolving power of these instruments is $\lambda/\Delta\lambda \approx 35,000$. A total of 81 spectra were obtained from 2000 February to 2004 July, with signal-to-noise ratios of 47–75 per resolution element of 8.5 km s^{-1} .

Radial velocities for the two components were derived with the two-dimensional cross-correlation algorithm TODCOR (S. Zucker & T. Mazeh 1994), which allows velocities to be obtained reliably even when the spectral lines are blended. This technique uses two templates, one for each component of the binary. They were selected from an extensive library of calculated spectra based on model atmospheres by R. L. Kurucz (see B. Nordström et al. 1994; D. W. Latham et al. 2002), and a line list manually tuned to better match real stars. These calculated spectra are available for a wide range of effective temperatures (T_{eff}), projected rotational velocities ($v \sin i$), surface gravities ($\log g$), and metallicities. Experience has shown that the radial velocities are most sensitive to the rotational velocity and temperature adopted, and less dependent on surface gravity and metallicity. Consequently, we first determined the optimum template for each star from grids of cross-correlations over broad ranges in T_{eff} and $v \sin i$, seeking to maximize the average correlation value weighted by the strength of each exposure. The metallicity was held at the solar value, and surface gravities were set to values appropriate for giant stars. Subsequently, we explored the possibility of determining the $\log g$ values as well, even though this has usually been very difficult to do for double-lined spectroscopic binaries. We repeated the temperature and rotational velocity determinations at fixed values of $\log g$ from 0.5 to 4.5 for each star and found that there was a distinct preference for surface gravities near 2.0 for both. Interpolation yielded the final values of $\log g = 1.9 \pm 0.2$ for the brighter of the two stars (hereafter star A), which turns out to be the less massive one in the system, and $\log g = 2.0 \pm 0.3$ for the other (star B). The effective temperatures we determined for the two components are 4620 ± 100 and 4880 ± 150 K, respectively. The rotational velocities that give the highest average correlation are 7 ± 2 for star A and $8 \pm 3 \text{ km s}^{-1}$ for star B. However, we caution that these values may well be overestimated, as they are based on a comparison with synthetic spectra computed for a macro-turbulent velocity $\zeta_{\text{RT}} = 1 \text{ km s}^{-1}$ (the only value available in our template library) that is more appropriate for dwarfs than giants. The $v \sin i$ values we have derived may simply be

Table 1
CfA Radial Velocity Measurements for HD 174881

HJD (2,400,000+)	Year	Phase	RV_A (km s^{-1})	RV_B (km s^{-1})
51596.9077	2000.1421	0.8531	-1.10 ± 0.48	-33.98 ± 0.55
51611.8966	2000.1832	0.9227	-10.87 ± 0.47	-27.10 ± 0.53
51627.8306	2000.2268	0.9968	-23.21 ± 0.45	-14.96 ± 0.51
51665.8192	2000.3308	0.1734	-40.98 ± 0.47	2.67 ± 0.53
51690.7850	2000.3991	0.2895	-35.74 ± 0.41	-1.92 ± 0.46

Note. Orbital phases were calculated using the ephemeris in Table 6. Star A is the less massive star.

(This table is available in its entirety in machine-readable form in the [online article](#).)

compensating to some extent for the increased line broadening from macroturbulence that is more common in more luminous stars such as these. Indeed, J. R. De Medeiros & S. Udry (1999) have reported a rotational broadening of approximately 1 km s^{-1} for both components of HD 174881. To measure the radial velocities, we adopted templates from our library with parameters nearest to those reported above. The stability of the zero-point of our velocity system was monitored by means of exposures of the dusk and dawn sky, and small run-to-run corrections were applied in the manner described by D. W. Latham (1992).

In addition to the radial velocities, we derived the spectroscopic light ratio between the two stars following S. Zucker & T. Mazeh (1994). We obtained $(F_B/F_A)_{\text{sp}} = 0.752 \pm 0.011$, corresponding to a brightness difference of $\Delta m = 0.31 \pm 0.02$ mag at the mean wavelength of our observations (5187 Å). Star A is, therefore, brighter and cooler, but less massive than star B.

Due to the narrow wavelength coverage of the CfA spectra, there is the potential for systematic errors in the velocities resulting from lines of the stars moving in and out of the spectral window with orbital phase (D. W. Latham et al. 1996). These errors are occasionally significant, and experience has shown that this must be checked on a case-by-case basis (see, e.g., G. Torres et al. 1997, 2000). For this, we performed numerical simulations in which we generated artificial composite spectra by adding together synthetic spectra for the two components, with Doppler shifts appropriate for each actual time of observation, computed from a preliminary orbital solution. The light ratio adopted is that reported above. We then processed these simulated spectra with TODCOR in the same manner as the real spectra, and compared the input and output velocities. The differences were all well below 1 km s^{-1} . Nevertheless, we applied these differences as corrections to the raw velocities, and the final velocities including these adjustments are given in Table 1. Similar corrections were derived for the light ratio, and are already accounted for in the value listed above.

In addition to our own velocities of HD 174881, a data set of similar quality was reported by J. R. De Medeiros & S. Udry (1999), obtained with the CORAVEL spectrometer on the 1 m Swiss telescope at the Haute-Provence Observatory (France). Separate spectroscopic orbital solutions with our data and those of J. R. De Medeiros & S. Udry give consistent velocity semiamplitudes. We have therefore incorporated the CORAVEL data into our analysis below.

Table 2
PTI Visibility Measurements for HD 174881

JD – 2,400,000	Year	Phase	λ (μm)	V^2	u (m)	v (m)
51667.9231	2000.3365	0.7637	2.2225	0.1191 ± 0.0100	–59.36425	–92.01252
51667.9254	2000.3365	0.7641	2.2215	0.1209 ± 0.0100	–58.81588	–92.42476
51667.9466	2000.3366	0.7680	2.2170	0.1356 ± 0.0116	–53.18509	–96.03746
51667.9666	2000.3367	0.7617	2.2246	0.2007 ± 0.0231	–47.02468	–99.07473
51677.9241	2000.3639	0.5891	2.2342	0.4462 ± 0.0219	–51.78284	–96.79841

Note. Orbital phases were calculated using the ephemeris in Table 6. The λ values correspond to the effective (flux-weighted) center-band wavelengths of the PTI passband.

(This table is available in its entirety in machine-readable form in the [online article](#).)

3. Interferometric Observations

3.1. PTI

Near-infrared, long-baseline interferometric measurements of HD 174881 and calibration sources were conducted with the PTI (M. M. Colavita et al. 1999) in the H and K bands ($\lambda \sim 1.6$ and $\sim 2.2 \mu\text{m}$, respectively) between 2000 and 2006. The maximum PTI baseline (110 m) provided a minimum K -band fringe spacing of approximately 4 mas, making the HD 174881 system readily resolvable.

The PTI interferometric observable used for these measurements is the fringe contrast or “visibility” (specifically, the power-normalized visibility modulus squared, or V^2) of the observed brightness distribution on the sky. HD 174881 was typically observed in conjunction with calibration objects, and each observation (or scan) was approximately 130 s long. As in previous publications, PTI V^2 data reduction and calibration follow standard procedures described by M. Colavita et al. (2003) and A. F. Boden et al. (1998), respectively. Observations of HD 174881 and associated calibration sources (HD 173667 and HD 182488) resulted in 466 calibrated K -band visibility scans on a total of 76 nights spanning a period of nearly 6 yr, or about 10 orbital periods. The measurements are listed in Table 2.

3.2. CHARA

The CHARA Array is the world’s longest baseline optical/infrared interferometer, with six 1 m telescopes spread across Mt. Wilson, California (T. A. ten Brummelaar et al. 2005). The maximum baseline of 330 m affords an angular resolution of $\Theta \sim \lambda/(2B_{\text{max}}) = 0.5$ mas, when observing in the near-infrared H band ($\lambda \sim 1.65 \mu\text{m}$).

HD 174881 was observed in the H band on the nights of UT 2007 July 4 and UT 2007 July 7, with the (then) recently commissioned Michigan InfraRed Combiner (MIRC; J. D. Monnier et al. 2004). At that time, MIRC could combine light from any four CHARA telescopes, measuring six baselines and four closure phases simultaneously. These archival data were processed with an IDL pipeline that used conventional Fourier Transform techniques to extract the visibility and phases from the fringes created in the image plane. The calibrated data were saved in the OI-FITS format (T. A. Pauls et al. 2005), and will be deposited with the OI Database hosted at the Jean-Marie Mariotti Center.⁵

The first night of data (UT 2007 July 4) was rather limited, including only three CHARA telescopes (S1-W1-W2) and using the calibrator γ Lyr (uniform-disk angular diameter $\phi_{UD} = 0.737 \pm$

Table 3
CHARA Measurements for HD 174881

MJD	UT Date	θ (deg)	ρ (mas)	σ_{maj} (mas)	σ_{min} (mas)	ψ (deg)
54285.326	2007 July 4	315.1	3.09	0.216	0.04	45.1
54288.250	2007 July 7	320.64	3.051	0.015	0.0149	50.64

Note. Columns σ_{maj} and σ_{min} represent the major and minor axes of the 1σ error ellipse for each measurement, and ψ gives the orientation of the major axis relative to the direction to the north. Position angles are referred to the International Celestial Reference Frame (effectively J2000).

0.15 mas). The second night (UT 2007 July 7) had more and better quality data using four telescopes (S1-E1-W1-W2), with σ Cyg as the primary calibrator ($\phi_{UD} = 0.54 \pm 0.02$ mas). Calibrator diameter estimates were based on a combination of an internal MIRC calibrator study (unpublished) and visible-light measurements with the PAVO instrument (V. Maestro et al. 2013).

Fitting simultaneously for binary separation, flux ratio, and component diameters allowed us to measure the sizes of the individual components of HD 174881. Using only the data from the higher-quality UT 2007 July 7 data set, we measured uniform-disk diameters of 0.817 ± 0.030 mas for star A, 0.50 ± 0.05 mas for star B, and a flux ratio (B/A) of 0.458 ± 0.003 in the H band. Table 3 contains the measured separations and position angles between the components from both dates. Note that the component sizes from UT 2007 July 7 were used as fixed values for fitting the binary model for UT 2007 July 4, as the earlier and smaller data set could not constrain the sizes on its own.

While model fitting is the most reliable and precise way to characterize the MIRC data, we also produced an image reconstruction of HD 174881 using the MACIM algorithm (M. J. Ireland et al. 2006). Because of the highly sparse uv coverage, we used an image prior of two Gaussians (with FWHM of 0.5 mas) centered on the expected locations of the stars based on modeling. We further employed a “uniform disk” regularizer, which is the ℓ_1 -norm of the spatial gradient of the image, first described by F. Baron et al. (2014). Figure 1 shows the MACIM image along with diameter circles from the model fitting. The agreement between model and image is excellent. A more detailed comparison between the observations and the model is provided in the [Appendix](#).

4. Spectral Energy Distribution

A spectral energy distribution (SED) analysis of the HD 174881 system was used to infer the radiometric

⁵ <https://jmmc.fr>

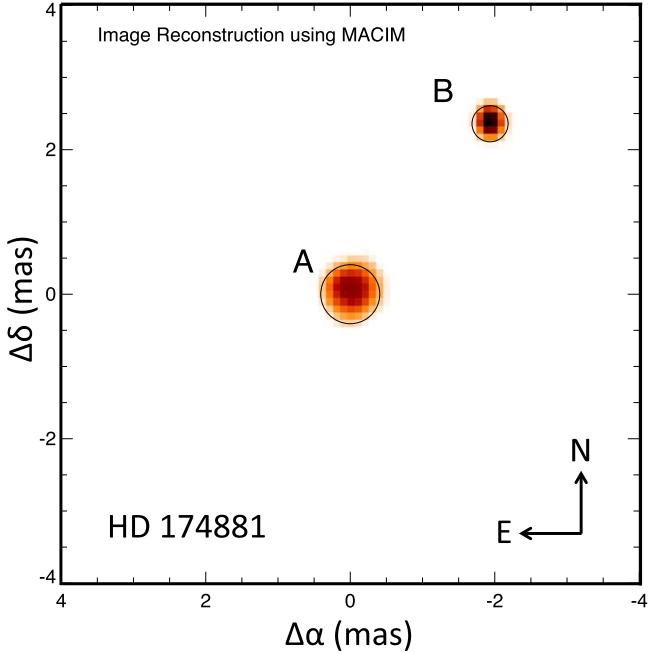


Figure 1. Image reconstruction of HD 174881 from the MIRC data of UT 2007 July 7, using the MACIM algorithm. The location and uniform diameters from the model-fitting procedure are overlaid.

parameters (e.g., effective temperature, bolometric flux f_{bol} , and eventually luminosity, when combined with system distance) for each of the components. Flux inputs to the SED modeling presented here are the large collection of archival combined-light photometry and flux measurements available from the literature, in the following photometric systems: Johnson (J.-C. Mermilliod 1987), David Dunlap Observatory (DDO; R. D. McClure & W. T. Forrester 1981), Straizys (V. Straizys et al. 1989), Two Micron All Sky Survey (2MASS; R. M. Cutri et al. 2003),⁶ AKARI (H. Murakami et al. 2007), Wide-field Infrared Survey Explorer (WISE; R. M. Cutri et al. 2012), and IRAS (C. A. Beichman et al. 1988). Additionally, we used the Gaia BP/RP low-dispersion spectra (Gaia Collaboration et al. 2023), with corrections as recommended by B. Huang et al. (2024), and importantly also, the in-band component flux ratios. The latter were derived from the system optical spectra at 5187 Å, and the interferometric observables in the H and K bands from CHARA and PTI, respectively, as described in the preceding sections. These flux and flux ratio data were jointly analyzed with a custom two-component SED modeling code introduced in the work of A. F. Boden et al. (2005), using solar metallicity PHOENIX model spectra from T.-O. Husser et al. (2013). The model atmospheres underlying these spectra adopt spherical geometry for the stellar structure.

Numerical quadratures of the resulting component SED models directly yield estimates for the bolometric fluxes of the individual components. Our modeling suggested that modest extinction along the line of sight is necessary to reproduce the flux set, and this, in turn, couples into the estimates for component temperatures (through reddening) and bolometric fluxes (which must account for estimated extinction). To robustly estimate component radiometric parameters and uncertainties, we directly evaluated a large grid (roughly 10^5

⁶ An additional K_S -band measurement was obtained for this work and is described below in Section 6.

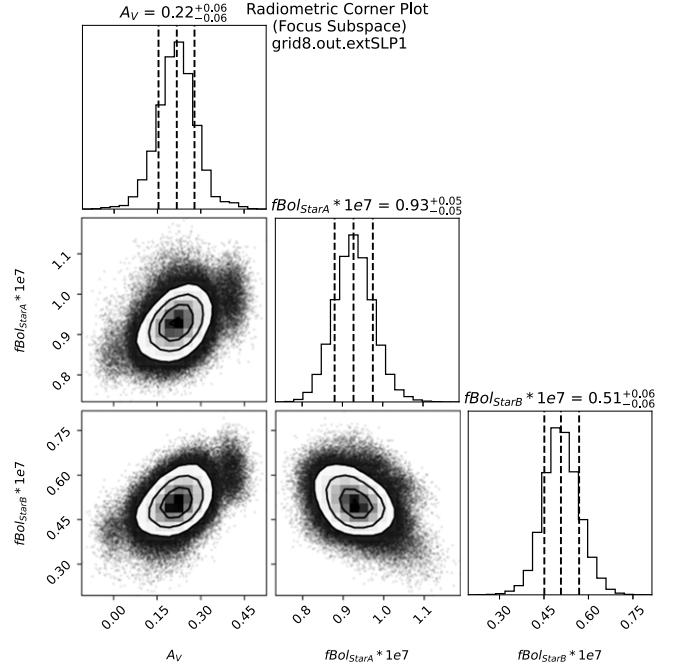


Figure 2. Corner plot showing the correlations among a selection of the fitted parameters of the radiometric analysis.

cases) spanning the range of viable component temperatures, surface gravities, and system extinction. Those ensemble results were then used to seed Monte Carlo simulations of radiometric parameter a posteriori distributions, and corresponding angular diameter estimates for the stars via $\phi_{\text{rad}}^2 = 4f_{\text{Bol}}/\sigma T_{\text{eff}}^4$, where σ is the Stefan–Boltzmann constant. Figure 2 illustrates the posterior distributions for the visual extinction and individual component bolometric fluxes, which are the properties showing the strongest correlations.

We note here that our radiometric diameter ϕ_{rad} is not necessarily the same as the wavelength-dependent angular diameters derived interferometrically (even after accounting for limb darkening), such as from MIRC or PTI, although both tell us something about the size of the star. It has been pointed out previously (see, e.g., D. Mihalas 1990; B. Baschek et al. 1991; M. Scholz 1997) that the “radius” of a star is not a well-defined quantity, as it depends on how it is measured, particularly for giants. In this paper, we follow the practice of other authors (e.g., K.-H. Hofmann & M. Scholz 1998a; K.-H. Hofmann et al. 1998b; M. Wittkowski et al. 2004, 2006b, 2006a) and interpret our radiometric angular diameter to be a measure of the size of a star at a Rosseland optical depth of unity. This definition of the radius is commonly used in atmospheric modeling, and in formulating the boundary conditions for interior models.

Independent SED-estimated component parameter values for HD 174881 were found to be in good agreement with the spectroscopic analysis from Section 2. Therefore, our preferred a posteriori distributions incorporated Gaussian priors for the component temperatures ($T_{\text{eff}} = 4620 \pm 100$ and 4880 ± 150 K for stars A and B, respectively), as derived in that section. Table 4 summarizes the results, in support of subsequent steps in the analysis of the system. The flux measurements along with our model are presented graphically in Figure 3.

Table 4
Radiometric Results for HD 174881

Parameter	Spectroscopy	SED, No T_{eff}	SED, with T_{eff}
		Priors	Priors
Star A			
T_{eff} (K)	4620 ± 150	4631^{+138}_{-149}	4630^{+93}_{-85}
ϕ_{rad} (mas)	...	$0.78^{+0.04}_{-0.04}$	$0.78^{+0.03}_{-0.03}$
f_{bol} (10^{-7} erg s $^{-1}$ cm $^{-2}$)	...	$0.94^{+0.06}_{-0.07}$	$0.93^{+0.05}_{-0.05}$
$A(V)$ (mag)	...	$0.22^{+0.07}_{-0.07}$	$0.22^{+0.06}_{-0.06}$
Star B			
T_{eff} (K)	4880 ± 150	4963^{+190}_{-197}	4908^{+133}_{-132}
ϕ_{rad} (mas)	...	$0.51^{+0.04}_{-0.05}$	$0.52^{+0.03}_{-0.04}$
f_{bol} (10^{-7} erg s $^{-1}$ cm $^{-2}$)	...	$0.51^{+0.08}_{-0.06}$	$0.51^{+0.06}_{-0.06}$
$A(V)$ (mag)	...	$0.22^{+0.07}_{-0.07}$	$0.22^{+0.06}_{-0.06}$

Note. Our adopted SED solution is the one that includes the temperature priors.

During our SED analysis, it became apparent that archival flux measurements for HD 174881 beyond around 5 μm exhibited excess flux relative to photospheric expectations. The situation is depicted in Figure 4, which shows long-wavelength flux measurements plotted against the (sum of Rayleigh–Jeans extensions for) stellar component SEDs. Modest IR excess flux is apparent over most of the range from 5 to 50 μm . Apparent excesses in the IRAS bands at 60 and 100 μm are much more dramatic. A simplistic blackbody model fit against these apparent excesses would suggest significant amounts of cool (15–20 K) dust in the HD 174881 system, and this would also seem consistent with the levels of apparent extinction in the radiometric modeling (Table 4). Further investigation of this IR excess will be the topic of ongoing study.

5. Orbital Solution

The PTI observations and radial-velocity measurements from our own observations, as well as those of J. R. De Medeiros & S. Udry (1999), were analyzed together to derive the astrometric and spectroscopic orbital parameters of HD 174881 simultaneously. The usual elements are the orbital period (P), a reference time of periastron passage (T_{peri}), the eccentricity (e) and argument of periastron for star A (ω_A), the velocity semiamplitudes (K_A, K_B), the center-of-mass velocity (γ), the angular semimajor axis (a''), the inclination angle (i), and the position angle of the ascending node (Ω). The K -band flux ratio ($F_B/F_A)_K$, which is constrained by the PTI observations, is an additional parameter in this case. The angular diameters of the components also need to be specified (see below). For convenience, the eccentricity and ω_A were recast for our analysis as $\sqrt{e} \cos \omega_A$ and $\sqrt{e} \sin \omega_A$ (see, e.g., D. R. Anderson et al. 2011; J. Eastman et al. 2013), and the inclination angle as $\cos i$. We also allowed for a possible systematic shift (Δ_{RV}) between the J. R. De Medeiros & S. Udry (1999) velocities and our own.

The analysis was carried out in a Markov Chain Monte Carlo (MCMC) framework using the EMCEE⁷ package of D. Foreman-Mackey et al. (2013). We applied uniform priors over suitable ranges for all of the above adjustable parameters. We

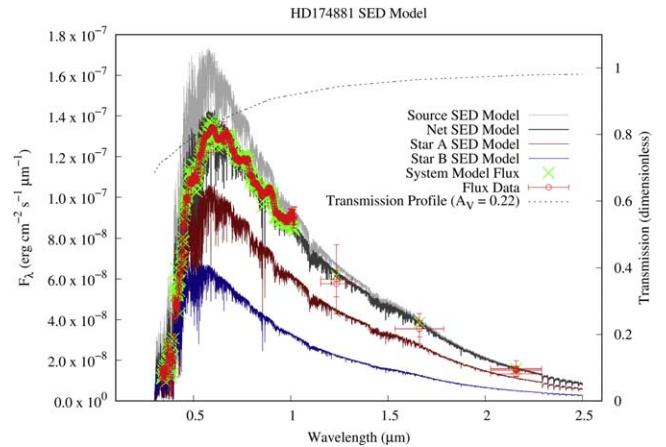


Figure 3. Spectral energy distribution of HD 174881.

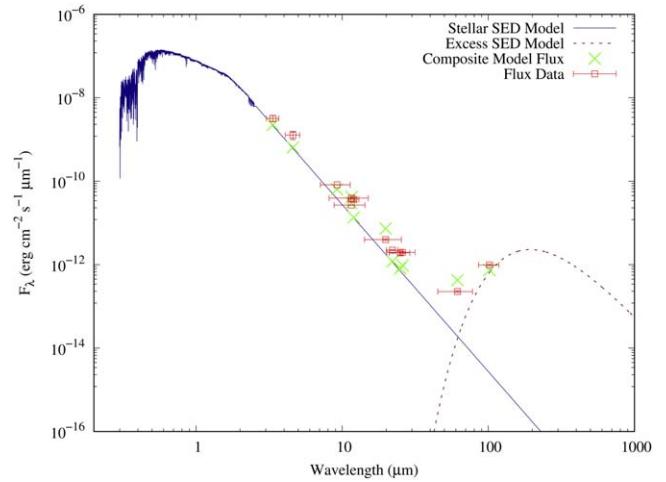


Figure 4. Spectral energy distribution for HD 174881 extended to the infrared via a Rayleigh–Jeans approximation, showing an apparent flux excess longward of about 5 μm . A blackbody model corresponding to a temperature of 15 K provides a reasonable representation of that excess.

verified convergence by visual inspection of the chains and also required a Gelman–Rubin statistic of 1.05 or smaller (A. Gelman & D. B. Rubin 1992).

To guard against internal observational errors that may be either too small or too large, we included additional free parameters representing multiplicative scaling factors f for all uncertainties, separately for the radial velocities of star A and star B from the CfA and from J. R. De Medeiros & S. Udry (1999), as well as for the squared visibilities from the PTI. These scale factors were solved simultaneously and self-consistently with the other free parameters (see P. C. Gregory 2005), using log-uniform priors.

Estimates of the angular size of star A, from MIRC and Section 4, indicated it may be resolved by the PTI. We therefore added its (uniform-disk) angular diameter $\phi_{\text{UD},A}$ as a freely adjustable parameter. The other component, on the other hand, is too small to be resolved. Nevertheless, rather than holding the value of $\phi_{\text{UD},B}$ fixed, we allowed it to vary within wide ranges, subject to priors based on the results from MIRC and Section 4. The motivation for this is to allow any uncertainty in $\phi_{\text{UD},B}$ to propagate through the analysis to all other parameters. The MIRC diameter was measured in the H band, rather than K , and estimating what it would translate to in

⁷ <https://emcee.readthedocs.io/en/stable/index.html>

Table 5
Apparent Angular Diameter Estimates for HD 174881

Source	ϕ_A (mas)	ϕ_B (mas)
MIRC (ϕ_{UD})	0.817 ± 0.030	0.50 ± 0.05
SED Analysis (ϕ_{rad})	$0.78^{+0.03}_{-0.03}$	$0.52^{+0.03}_{-0.04}$
Initial PTI Analysis ^a (ϕ_{UD})	$0.803^{+0.020}_{-0.025}$	$0.534^{+0.044}_{-0.052}$
Final PTI Analysis ^b (ϕ_{UD})	$0.807^{+0.018}_{-0.018}$	$0.521^{+0.047}_{-0.044}$

Notes.

^a This MCMC analysis imposed simultaneous priors on ϕ_B based on results from MIRC and the SED (see the main text) but left ϕ_A completely free. It was meant to verify that the constraint on the diameter of star A from the PTI alone is consistent with the estimates from the two methods above. The exercise proved that to be the case.

^b These estimates used the same priors on ϕ_B as above and incorporated the information from MIRC and the SED fit in the form of additional priors on ϕ_A .

K would require detailed modeling for HD 174881 to account for differences in opacities and other atmospheric properties at both wavelengths. As we expect the difference to be smaller than the formal uncertainty, here we have simply chosen to use the H -band value to establish a Gaussian K -band prior from MIRC. And as our wavelength-independent ϕ_{rad} value from Section 4 is not directly related to what is measured by the PTI, in this case, we chose to define a loose uniform prior with a conservative 3σ half-width. Both of these priors were applied simultaneously to determine $\phi_{UD,B}$.

An initial solution for the uniform-disk diameter of star A produced the value $\phi_{UD,A} = 0.803^{+0.020}_{-0.025}$ mas. This is of the same order as our earlier estimates from MIRC (0.817 ± 0.030 mas) and from the independent radiometric analysis of Section 4 (0.78 ± 0.03 mas). Having verified that there are no serious disagreements, for our final MCMC solution, we incorporated the information from the latter two measurements by applying priors on $\phi_{UD,A}$ in the same way as done above for star B. As the main goal of this analysis was to derive accurate orbital parameters for HD 174881, $\phi_{UD,A}$ and $\phi_{UD,B}$ are regarded here merely as nuisance parameters. The different estimates of the angular diameters for stars A and B are summarized in Table 5.

The complete results of our orbital analysis are presented in Table 6. Our astrometric orbit model is shown in Figure 5, in which the PTI V^2 measurements, which cannot be represented in this plot, are shown as triangles at their predicted locations. The inset displays the two archival CHARA observations, which were not included in the fit but match the predicted relative positions well within their uncertainties. The radial velocities are shown with the spectroscopic orbit in Figure 6. An illustration of the fit to the PTI visibilities is presented in Figure 7.

We note that the position angle of the ascending node (Ω), as determined from the combination of PTI measurements and radial velocities, still suffers from a 180° ambiguity due to the fact that the interferometric squared visibilities are invariant under a point-symmetric inversion around the binary origin. The MIRC observations of HD 174881 break that degeneracy.

The Gaia mission has reported a spectroscopic orbit for HD 174881 (source ID 2040514502502017536) in its most recent data release (DR3; Gaia Collaboration et al. 2023), in which the velocities of both components were measured. The elements are reproduced in Table 7, for easier comparison with the results of this paper. While the Gaia orbit is largely correct, several of the elements show significant deviations from our more precise values.

Table 6
Results of our Orbital Analysis for HD 174881

Parameter	Value	Prior
P (day)	$215.1166^{+0.0092}_{-0.0072}$	[100, 300]
T_{peri} (HJD−2,400,000)	$51843.62^{+0.20}_{-0.17}$	[51800, 51900]
$\sqrt{e} \cos \omega_A$	$-0.0739^{+0.0019}_{-0.0021}$	[−1, 1]
$\sqrt{e} \sin \omega_A$	$+0.3409^{+0.0013}_{-0.0010}$	[−1, 1]
a'' (mas)	$3.3684^{+0.0060}_{-0.0071}$	[1, 10]
$\cos i$	$0.7801^{+0.0019}_{-0.0018}$	[−1, 1]
Ω (deg)	$263.65^{+0.15}_{-0.15}$	[0, 360]
γ (km s ^{−1})	$-19.101^{+0.034}_{-0.043}$	[−30, 0]
K_A (km s ^{−1})	$21.594^{+0.053}_{-0.053}$	[10, 50]
K_B (km s ^{−1})	$20.924^{+0.062}_{-0.057}$	[10, 50]
Δ_{RV} (km s ^{−1})	$+0.193^{+0.082}_{-0.064}$	[−5, 5]
$(F_B/F_A)_K$	$0.4594^{+0.0022}_{-0.0026}$	[0.1, 3.0]
$\phi_{UD,A}$ (mas)	$0.807^{+0.018}_{-0.018}$	$G \times U$
$\phi_{UD,B}$ (mas)	$0.521^{+0.047}_{-0.044}$	$G \times U$
$f_{\text{CfA},A} \cdot \sigma_A$ (km s ^{−1})	$0.984^{+0.091}_{-0.066}, 0.50$	[−5, 5]
$f_{\text{CfA},B} \cdot \sigma_B$ (km s ^{−1})	$0.988^{+0.100}_{-0.061}, 0.45$	[−5, 5]
$f_{\text{DM},A} \cdot \sigma_A$ (km s ^{−1})	$1.10^{+0.16}_{-0.11}, 0.56$	[−5, 5]
$f_{\text{DM},B} \cdot \sigma_B$ (km s ^{−1})	$1.17^{+0.17}_{-0.11}, 0.47$	[−5, 5]
$f_{\text{PTI}} \cdot \sigma_{V^2}$	$1.106^{+0.042}_{-0.031}, 0.016$	[−5, 5]
Derived quantities		
e	$0.12162^{+0.00063}_{-0.00064}$...
ω_A (deg)	$101.98^{+0.36}_{-0.34}$...
i (deg)	$38.73^{+0.17}_{-0.17}$...
Total mass (M_\odot)	$6.838^{+0.093}_{-0.079}$...
M_A (M_\odot)	$3.367^{+0.045}_{-0.041}$...
M_B (M_\odot)	$3.476^{+0.043}_{-0.043}$...
$q \equiv M_B/M_A$	$1.0318^{+0.0040}_{-0.0037}$...
a (au)	$1.3336^{+0.0060}_{-0.0051}$...
π_{orb} (mas)	$2.525^{+0.014}_{-0.015}$...
Distance (pc)	$396.0^{+2.4}_{-2.2}$...
R_A (R_\odot)	$34.0^{+1.3}_{-1.3}$...
R_B (R_\odot)	$22.7^{+1.8}_{-1.8}$...
$\log g_A$ (cgs)	$1.903^{+0.033}_{-0.033}$...
$\log g_B$ (cgs)	$2.262^{+0.075}_{-0.059}$...

Note. The values listed correspond to the mode of the posterior distributions, and the uncertainties are the 68.3% credible intervals. $f_{\text{CfA},A}$ and $f_{\text{CfA},B}$ are the scale factors for the internal errors of the CfA radial velocities of the two components. A similar notation is used for the radial velocities of J. R. De Medeiros & S. Udry (1999), and the PTI. Values following these scale factors on the same line are the weighted rms residuals, after application of the scale factors. Priors in square brackets are uniform over the ranges specified, except for those of the error scaling factors f , which are log-uniform. For $\phi_{UD,A}$ and $\phi_{UD,B}$, the $G \times U$ notation indicates the product of Gaussian and uniform priors as described in the main text. All derived quantities in the bottom section of the table were computed directly from the Markov chains of the fitted parameters involved. The absolute radii depend on the radiometric angular diameters ϕ_{rad} from Section 4 and our distance. With the masses, we then computed $\log g$.

Our inferred distance for HD 174881, $396.0^{+2.4}_{-2.2}$ pc, is in excellent agreement with the value derived from the Gaia DR3 parallax, after adjusting it for the zero-point offset reported by L. Lindegren et al. (2021). The Gaia value is 397.4 ± 5.0 pc.

6. Discussion

The main properties of the HD 174881 stars are collected in Table 8. The fainter component (star B) is the more massive

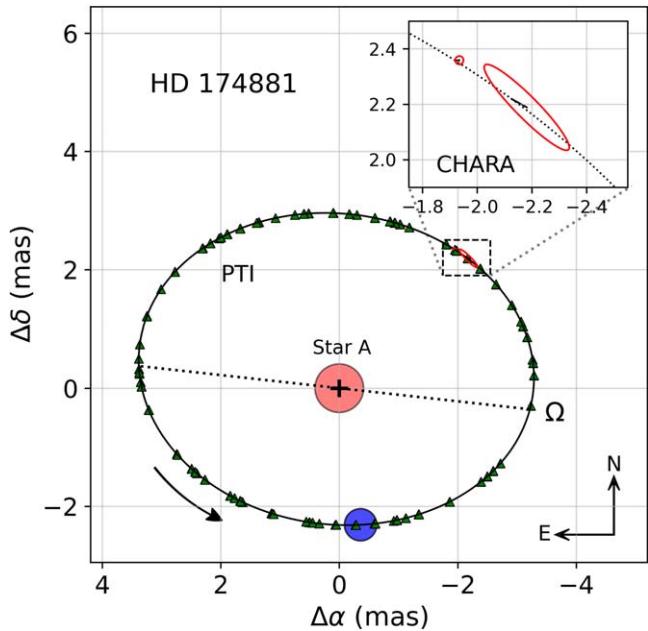


Figure 5. Astrometric model for HD 174881. Neither the PTI visibilities nor their uncertainties can be plotted on the plane of the sky, but we represent them here as green triangles at their predicted locations in the orbit, to illustrate the phase coverage they provide. The components are drawn with their sizes to scale relative to the orbit, and star B (the smaller and more massive component, in blue) is rendered at periastron. The dotted line marks the line of nodes, and the ascending node is indicated with the “Ω” symbol. In accordance with the classical convention, Ω is the node at which star B is receding from the observer relative to γ . The enlargement in the inset shows the two archival CHARA observations, with their corresponding error ellipses. The short line segments connecting the measured and predicted CHARA positions represent the residuals from the model.

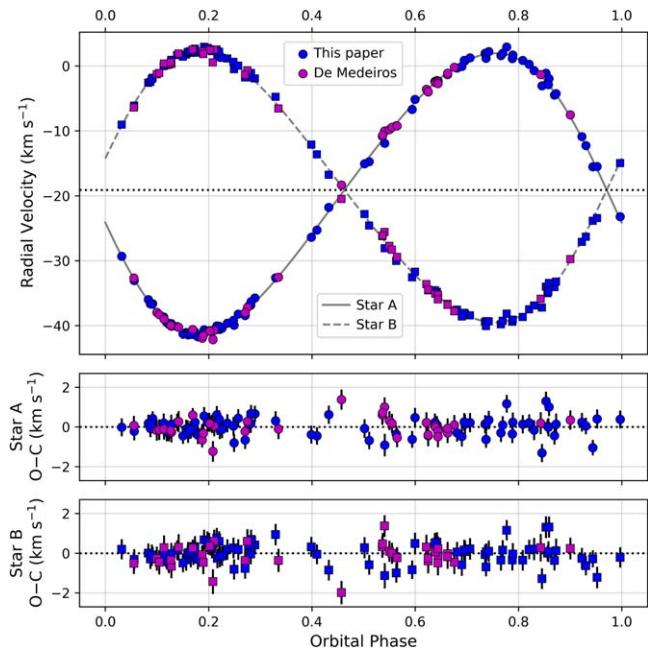


Figure 6. Spectroscopic orbit for HD 174881, together with our radial velocity measurements and those of J. R. De Medeiros & S. Udry (1999). The dotted line in the top panel marks the center-of-mass velocity of the system. Residuals are shown at the bottom.

one, and is therefore more evolved. It would typically be referred to as the “primary” in the system. It is smaller and hotter than its companion.

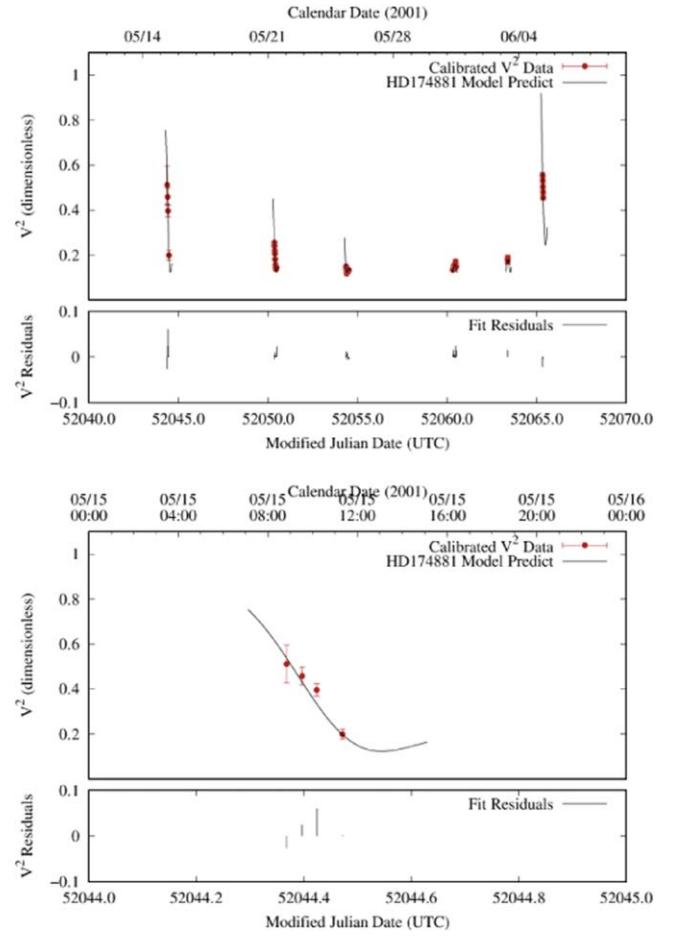


Figure 7. Visualization of the fit of our orbit model to the calibrated PTI visibilities for HD 174881. The top panel shows the measurements and model for six nights over a one month stretch in 2001, and the bottom panel presents an enlargement of the first of those nights (2001 May 15). The visibility residuals are shown in both panels.

Table 7
Spectroscopic Orbital Solution for HD 174881 from Gaia DR3

Parameter	Value
P (days)	215.654 ± 0.063
T_{peri} (HJD – 2,400,000) ^a	57421.82 ± 0.97
e	0.1220 ± 0.0025
ω_A (deg)	75.4 ± 1.6
γ (km s ⁻¹)	-19.420 ± 0.035
K_A (km s ⁻¹)	21.531 ± 0.075
K_B (km s ⁻¹)	19.280 ± 0.073

Note.

^a This time of periastron passage is shifted forward by 26 orbital cycles from our value in Table 6. Adjusting it backwards using our more precise period gives 51828.76.

Here we compare these properties against two sets of recent stellar evolution models, under the assumption that the components are coeval. To further constrain the models, we have added to the wavelength-independent dynamical properties and the bolometric luminosities the (extinction-corrected) absolute magnitudes of the components in the V , H , and K_S bandpasses. They depend on the combined-light brightness, the in-band flux ratios, and our distance estimate. The flux ratio in the V band was obtained by applying a small correction to our

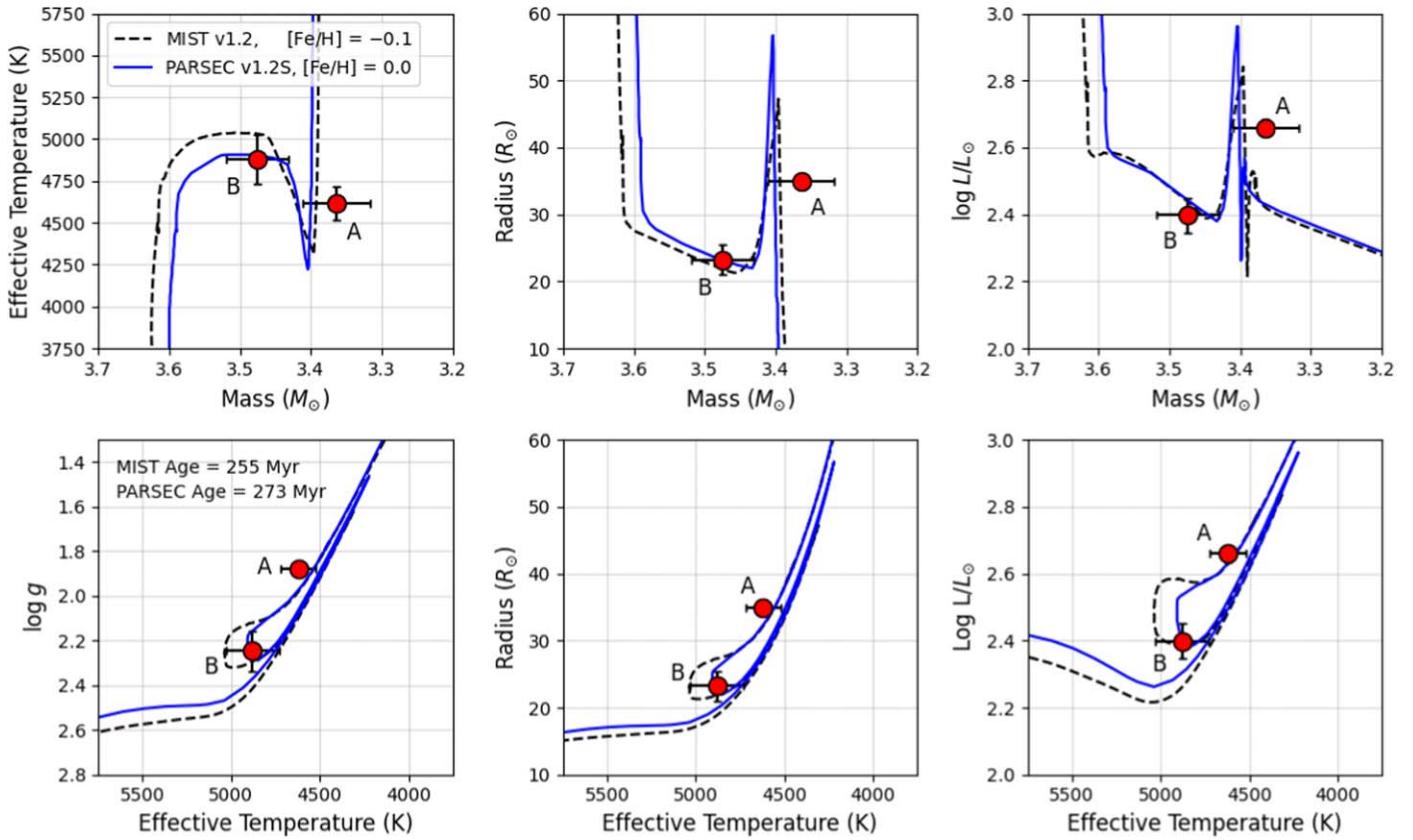


Figure 8. Comparison of the observed properties of HD 174881 against model isochrones from the MIST series (J. Choi et al. 2016) and the PARSEC series (Y. Chen et al. 2014). Rotation is not considered. The panels display the physical properties of the components (labeled) as a function of mass and temperature. The best compromise between the observations and theoretical predictions is reached for a metallicity of $[Fe/H] = -0.1$ for MIST, and solar composition for PARSEC. The corresponding ages are 255 and 273 Myr, respectively.

spectroscopic value reported in Section 2, with the aid of PHOENIX model spectra from T.-O. Husser et al. (2013) appropriate for the two stars. We obtained $(F_B/F_A)_V = 0.679 \pm 0.020$. The values in the near-infrared have been reported earlier, and are $(F_B/F_A)_H = 0.458 \pm 0.010$ and $(F_B/F_A)_K = 0.459 \pm 0.010$, with slightly more conservative uncertainties adopted here than the nominal ones. The apparent magnitude of the system in the visual band was taken to be $V = 6.18 \pm 0.02$ (J.-C. Mermilliod 1987). Due to its near-infrared brightness, HD 174881 is saturated in the 2MASS H and K_S bands. For H , we had little choice but to adopt the 2MASS value as published ($H = 3.74 \pm 0.23$), with its correspondingly large uncertainty. For the K_S band, we were able to gather new measurements with the generous help of our colleague Cullen Blake, on the nights of 2006 November 2 and 2006 November 8. These observations were made on the 1.3 m PAIRITEL telescope (C. H. Blake et al. 2008), located at the Fred L. Whipple Observatory, which was equipped with the same near-infrared camera that was originally used for the southern portion of the 2MASS survey. The average for the two nights is $K_S = 3.62 \pm 0.06$, which is consistent with, but more precise than, the original 2MASS value of 3.58 ± 0.26 .

Figure 8 presents the comparison of the HD 174881 properties with isochrones from the MIST v1.2 models of J. Choi et al. (2016), as well as the PARSEC v1.2S models of Y. Chen et al. (2014). Both sets of models use plane-parallel geometry for the atmospheres at the $\log g$ values of the A and B components, although differences compared to spherical geometry should not be important at these surface gravities. The six panels illustrate the

Table 8
Summary of the Physical Properties of HD 174881

Parameter	Star A	Star B
$M (M_\odot)$	$3.367^{+0.045}_{-0.041}$	$3.476^{+0.043}_{-0.043}$
$R (R_\odot)$	$34.0^{+1.3}_{-1.3}$	$22.7^{+1.8}_{-1.8}$
$\log g$ (cgs)	$1.903^{+0.033}_{-0.033}$	$2.262^{+0.075}_{-0.059}$
T_{eff} (K)	4620 ± 100	4880 ± 150
$\log L/L_\odot$	2.659 ± 0.024	2.398 ± 0.052
Distance (pc)		$396.0^{+2.4}_{-2.2}$
$A(V)$ (mag)		$0.22^{+0.06}_{-0.06}$
M_V (mag)	-1.462 ± 0.065	-1.042 ± 0.066
M_H (mag)	-3.87 ± 0.23	-3.02 ± 0.23
M_{K_S} (mag)	-3.984 ± 0.063	-3.138 ± 0.064

Note. The sources of the above properties are as follows: M , R , $\log g$, and the distance are taken from Table 6. The temperatures are spectroscopic (Section 2). The luminosities rely on the bolometric fluxes from the radiometric analysis and the distance. Extinction also comes from the radiometric analysis. The absolute magnitudes depend on the system magnitudes in each bandpass, extinction, the measured flux ratios, and the distance (see the main text).

match to the masses, temperatures, radii, surface gravities, and bolometric luminosities. The wavelength-dependent absolute magnitudes (V , H , and K_S) are shown in Figure 9, as a function of mass and effective temperature. For the MIST models, the best compromise overall was found for a model with a slightly subsolar composition of $[Fe/H] = -0.1$. The corresponding age of the best-fit model is 255 Myr. For PARSEC, a solar

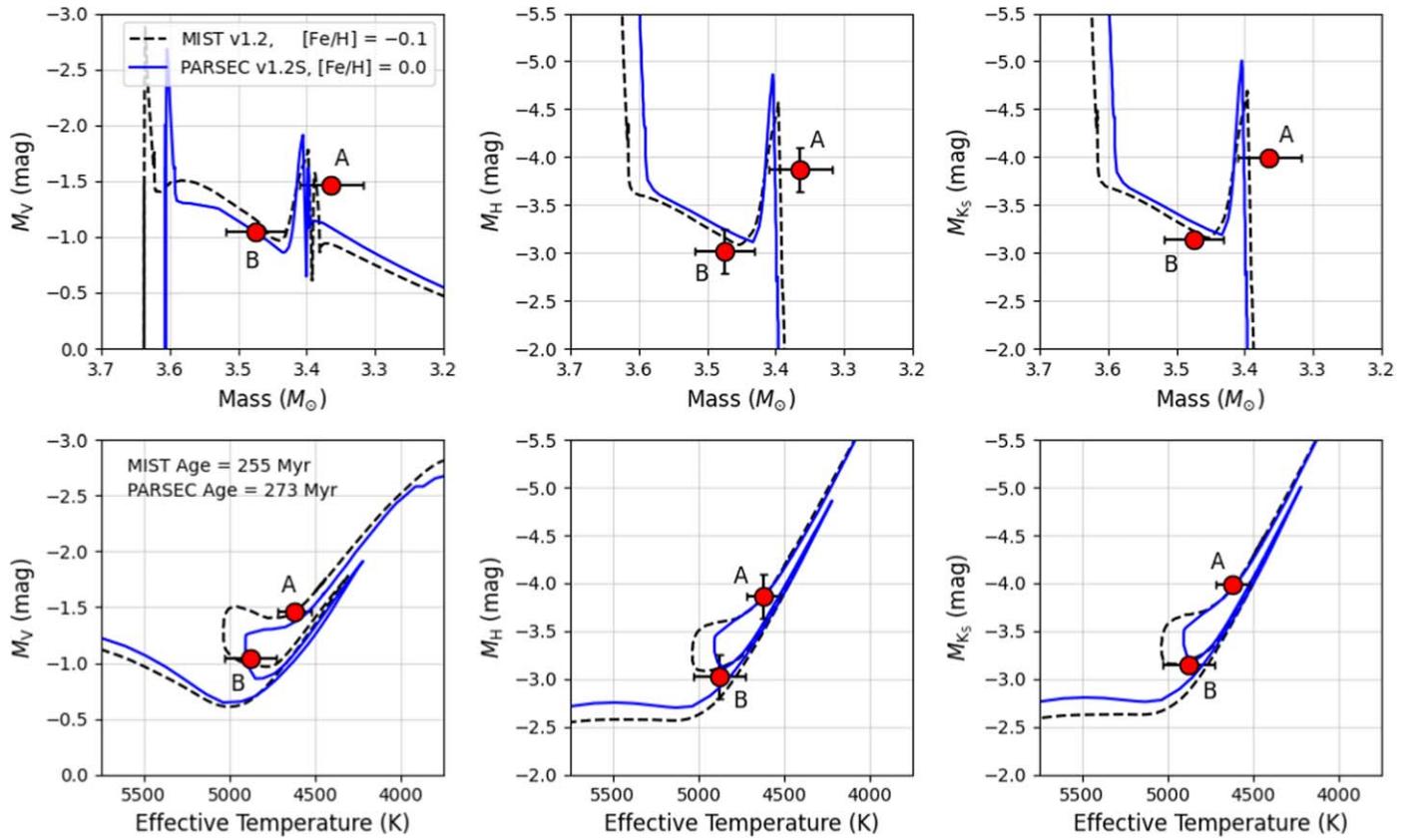


Figure 9. Similar to Figure 8, for the absolute magnitudes of HD 174881 in V , H , and K_S , as a function of M and T_{eff} .

composition isochrone produces a better fit than subsolar, although it is somewhat worse than the best MIST match. The age in this case is 273 Myr.

Neither model is able to reproduce all eight measured quantities simultaneously for both stars, within their respective uncertainties. In particular, both isochrones predict that star A (the less massive and therefore less evolved one) should be somewhat cooler and/or less luminous than we observe, if its location is to be consistent with its less evolved state. Despite these discrepancies, the precision of the observables is such that they easily show the two stars to be in different evolutionary stages. While the more massive component (star B) is clearly located in the helium-burning clump, the location of the other star is either on the first ascent of the giant branch or on its way down to the clump. The former position appears more likely, based on the sum total of the observations (e.g., top panels of Figures 8 and 9).

The progenitors of both components were late B-type stars. Such objects typically have relatively high initial rotation rates on the zero-age main sequence, which theory shows can affect their observable properties at later stages of evolution (see, e.g., G. Meynet & A. Maeder 1997). An additional comparison (not shown) was made against a version of the MIST isochrones that includes the effects of rotation ($\omega/\omega_0 = 0.4$, where ω here is the angular rotation rate, and ω_0 is the value at breakup). The results are rather similar to the nonrotating case, with the best match to the observations being achieved at a marginally older age of 259 Myr.

7. Conclusions

Precise, model-independent mass determinations for giant stars are still relatively uncommon, compared to similar studies

for main-sequence stars. In this paper, we have combined long-baseline interferometry and high-resolution spectroscopy for the giant system HD 174881, to derive absolute masses with precisions of 1.3% for both components, along with a distance (orbital parallax) good to 0.6%. We have also determined the absolute radius of the less massive, larger, and cooler star with an error of just 3.8%, while the size of the other star is less well determined (7.9%). The effective temperatures of both components have been inferred from spectroscopy. Additionally, by incorporating flux measurements in a number of bandpasses, we have derived estimates of the bolometric luminosities as well as the absolute magnitudes in three different bandpasses (V , H , and K_S), in ways that are not completely dependent on the previously determined properties, thereby adding new information.

In aggregate, these properties provide stringent constraints on models of stellar evolution for evolved stars. Comparisons against two sets of current models (MIST v1.2 and PARSEC v1.2S) indicate fair agreement for compositions near solar and ages in the range 255–273 Myr, although discrepancies remain for some of the measured properties. The more massive star resides in the helium-burning clump, while the location in the H-R diagram of the other, less evolved component is still somewhat ambiguous. It is either on the first ascent of the giant branch or on the subsequent descent toward the clump, the former being favored by the observations.

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mission Gaia (<https://www.cosmos.esa.int/gaia>), processed by the Gaia Data Processing and Analysis Consortium (DPAC, <https://www.cosmos.esa.int/web/gaia/dpac/consortium>). Funding for the DPAC has been provided by national institutions, in particular, the institutions participating in the Gaia Multilateral Agreement. The computational resources used for this research include the Smithsonian High Performance Cluster (SI/HPC), Smithsonian Institution (doi:10.25572/SIHPC).

Appendix

Comparison of our 2007 July 7 MIRC Data and the MACIM Image Model

Figures 10, 11, and 12 compare our MIRC squared visibilities, closure phases, and triple amplitude measurements from the 2007 July 7 observation with the model for the image of HD 174881 displayed in Figure 1. The reduced χ^2 values we obtained from the fit are 0.753 for the visibilities, 0.406 for the closure phases, and 1.571 for the triple amplitudes.

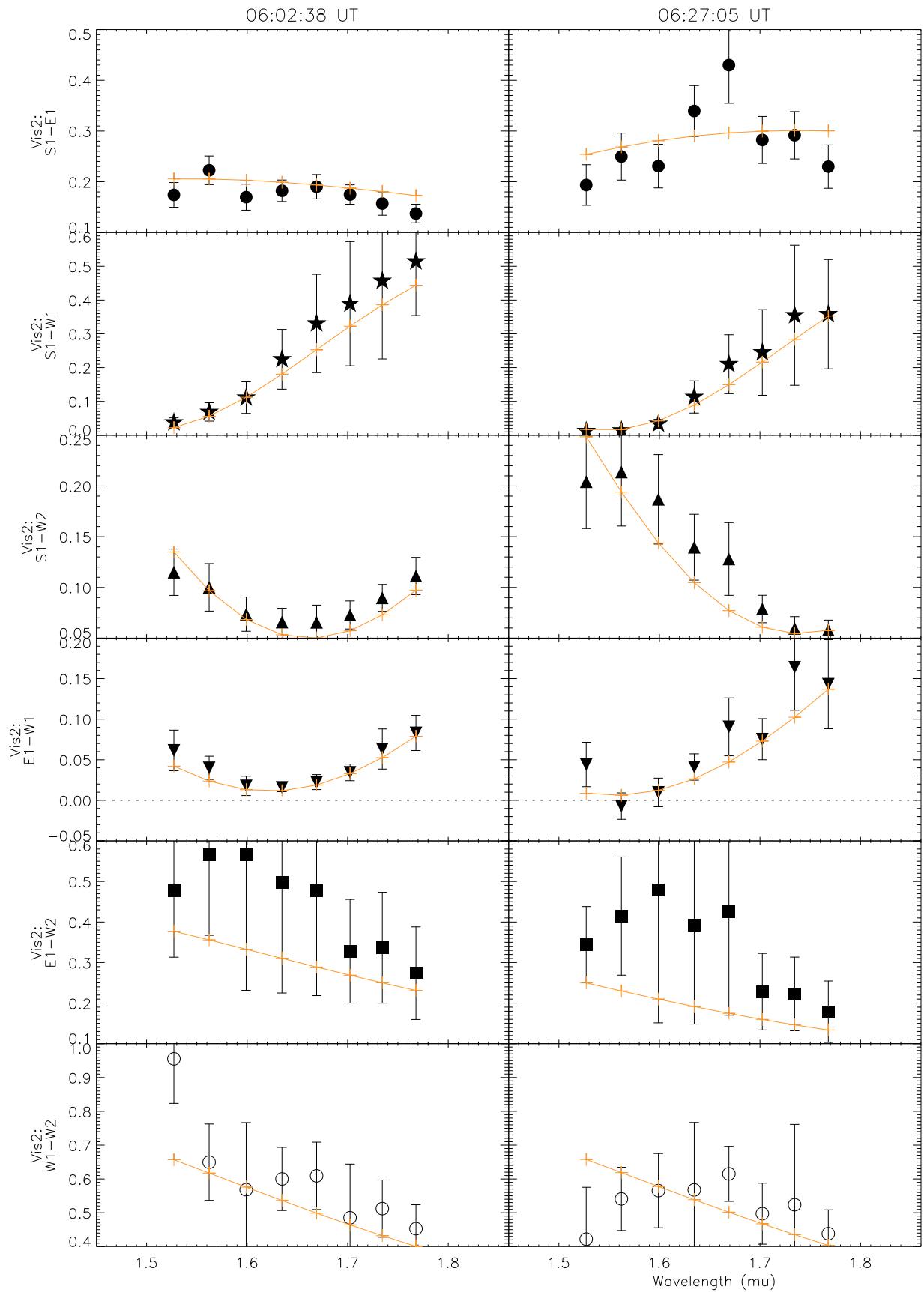


Figure 10. Comparison of the measured MIRC squared visibilities from our 2007 July 7 observation with the model (solid lines) for the MACIM image in Figure 1.

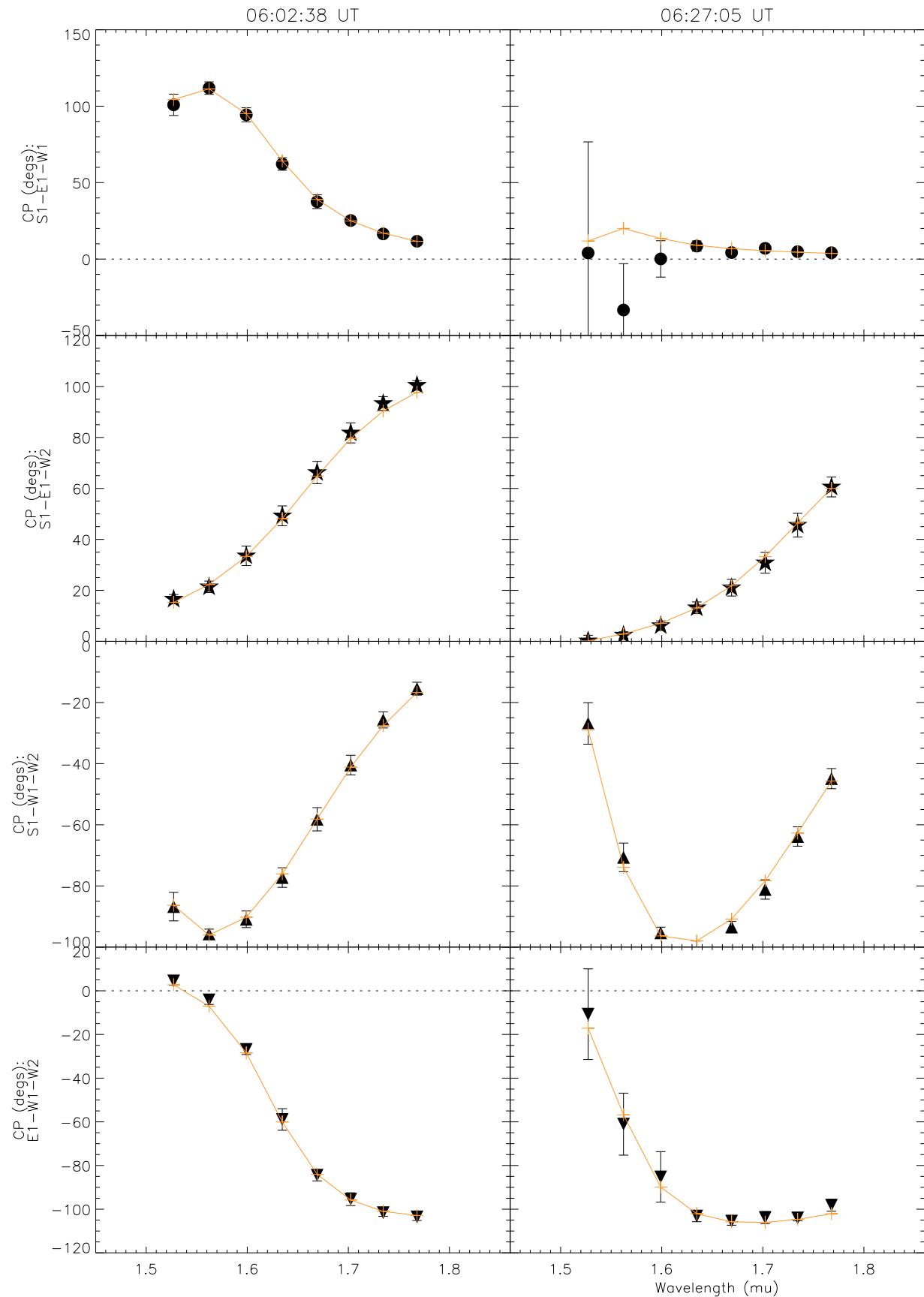


Figure 11. Similar to Figure 10, for the closure phases.

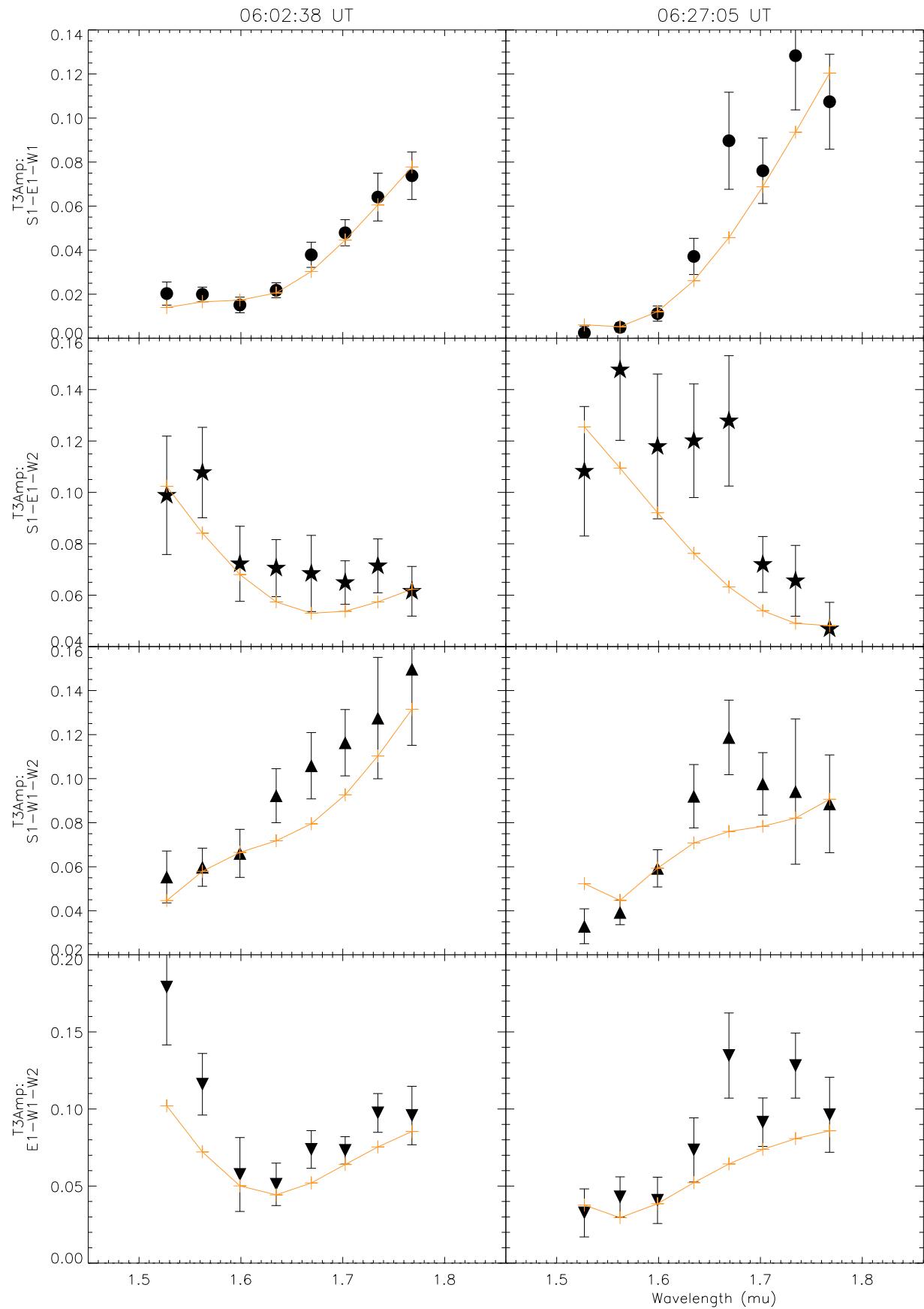


Figure 12. Similar to Figure 10, for the triple product amplitudes.

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