

1 **Delaying the First Nucleation Event of Amorphous Solid Dispersions above the Polymer Overlap Concentration**  
2 **( $c^*$ ): PVP and PVPVA in Posaconazole**

3 Sichen Song<sup>1,2</sup>, Xin Yao<sup>3</sup>, Chenguang Wang<sup>1</sup>, Changquan Calvin Sun<sup>1</sup>, and Ronald A. Siegel<sup>1,4,\*</sup>

4 <sup>1</sup> Department of Pharmaceutics, University of Minnesota, Minneapolis, MN 55455

5 <sup>2</sup> School of Mathematics, University of Minnesota, Minneapolis, MN 55455

6 <sup>3</sup> Research and Development, AbbVie Inc., North Chicago, IL 60064

7 <sup>4</sup> Department of Biomedical Engineering, University of Minnesota, Minneapolis, MN 55455

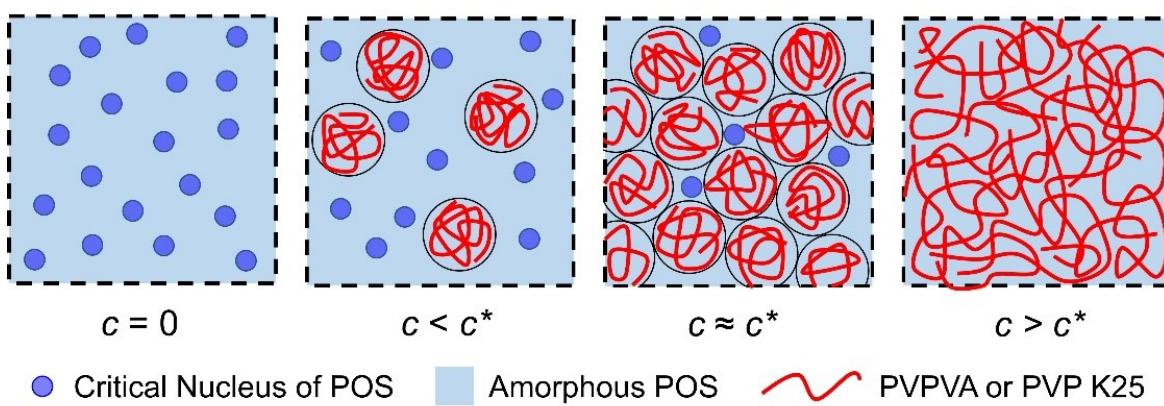
8 \* Corresponding Author: [siege017@umn.edu](mailto:siege017@umn.edu) (R.A.S.)

9 **ABSTRACT:**

10 A thorough understanding of effects of polymers on crystallization of amorphous drugs is essential for rational design of  
11 robust amorphous solid dispersion (ASD), since crystallization of the amorphous drug negates their solubility advantage.  
12 In this work, we measured the first nucleation time ( $t_0$ , time to form the first critical nucleus in fresh liquid/glass) in  
13 posaconazole (POS)/polyvinylpyrrolidone vinyl acetate (PVPVA) and POS/polyvinylpyrrolidone (PVP K25) ASDs and  
14 showed that the polymer overlap concentration ( $c^*$ , concentration above which adjacent polymer chains begin to contact)  
15 is critical in controlling crystallization of ASDs. When polymer concentration  $c$  is less than  $c^*$ ,  $t_0$  of POS ASDs is  
16 approximately equal to that of the neat amorphous POS, but it increases significantly when  $c > c^*$ . This observation  
17 supports the view that the effective inhibitory effect of crystallization in ASDs above  $c^*$  is primarily correlated with delay  
18 in the first nucleation event. Our finding is useful in efficient polymer selection and performance prediction of high drug  
19 loaded ASD formulations.

20

21 **Graphical Abstract**



22  
23  
24 **Keywords:** Amorphous solid dispersion (ASD), physical stability, crystal nucleation, crystal growth, polymer overlap  
25 concentration ( $c^*$ )

26 **INTRODUCTION**

27 Amorphous solid dispersions (ASDs) have been an increasingly used to improve aqueous solubility and hence oral  
28 bioavailability of poorly soluble drugs.<sup>1,2</sup> A typical binary ASD contains an amorphous drug and a polymer. The polymer  
29 excipient in an ASD has a strong impact on its performance, including dissolution rate and supersaturation maintenance,  
30 manufacturability, and physical stability against crystallization during storage.<sup>2-6</sup>

31 Rational design of robust ASDs requires understanding the effects of polymer on the crystallization of the  
32 amorphous drug.<sup>7-9</sup> Crystallization includes two steps, i.e. nucleation followed by growth, with distinct kinetics.<sup>10-14</sup> A  
33 thorough understanding of both processes is necessary to predict overall crystallization propensity. Currently, effects of  
34 polymers on crystal growth of glass forming molecular liquids/glasses are better understood than the nucleation process.<sup>15-</sup>  
35<sup>19</sup> However, nucleation kinetics have been measured in only a few multicomponent amorphous systems.<sup>20-22</sup>

36 Recently, we studied the effect of polymer concentration on crystal nucleation and growth and proposed a  
37 potential correlation between the polymer overlap concentration,  $c^*$ , (the concentration above which adjacent polymer  
38 chains begin to interpenetrate<sup>23,24</sup>, illustrated in Scheme 1b) and the first nucleation time,  $t_0$ , (the time to form the first  
39 critical nucleus from a fresh liquid/glass).<sup>25</sup> Using the example of D-sorbitol/PVPs (molecular weights ranging from 4K to  
40 55K), we showed that, in general, when polymer concentration  $c$  is less than  $c^*$ ,  $t_0$  of D-sorbitol/PVPs is approximately  
41 equal to that of the neat D-sorbitol liquid. However, when  $c > c^*$ , the first nucleation event is significantly retarded. At  
42 steady state, nucleation and growth rates both decrease exponentially with  $c$ , with no abrupt change occurring when  $c \approx$   
43  $c^*$ . Based on the above observations, we concluded that the effective inhibition against crystallization in binary ASDs  
44 above  $c^*$  is primarily correlated with the delay of the first nucleation event.<sup>25-27</sup>

45 In the present work, we apply the two stage (Tammann) method to investigate the role of polymer concentration  $c$ ,  
46 particularly  $c^*$ , on crystallization kinetics, including the first nucleation time  $t_0$  and steady state rate of nucleation and  
47 growth, in posaconazole (POS)/polyvinylpyrrolidone/vinyl acetate (PVPVA) and POS/polyvinylpyrrolidone (PVP K25)  
48 ASDs.<sup>10,28</sup> POS is a model amorphous system whose crystallization and polymorphism have been studied.<sup>14,29</sup> PVPVA and  
49 PVP K25 are of approximately the same molecular weight, which allows examination of the impact of variation of  
50 polymer structure on crystallization of amorphous drugs. We find that for both POS/PVPVA and POS/PVP K25 ASDs,  
51 when  $c \leq c^*$ ,  $t_0$ s for dilute POS ASDs are identical to that of the neat amorphous POS. The value of  $t_0$  increases gradually  
52 when  $c > c^*$ . Crystal nucleation and growth rates decrease exponentially against  $c$  at similar rates. Interestingly, PVP K25  
53 provides a stronger crystallization inhibitory effect compared to PVPVA. These observations are in complete agreement  
54 with our previous results for D-sorbitol/PVPs. Our finding is relevant to the rational design of high drug loaded ASDs  
55 with minimal polymer content, which have advantages such as improving patient compliance by reducing tablet size and  
56 dosage units and lowering the cost of large scale manufacturing.

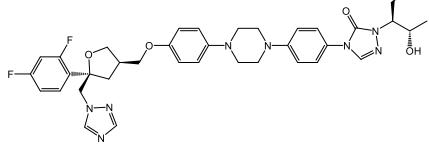
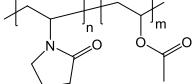
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58

59 **MATERIALS AND METHODS**

60 **Materials.** Posaconazole (POS; form I, purity  $\geq 99\%$ ) was provided by Merck. Polyvinylpyrrolidone/vinyl acetate  
 61 (PVPVA) and polyvinylpyrrolidone (PVP K25) were obtained from BASF. Molecular structures and relevant physical  
 62 properties of POS, PVPVA, and PVP K25 are shown in Table 1.

63 **Table 1.** Molecular Structures and Relevant Physical Properties of POS, PVPVA, and PVP K25.

|         | Molecular structure   | $M_w$ (g/mol) | $D$ ( $M_w/M_n$ ) | $T_g$ (K, onset) | $T_m$ (K, onset) |
|---------|---|---------------|-------------------|------------------|------------------|
| POS     |  | 700.8         | -                 | 333.5            | 440.3            |
| PVPVA   |  | 44,300        | 3.52              | 380              | -                |
| PVP K25 |  | 49,500        | 1.92              | 438              | -                |

64  
 65 **Sample Preparation.** POS/PVPVA and POS/PVP K25 uniform physical mixtures were prepared by cryogenic milling  
 66 with a Spex SamplePrep Grinder 6770 (liquid  $N_2$  as coolant). Cryomilling was performed at 10 Hz for five 2 min cycles,  
 67 each followed by a 2 min cool down. Neat POS crystalline powder, POS/PVPVA or POS/PVP K25 powder mixture was  
 68 placed on a glass slide and melted at 455 K for  $\sim 2$  min. A coverslip was then placed on the melt to produce a sandwiched  
 69 film of  $\sim 40$   $\mu\text{m}$  thickness. The sandwiched liquid film was quenched to 365 K by contacting a preheated metal block.

70 **Rheometry.** Zero shear rate viscosity ( $\eta$ ) of pure POS, POS/PVPVA, and POS/PVP K25 melts was measured using an  
 71 ARES rheometer. A parallel plate geometry with diameter 25 mm was employed. Briefly,  $\sim 600$  mg of powder was placed  
 72 on the bottom plate after zero torque, normal force, and gap calibrations. The gap between the parallel plates was fixed at  
 73 approximately 1 mm. Powder samples were melted at 448 K and equilibrated for  $\sim 3$  min to guarantee complete melting  
 74 before each measurement. A steady rate sweep test was performed with an initial rate of  $1 \text{ s}^{-1}$  and final rate of  $100 \text{ s}^{-1}$  with  
 75 continuous  $N_2$  purge at a flow rate of 3 standard cubic feet per minute.

76 **First Nucleation Times.** Freshly prepared pure POS, POS/PVPVA, and POS/PVP K25 thin films were held isothermally  
 77 at 365 K using a Linkam LTS420 thermal stage (thermal stability  $\leq 0.1$  K, with dry  $N_2$  purge to avoid moisture) for an  
 78 arbitrary time (the first stage) to allow crystal nuclei to form. Then, temperature was raised to 403 K with 1-10 min hold  
 79 (the second stage, no new nuclei formed) to grow nuclei into crystals with visible sizes by an Olympus BX51 polarized  
 80 light microscope. This process was repeated with progressively shorter isothermal holding times in the first stage until  
 81 visible crystals were not observed in the second stage. The first nucleation time  $t_0$  was taken as the midpoint of the last  
 82 two consecutive hold times ( $t_1$  and  $t_2$ ), i.e.,  $t_0 = (t_1+t_2)/2$ . Each reported  $t_0$  value was an average of three measurements of  
 83 three separate samples ( $n = 9$ ).

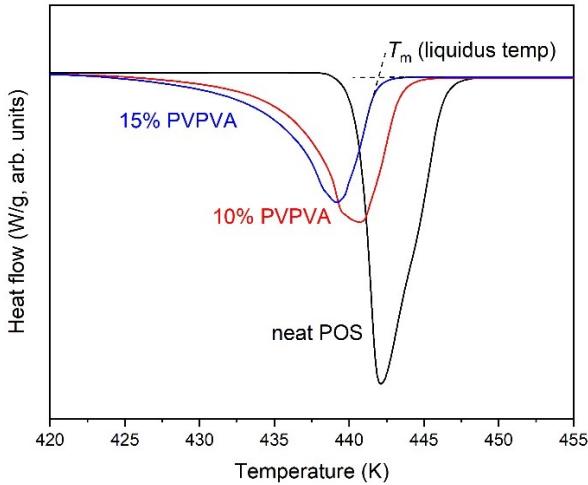
84 **Crystal Growth Rates.** Crystal growth rates of POS without or with PVPVA or PVP K25 at 365 K were measured  
85 through the thermal stage microscope (with dry N<sub>2</sub> purge to avoid moisture) by tracking the advance of spherulite growth  
86 fronts over time. Each reported rate was an average of 10 measurements of three separate samples. All growth rates were  
87 found to be constant over time.

88 **Nucleation Rates.** Freshly prepared sandwiched samples were stored in desiccators (0% relative humidity) at 365 K,  
89 maintained within a heating chamber (temperature stability  $\leq 0.4$  K) for an arbitrary observation time  $t$ , after which the  
90 temperature was raised to 403 K for 1-10 min, allowing nuclei to grow to a visible size and be counted. The nucleation  
91 rate was extrapolated from the nuclei density - time plot at steady state.

92 **Solid state characterization.** Differential scanning calorimetry (DSC) was performed with a TA Q1000 calorimeter in a  
93 Tzero aluminum pan with a pin hole under continuous helium purge at a flow rate of 25 mL/min. Samples (5-10 mg) were  
94 first heated from 273 to 458 K at 10 K/min to erase thermal history, quenched to 273 K, held isothermally for 2 min, and  
95 reheated at 10 K/min to 458 K. Melting point depression of POS by PVPVA and PVP K25 was evaluated from the first  
96 heating cycle, while glass transition temperatures,  $T_g$ , were measured from the second heating cycle. A Thermo DXR2  
97 Raman microscope was used to examine the solid form. Raman scattering was excited by a diode pumped solid state laser,  
98 with a central wavelength of 532 nm. Laser power was fine tuned to 7 mW, ensuring that the sample remained undamaged  
99 while retaining spectral sensitivity. A pixel element CCD detector with an aperture size of 25  $\mu\text{m}$  was employed to  
100 facilitate a resolution of roughly 3  $\text{cm}^{-1}$  and spot size of 0.6  $\mu\text{m}$ . Essential elements such as the detector, laser, apertures,  
101 and laser power underwent calibration prior to the analyses.

## 102 RESULTS AND DISCUSSION

103 **The overlap concentration,  $c^*$ , of PVPVA and PVP K25 in POS.** Before determining the overlap concentration,  $c^*$ , of  
104 PVPVA and PVP K25 in POS, it is necessary to exclude potential liquid-liquid phase separation during high temperature  
105 rheological measurements. We confirmed that POS serves as good solvent for both PVPVA and PVP K25 with favorable  
106 intermolecular interactions. This conclusion was based on a systemic depression of the liquidus temperature ( $T_{\text{liq}}$ , the  
107 lowest temperature at which a drug/polymer mixture is a completely liquid) of POS with an increasing polymer content.  
108 Figure 1 illustrates the  $T_{\text{liq}}$  depression of POS crystal (form I) doped with an increasing PVPVA concentration from neat  
109 POS (446.4 K), to 10% doped POS (443.5 K), and to 15% doped POS (441.8 K). Similar observation of POS/PVP K25  
110 combination is shown in Figure S1.



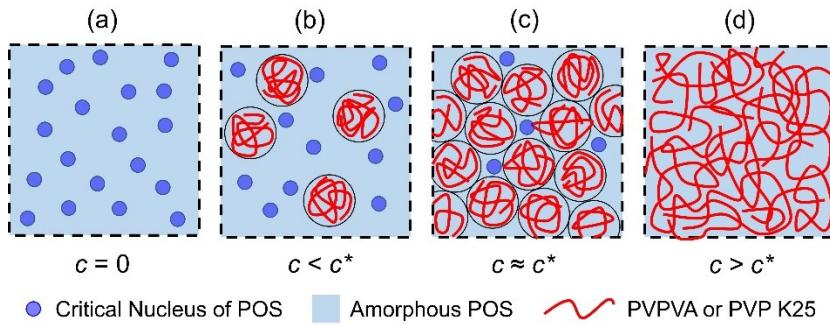
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112 **Figure 1.** Melting endotherms of neat POS crystal (form I) and POS/PVPVA crystalline physical mixtures.  
113

114 According to polymer solution theory, in a good solvent, polymer solutions can be roughly categorized into three  
115 regimes, i.e., dilute, semidilute, and concentrated.<sup>23,30</sup> In the dilute regime, polymer concentration is sufficiently low that  
116 coils are isolated from each other (Scheme 1b). Therefore, intermolecular interactions between adjacent coils are  
117 negligible, and the overall (zero shear rate) viscosity ( $\eta$ ) of a dilute polymer solution is a linear function with respect to  
118 polymer concentration ( $c$ , wt %)

119 
$$\eta = \eta_s(1 + c[\eta]_w) \quad (1)$$

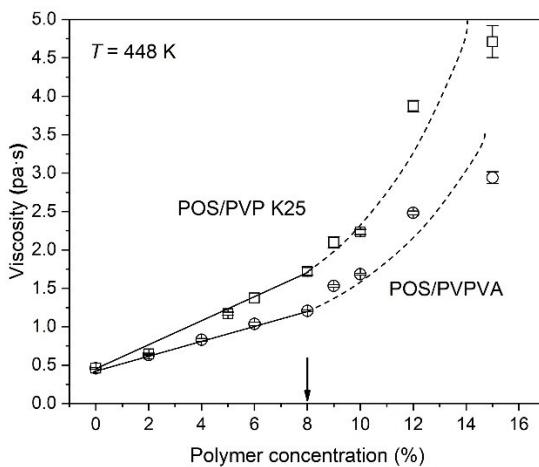
120 where  $\eta_s$  is the viscosity of the pure solvent (small molecule drug melt) and  $[\eta]_w$  is the intrinsic viscosity of the  
121 polymer/solvent combination, in unit of  $\text{%-}^1$ . Notice that  $[\eta]_w$  is slightly different from the conventional intrinsic viscosity,  
122  $[\eta]$ , in that the latter is expressed as  $\text{cm}^3/\text{g}$ , based on w/v polymer concentrations.<sup>26,30</sup>

123 As the polymer concentration increases, individual polymer coils come closer and start to contact each other at the  
124 coil overlap concentration,  $c^*$ , in the semidilute regime (Scheme 1c). Hence intermolecular interactions between adjacent  
125 polymer coils start to contribute to  $\eta$ , leading to nonlinearity of the viscosity-composition curve. The transition between  
126 dilute and semidilute regimes occurs at  $c^*$ .<sup>23,26,30,31</sup> However, this crossover is not sharp since the transition between dilute  
127 and semidilute regions is not a critical phenomenon and  $c^*$  corresponds to a narrow range of polymer concentrations.  
128 Notice that  $c^*$  is generally quite small. It depends on the polymer molecular weight ( $M_w$ ) according to the scaling relation  
129  $c^* \sim M_w^{-0.8}$ .<sup>23</sup> A smaller fraction of a higher  $M_w$  polymer is needed to attain  $c^*$  by pervading the entire space. In the  
130 concentrated regime,  $\eta$  increases more steeply than in the semidilute regime, partially due to polymer chain entanglement  
131 (Scheme 1d) and slower polymer segmental dynamics corresponding to a higher  $T_g$ . To summarize, the  $c^*$  value (the  
132 transition between the dilute and semidilute regimes) can be estimated by identifying the crossover between linear and  
133 non-linear portion in a viscosity – composition diagram.<sup>26</sup> However, there is no general equation to describe the non-linear  
134 behavior of the  $\eta – c$  curve in the semidilute and concentrated regimes.



135  
136 **Scheme 1.** Illustration of the delay of the first nucleation event in semidilute/concentrated (c-d) polymer solutions. Light  
137 background indicates amorphous POS serving as a good solvent, red coils indicate polymer PVPVA or PVP K25  
138 dissolved in POS, and blue circles indicate critical nuclei of POS.

139  
140 Figure 2 shows the viscosity of POS/PVPVA and POS/PVP K25 melts plotted against polymer concentration,  
141 measured at 448 K, which is approximately 8 K above  $T_m$  of POS (form I), to guarantee complete melting. When polymer  
142 concentration,  $c$ , is less than 8%, the overall viscosity  $\eta$  of POS/PVPVA and POS/PVP K25 melts increase linearly as a  
143 function of  $c$ . However, when  $c$  is greater than 8%, the  $\eta - c$  curves for both POS/PVPVA and POS/PVP K25 become  
144 nonlinear. The  $c^*$  value was determined as the transition between linear and nonlinear regions of the  $\eta - c$  curves, i.e., 8%  
145 for both POS/PVPVA and POS/PVP K25. Similarity of the two values of  $c^*$  may be due to the roughly comparable weight  
146 average  $M_w$  of PVPVA (44,300 g/mol) and PVP K25 (49,500 g/mol), even though the  $[\eta]_w$  of PVP K25 (0.3556 %<sup>-1</sup>) is  
147 greater than that of PVPVA (0.2076 %<sup>-1</sup>).



148  
149 **Figure 2.** Viscosity-composition diagram of POS/PVPVA and POS/PVP K25 melts at 448 K. Arrows correspond to  $c^*$ ,  
150 where there is a break in the slopes of the individual viscosity-polymer concentration curves.

151  
152 **The first nucleation time of POS/PVPVA and POS/PVP K25.** In our previous article, we proposed an explanation for  
153 observations that the inhibitory effect against crystallization in ASDs only occurs when  $c > c^*$ .<sup>25,26</sup> We argued that for a  
154 dilute ASD when  $c < c^*$ , the presence of the pure amorphous drug domains between isolated polymer coils (Scheme 1b)  
155 permits the formation of critical nuclei in the same manner as is seen with neat amorphous drug (Scheme 1a).

Consequently, the first nucleation time,  $t_0$ , defined as the time to form the first critical nucleus (or the first group critical nuclei) of fresh amorphous solids, of dilute ASDs is approximately identical to that of the neat amorphous drug. However, when  $c > c^*$ , the first nucleation event can be significantly retarded due to the absence of pure amorphous drug domains (Scheme 1d). When  $c \approx c^*$ , retardation of the first nucleation event, or lack thereof, depends on the radius of the critical nucleus,  $r_c$ , polymer coil's radius of gyration,  $R_g$ , which depends on  $M_w$  according to the scaling law  $R_g \sim M_w^{0.6}$ .<sup>24</sup> Specifically, when  $r_c \ll R_g$ , “nooks and crannies” between adjacent polymer coils are large enough to permit crystal nuclei to form, whereas no such spaces are available when  $r_c \approx R_g$ .

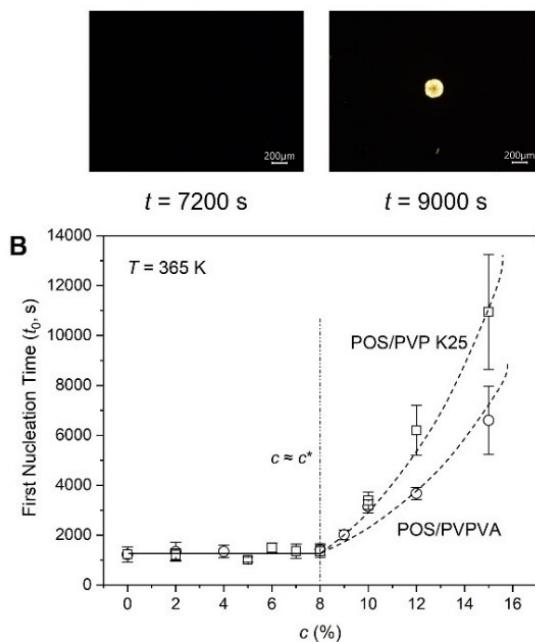
Previously,  $t_0$ s of D-sorbitol/PVPs were determined by the one stage method (i.e. at a single temperature), since D-sorbitol spherulites exhibit relatively fast growth following nucleation. However, this method is unsuitable for systems with slow crystal growth.<sup>10</sup> An alternative two stage approach (Tammann's method) has been employed to determine  $t_0$  of ASDs exhibiting fast crystal nucleation but slow growth.<sup>10,14,28</sup> Here, critical nuclei form without visible growth at a low temperature (the first stage) and the temperature is raised to rapidly grow the nucleus to an observable spherulite without forming new nuclei (the second stage). This two stage approach was applied to POS, whose crystals grow slowly.

Figure 3a shows examples of images used to determine  $t_0$  values of neat amorphous POS, POS/PVPVA, and POS/PVP K25 ASDs using the two stage approach. A freshly prepared thin film sample of POS containing 15% PVPVA spent  $t_1 = 9000$  s at 365 K (the first stage) to allow crystal nucleus to form. Then, temperature was raised to 403 K and for 8 min (the second stage, no new nuclei formed) to grow the nucleus into a spherulite with a visible size. This process was repeated with a shorter isothermal holding time  $t_2 = 7200$  s in the first stage such that visible crystals were not observed in the second stage. The first nucleation time  $t_0$  of 15% PVPVA/POS ASD was taken as the midpoint of the two consecutive hold times ( $t_1$  and  $t_2$ ), i.e.,  $t_0 = (t_1+t_2)/2 = 8100$  s.

Figure 3b plots values of  $t_0$  for POS as a function of polymer concentration,  $c$ , for PVPVA and PVP K25, at 365 K. The  $t_0$  values for POS/PVPVA and POS/PVP K25 are approximately identical to  $t_0$  for neat amorphous POS when  $c \leq c^*$  (8% of PVPVA and PVP K25 content), but increase gradually when  $c > c^*$ , as visualized by the dashed curves in Figure 3b. It is worth noting that the delay of the first nucleation event by PVP K25 is more significant compared to that by PVPVA, even though their  $M_w$ s are approximately comparable. This may be attributed to the higher  $T_g$  of PVP K25, leading to a lower segmental mobility relative to the amorphous POS.<sup>19,32,33</sup> Apparently the chemical structure of polymers plays an important role in controlling nucleation kinetics of ASDs.

It is worth noting that in the presence of low concentration ( $\leq 15\%$ ) PVPVA and PVP K25, spontaneous nucleation of POS yields the same dominant polymorph at 365 K, except for 10% POS/PVP K25. Raman mapping reveals that a new polymorph emerges alongside the dominant form within the crystal spherulite in 10% POS/PVP K25 (Figure S2). Since the presence of polymorphs does not impact the diffusion-controlled growth rate, the polymorph effect is considered negligible under this condition.

**A 15% PVPVA in POS:  $t$  at 365 K + 8 min at 403K**



188

189 **Figure 3.** (a) First crystal(s) observed after POS in the presence of 15% PVPVA spent different times at 365 K (7200 or  
190 9000 s) and then 8 min at 403 K to grow. Before heating to 403 K, no crystals were observed. (b) First nucleation time of  
191 POS/PVPVA and POS/PVP K25 as a function of polymer concentration at 365 K. Dashed curves are drawn to follow  
192 trends of increased first nucleation times with increasing polymer concentration ( $n = 9$ ).

193

194 The above result mirrors those previously reported for D-sorbitol doped with relatively high  $M_w$  grade PVP K25  
195 and K30, where the large  $R_g$  of the polymer compared to the critical nucleus radius,  $r_c$ , of D-sorbitol guaranteed enough  
196 space for the formation of critical nuclei of the amorphous drug when  $c \approx c^*$ , and a significant delay of the first nucleation  
197 event occurred only when  $c > c^*$ .<sup>25</sup> To further verify this phenomenon, we compare  $r_c$  of POS and  $R_g$  of PVPVA and PVP  
198 K25 dissolved in POS, at 365 K. According to classical nucleation theory (CNT),  $r_c = 2\sigma/\Delta G_v$ , where  $\sigma$  is the interfacial  
199 free energy between crystal nucleus and liquid, and  $\Delta G_v$  is the bulk crystal/liquid free energy difference.<sup>10,11,28</sup> Also  
200 according to CNT, the crystal nucleation rate  $J$  is given by

$$201 \quad J = k_J \exp(-w_c/k_B T) \quad (2)$$

202 where  $k_J$  is the kinetic factor describing the attempt frequency at which molecules join the nucleus,  $w_c = \frac{16\pi}{3} \frac{\sigma^3}{\Delta G_v^2}$  is the  
203 thermodynamic barrier of forming a critical nucleus assuming nuclei are of spherical shape,  $k_B$  is the Boltzmann constant,  
204 and  $T$  is the absolute temperature.<sup>10,11,28</sup> Huang *et al.* and Yue *et al.* have suggested that the crystal growth rate  $u$  can be  
205 used to represent the kinetic factor  $k_J$ .<sup>10,11</sup>

206 Following CNT,  $\sigma$  of POS can be inferred by plotting  $\ln(J/u)$  vs.  $1/(T\Delta G_v^2)$ , using the data of nucleation and  
207 growth rates  $J$  and  $u$  with respect to temperature, as reported by Yao *et al.* (Figure 4a).<sup>14</sup> Figure 4b shows such a plot for  
208 POS polymorph I in bulk. Linearity of the plot indicates that the CNT can describe the data and that POS exhibits  
209 homogeneous nucleation. [Note that POS also exhibits homogeneous nucleation in the presence of PVPVA and PVP K25.

210 This was verified based on the stochastic nature (occurrence in the entire volume of the sample) of homogeneous  
 211 nucleation. For example, 15% PVPVA/POS with a 4.7-fold sample thickness difference showed a 4.9-fold nuclei number  
 212 per area under the same condition, indicating a true volume process as expected for homogeneous nucleation]. The  
 213 interfacial tension between nucleus and liquid of POS, obtained by the slope of the plot, is  $\sigma = 0.0123 \text{ J/m}^2$ .

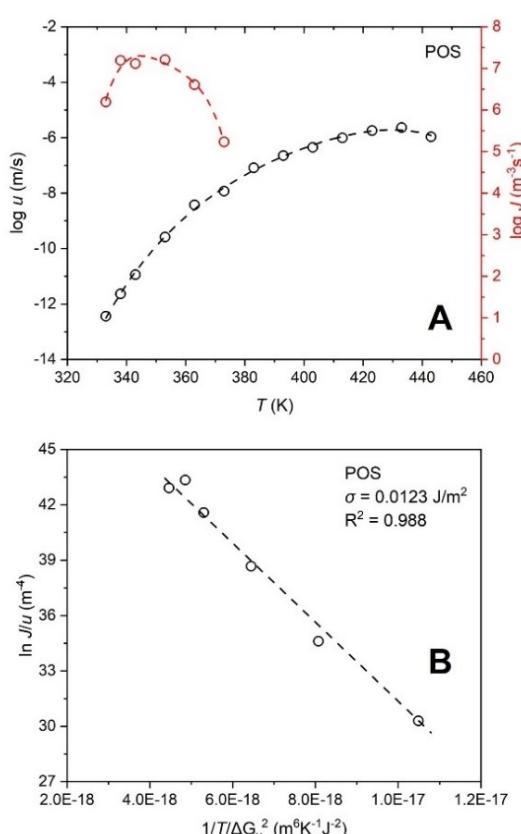
214 The value of bulk crystal/liquid free energy difference  $\Delta G_v$  of POS was calculated from  $\Delta G_v = \Delta G/V$ , where  $V$  is  
 215 molar volume, obtained from the crystal densities at nucleation temperatures, and  $\Delta G$  is the molar Gibbs free energy of  
 216 crystallization following

217 
$$\Delta G = \Delta H - T\Delta S \quad (3)$$

218 
$$\Delta H = \Delta H_m - k \cdot \Delta H_m \cdot T_m \cdot \ln \frac{T}{T_m} \quad (4)$$

219 
$$\Delta S = \Delta S_m - k \cdot \Delta H_m \cdot T_m \cdot \left( \frac{1}{T_m} - \frac{1}{T} \right) \quad (5)$$

220 where  $\Delta H_m$  is the heat of fusion,  $T_m$  is the melting temperature, and  $k = [(C_{p,L} - C_p) \text{ at } T_m]/\Delta H_m$ , estimated as  $0.003 \text{ K}^{-1}$ .<sup>11,34</sup>  
 221 According to the above analysis, for POS at 365 K,  $\Delta G_v \approx 9.6 \text{ kJ/mol}$ . Therefore,  $r_c = 2\sigma/\Delta G_v \approx 1.3 \text{ nm}$  for POS form I at  
 222 365 K.



224  
 225 **Figure 4.** (a) The rate of crystal nucleation (red) and growth (black) of POS vs. temperature. Data are from Yao *et al.*<sup>14</sup> (b)  
 226 CNT fitting for POS.  $\ln(J/u)$  is plotted against  $1/(T\Delta G_v^2)$ . A straight line indicates that the CNT holds with a constant  $\sigma$ .

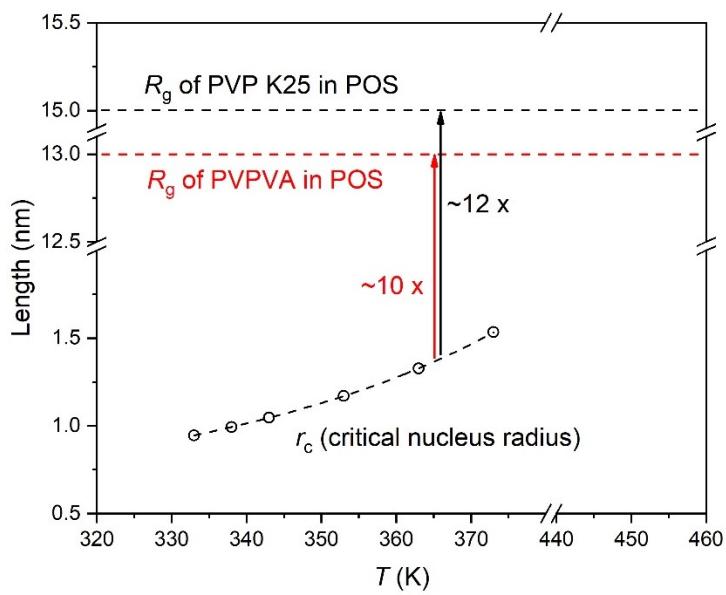
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228 At present, there is no experimental data on the  $R_g$  of PVPVA and PVP K25 dissolved in POS. Nevertheless,  
 229 judging from literature data on common synthetic polymers,<sup>24</sup>  $R_g$  of PVP K25 is estimated as approximately 15 nm  
 230 according to

231 
$$R_g = \sqrt{Nb^2/6} \quad (6)$$

232 where degree of polymerization,  $N$ , is approximately 446, and statistical segment length,  $b$ , is assumed to be 0.7 nm. The  
 233 value of  $R_g$  of PVPVA is estimated from the relation  $[\eta] \sim \frac{R_g^3}{M_w}$ .<sup>24</sup> Therefore,  $R_{g,PVPVA} = R_{g,PVP\ K25} \cdot \left( \frac{[\eta]_{w,PVPVA}}{[\eta]_{w,PVP\ K25}} \right)^{\frac{1}{3}} \approx$   
 234 13 nm.

235 Figure 5 compares the estimated  $R_g$  of PVPVA and PVP K25 and  $r_c$  of POS as a function of temperature. Due to  
 236 the relatively high  $M_w$ , the  $R_g$  value of PVPVA and PVP K25 is much greater than  $r_c$  of POS across the entire temperature  
 237 range. In particular,  $R_g$  is approximately twelvefold larger than  $r_c$  at 365 K. Because of the significant size difference, the  
 238 amorphous POS domain between polymer coils at  $c^*$  are still large enough for the first nucleation event to occur  
 239 unhindered (Scheme 1d). Consequently, the delay in the first nucleation event is observed only when  $c > c^*$ . The POS data  
 240 mirrors the D-sorbitol/PVPs case in our previous work.<sup>25</sup>



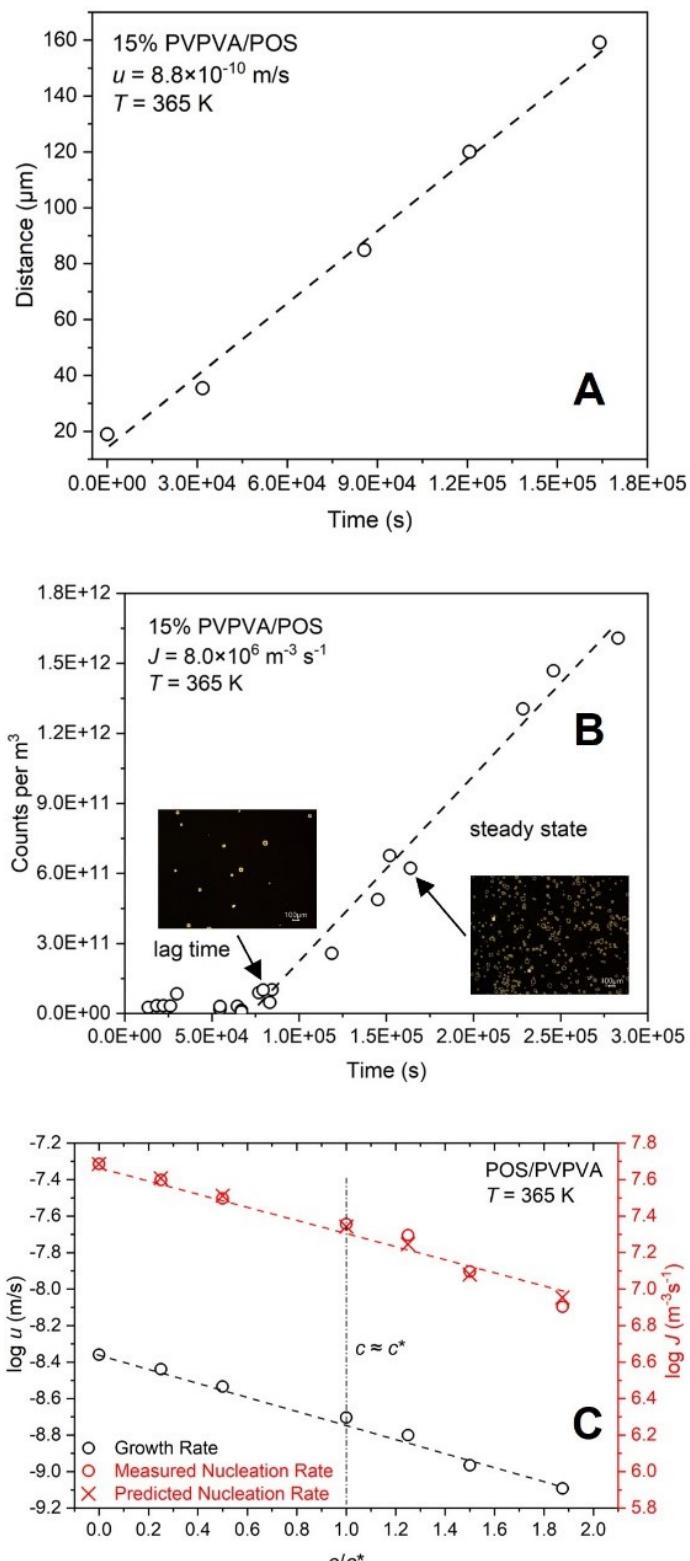
241

242 **Figure 5.** Relative sizes of the PVPVA or PVP K25 coil in POS vs. the critical nucleus,  $r_c$ , of POS against temperature.

243 **Crystal nucleation and growth rates of POS/PVPVA and POS/PVP K25.**

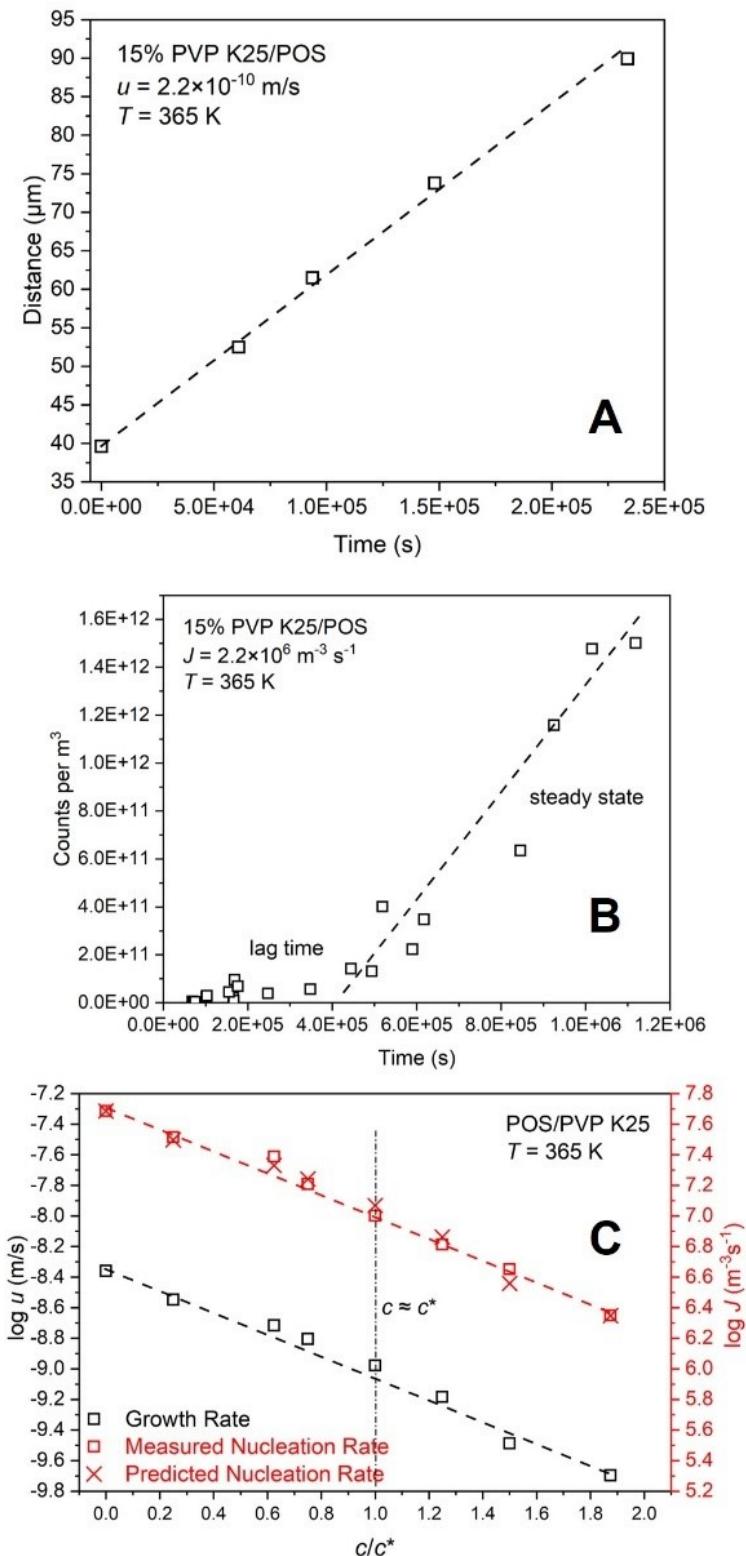
To confirm the exclusive role of  $c^*$  on the delay of the first nucleation event, the effects of polymer concentration on crystal nucleation rate,  $J$ , and growth rate,  $u$ , need to be accounted for. Figure 6a and 7a show typical data collected to measure crystal growth rate. Linearity of the POS spherulite growth distance – time plot indicates a constant growth rate. Figures 6b and 7b show typical data collected to determine crystal nucleation rates by the two-stage method. POS without and with PVPVA/PVP K25 samples were held for different times at 365 K, and then jumped to 403 K for 1-10 minutes, depending on polymer concentration (higher polymer concentration samples require longer time to grow nuclei). For example, POS containing 15% PVPVA after 70,560 s developed fewer crystals than after 163,920 s (Figure 6b). The nuclei density – time plot shows that after an induction period (lag time), a steady state is reached where the density of nuclei (counts/m<sup>3</sup>) increases linearly with time. The slope at steady state is the nucleation rate  $J$  (counts/m<sup>3</sup>/s).<sup>10,28</sup>

Figures 6c and 7c show the effect of PVPVA and PVP K25 concentration on crystal nucleation rate  $J$  and growth rate  $u$  in POS at 365 K, respectively. As polymer concentration increases, both  $J$  and  $u$  decrease at similar rates, following the relation  $\log (J/u) \approx 16.0 \text{ m}^{-4}$ . This suggests that both nucleation and growth share the same kinetic barrier and exhibit similar molecular motions. Lodge and others proposed that the presence of polymer alters the “local viscosity” or the intrinsic effective solvent viscosity and affects the mean rotational mobility of the amorphous drug.<sup>32,33</sup> Yao *et al.* proposed that the nucleation rate of binary ASDs can be predicted following  $J = J_0(u/u_0)$ , where  $J_0$  and  $u_0$  are the measured nucleation and growth rates of neat amorphous drug.<sup>20</sup> The predicted nucleation rates at different polymer concentrations,  $c$ , based on the experimentally measured growth rate of POS/PVPVA and POS/PVP K25, are in excellent agreement with the experimentally determined nucleation rates (Figure 6c and 7c). The smooth dependence of  $J$  and  $u$  on  $c$ , both below and above  $c^*$ , for both PVPVA and PVP K25 confirms that the significant suppression of crystallization above  $c^*$  is primarily correlated with the delay of the first nucleation event, rather than steady state rate of crystal nucleation or growth. Finally, it is worth mentioning that although their  $M_{ws}$  are roughly comparable, the higher  $T_g$  polymer PVP K25 exhibits a stronger inhibitory effect on nucleation and growth than PVPVA, once again emphasizing the important role of polymer chemical structure on the crystallization kinetics modification.<sup>35</sup>



267

268 **Figure 6.** (a) POS crystal growth distance vs. time in the presence of 15% PVPVA, the slope is the growth rate  $u$ . (b) Two-  
269 stage method for measuring POS nucleation rate in the presence of 15% PVPVA at 365 K. The nucleation rate,  $J$ , is the  
270 slope of the nuclei density – time plot at steady state (dashed line). (c) Effect of PVPVA concentration on the steady state  
271 rates of crystal nucleation,  $J$ , and growth,  $u$ , in POS at 365 K. The errors are  $\pm 0.1$  and  $\pm 0.4$  for each reported value of  $\log$   
272  $u$  and  $\log J$ , respectively.



273

274 **Figure 7.** (a) POS crystal growth distance vs. time in the presence of 15% PVP K25, the slope is the growth rate  $u$ . (b)  
275 Two-stage method for measuring POS nucleation rate in the presence of 15% PVP K25 at 365 K. The nucleation rate,  $J$ , is  
276 the slope of the nuclei density – time plot at steady state (dashed line). (c) Effect of PVP K25 concentration on the steady  
277 state rates of crystal nucleation,  $J$ , and growth,  $u$ , in POS at 365 K. The errors are  $\pm 0.1$  and  $\pm 0.4$  for each reported value  
278 of  $\log u$  and  $\log J$ , respectively.

279

280 **CONCLUSIONS**

281 This work investigated the effect of polymer concentration, particularly the overlap concentration  $c^*$ , on the first  
282 nucleation time,  $t_0$ , of POS with polymer PVPVA and PVP K25. When polymer concentration  $c$  is less than or equal to  $c^*$ ,  
283  $t_0$  of dilute POS/PVPVA and POS/PVP K25 ASDs are approximately identical to that of neat amorphous POS. When  $c >$   
284  $c^*$ , the first nucleation event is significantly delayed due to the elimination of the pure amorphous drug domain. However,  
285 no abrupt change in the dependence of steady state rate of crystal nucleation and growth can be observed on  $c$ , particularly  
286 at  $c \approx c^*$ . These observations argue that the effective inhibitory effect on crystallization in binary ASDs above  $c^*$  is  
287 primarily correlated with the delay in the first nucleation event. Our new results of POS ASDs are in complete agreement  
288 with the previous work of D-sorbitol/PVPs.<sup>25</sup> This knowledge is useful in the rational design of high drug loaded ASD  
289 formulations with sufficient physical stability against crystallization during storage. Future direction in this field will  
290 benefit from developing an effective model to predict how the local dynamics, including the first nucleation time and  
291 steady state rate of nucleation and growth of amorphous drug in an ASD, are modified relative the unmixed state.

292 **ASSOCIATED CONTENT**

293 **Supporting Information.** Melting endotherms of neat POS crystal and POS/PVP K25 crystalline physical mixtures.  
294 Raman mapping of 10% POS/PVP K25 growth rings.

295 **Declaration of Competing Interests.** The authors declare no competing financial interest.

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