

1                   **Growth couples temporal and spatial fluctuations of tissue**  
2                   **properties during morphogenesis**

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## Abstract

Living tissues display fluctuations – random spatial and temporal variations of tissue properties around their reference values – at multiple scales. It is believed that such fluctuations may enable tissues to sense their state or their size. Recent theoretical studies developed specific models of fluctuations in growing tissues and predicted that fluctuations of growth show long-range correlations. Here we elaborated upon these predictions and we tested them using experimental data. We first introduced a minimal model for the fluctuations of any quantity that has some level of temporal persistence or memory, such as concentration of a molecule, local growth rate, or mechanical property. We found that long-range correlations are generic, applying to any such quantity, and that growth couples temporal and spatial fluctuations, **through a mechanism that we call ‘fluctuation stretching’** — **growth enlarges the lengthscale of variation of this quantity**. We then analysed growth data from sepals of the model plant *Arabidopsis* and we quantified spatial and temporal fluctuations of cell growth using the previously developed Cellular Fourier Transform. Growth appears to have long-range correlations. We compared different genotypes and growth conditions: mutants with **lower or higher** response to mechanical stress have lower temporal correlations and longer-range spatial correlations than wild-type plants. Finally, we used theoretical predictions to **merge** experimental data from all conditions and developmental stages **into an unifying curve**, validating the notion that temporal and spatial fluctuations are coupled by growth. Altogether, our work reveals kinematic constraints on spatiotemporal fluctuations that have an impact on the robustness of morphogenesis.

## Significance Statement

How do organs and organisms grow and achieve robust shapes in the face of subcellular and cellular variability? In order to address this outstanding mystery, we investigated the variability of growth at multiple scales and we analysed experimental data from growing plant tissues. Our results support the prediction that tissue expansion couples temporal memory of growth with spatial variability of growth. Our work reveals a constraint on the spatial and temporal variability of growth that may impact the robustness of morphogenesis.

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26 INTRODUCTION

27 The impact of noisy perturbations on organism development is the subject of active re-  
28 search [1]. Fluctuations – the random spatial and temporal variations of tissue properties  
29 around their reference values – have been observed at multiple scales, from cytoskeleton [2]  
30 to cell [3] and tissue [4]. In the fruit fly, for example, actomyosin pulses were shown to cause  
31 fluctuations of cell shape [5–7], while fluctuations of the position of cell junctions were found  
32 to favor cell rearrangements during tissue extension [8, 9]. It was proposed that fluctuations  
33 are required for symmetry breaking and pattern formation during development [10, 11] or  
34 for cells and tissues to sense their neighbourhood [12]. Fluctuations in gene expression or  
35 morphogens seems particularly important for cell differentiation. Fluctuations in gene tran-  
36 scription seem required for the maintenance of pluripotency [13, 14], and specific properties  
37 of fluctuations are a signature of cell differentiation [15–18]. Nevertheless, the robustness  
38 of tissue patterning appears sensitive to fluctuations in molecule concentrations [19, 20].  
39 Fluctuations in growth induce mechanical stress [12, 21–23] because, for instance, cells with  
40 higher growth rate exert forces on neighbouring cells, which may sense and respond to such  
41 mechanical stress. Robust development of the fruit fly wing partially relies on cell compe-  
42 tition, i.e. on mismatch of growth rates between cells, and on the ensuing modulation of  
43 proliferation and apoptosis [24, 25]. In this context, it is important to understand whether  
44 fluctuations of a cell affect its local neighbourhood or the whole tissue. Here, we analysed  
45 the spatial structure of fluctuations in experimental data from growing tissues.

46 Recent models of tissue mechanics and growth accounted for temporal and spatial fluctua-  
47 tions of growth and investigated their role in robustness of morphogenesis [26–28]. Temporal  
48 fluctuations are characterised by their degree of persistence, quantified with the persistence  
49 time (or correlation time), the characteristic time over which memory of previous fluctu-  
50 ations is lost. It could be the time needed for remodelling of the cytoskeleton or of the  
51 extra-cellular matrix (in animals) / the cell wall (in plants). Spatial fluctuations are char-  
52 acterised by their degree of spatial consistency, quantified by the correlation length, the  
53 characteristic length over which cells (or subcellular domains) behave similarly, or by cell-  
54 to-cell variability over a small neighbourhood. For instance, the shape of a plant organ was  
55 found to be less robust in a mutant with lower cell-to-cell variability [26]. However, spatial  
56 fluctuations may have a more complex structure. Indeed, theoretical models of the expand-

57 ing universe [29, 30] and of growing tissues [27, 28] predicted long-range spatial correlations,  
58 i.e. a significant level of correlations between fluctuations of two distant parts of the system;  
59 accordingly, growing systems are expected to exhibit fluctuations at multiple scales. Here  
60 we focus on the underlying mechanism, which we call fluctuation stretching – the increase  
61 in the lengthscale of fluctuations of a tissue property or of the concentration of a molecule,  
62 due to tissue expansion.

63 To assess the experimental relevance of this mechanism, we analyzed growth fluctuations  
64 in the model plant *Arabidopsis thaliana*. We considered the sepal, the green leaf-like organ  
65 that protects a flower prior to its opening. We characterised sepals from wild-type indi-  
66 viduals in different culture conditions as well as mutant plants. We considered *spiral2* and  
67 *katanin* mutant plants since they were found to be less robust to variability in the num-  
68 ber of trichomes (epidermal hair-like cells) than wild type plants [31], suggesting a greater  
69 impact of cellular scales on organ ones. The lack of SPIRAL2 and KATANIN function led  
70 respectively to stronger [31–33] and weaker [31, 32, 34] cortical microtubule co-alignment  
71 and reorientation in response to mechanical stress [35, 36]. Microtubules guide the deposi-  
72 tion of cellulose fibers in the cell wall (the plant extra-cellular matrix) [37]. Cellulose fibers  
73 being the main load-bearing component of the cell wall, the response of microtubules to  
74 mechanical stress is generally considered as a mechanical feedback on growth and *spiral2*  
75 and *katanin* as mutants with altered feedback.

76 In this Article, we first present a simple model for fluctuation stretching. We estimate  
77 spatial and temporal correlations of tissue growth fluctuations in *Arabidopsis* sepals using  
78 previous live imaging data [31, 32] and the Cellular Fourier Transform (CFT) [38]. We  
79 investigate how correlations vary within and between datasets and we test the relevance of  
80 fluctuation stretching.

## 81 RESULTS

### 82 A minimal models predicts the stretching of fluctuations in growing tissues

83 Fluctuation stretching, the enlargement of the lengthscales of fluctuations by medium  
84 expansion, was predicted by different models of expanding media, the early universe [29, 30]  
85 and living tissues [27, 28]. Here we introduce a minimal model for fluctuation stretching.

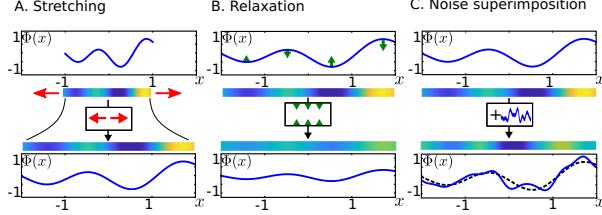


FIG. 1. **Distinct effects of tissue expansion, time relaxation (loss of memory), and noise source on the spatial pattern of a tissue property.** The figure shows initial spatial patterns and their temporal evolution under the three mechanisms. The variable property  $\Phi(x)$  is plotted as a function of position  $x$  and shown in colorscale (blue and yellow for low and high values, respectively) along a strip standing for the growing tissue. **A** Tissue expansion induces fluctuation stretching, defined as the enlargement of the lengthscales of fluctuations. **B** Relaxation associated with loss of memory induces a decay in the amplitude of fluctuations (depicted by green arrows). **C** Noise causes the superimposition of new fluctuations on the preceding pattern (represented by a dashed line in the lower panel). We schematically represent stretching, relaxation, and noise superimposition by function block diagrams containing horizontal red arrows, vertical green arrows, and a noisy signal, respectively. These block diagrams are used in Fig. 2.

86 For a primarily mostly interested in experimental data, Eq. 2 is the main theoretical result  
 87 that we test in growing sepals.

88 We consider a variable property  $\Phi$  that is defined on a tissue growing isotropically at  
 89 average rate  $\bar{G}$  and that depends on position vector  $x$  and time  $t$ . This variable  $\Phi$  could  
 90 reflect gene expression, signalling, metabolism, cell size, or cell growth, for instance. We  
 91 assume that (i)  $\Phi$  is inherited through tissue growth, so that it is advected (transported) by  
 92 the average growth velocity  $\bar{G}x/D$  ( $D$  is the space dimension:  $D=1$  in Figures 1-2 and  $D=2$   
 93 for a thin organ like the sepal), (ii)  $\Phi$  relaxes to its average value  $\langle\Phi\rangle$  with a characteristic  
 94 memory (persistence/correlation) time  $\tau$ , and (iii)  $\Phi$  is subject to a source of noise  $\xi(x, t)$   
 95 that is random in space and time. As a consequence,

$$\frac{\partial\Phi}{\partial t} + \frac{\bar{G}x}{D} \cdot \frac{\partial\Phi}{\partial x} = -\frac{1}{\tau} (\Phi(x, t) - \langle\Phi\rangle) + \xi(x, t). \quad (1)$$

96 In this equation, the first term is the temporal derivative of  $\Phi(x, t)$ . The second term  
 97 (in right-hand side) represents the effect of tissue expansion, i.e. advection by growth, and  
 98 contains the spatial derivative of  $\Phi$  (the dot  $\cdot$  stands for the vectorial product, which reduces

<sup>99</sup> to a multiplication for  $D = 1$ ). The third term (left-hand side) describes relaxation (loss of  
<sup>100</sup> memory) of  $\Phi$ .

<sup>101</sup> The consequences of tissue expansion, loss of memory (time persistence), and noise on  
<sup>102</sup> the variations of  $\Phi$  are schematized in Fig. 1, for one time step. Tissue expansion induce  
<sup>103</sup> ‘fluctuation stretching’, i.e. enlarges the lengthscales of spatial variations (panel **A**). Time  
<sup>104</sup> persistence determines how fast fluctuations relax toward their reference level (**B**). Noise  
<sup>105</sup> superimpose new fluctuations on the preceding pattern (**C**).

<sup>106</sup> When iterated over time, fluctuation stretching and noise give rise to multiscale fluctua-  
<sup>107</sup> tions, while the degree of time persistence (or memory level) controls how far fluctuations ex-  
<sup>108</sup> tend toward large space-scales. This is illustrated in Fig. 2A. in three regimes: for full, inter-  
<sup>109</sup> mediate, and vanishing time persistence. For full time persistence ( $\tau \bar{G} = +\infty$ ) the pattern is  
<sup>110</sup> stretched, increasing its the lengthscale of variations of  $\Phi$  and fluctuations are added at small  
<sup>111</sup> scale. For intermediate time persistence ( $\tau \bar{G} \sim 1$ ), the same process occurs but the preexist-  
<sup>112</sup> ing pattern is attenuated due to relaxation. In the absence of temporal persistence ( $\tau = 0$ ),  
<sup>113</sup> the preceding pattern disappears and only the newly superimposed noise remains. Mathe-  
<sup>114</sup> matically, the solutions to Eq. 1 take the form  $\Phi(x, t) = \langle \Phi \rangle + \int_0^{+\infty} ds e^{-s/\tau} \xi(x e^{-s \bar{G}/D}, t - s)$   
<sup>115</sup> (see Supplementary note, for details). The integral indicates the superimposition while  
<sup>116</sup> the exponential factor  $e^{-s/\tau}$  accounts for time relaxation or loss of memory. Fluctuation  
<sup>117</sup> stretching corresponds to the exponential factor  $e^{s \bar{G}/D}$  applied to the spatial variation of the  
<sup>118</sup> noise.

<sup>119</sup> The space correlation function,  $C(l)$ , is the pairwise correlation between the values  $\Phi(x)$   
<sup>120</sup> and  $\Phi(x + l)$  of the variable  $\Phi$  at positions distant of length  $l$ , as illustrated in Fig. 2 B.  $C(l)$   
<sup>121</sup> generally decrease with the distance  $l$ : for  $l = 0$ ,  $\Phi(x) = \Phi(x + l)$  and so the correlation is  
<sup>122</sup> complete,  $C(0) = 1$ , while at large distance  $l$ ,  $\Phi(x + l)$  is expected to be independent of  $\Phi(x)$   
<sup>123</sup> and the correlation vanishes as illustrated in the plot on the right of panel **B**. In our mini-  
<sup>124</sup> mal model, the correlation function takes the form  $C(l) = \int_0^{+\infty} (2 ds/\tau) e^{-2s/\tau} g(|l| e^{-s \bar{G}/D})$ ,  
<sup>125</sup> assuming the permanent noise source  $\xi(x, t) = 0$  has zero mean and correlation function  
<sup>126</sup>  $\langle \xi(x, t) \xi(x + l, t + s) \rangle$  proportional to  $\delta(s)g(l)$  ( $\delta$  is the Dirac distribution, see Supplemen-  
<sup>127</sup> tary note, for details). Here again  $C(l)$  appears as a weighted sum of the space correlation  
<sup>128</sup> function  $g$  of the noise source stretched at different spatial scales. The correlation function  $g$   
<sup>129</sup> is assumed to have a correlation length  $\ell$  that sets the reference scale for spatial variations of  
<sup>130</sup>  $\Phi$ ;  $\ell$  cannot be assumed to be zero without causing issues of mathematical convergence. In

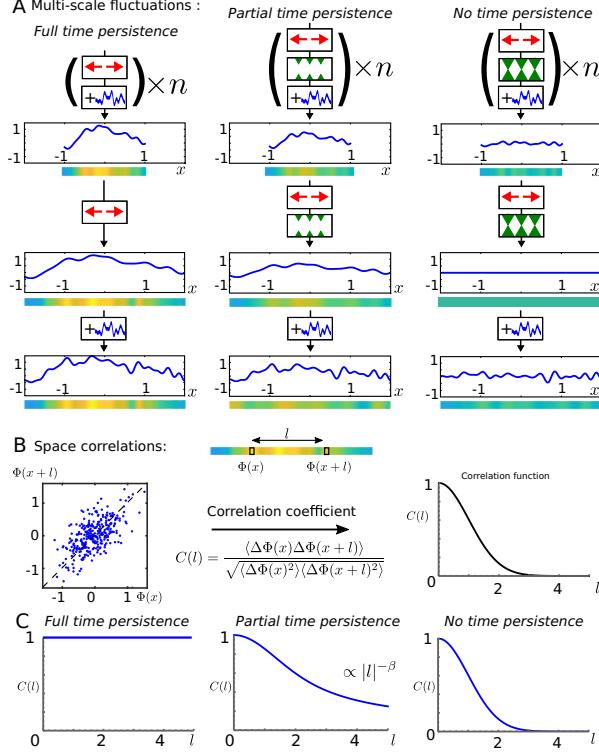


FIG. 2. **Multiscale fluctuations as a consequence of fluctuation stretching.** Spatial correlations of tissue properties depend on the level of temporal persistence of fluctuations. Three levels of temporal persistence are considered: full (no time relaxation), intermediate (moderate relaxation), and none (instantaneous relaxation). **A** Spatial pattern resulting from the iteration of fluctuation stretching, relaxation, and noise, schematically represented by function block diagrams in series, as defined in Fig. 1; patterns are represented under the form of plots and color stripes as in Fig. 1. Top: patterns after  $n$  iterations; middle: patterns after one additional iteration of stretching and (if appropriate) relaxation; bottom: patterns after one additional superimposition of noise. **B** Quantification of spatial correlations. Top: This involves comparing the values of the variable at positions  $x$  and  $x + l$ , as illustrated in the colored strip. Left: Typical scatter plot showing  $\Phi(x + l)$  as a function of  $\Phi(x)$  for multiple values of  $x$ . Middle:  $C(l)$  is defined as the correlation coefficient between  $\Phi(x + l)$  and  $\Phi(x)$ ;  $\langle \rangle$  stands for the statistical average of the expression between brackets and  $\Delta\Phi(x) = \Phi(x) - \langle \Phi(x) \rangle$ . Right: the correlation  $C(l)$  as a function of the distance  $l$ . **C** Spatial correlation function  $C(l)$  for full, partial, and no time persistent fluctuations. Models predict that the space correlation function is a power-law of  $l$ ,  $C(l) \propto |l|^{-\beta}$ .

131 practice, we took  $g(l) = e^{-|l|^2/(2\ell^2)}(2\pi\ell^2)^{-D/2}$ . Because of fluctuation stretching, space corre-  
 132 lations functions for time persistent fluctuations are predicted to be long-ranged *i.e.* to have  
 133 their tails which follow a power law  $\propto l^{-\beta}$ . As shown in the Supplementary note, this can  
 134 be made explicit by rewriting the space correlation function  $C(l) = |l|^{-2D/(\tau\bar{G})}h(|l|)$ , where  
 135 the increasing function  $h(|l|) = \int_0^{|l|} du u^{2D/(\tau\bar{G})-1}g(u)$  reaches an asymptotic value when  $|l|$   
 136 becomes large compared to the correlation length  $\ell$  of  $\xi$ . Therefore, the correlation function  
 137  $C(l)$  of the variable of interest  $\Phi$  mostly behaves as a power-law  $C(l) \sim l^{-\beta}$  of exponent

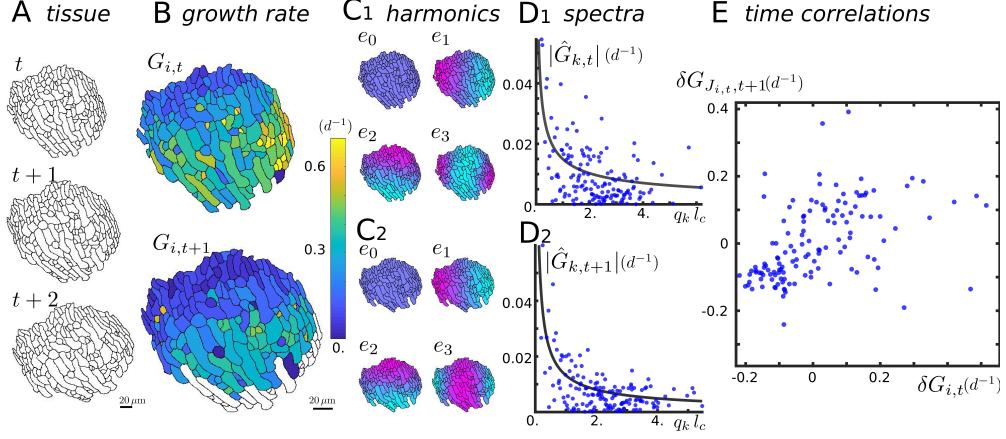
$$\beta = \frac{2D}{\tau\bar{G}}. \quad (2)$$

138

139 This scaling law indicates that the values of the variable  $\Phi$  considered in two distant points  
 140 decorrelate slowly as their distance is increased, which reflects the fact that fluctuations are  
 141 a superimposition of patterns with different spatial lengthscales.  $\beta$  estimates this spatial  
 142 decrease in correlations, the higher the memory (the larger  $\tau\bar{G}$ ), the higher correlations  
 143 between distant regions. Fig. 2 C show the space correlation functions for full, partial,  
 144 and no memory. Full temporal persistence is simply the limit where the persistence time  
 145 is infinite, leading to an accumulation of fluctuations at large lengthscales. The weight of  
 146 large scaled fluctuations continuously increases so that the correlation function tends toward  
 147 a constant. In contrast, in the absence of temporal persistence, spatial correlations vanish  
 148 beyond the correlation length of the noise. Hereafter, we tested this prediction using previous  
 149 experimental data about growing plant organs.

150 **Live imaging and spectral analysis provide estimates for spatiotemporal correlations  
 151 of cell growth**

152 Next we aimed at a quantitative description of spatial and temporal correlations of growth  
 153 fluctuations in expanding tissues. We used experimental data where sepals were imaged live  
 154 to track morphogenesis over time, with similar culture and imaging conditions [31, 32].  
 155 We examined whether fluctuations stretching applies to cell areal growth rate. Each sepal  
 156 was imaged at multiple times, labeled  $t = 0, 1, 2, \dots$  and separated by 24 hours intervals  
 157 as illustrated by Fig. 3A, which shows an example of cells segmented in a sepal, at three  
 158 successive time steps  $t, t+1$  and  $t+2$ . Growth was defined from cell surface area at successive



**FIG. 3. Quantification of spatial and temporal fluctuations in cell growth.** Day ( $d$ ) is used as a unit of time. **A** Three snapshots of a plant tissue (abaxial sepal epidermis from wild-type plant) taken at one-day intervals. Black lines represent cell contours. **B** Heatmaps of relative areal growth rate between times  $t$  and  $t + 1$ ,  $G_{i,t}$ , and between  $t + 1$  and  $t + 2$ ,  $G_{i,t+1}$  for cell  $\#i$ . A growth rate of  $1d^{-1}$  corresponds to a relative increase of area of 100% in 1 day. Growth rate of white cells could not be computed because they were not imaged at  $t + 2$ . **C<sub>1</sub>-C<sub>2</sub>** The first 4 harmonics  $e_k$  ( $k = 0, 1, 2$ , and  $3$ ) of the Cellular Fourier Transform (CFT) of the tissue at  $t$  and  $t + 1$  (the white cells in **B** are not included), represented by a cyan (low value) to magenta (high values) color scheme. The harmonics  $e_k$  generalise sinusoidal waves and can be used to decompose the growth fields  $G_{i,t}$  and  $G_{i,t+1}$  into their respective CFTs  $\hat{G}_{k,t}$  and  $\hat{G}_{k,t+1}$ . **D<sub>1</sub>-D<sub>2</sub>** Fourier spectra (blue dots) correspond to the absolute values  $|\hat{G}_{k,t}|$  and  $|\hat{G}_{k,t+1}|$  of the CFTs and are shown as function of the wavenumber  $q_k$  of the harmonics  $e_k$ . Wavenumbers were non-dimensionalised using mean cell size  $l_c$ . A representative power-law (solid line)  $\Delta G_t q_k^{-\alpha_t} / (\sum_k q_k^{-2\alpha_t})^{1/2}$  was obtained as explained in the text. Each spectrum is then characterised by two numbers, the standard deviation of cell growth  $\Delta G_t$  and the spatial exponent of spatial correlations,  $\alpha_t$ . Here  $\alpha_t = 0.54 \pm 0.08$  ( $\pm$  standard error of the mean),  $\alpha_{t+1} = 0.71 \pm 0.08$ ,  $\Delta G_t = 0.157 \pm 0.012 d^{-1}$  and  $\Delta G_{t+1} = 0.134 \pm 0.012 d^{-1}$ . **E** For temporal analyses, detrended areal growth rate  $\delta G_{i,t}$  was computed as the excess areal growth rate of a cell with respect to a local neighborhood. The coordinates of each blue dot are the detrended growth  $\delta G_{i,t}$  of a cell  $i$  between  $t$  to  $t + 1$  (horizontal axis) and the detrended growth  $\delta G_{J_{i,t},t+1}$  of the set  $J_{i,t}$  of its daughters between  $t + 1$  and  $t + 2$  (horizontal axis). The degree of growth temporal correlation is quantified by the value of the Kendall correlation coefficient, here  $\Gamma_t = 0.400 \pm 0.052$  ( $\pm$  standard error). Two outliers were excluded from the plot to improve the readability of the figure.

159 time steps. Fig. 3B shows cell areal relative growth rate  $G_{i,t}$  and  $G_{i,t+1}$  from  $t$  to  $t+1$  and  
 160 from  $t+1$  to  $t+2$  respectively, deduced from segmentation of sepals into cells, as showed  
 161 in panel **A** and mapped on the reference tissues at  $t$  and  $t+1$ , respectively. When a cell  
 162 has divided between  $t$  to  $t+1$ , we used the total surface area of its daughter cells at  $t+1$   
 163 to define  $G_{i,t}$ , see Datasets and Methods for details.

164 To dissect spatial variations of growth in the tissue, we used the Cellular Fourier Trans-  
 165 form (CFT) [38]. The CFT consists of decomposing the signal into a linear combination of  
 166 ad hoc harmonics that account for the subdivision of the tissue into cells of variable size  
 167 and shape. These harmonics are the equivalent of sinusoidal waves in an infinite continuous  
 168 medium. The  $k$ -th harmonic,  $e_k$ , has wavenumber  $q_k$ , and varies on a lengthscale that de-  
 169 creases with the rank  $k$ . The CFT coefficients  $\hat{G}_{k,t}$  give the weights with which cell relative  
 170 areal growth is decomposed into the harmonics  $e_k$ . The Fourier spectrum is obtained by  
 171 plotting the amplitude  $|\hat{G}_{k,t}|$  as a function the corresponding wave number  $q_k$ . This spectrum  
 172 is well-suited to describe fluctuations of  $G$  at multiple scales.

173 We investigated spatial correlations from Fourier spectra such as those shown in Fig. 3.D.  
 174 The amplitudes of spectra appear significantly higher for low wave numbers, suggesting  
 175 long-range correlations. To further test this, we sought a characteristic lengthscale for  
 176 fluctuations and we considered the smallest index  $K$  for which  $\sum_{k=1}^K \hat{G}_k^2 \geq 1/2 \sum_{k=1}^{N-1} \hat{G}_k^2$ , so  
 177 as to quantify the repartition of fluctuations between low and large scales. If fluctuations  
 178 were short-ranged, then the ratio of largest to characteristic wavenumbers,  $q_1/q_K$ , would  
 179 be a good estimate of the ratio of correlation length to sample size, and would therefore  
 180 be small compared to 1. In contrast, we found the ratio  $q_1/q_K$  to be 0.54 on average  
 181 (standard deviation 0.29 and range 0.086 – 1, over all study samples), indicating long-range  
 182 correlations. This qualitative agreement with the predictions of the minimal model prompted  
 183 us to use power-laws to represent Fourier spectra. We note that the prediction  $C(l) \sim l^{-\beta}$   
 184 corresponds to a spectrum scaling like  $q^{-\alpha}$ , with  $\alpha = 1 - \beta/2$  (see section Datasets and  
 185 Methods). Although the limited range of wavenumbers did not allow us to test the power-  
 186 law behavior, we obtained a representative power-law as follows. As the CFTs can be  
 187 positive or negative, we assumed each CFT to follow a Gaussian distribution of zero mean  
 188 and of standard deviation  $\sigma_{k,t}$ , which was fitted to the equation  $\Delta G_t q_k^{-\alpha_t} / (\sum_k q_k^{-2\alpha_t})^{1/2}$ .  
 189 Each spectrum is then characterised by two numbers, its amplitude  $\Delta G_t$  and its exponent,  
 190  $\alpha_t$ . The specific choice made for the fit is such that, following the Parseval theorem,  $\Delta G_t$

measures the standard deviation of growth while  $\alpha_t$  measures its spatial correlations. We used statistical inference to estimate  $\alpha_t$  and  $\Delta G_t$ . The scaling exponent,  $\alpha_t$ , is expected to vary between 0 and 1, which correspond to short-range and to extremely long-range correlations, respectively. We found  $\alpha_t$  to approximately range between 0.1 to 0.9, indicating large differences between samples and time points in terms of range of correlations (but see below for the comparison between genotypes). We found the standard deviation of growth  $\Delta G_t$  to range between 0.1 and  $0.6 d^{-1}$ , values that are of the order of half the growth rate of a sample averaged over all cells between two time points, indicating relatively strong fluctuations of cell growth rate.

The temporal resolution ( $1d$ ) and the number of consecutive images of a sample (3 to 7) were in general too low to compute persistence time from experimental data. We therefore estimated temporal persistence of growth using correlation coefficients. We considered the correlations between relative areal cell growth  $G_{i,t}$  from  $t$  to  $t+1$  and  $G_{J_{i,t},t+1}$  from  $t+1$  to  $t+2$ , where the set  $J_{i,t}$  in subscript contains the labels of all daughters of cell  $i$  at time  $t$  and  $G_{J_{i,t},t+1}$  is their areal growth rate, see section Datasets and Methods for details. To avoid any bias due to overall gradients in growth rate [32], we computed detrended cell growth  $\delta G_{i,t}$  by subtracting from the areal growth rate of a cell the average areal growth in a local neighborhood, see Supplementary note. The scatter plot in Fig. 3E of  $\delta G_{J_{i,t},t+1}$  as a function of  $\delta G_{i,t}$  shows that growth is relatively persistent in time: For instance cells that grow more than their neighbors between  $t$  and  $t+1$  tend to remain so between  $t+1$  and  $t+2$ . We quantified temporal correlations of growth using Kendall's correlation coefficient,  $\Gamma_t$ , because it is based on the rank of data and is less sensitive to outliers than the more classical rank-based Spearman correlation coefficient [39]. Over all sepals and time points considered,  $\Gamma_t$  approximately ranges from  $-0.1$  to  $0.6$ . Almost all values of  $\Gamma_t$  were positive, while the negative values of  $\Gamma_t$  were not significantly different from zero (see below), indicating that, in general, growth is persistent over a time comparable to experimental time resolution ( $1d$ ).

We thus obtained a minimal set of parameters to describe growth fields and their fluctuations: average growth rate,  $\bar{G}_t$ , extent (exponent) of spatial correlations,  $\alpha_t$ , amplitude of spatial correlations,  $\Delta G_t$ , and temporal correlation coefficient  $\Gamma_t$ . Next, we analysed differences and common features between sepals based on this minimal set of parameters.

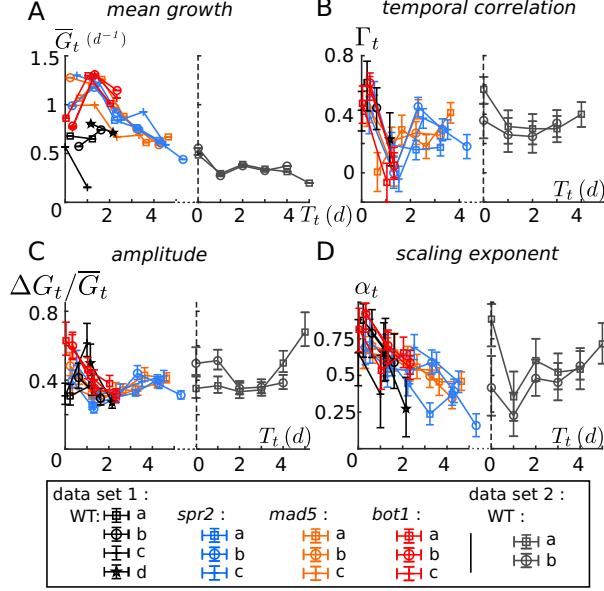


FIG. 4. **Parameters that characterise growth fields in sepals from wild-type and mutant plants.** The sequences were temporally aligned and parameters are shown as a function of the synchronized time  $T_t$ . **A** Growth rate averaged over the tissue  $\bar{G}_t$ . **B** Temporal correlation coefficient  $\Gamma_t$ . **C** Dimensionless amplitude of the Cellular Fourier Transform (CFT)  $\Delta G_t / \bar{G}_t$  (also coefficient of variation of growth). **D** Scaling exponent of the CFT  $\alpha_t$ . The two datasets correspond to two slightly different culture conditions. Black, blue, orange and, red symbols/lines correspond respectively to wild-type, *spr2* mutant, *mad5* mutant, and *bot1* mutant from the first dataset, while gray symbols/lines correspond to wild-type plants from the second set. Error bars indicate the 90% confidence intervals; error bars are not shown in **A** because they are comparable to symbol size.

221      **Temporal and spatial correlations of cell growth vary across genotypes and culture**  
 222 **conditions**

223      We analyzed growth fluctuations in several genotypes and culture conditions. As ex-  
 224 plained in the introduction, we chose to focus on mutants affected in responses to mechani-  
 225 cal stress, *spiral2* (*spr2*) and *katanin* (two alleles, *bot1* and *mad5*), in addition to wild-type  
 226 plants. We analyzed sepals from 4 genotypes in 2 culture conditions and at different devel-  
 227 opmental stages. In order to enable the comparison between several sepals that were imaged  
 228 starting from different stages, we temporally aligned live imaging sequences along a common  
 229 time frame using sepal width, building upon the approach developed in [40], see Datasets

230 and Methods. The parameters that characterise growth fields in all these sequences are  
231 shown in Fig. 4.

232 We first noticed a significant variability within and between genotypes/conditions and  
233 trajectories that seem heterogeneous in time. Some of this variability might be due to ex-  
234 perimental constraints; for instance, the imaged regions of sepals varied in time and between  
235 individuals. We nevertheless observed a few trends that hold for several genotypes and con-  
236 ditions. Mean growth rate (panel **A**) decreases in time for trajectories that are long enough  
237 (*spr2*, *mad5* and wild-type in dataset 2), which is a general trend in organ morphogenesis.  
238 Temporal correlations (panel **B**) decrease between the first and the second time point, possi-  
239 bly associated with the strong decrease in growth anisotropy observed after the second time  
240 interval [32]. The relative amplitude of growth fluctuations (panel **C**) decreases for the first  
241 stages in mutants before stabilizing around 0.4. The extent of spatial correlations (panel **D**)  
242 tends to decrease with time in dataset 1.

243 In order to quantify differences induced by mutations or culture conditions, we used wild-  
244 type plants from dataset 1 as a reference and we estimated the shift in growth parameters  
245 between the reference and other genotypes or culture condition, see Fig. 5. As the amount  
246 of information available varied with genotype, culture condition, or temporal stage, we de-  
247 veloped a method that enables a consistent comparison of differences by taking into account  
248 developmental stages, see Datasets and Methods for details. Briefly, we considered all pairs  
249 formed by a reference sepal (wild-type from dataset 1) and another sepal. We computed the  
250 shift between a reference sepal to another sepal at a given temporal stage and we averaged  
251 shifts over time and sepal pairs to obtain a mean shift, shown in Fig. 5 for all comparisons.  
252 This mean shift can be understood as the representative vertical difference between refer-  
253 ence wild-type curves and mutant or dataset 2 curves from Fig. 4. We then estimated the  
254 standard error of these shifts, which results from the uncertainties of both reference sepals  
255 (wild-type from dataset 1) and sepals of the condition of interest.

256 In wild-type, datasets 1 and 2 do not differ in temporal correlations (panel **B**) and  
257 amplitude of fluctuations (Fig. 5.C) within the range of uncertainty on these parameters.  
258 Average growth rate (Fig. 5.A) and extent of spatial correlations (Fig. 5.D) are lower in  
259 dataset 2, indicating that these two parameters are more sensitive to culture conditions.  
260 Average growth  $\bar{G}_t$  is higher in mutants than in wild-type (Fig. 5.A) over the temporal  
261 window considered; this might be compensated by lower growth in mutants at later stages

262 or by earlier growth arrest in mutants, because mutant sepals are about 20% smaller in  
263 area than wild type sepals [31]. The amplitude of fluctuations  $\Delta G_t$  is smaller in *spiral2*,  
264 but it is not possible to conclude about *katanin*, because the two alleles (*bot1* and *mad5*)  
265 show different trends (Fig. 5.C). When comparing mutants to wild-type plants, temporal  
266 correlations are lower (Fig. 5.B), suggesting lower persistence time in mutants. The changes  
267 in temporal correlations  $\Gamma_t$  are lower than in growth rates, so that the changes in non-  
268 dimensional persistence time  $\tau_t \bar{G}_t$  are expected to be dominated by those in growth  $\bar{G}_t$ , with  
269 higher  $\tau_t \bar{G}_t$  in mutants. This might be ascribed to differences in mechanical responses in  
270 these mutants — assuming wild-type plants to have optimal mechanical responses, both over-  
271 reaction and under-reaction to mechanical stress would increase the timescale of changes in  
272 growth rates [27]. Based on our minimal model of fluctuation stretching (see Eq. 2), smaller  
273 non-dimensional persistence time  $\tau_t \bar{G}_t$  would yield higher extent  $\alpha_t$  of spatial correlations.  
274 Indeed, the exponent of the Fourier spectrum appears higher in mutants (Fig. 5.D), although  
275 the level of uncertainty makes it difficult to draw a firm conclusion. In the following section,  
276 we further test whether fluctuations stretching applies to cell growth in sepals.

## 277 A conserved relation between growth parameters supports fluctuation stretching

278 We sought relations between growth parameters that would hold across genotypes, data  
279 sets, and developmental stages. We first considered the pairwise relations between the growth  
280 parameters defined for each sepal: mean growth rate,  $\bar{G}_t$ , temporal correlation coefficient,  
281  $\Gamma_t$ , normalised amplitude of spatial fluctuations,  $\Delta G_t / \bar{G}_t$ , and extent (exponent) of spatial  
282 fluctuations,  $\alpha_t$ . The corresponding scatter plots are shown in Fig. 6.A-F. To assess these  
283 pairwise relations, we computed Kendall's correlation coefficient between pairs of param-  
284 ters. We found rather weak trends overall. The strongest trends were between the exponent,  
285  $\alpha_t$ , and the temporal correlation coefficient,  $\Gamma_t$ , and between  $\alpha_t$  and the average growth  $\bar{G}_t$ .  
286 Interestingly, these trends are consistent with fluctuation stretching: larger spatial extent of  
287 fluctuations is favored by higher growth rate and by higher temporal persistence, see Eq. 2.  
288 We therefore tested more directly the predictions of fluctuation stretching.

289 Fluctuation stretching does not reduce to a pairwise relation between growth parameters  
290 because it relates spatial correlations to time persistence and growth rate. If this phe-  
291 nomenon is at play in sepals, then Eq. 2 and the relation  $\alpha = 1 - \beta/2$  (see section Datasets

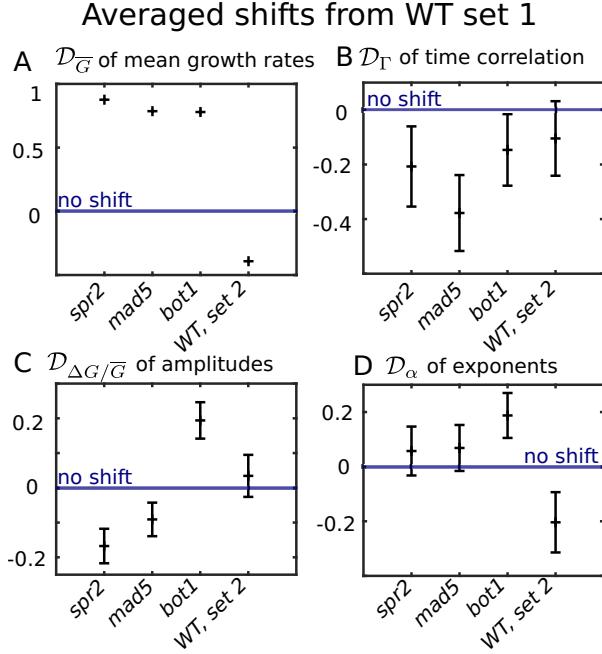


FIG. 5. **Differences in growth parameters due to mutations or to change in culture conditions.** Data are shown for mutants from dataset 1 and wild-type (WT) from dataset 2; wild-type from dataset 1 was used as a reference in all cases. Symbols show the mean shifts  $D_{\bar{G}}$ ,  $D_{\Gamma}$ ,  $D_{\Delta G/\bar{G}}$  and  $D_{\alpha}$  of : **A**, growth rates averaged over sepals,  $\bar{G}_t$ , **B**, temporal correlation coefficients,  $\Gamma_t$ , **C**, dimensionless amplitudes of growth fluctuations,  $\Delta G_t/\bar{G}_t$ , and **D**, exponents quantifying spatial extents of growth fluctuations,  $\alpha_t$ , respectively. Symbols and errors bars correspond to the mean and standard error of the difference, respectively; error bars correspond to the errors on the shifts  $D_{\Phi}$  computed from the error on the data of interest (mutants or WT dataset 2) and on the reference one (WT dataset 1).

and Methods) imply  $\alpha_t = 1 - 2/(\tau_t \bar{G}_t)$ , where  $\tau_t$  is the persistence time. We could measure all parameters of this relation but  $\tau_t$ . Nevertheless the temporal correlation coefficient,  $\Gamma_t$ , should be a decreasing function of  $\Delta t/\tau_t$ ,  $\Gamma_t = f(\Delta t/\tau_t)$ , where  $f$  is an unknown function and  $\Delta t = 1d$  is the time delay between two steps of live imaging, because correlations between states of the sepal at consecutive time steps are higher if the time delay is small compared to the persistence time. By eliminating  $\tau_t$  from the preceding equations, we found that the time correlation coefficient depends on a combination of the other parameters,

$$\Gamma_t = f(\Delta t \bar{G}_t (1 - \alpha_t)/2). \quad (3)$$

We plotted in Fig. 6G. the time correlation coefficient  $\Gamma_t$  as a function of  $\Delta t \bar{G}_t (1 - \alpha_t)/2$ .

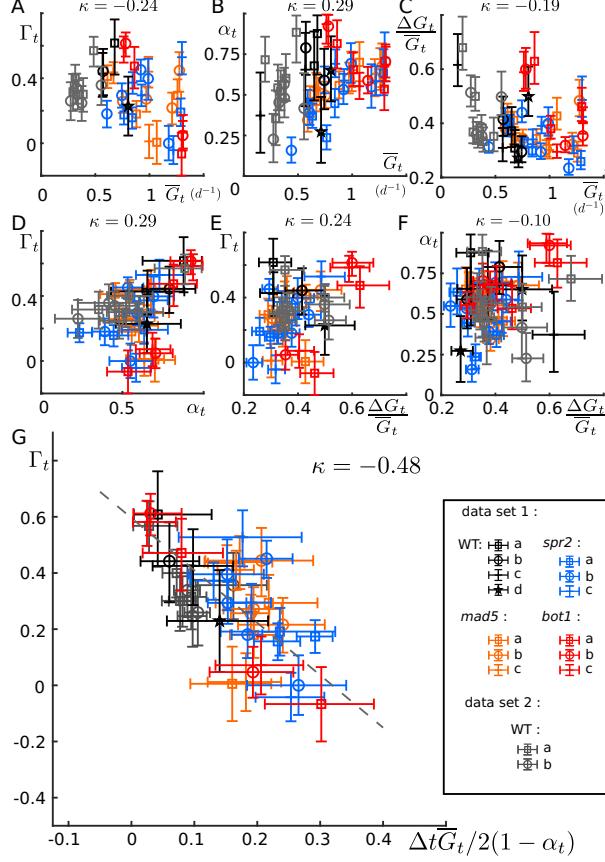


FIG. 6. Relations between parameters of growth (fluctuations). **A-F** Pairwise scatter plots of all growth parameters. **A-C** Temporal correlation coefficient  $\Gamma_t$ , exponent of spatial fluctuations  $\alpha_t$ , and dimensionless amplitude of spatial fluctuations,  $\Delta G_t/\bar{G}_t$ , respectively, as function of average growth  $\bar{G}_t$ . **D-E** Temporal correlation coefficient,  $\Gamma_t$ , as function of exponent of spatial fluctuations,  $\alpha_t$ , and dimensionless amplitude of spatial fluctuations,  $\Delta G_t/\bar{G}_t$ , respectively. **F** Exponent of spatial fluctuations,  $\alpha_t$ , as function of their dimensionless amplitude,  $\Delta G_t/\bar{G}_t$ . **G** Test of the coupling between temporal and spatial fluctuations, as resulting from fluctuation stretching. Temporal correlation coefficient  $\Gamma_t$  as a function of the combination  $\Delta t \bar{G}_t (1 - \alpha_t)/2$  where  $\Delta t = 1 d$  is the time step of live imaging. The dashed line corresponds to a linear fit,  $\Gamma_t = \beta_0 + \beta_1 \Delta t \bar{G}_t (1 - \alpha_t)/2$ , with fit parameters  $\beta_0 = 0.596 \pm 0.024$  and  $\beta_1 = -1.87 \pm 0.15$ . The analysis of the fit residuals supports a deterministic relation between the two, see Supplementary note. In all panels, error bars show the 90 % confidence intervals; black, blue, orange, and red symbols correspond to wild-type, *spr2*, *mad5* and *bot1* sepals from dataset 1, respectively, while gray symbols correspond to wild-type sepals from dataset 2. Kendall's correlation coefficient,  $\kappa$ , is shown above each plot.

300 The trend is much clearer than in all other panels of Fig. 6 (Kendall’s coefficient  $\kappa = -0.48$ )  
301 and the data seem to collapse along a line. We used statistical inference to perform a  
302 linear fit of the data,  $\Gamma_t = \beta_0 + \beta_1 \Delta t \bar{G}_t (1 - \alpha_t)/2$ , see Supplementary note. We obtained  
303 fit parameters  $\beta_0 = 0.596 \pm 0.024$  and  $\beta_1 = -1.87 \pm 0.15$ , with relatively small standard  
304 deviations. We then confirmed with a Kolmogorov-Smirnov test that the residuals (the  
305 spread of the data around the fit) could be explained by the uncertainty on the estimates of  
306  $\tau_t$  and  $\Gamma_t$ , see Supplementary note, while the same analysis for the other plots (Fig. 6A-F)  
307 confirmed that none of these plots was consistent with a linear behavior. Altogether these  
308 results support the hypothesis of a deterministic relation between  $\Gamma_t$  and  $\Delta t \bar{G}_t (1 - \alpha_t)/2$   
309 and therefore indicate that fluctuation stretching is at play in growing sepals.

## 310 DISCUSSION

311 Our analysis provides evidence that growth stretches temporally persistent fluctuations:  
312 while no clear pairwise relation could be made among the different growth parameters, see  
313 Fig. 6A-F, the clear trend of panel G suggest that the persistence time can be deduced  
314 from space correlations and tissue growth. This phenomenon explains why higher correla-  
315 tion between cells (higher spatial correlations) may induce more variable organ shape and  
316 size [26]. Fluctuation stretching gives a prominent role to the persistence time (correlation  
317 time) in controlling spatial correlations in the tissue. Any mechanism that would decrease  
318 persistence time would reduce spatial correlations and, as a consequence, variability of organ  
319 contours. Accordingly, reducing persistence time would yield robust morphogenesis.

320 Surprisingly, we found that the temporal correlation coefficient,  $\Gamma_t$ , is generally not much  
321 smaller than unity, implying that the persistence time,  $\tau_t$ , is not much smaller than the time  
322 scale of growth  $1/\bar{G}_t$ . This might be specific to plants. The cell wall sets the local growth  
323 rate, and, at the same time, is remodelled at the pace of growth, so that the persistence  
324 time of fluctuations of cell wall properties is given by the time scale of growth. It would  
325 be worthwhile to extend our study to expanding animal tissues imaged live such as the  
326 imaginal disc of the fruit fly [41]. In animal tissues that undergo convergent extension, we  
327 would expect fluctuation stretching to operate only in the direction of extension, and so  
328 spatial correlations to be highly anisotropic.

329 As a consequence of fluctuation stretching, the level of time persistence, or more rigorously

330 its product with average growth rate  $\tau\bar{G}$ , has a strong impact on variability of organ shape  
331 and size variability. Indeed, the shape and size of an organ result from the growth of its cells  
332 (or of its subcellular elements) integrated over time. If cell growth has a random component,  
333 well-defined shape and size may still be obtained through spatiotemporal averaging [26], the  
334 cancellation of random effects over large samples (number of cells or time points) — a local  
335 excess of growth may be compensated by lower growth later or elsewhere in the tissue.  
336 Higher temporal or spatial correlations reduce spatiotemporal averaging since an excess of  
337 growth is less likely to be compensated. Accordingly, higher temporal persistence (scaled  
338 with growth rate) reduces the robustness of organ shape and size.

339 We found a higher spatial extent of correlations (higher  $\alpha_t$ ) in mutant genotypes, suggest-  
340 ing higher  $\tau\bar{G}$ . This means that these mutants potentially have more variable shapes or are  
341 less robust to perturbations, consistent with the observation that the width of sepals in *bot1*  
342 and *spr2* varies more with trichome number in WT plants [31]. We previously predicted  
343 that variability of organ contours is minimal for a well-defined level of feedback from me-  
344 chanical stress to cellulose synthesis [27], leading to the hypothesis that in wild-type sepals  
345 the level of mechanical feedback is optimised so as to reduce variability of sepal shape, com-  
346 pared to mutants with lower (*bot1*) or with higher (*spr2*) mechanical feedback. This level of  
347 mechanical feedback also corresponds to a minimum of the persistence time of fluctuations  
348 (scaled with average growth rate),  $\tau\bar{G}$ , highlighting the importance of this factor in setting  
349 the robustness of organ shape and size.

350 Fluctuation stretching is a kinematic phenomenon: properties of cells or of regions of  
351 cells are carried (adverted) by tissue growth and deformation; the persistence time of these  
352 properties sets how they are carried to larger or smaller spatial scales, in the case of tissue  
353 expansion or tissue shrinkage, respectively. This kinematic phenomenon applies to any  
354 type of property or field as long as it is carried by tissue growth and deformation, such as  
355 protein concentrations in cells. Although fluctuation stretching not only applies to scalar  
356 quantities but also to vector fields (e.g. cell polarity) or tensorial fields (e.g. organisation of  
357 cytoskeleton), we limited our study to a scalar (areal growth) and did not consider growth  
358 anisotropy to avoid the difficulty of taking into account the curved geometry of sepals.  
359 Mathematical formalisms such as quasiconformal transforms [42] may nevertheless help to  
360 circumvent this difficulty. In the case of complex advective flows, effects associated to co-  
361 rotation may arise for non scalar fields. Advection also applies to non-random properties,

362 in line with theoretical models of polarity fields showing that a combination of morphogens,  
363 advection, and time persistence can reproduce the shapes of leaves [43], or with models of  
364 leaf vasculature that show that areole (region delimited by veins) shape is advected by leaf  
365 growth [44].

366 Altogether, our work sheds light on the role of persistence time, that is the memory of  
367 previous states of a given property, in the robustness of morphogenesis. The investigation of  
368 spatiotemporal fluctuations may provide a new avenue to characterize organ development.

### 369 AUTHORS CONTRIBUTIONS

370 Conceptualisation: AF, AB. Data curation: LH, AF. Investigation: AF. Methodology:  
371 AF. Writing – original draft: AF, AB. Writing – review and editing: all authors. Supervision:  
372 AR, CBL, AB. Funding acquisition: AR, CBL, AB.

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### 381 DATASETS AND METHODS

#### 382 Model for fluctuation stretching

383 We introduced a simple model for the dynamics of a quantity  $\Phi(x, t)$  that varies with  
384 position vector,  $x$ , in  $D$ -dimensional Cartesian space and with time,  $t$ . We assumed  $\Phi$  to  
385 be advected by tissue growth at rate  $\bar{G}$ , to have a persistence time  $\tau$ , relaxing towards its  
386 reference value  $\langle \Phi \rangle$ , and to be driven by a stochastic source  $\xi(x, t)$ , so that

$$\partial_t \Phi(x, t) + \bar{G}/D x \cdot \partial_x \Phi(x, t) = -(\Phi(x, t) - \langle \Phi \rangle)/\tau + \xi(x, t). \quad (4)$$

387 This equation can be solved as shown in the Supplementary note.

388 **Experimental datasets**

389 In order to reliably analyse fluctuations of growth rate, we chose datasets of sepals imaged  
390 with the highest spatial resolution possible among those published. We used live imaging se-  
391 quences from [32] (dataset 1) and from [31] (dataset 2). Voxel size was  $0.12 \times 0.12 \times 0.50 \mu\text{m}^3$ .  
392 All plant lines in these sequences were crosses between Ws-4 and Col-0 ecotypes, harbour-  
393 ing respectively the microtubule reporter *p35S::GFP-MBD* and the membrane reporter  
394 *pUQ10::Lti6b-2xmCherry* [32]. The two datasets had slightly different culture conditions  
395 (type of lighting). Dataset 1 contained wild-type plants, the *spr2-2* allele of *SPIRAL2* that  
396 was originally obtained in a Col-0 background, the *bot1-7* allele of *Katanin* that was orig-  
397 inally obtained in a Ws-4 background, and the *mad5* allele of *Katanin* that was originally  
398 obtained in a Col-0 background (for *mad5*, unpublished sequences were obtained in parallel  
399 with those from [32]).

400 **Segmentation**

401 For sepals not already processed in [31, 32], cells of the abaxial epidermis were segmented  
402 and tracked in time using MorphoGraphX [45]. A triangular mesh was obtained for the  
403 outer organ surface in which cells were identified and well-delimited.

404 **Computation of growth rates**

405 We aimed at analysing fluctuations of cell relative areal growth rates tangentially to the  
406 sepal and therefore to get rid of the curvature of the outer surface of cells. To do so, we  
407 redefined the surface of cells from the linear interpolation of their contours by a flat surface.  
408 Areal growth rate was computed from the cell surface area at successive time steps. At time  
409  $t$ , each cell is labeled by an index  $i$  and has surface area  $S_{i,t}$ . Cell  $i$  may divide between  $t$   
410 and  $t+1$ ; the set  $J_{i,t}$  contains the labels of all daughters of cell  $i$  at time  $t+1$  ( $J_{i,t}$  is reduced  
411 to a single label if cell  $i$  has not divided). We only consider cells which or whose daughthers  
412 remain in the segmented region from  $t$  to  $t+1$ . The areal growth rate of the cell  $i$  at a time

413  $t$  is then defined as

$$G_{i,t} = \left( \sum_{j \in J_{i,t}} S_{j,t+1} \right) / S_{i,t} - 1. \quad (5)$$

414 Average (tissular) growth is in turn defined as  $\bar{G}_t = (\sum_i \sum_{j \in J_{i,t}} S_{j,t+1}) / (\sum_i S_{i,t}) - 1$ .

## 415 Cellular Fourier Transforms

416 The Fourier harmonics are built from a coarse and discrete version of the Laplace operator. To compute this operator we triangularized cell surfaces using the ‘MESH2D’ matlab 417 algorithm [46, 47]. More details can be found in the Supplementary note. The Cellular 418 Fourier Transform (CFT)  $\hat{G}_{k,t}$  of cell relative areal growth gives the weights by which 419 growth is decomposed over the harmonics  $e_k$  of the CFT. In this paper, the definition of 420 the CFT differ from the one in [38] by a prefactor  $1/\sqrt{S_t}$  where  $S_t$  is the total surface area. 421 This change simplifies the interpretation of Fourier spectra: the coefficients have the same 422 physical dimension as the original signal and the first coefficient is the average of the signal. 423

## 424 Scaling exponent and amplitude of fluctuations

425 We quantified spatial correlations in the tissue by fitting the spectral density with a power 426 law. To do so, we assumed a Gaussian distribution for the CFT, centred around 0 with a 427 standard deviation verifying,

$$\sigma_{k,t} = \Delta G_t q_k^{-\alpha_t} / \sqrt{\sum_l q_l^{-2\alpha_t}} \quad (6)$$

428 where  $\Delta G_t$  and the scaling exponent  $\alpha_t$  are the fit parameters characterizing respectively 429 the amplitude and the extent of spatial correlation of growth fluctuations. For the fit, we 430 used statistical inference as detailed in the Supplementary note. Doing so, we estimated a 431 probability for the parameters  $\Delta G_t$  and  $\alpha_t$ , their expected value, their standard error, and 432 median values. We also estimated the 90% confidence interval, from the fifth to the ninety 433 fifth percentiles.

434     **Temporal correlations**

435     We estimated temporal correlations of relative areal growth in considering cell growth  
 436  $G_{i,t}$  from  $t$  to  $t+1$  and cells growth  $G_{J_{i,t},t+1}$  from  $t+1$  to  $t+2$ .  $G_{J_{i,t},t+1}$  is simply the areal  
 437 growth rate from  $t$  to  $t+1$  of the descendants of the cell  $i$  in the segmentation at  $t$ :

$$G_{J_{i,t},t+1} = \frac{\sum_{j \in J_{i,t}} \sum_{l \in J_{j,t+1}} S_{l,t+2}}{\sum_{j \in J_{i,t}} S_{j,t+1}} - 1. \quad (7)$$

438     To avoid any bias due to systematic variation of growth at organ scale [32], we used the  
 439 detrended cell growth  $\delta G_{i,t}$ , which can be defined by subtracting average growth in a lo-  
 440 cal neighborhood from cell growth, see Supplementary note. Temporal correlations were  
 441 computed as Kendall's correlation coefficient  $\Gamma_t$  of  $\delta G_{i,t}$  and  $\delta G_{J_{i,t},t+1}$ . Kendall's correlation  
 442 coefficient is rank-based and so is less sensitive to outliers [39]. We used bootstrapping to  
 443 obtain confidence intervals and uncertainties.

444     We note that  $\Gamma_t$  tends to be underestimated: A positive error on  $S_{J_{i,t},t+1}$  leads to an  
 445 overestimation of  $\delta G_{i,t}$  and an underestimation of  $\delta G_{J_{i,t},t+1}$ , inducing a negative correlation  
 446 between  $\delta G_{i,t}$  and  $\delta G_{J_{i,t},t+1}$ . This may explain the few negative values of  $\Gamma_t$ . We found  
 447 this negative bias to be stronger when we defined growth from the cells outer surface area,  
 448 leading us to use the interpolation of cell contours instead (see above).

449     **Comparing genotypes**

450     To describe the impact of mutations or culture conditions on growth parameters, we com-  
 451 pared tissues at equivalent developmental stages. We first synchronized all the live imaging  
 452 sequences from a dataset by building upon the approach developed in [40]. We considered  
 453 the time curves of organ width for every sepal and finding the time delays ensuring the best  
 454 superposition between width vs. time curves, leading to a corrected time  $T_t$ . We checked  
 455 that this temporal alignment was consistent with stages of guard cell differentiation, indi-  
 456 cating that sepal width is a good proxy of developmental stage in the genotypes/conditions  
 457 that we studied. We defined the mean shift of a quantity  $\Phi_t$  as

$$\mathcal{D}_\Phi = \frac{\sum_{n',t'} \sum_{n,t} W_{t',t}^{(n',n)} (\Phi_{t'}^{(n')} - \Phi_t^{(n)})}{\sum_{n',t'} \sum_{n,t} W_{t',t}^{(n',n)}}, \quad (8)$$

458 where  $n'$  and  $n$  label the pair of sepals compared (e.g. one mutant and the reference wild-  
 459 type) and  $t'$  and  $t$  correspond to the time in the sequence of live-imaging of those two sepals.

<sub>460</sub> The sums  $\sum_{n',t'}$  and  $\sum_{n,t}$  are over all sequences of the mutant and the WT respectively.  
<sub>461</sub>  $W_{t',t}^{(n',n)}$  gives the weights at which each pair is considered. A weight differs from 0 only if  
<sub>462</sub> the values of synchronized times  $T_t$  of the pair are close, see Supplementary note for details.  
<sub>463</sub>  $\mathcal{D}_\Phi$  quantifies how much, in average, the quantities  $\Phi_t$  for the mutants (or for WT in dateset  
<sub>464</sub> 2) are shifted from the reference WT.

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## Supplementary note

## Growth couples temporal and spatial fluctuations of tissue properties during morphogenesis

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## I. MODEL FOR FLUCTUATION STRETCHING

## A. Model

25 In line with the explanation of fluctuation stretching proposed in Figs. 1-2, we model the dynamics of a quantity  
 26  $\Phi$  advected in a growing medium. If the medium grows isotropically and uniformly, its strain rate tensor in the  
 27  $D$ -dimensional space is  $\bar{G}/D\delta_{ij}$  where  $\bar{G}$  is the line, surface or volume growth for  $D = 1, 2$ , or  $3$  respectively and  $\delta_{ij}$   
 28 is the Kronecker delta tensor. We assume the dynamics of the quantity  $\Phi$  to be ruled by intrinsic cellular processes  
 29 among which some are stochastic. For simplicity, we restrict our model to lowest order and consider a linear partial  
 30 differential equation. Denoting time by  $t$  and the Cartesian space coordinate vector by  $x$ , we assume the evolution of  
 31  $\Phi(x, t)$  to be given by

$$\partial_t \Phi(x, t) + \overline{G}/D \, x \cdot \partial_x \Phi(x, t) = -(\Phi(x, t) - \langle \Phi \rangle)/\tau + \xi(x, t), \quad (1)$$

32 where the material point at  $x = 0$  serves as the origin of the spatial coordinate system.  $\partial_t$  and  $\partial_x$  respectively stand  
 33 for the partial derivative with respect to time and for the gradient. The left hand side of (1) corresponds to the  
 34 material time derivative. The first term in the right hand side ensures the relaxation of  $\Phi$  toward its reference value  
 35  $\langle \Phi \rangle$  with a time scale  $\tau$ , while the second term accounts for stochasticity through the noise  $\xi$ .

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36

## B. Linear response

37 We denote the deviation of  $\Phi$  from its reference value by  $\Delta\Phi(x, t) = \Phi(x, t) - \langle\Phi\rangle$ . The persistence time  $\tau$  sets the  
 38 memory of the system as can be seen in the explicit solution of (1),

$$\Delta\Phi(x, t) = e^{-t/\tau} \Delta\Phi(x e^{-t\bar{G}/D}, 0) + \int_0^t \frac{ds}{\tau} e^{-(t-s)/\tau} \xi(x e^{-(t-s)\bar{G}/D}, s). \quad (2)$$

39 In this equation,  $\tau$  sets the time over which initial conditions persist and the delay over which the noise impacts the  
 40 value of  $\Phi$ .

41

## C. Spatial correlation function

42 To describe the statistical properties of  $\Phi$ , we assume the noise to be Gaussian, with  $\langle\xi(x, t)\rangle = 0$  and  $\langle\xi(x, t)\xi(x +$   
 43  $l, t + s)\rangle = K\delta(s)g(|l|)$ .  $\langle.\rangle$  stands for an ensemble average,  $K$  is the noise strength, and  $\delta(.)$  is the Dirac distribution.  
 44 The function  $g(l) = \langle\xi(x, t)\xi(x + l, t)\rangle/\langle|\xi(x, t)|^2\rangle$  describes the spatial correlations of  $\xi$ , assumed to be regular and to  
 45 vanish at infinity. As a consequence of the long-ranged correlations that we predict, small scales cannot be neglected  
 46 and a Dirac distribution cannot be substituted to  $g$  without causing problems of convergence, unless a cutoff is  
 47 introduced by hand. The correlations of  $\Phi$  can be computed using (2) with  $t = -\infty$  as initial time. The space  
 48 correlation function  $C(l) = \langle\Delta\Phi(x, t)\Delta\Phi(x + l, t)\rangle/\langle|\Delta\Phi(x, t)|^2\rangle$  can then be written as,

$$C(l) = \int_0^{+\infty} (2ds/\tau) e^{-2s/\tau} g(|l| e^{-s\bar{G}/D}). \quad (3)$$

49 The space correlation function  $C(l)$  is obtained by stretching the variation lengthscales of  $g$  by a factor  $e^{-s\bar{G}/D}$  and  
 50 summing the stretched functions with weights  $e^{-2s/\tau}$ . Changing the integration variable, we rewrite (3) as,

$$C(l) = |l|^{-2D/(\tau\bar{G})} h(|l|), \quad (4)$$

51 where the increasing function  $h(|l|) = \int_0^{|l|} du u^{2D/(\tau\bar{G})-1} g(u)$  is expected to reach an asymptotic value as  $|l|$  is large  
 52 compared to the correlation length of  $\xi$ . (4) makes therefore explicit the long-ranged property of  $C$ , characterized by  
 53 the scaling exponent  $\beta = 2D/(\tau\bar{G})$ .

54

## D. Fourier spectrum

55 The Fourier transform  $\hat{\Phi}(q, t) = \int dx e^{-Iq \cdot x} \Phi(x, t)$  can be used to estimate the space correlation function  $C(l)$ . More  
 56 exactly, the mean squared spectrum  $\langle|\hat{\Phi}(q, t)|^2\rangle$  is proportional to the Fourier transform  $\hat{C}(q) = \int dle^{-Iq \cdot l} C(l) =$   
 57  $|q|^{\beta-D} h(|q|)$  with  $h(|q|) = \int d^D u |u|^{-\beta} f(|u|/|q|) e^{Iu \cdot \hat{y}}$  and  $\hat{y}$  a unit vector. It exhibits a singularity for  $|q| \rightarrow 0$  where it  
 58 scales like  $|q|^{-2\alpha}$ , with

$$\alpha = D/2 - \beta/2 = D/2 - D/(\tau\bar{G}). \quad (5)$$

59 If the correlation length of the noise source is small with respect to system size, the root mean squared spectrum can  
 60 be approximated by a power law whose amplitude relate to the standard deviation through Parseval's theorem and  
 61 whose exponent  $\alpha$  is given by the persistence time  $\tau$  and growth rate  $\bar{G}$  according to (5).

62

## II. CELLULAR FOURIER TRANSFORM

63 Here we present the computation of cell surface area, we define the discrete Laplace operator, we explain how we  
 64 built the Fourier harmonics based on this Laplace operator, and we define the Cellular Fourier Transform (CFT). The  
 65 theoretical basis of the CFT may be found in [1].

66

### A. Cell area and discrete Laplace operator

67 We compute cell area from the linear interpolation of cell contour. More precisely, we project the contour on a  
 68 plane that is perpendicular to the surface vector. The contour being polygonal, the surface factor can be written  
 69  $1/2 \sum_n \vec{r}_n \wedge \vec{r}_{n+1}$  where the sum is over the contour vertexes,  $\vec{r}_n$  is their position,  $n$  indexes the position around the  
 70 contour and  $\wedge$  is the exterior product. We then triangulate the surface enclosed in the projected contour using the  
 71 MESH2D Matlab package [2, 3]. To obtain a 3D mesh and determine the position of the mesh along the surface  
 72 vector, we performed a linear interpolation of the cell contours. The area  $S_{i,t}$  for cell  $i$  at time  $t$  is then computed as  
 73 the sum of areas of triangles in the triangulation,  $S_{i,t} = \sum_m^{(i,t)} dS_m$ , where  $m$  spans triangles of cell  $i$  at time  $t$  and  
 74  $dS_m$  is the area of triangle  $\#m$ . The tissue is made of  $N$  cells that are followed from  $t$  to  $t+1$ .

75 The discrete Laplace operator is a square matrix of size  $N \times N$  and its components are given by

$$\bar{L}_{ij,t} = \delta_{ij} - \bar{W}_{ij,t}, \text{ with, } \bar{W}_{ij,t} = \sqrt{\frac{S_{i,t}}{S_{j,t}}} \frac{\sum_m^{(i,t)} dS_m \sum_n^{(j,t)} dS_n \exp(-d_{mn}/(5\ell_c))}{\sum_m^{(i,t)} dS_m \sum_j \sum_n^{(j,t)} dS_n \exp(-d_{mn}/(5\ell_c))}, \quad (6)$$

76 where indices  $i = 0, 1, \dots, N-1$  and  $j = 0, 1, \dots, N-1$  span the  $N$  cells of the tissue.  $d_{mn}$  is the distance between  
 77 triangle  $m$  from cell  $i$  and triangle  $n$  from cell  $j$ , both considered at time step  $t$ . The unit of length is mean cell size  
 78  $\ell_c = \sqrt{S_t/N}$ , where  $S_t$  is the surface of the tissue at time  $t$  and  $N$  is the number of cells. Here we took the width  $5\ell_c$   
 79 for the coarse Laplace operator.

80

### B. Fourier harmonics

81 We define Fourier harmonics as the right singular vectors of the discrete Laplace operator  $\bar{L}$  defined in  
 82 Eq. 6. We showed in [1] that  $\bar{L}$  is a good representation of the coarse Laplace operator  $\mathcal{L}[f](x) =$   
 83  $\int dy \exp(|x-y|/(5\ell_c)) (f(x) - f(y))$ , applying to real functions  $f$  of the position vector. The singular vectors of  $\bar{L}_{ij,t}$   
 84 are, for example, expected to have the same oscillatory nature as the eigenfunctions of  $\mathcal{L}$  and their associated wave  
 85 number  $q_k$  to relate to their singular values through the same relation  $q_k = 1/(5\ell_c)Q(\lambda_k)$ , with  $Q(l) = \sqrt{(1-l)^{-2/3} - 1}$   
 86 associated to the kernel of the coarse Laplace operator [1]. The singular value decomposition of the Laplace operator  
 87  $\bar{L}$ , which yields left singular vectors  $V$ , right singular vectors  $U$ , and the singular values  $\hat{L}_k$ , is:

$$\bar{L}_{ij,t} = \sum_{k=0}^{N-1} \hat{L}_k V_{ki} U_{kj}. \quad (7)$$

88 The value taken by the  $k^{\text{th}}$ -harmonic in cell  $i$  at time step  $t$  is  $1/S_{i,t} U_{ki}$ , and its wave number is given by  $q_k =$   
 89  $1/5 Q(\hat{L}_k)$ . The harmonics are indexed so that their index grows with the wave number.

90

### C. Calculation of the CFT of cell growth

91 The areal growth rate of cell  $i$  at time step  $t$  is defined as  $G_{i,t} = \left( \left( \sum_{j \in J_{i,t}} S_{j,t+1} \right) / S_{i,t} - 1 \right) / \Delta t$  where  $J_{i,t}$  is  
 92 either the new label of cell  $i$  at time  $t+1$  or the set of labels of the daughters of cell  $i$  if it has divided, while the  
 93 time step is always  $\Delta t = 1d$ . The  $k^{\text{th}}$  CFT coefficient is then  $\hat{G}_{k,t} = \sum_i U_{ki} G_{i,t} \sqrt{S_{i,t}/S_t}$  where  $S_t$  is the total area  
 94  $S_t = \sum_i S_{i,t}$ . Here we use a convention that differs from [1] by a multiplicative factor  $1/\sqrt{S_t}$  in the definition of the  
 95 CFT. This makes the interpretation of CFTs simpler: they have the same dimensions (units) as the original signal  
 96 (here growth) and the first coefficient is equal to the average signal.

97

### III. SPATIAL CORRELATIONS

98 We estimated spatial correlations of growth from the Fourier spectra *i.e.* from the distribution of Fourier transforms  
 99  $\hat{G}_{k,t}$  and associated wavenumbers  $q_k$ . For this we used Bayesian inference.

100

### A. Inference methods applied to Fourier spectra

101 To quantify spatial correlations, we assumed the CFT coefficients,  $\hat{G}_{k,t}$  for  $k \geq 2$ , to be independent random  
 102 Gaussian variables whose mean squared deviation follows a power law with respect to the wave number  $q_k$ ,

$$\sigma_{k,t} = \Delta G_t^2 q_k^{-2\alpha_t} / \left( \sum_{l=2}^{N-1} q_l^{-2\alpha_t} \right), \quad (8)$$

103 with the parameters  $\Delta G_t$  and  $\alpha_t$  quantifying the amplitude of growth fluctuations and their space correlations,  
 104 respectively. We made the choice not to consider the first two CFT coefficients to avoid potential bias related to large  
 105 scale growth patterns, which should not be considered as fluctuations. For the derivation of the equations, it is more  
 106 convenient to rewrite (8) as  $\sigma_{k,t} = Q_k^{-2\alpha_t} / \xi$ , where  $Q_k = q_k / (\prod_{l=2}^{N-1} q_l)^{1/(N-2)}$  and  $\xi = \sum_{k=2}^{N-1} Q_k^{-2\alpha_t} / (2\Delta G_t^2)$ . We  
 107 write the probability distribution function of  $\hat{G}_{k,t}$  as

$$p_k(\hat{G}|\xi, \alpha_t) = e^{-\xi \hat{G}^2 Q_k^{2\alpha_t}} \sqrt{\frac{\xi Q_k^{2\alpha_t}}{\pi}}. \quad (9)$$

108 We use Bayesian inference to estimate  $\xi$  and  $\alpha_t$ , assuming a flat prior distribution for  $\xi \in [0, +\infty[$  and  $\alpha_t \in [0, 1]$ ,  
 109 which are the relevant range of parameters for (9). The posterior distribution for  $\xi$  and  $\alpha_t$  takes the form

$$\mathcal{P}(\xi, \alpha_t) = \frac{\prod_{k=2}^{N-1} p_k(\hat{G}_k|\xi, \alpha_t)}{\int_0^{+\infty} d\xi' \int_0^1 d\alpha' \prod_{l=2}^{N-1} p_l(\hat{G}_l|\xi', \alpha')}. \quad (10)$$

110 We then substitute the probabilities  $p_k$  by their explicit form, noting that, by construction,  $\prod_{k=2}^{N-1} Q_k = 1$ , and,  
 111 computing the first integral in the denominator, we get

$$\mathcal{P}(\xi, \alpha_t) = \frac{e^{-\xi \sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha_t}}}{\xi \Gamma(N/2) \int_0^1 d\alpha' (\xi \sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha})^{-N/2}}, \quad (11)$$

112 where  $\Gamma$  is Euler's gamma function.

### 113 B. Estimating amplitude of fluctuations and exponent of spatial correlations

114 To estimate  $\Delta G_t$ ,  $\alpha_t$  and their uncertainty, we consider the joint cumulative distribution function  $\mathcal{F}(\Delta G, \alpha)$ , of  
 115 having  $\Delta G_t$  and  $\alpha_t$  smaller than the values  $\Delta G$  and  $\alpha$ , respectively. This function can be written in terms of  $\mathcal{P}(\xi, \alpha)$   
 116 as

$$\mathcal{F}(\Delta G, \alpha) = \int_0^\alpha d\alpha' \int_{\sum_{k=2}^{N-1} Q_k^{-2\alpha'} / (2\Delta G^2)}^{+\infty} d\xi \mathcal{P}(\xi, \alpha'). \quad (12)$$

117 By using the expression  $\mathcal{P}(\xi, \alpha)$  in (11) and computing the second integral, we then get

$$\mathcal{F}(\Delta G, \alpha) = \frac{\int_0^\alpha d\alpha' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha'})^{-N/2} \Gamma\left(N/2, \sum_{k=2}^{N-1} \frac{\hat{G}_{k,t}^2}{2\Delta G^2 q_k^{-2\alpha'} / \sum_{l=2}^{N-1} q_l^{-2\alpha'}}\right)}{\int_0^1 d\alpha'' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha''})^{-N/2} \Gamma\left(N/2\right)}, \quad (13)$$

118 where  $\Gamma(a, z) = \int_z^{+\infty} dt t^{a-1} e^{-t}$  is the incomplete gamma function.

119 We used the median as a representative value of the different quantities we considered. We estimated  $\Delta G_t$  from the  
 120 median  $\mathcal{F}(\Delta G_t, 2) = .5$  and the 90% confidence interval  $[\Delta G_{1,t}, \Delta G_{2,t}]$  from the 5<sup>th</sup>,  $\mathcal{F}(\Delta G_{1,t}, 2) = .05$ , and the 95<sup>th</sup>  
 121 percentile,  $\mathcal{F}(\Delta G_{2,t}, 2) = .95$ . Similarly, we estimate  $\alpha_t$  from the median  $\mathcal{F}(+\infty, \alpha_t) = .5$  and the 90% confidence  
 122 interval  $[\alpha_{1,t}, \alpha_{2,t}]$  from the 5<sup>th</sup>,  $\mathcal{F}(+\infty, \alpha_{1,t}) = .05$ , and the 95<sup>th</sup> percentile,  $\mathcal{F}(+\infty, \alpha_{2,t}) = .95$ .

123 When we approximated their distributions by Gaussians (for fits or to estimate shifts from WT to mutants tissues),  
 124 we used the the expected value and the standard deviations of  $\alpha_t$  and  $\Delta G_t$ . We estimated the expected value of  $\alpha_t$ ,

$$\langle \alpha_t \rangle = \frac{\int_0^\alpha d\alpha' \alpha' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha'})^{-N/2}}{\int_0^1 d\alpha'' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha''})^{-N/2}}, \quad (14)$$

125 its standard deviation  $\delta\alpha = \sqrt{\langle\alpha_t^2\rangle - \langle\alpha_t\rangle^2}$  with,

$$\langle\alpha_t^2\rangle = \frac{\int_0^1 d\alpha' (\alpha')^2 (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha'})^{-N/2}}{\int_0^1 d\alpha'' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha''})^{-N/2}}, \quad (15)$$

126 the expected value of  $\Delta G_t$ ,

$$\langle\Delta G_t\rangle = \frac{\int_0^1 d\alpha' \sqrt{1/2 \left( \sum_{k=2}^{N-1} \hat{G}_{k,t}^2 * Q_k^{2\alpha} \right) \left( \sum_{l=2}^{N-1} Q_l \cdot^{-2\alpha} \right) (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha'})^{-N/2} \Gamma(N/2 - 1/2)}}{\int_0^1 d\alpha'' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha''})^{-N/2} \Gamma(N/2)}. \quad (16)$$

127 and the standard deviation  $\delta(\Delta G_t) = \sqrt{\langle\Delta G_t^2\rangle - \langle\Delta G_t\rangle^2}$

$$\langle\Delta G_t^2\rangle = \frac{\int_0^1 d\alpha' \left( 1/(N-2) \sum_{k=2}^{N-1} \hat{G}_{k,t}^2 * Q_k^{2\alpha} \right) \left( \sum_{l=2}^{N-1} Q_l \cdot^{-2\alpha} \right) (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha'})^{-N/2}}{\int_0^1 d\alpha'' (\sum_{k=2}^{N-1} \hat{G}_{k,t}^2 Q_k^{2\alpha''})^{-N/2}}. \quad (17)$$

128

#### IV. TEMPORAL CORRELATIONS

129 To quantify temporal correlations, we detrended growth from large-scale spatial patterns and we calculated Kendall's  
130 correlation coefficient of detrended growth.

131

##### A. Detrending

132 Before estimating time correlations, we corrected cellular growth using a local average of growth, aiming to detrend  
133 our estimate from large-scale deterministic spatial variations. We thus avoid potential bias induced by large scale  
134 growth variations that should not be considered as fluctuations. We use growth rate  $G_{i,t}$  of cell  $i$  between  $t$  and  
135  $t+1$ , as defined in Sec. II A. Computing local excess of growth is equivalent to apply a smooth Laplace operator to  
136 growth [1]. For convenience, we use the Laplace operator defined in (6), and we define  $\delta G_{i,t} = \sum_j L_{ij,t} \sqrt{S_{j,t}/S_{i,t}} G_{j,t}$ ,  
137 where  $j$  spans cells that can be tracked from  $t$  to  $t+2$ . Detrended growth at time  $t$  needs to be compared to detrended  
138 growth at time  $t+1$ ,  $\delta G_{J_{i,t},t+1} = \sum_{k \in J_{i,t}} \sum_j L_{kj,t+1} \sqrt{S_{k,t+1}/S_{j,t+1}} G_{j,t+1} / (\sum_{l \in J_{i,t}} S_{l,t+1})$ .

139

##### B. Kendall's correlation coefficient

140 Time correlations are quantified by Kendall's correlation coefficient  $\Gamma_t$  between  $\delta G_{i,t}$  and  $\delta G_{J_{i,t},t+1}$ . We used a  
141 bootstrap approach with  $10^4$  resamplings to quantify the statistical properties of  $\Gamma_t$ . We estimated  $\Gamma_t$  from the median  
142 of the bootstrap distribution and the bounds of the confidence interval are its 5<sup>th</sup> and its 95<sup>th</sup> percentile. Finally, we  
143 also considered  $\langle\Gamma_t\rangle$  and  $\delta\Gamma_t$  the expected value and the standard error of the distribution.

#### 144 V. ANALYSIS OF TEMPORAL VARIATIONS IN GROWTH PAREMETERS

145 We analyzed two datasets, the first containing wild-type and mutant plants while the second group contained wild-  
146 type plants grown in different conditions. We first synchronised the time series of the two datasets. We then compared  
147 mutants to wild-type sepals from plants cultured in the same conditions, or wild type sepals from plant cultured in  
148 different conditions.

149

##### A. Registration

To synchronize (register) the different time series (labeled with an upper index  $(n)$ ), we looked for the temporal  
shifts  $\Delta t^{(n)}$  that maximise the overlap of curves of width vs. time  $w_t^{(n)}$ . The perfect overlap being, in general, not  
possible, we define a distance between pairs of curves, and we choose the delays which minimise the quadratic sum

over all possible pairs  $S = \sum_{n,n'} d_{nn'}^2$ , of these distances. For two time series  $w_t^{(n)}$  and  $w_t^{(n')}$ , the distance from  $n$  to  $n'$  is defined as  $d_{nn'} = A_{nn'} - A_{n'n'}$ , where  $A_{nn'}$  is the area of the region in the Cartesian plane that is delimited to the left by the linear interpolation of  $w_t^{(n)}$  versus  $t$  and to the right by the linear interpolation of  $w_t^{(n')}$  versus  $t$ . This distance depends linearly on the the time-shifts,  $d_{nn'} = a_{nn'} - a_{n'n'} + h_{nn'}(\Delta t^{(n')} - \Delta t^{(n)})$  where  $a_{nn'}$  and  $a_{n'n'}$  are the areas  $A_{nn'}$  and  $A_{n'n'}$  before synchronization. The minimization problem is then simply quadratic and the shifts are given by the solution of

$$\sum_{n'} M_{nn'} \Delta t^{(n')} = Y_n,$$

with  $M_{nn'} = \delta_{nn'}(\sum_m h_{nm}) - h_{nn'}$  and  $Y_n = 2 \sum_{n'} (a_{nn'} - a_{n'n'}) h_{nn'}$ . The matrix  $M$  is not invertible due to invariance by translations in time, but this system can be solved by adding the condition that the smallest temporal shift (the smallest  $\Delta t^{(n)}$ ) has a value of 0. We denote by  $T_t^{(n)}$  the new temporal coordinate for live-imaging series  $n$  following registration. We checked that this temporal alignment was consistent with stages of guard cell differentiation, indicating that sepal width is a good proxy of developmental stage in the genotypes/conditions that we studied.

## 155 B. Differences between mutant and wild-type growth parameters

156 To compare a quantity  $\Phi_t$  (which could be  $\Gamma_t$ ,  $\Delta G_t$ ,  $\alpha_t$  or  $\bar{G}_t = (\sum_i \sum_{j \in J_{i,t}} S_{j,t+1}) / (\sum_i S_{i,t}) - 1$ ) between mutant 157 sepals or wild-type from dataset 2 and wild-type sepals from dataset 1, we defined the mean difference  $\mathcal{D}_\Phi$  as,

$$\mathcal{D}_\Phi = \frac{\sum_{n',t'} \sum_{n,t} W_{t't}^{(n',n)} (\Phi_{t'}^{(n')} - \Phi_t^{(n)})}{\sum_{n',t'} \sum_{n,t} W_{t't}^{(n',n)}} \quad (18)$$

158 where the upper indices  $(n')$  and  $(n)$  label the mutant and wild-type live-imaging sequences, respectively. The sums 159  $\sum_{n',t'}$  and  $\sum_{n,t}$  are over all the time points of the mutant and the wild-type, respectively.  $\mathcal{D}_\Phi$  quantifies how much, 160 on average, the quantities  $\Phi_t$  for the mutants differ from the WT. The weights  $W_{t',t}^{(n',n)}$  are defined as

$$W_{t',t}^{(n',n)} = \Lambda(T_{t'}^{(n')} - T_t^{(n)}), \quad (19)$$

161 where  $\Lambda(x) = \max(1 - |x|, 0)$  is the triangle function. This definition ensures that only differences between sepals of 162 comparable stages are considered in the distance  $\mathcal{D}_\Phi$ .

Approximating the distribution of  $\Phi_t$  to Gaussian,  $\mathcal{D}_\Phi$  has a Gaussian distribution and its expected value is

$$\langle \mathcal{D}_\Phi \rangle = \frac{\sum_{n,t} \sum_{n',t'} W_{t',t}^{(n',n)} (\langle \Phi_{t'}^{(n')} \rangle - \langle \Phi_t^{(n)} \rangle)}{\sum_{n,t} \sum_{n',t'} W_{t',t}^{(n',n)}},$$

where  $\langle \Phi_{t'}^{(n')} \rangle$  and  $\langle \Phi_t^{(n)} \rangle$  are the expected values of  $\Phi$  for the mutants and the wild-type tissues. The standard deviation is

$$\delta \mathcal{D}_\Phi = \frac{\sqrt{\sum_{n,t} \sum_{n',t'} W_{t',t}^{(n',n)} \left( (\delta \Phi_{t'}^{(n')})^2 - (\delta \Phi_t^{(n)})^2 \right)}}{\sum_{n,t} \sum_{n',t'} W_{t',t}^{(n',n)}},$$

163 where  $\delta \Phi_{t'}^{(n')}$  and  $\delta \Phi_t^{(n)}$  are the standard error of  $\Phi$  for the mutants and the WT tissues.

## 164 VI. LINEAR FIT AND RESIDUALS

165 We used statistical inference to determine which linear relation is the most likely to fit our data. We did this to test 166 if the master curve of  $\Gamma_t$  as function  $\Delta t / \tau_t$  can well be fitted by a linear relation. We also estimated the uncertainty 167 of the fit itself and tested whether the distribution of data around the fit can be explained by the data uncertainty, 168 in coherence with the hypothesis of a linear and deterministic relation between the two.

169

### A. Linear fit

170 We performed this analysis to fit the master curve  $\Gamma_t$  as function of  $\Delta t/\tau_t$ , but since we applied the same analysis  
 171 to other scatter plots, we considered here the relation between generic variables,  $x$  and  $y$ . To each measurement  
 172 performed (indexed  $i$ ) is associated a probability  $p_i(x_i, y_i)$  of finding a certain quantity  $x_i$  associated to the quantity  
 173  $y_i$ . Approximating  $p_i$  to a Gaussian distribution, and assuming no specific correlations for the error on  $x_i$  and  $y_i$ , we  
 174 can write

$$p_i(x_i, y_i) = \exp \left( -\frac{1}{2} \left( \frac{(x_i - \langle x_i \rangle)^2}{\delta x_i^2} + \frac{(y_i - \langle y_i \rangle)^2}{\delta y_i^2} \right) \right) / (2\pi\delta x_i \delta y_i), \quad (20)$$

175 where  $\langle x_i \rangle$  and  $\langle y_i \rangle$  are the expected values of  $x_i$  and  $y_i$  and  $\delta x_i$ , and  $\delta y_i$  are their standard errors. The probability of  
 176 finding the  $x$ -coordinate in  $x_i$  and of being on the line  $y = \beta_0 + \beta_1 x$  is then,  $p_i(x_i, \beta_0 + \beta_1 x_i)$  which can be written as

$$p_i(x_i, \beta_0 + \beta_1 x_i) = \exp \left( -\frac{1}{2} \left( \left( \frac{1}{\delta x_i^2} + \frac{1}{\delta y_i^2} \right) \left( x - \beta_1 \frac{\langle y_i \rangle - \beta_0 - \beta_1 \langle x_i \rangle}{\delta y_i^2 + \beta_1^2 \delta x_i^2} \right)^2 + \frac{(\langle y_i \rangle - \beta_0 - \beta_1 \langle x_i \rangle)^2}{\delta y_i^2 + \beta_1^2 \delta x_i^2} \right) \right) / (2\pi\delta x_i \delta y_i), \quad (21)$$

177 where we rearranged the argument of the exponential to write the dependence with  $x$  as a square. Integrating over  
 178  $x_i$ , we obtain the probability that the data measured in  $i$  falls on the line  $y = \beta_0 + \beta_1 x$  as

$$p_i(y = \beta_0 + \beta_1 x) = e^{-\frac{(\langle y_i \rangle - \beta_0 - \beta_1 \langle x_i \rangle)^2}{2(\delta y_i^2 + \beta_1^2 \delta x_i^2)}} / \sqrt{2\pi(\delta y_i^2 + \beta_1^2 \delta x_i^2)}, \quad (22)$$

179 The probability of having the  $n$ , assumed independent, measurements falling on  $y = \beta_0 + \beta_1 x$  is then  $\prod_{i=1}^n p_i(y =$   
 180  $\beta_0 + \beta_1 x)$ , and using flat prior for  $\beta_0$  and a Cauchy distribution as a prior for  $\beta_1$ , which is equivalent to assume a flat  
 181 prior for the orientation of the line  $y = \beta_0 + \beta_1 x$ , we get

$$P(\beta_0, \beta_1) = \frac{e^{-\frac{1}{2} \sum_{i=1}^n \frac{(\langle y_i \rangle - \beta_0 - \beta_1 \langle x_i \rangle)^2}{\delta y_i^2 + \beta_1^2 \delta x_i^2}}}{Z(1 + \beta_1^2) \sqrt{2\pi} \prod_{i=1}^n \sqrt{\delta y_i^2 + \beta_1^2 \delta x_i^2}} \quad (23)$$

182 where the constant  $Z$  given below is defined so that  $\int_{-\infty}^{+\infty} d\beta_0 \int_{-\infty}^{+\infty} d\beta_1 P(\beta_0, \beta_1) = 1$ . Introducing  $a(\beta_1) =$   
 183  $\sum_{i=1}^n 1/(\delta y_i^2 + \beta_1^2 \delta x_i^2)$ ,  $b(\beta_1) = \sum_{i=1}^n (\beta_1 \langle x_i \rangle - \langle y_i \rangle) / (\delta y_i^2 + \beta_1^2 \delta x_i^2)$ ,  $c(\beta_1) = \sum_{i=1}^n (\beta_1 \langle x_i \rangle - \langle y_i \rangle)^2 / (\delta y_i^2 + \beta_1^2 \delta x_i^2) +$   
 184  $\ln(\delta y_i^2 + \beta_1^2 \delta x_i^2)$ , we can write

$$P(\beta_0, \beta_1) = \frac{e^{-1/2(\beta_0^2 a(\beta_1) + 2\beta_0 b(\beta_1) + c(\beta_1))}}{Z(1 + \beta_1^2)}. \quad (24)$$

185 Then,  $Z = \int_{-\infty}^{+\infty} d\beta_0 \int_{-\infty}^{+\infty} d\beta_1 \frac{e^{-1/2(\beta_0^2 a(\beta_1) + 2\beta_0 b(\beta_1) + c(\beta_1))}}{(1 + \beta_1^2)}$  can be rewritten, computing the first integral, as

$$Z = \int_{-\infty}^{+\infty} d\beta_1 \frac{e^{-1/2(c(\beta_1) - b(\beta_1)^2/a(\beta_1))}}{(1 + \beta_1^2) \sqrt{a(\beta_1)}}. \quad (25)$$

186 The expected value for  $\beta_1$  is thus

$$\langle \beta_1 \rangle = \int_{-\infty}^{+\infty} d\beta_1 \beta_1 \frac{e^{-1/2(c(\beta_1) - b(\beta_1)^2/a(\beta_1))}}{Z(1 + \beta_1^2) \sqrt{a(\beta_1)}}. \quad (26)$$

187 and the standard deviation is  $\delta \beta_1 = \sqrt{\langle \beta_1^2 \rangle - \langle \beta_1 \rangle^2}$ , where

$$\langle \beta_1^2 \rangle = \int_{-\infty}^{+\infty} d\beta_1 \beta_1^2 \frac{e^{-1/2(c(\beta_1) - b(\beta_1)^2/a(\beta_1))}}{Z(1 + \beta_1^2) \sqrt{a(\beta_1)}}. \quad (27)$$

188 The expected value for  $\beta_0$  is

$$\langle \beta_0 \rangle = - \int_{-\infty}^{+\infty} d\beta_1 \frac{b(\beta_1)}{a(\beta_1)} \frac{e^{-1/2(c(\beta_1) - b(\beta_1)^2/a(\beta_1))}}{Z(1 + \beta_1^2) \sqrt{a(\beta_1)}}, \quad (28)$$

189 and the standard deviation  $\delta\beta_1 = \sqrt{\langle\beta_1^2\rangle - \langle\beta_1\rangle^2}$ , where

$$\langle\beta_1^2\rangle = \int_{-\infty}^{+\infty} d\beta_1 \left( \frac{1}{a(\beta_1)} + \left( \frac{b(\beta_1)}{a(\beta_1)} \right)^2 \right) \frac{e^{-1/2(c(\beta_1) - b(\beta_1)^2/a(\beta_1))}}{Z(1 + \beta_1^2)\sqrt{a(\beta_1)}}. \quad (29)$$

190 We computed these integrals numerically to estimate the fitting parameters and their standard deviations.

191

## B. residuals

192 We would like to test whether the expected values  $\langle\beta_0\rangle$  and  $\langle\beta_1\rangle$  enable to adequately fit the set of data. We gave  
193 in Eq. 22 the probability of having a linear relation  $y = \beta_0 + \beta_1 x$  in measurement  $i$ . For  $\beta_0 = \langle\beta_0\rangle$  and  $\beta_1 = \langle\beta_1\rangle$ ,  
194 this probability is

$$p_i(y) = \langle\beta_0\rangle + \langle\beta_1\rangle x = e^{-\frac{(\langle y_i \rangle - \langle\beta_0\rangle - \langle\beta_1\rangle \langle x_i \rangle)^2}{2(\delta y_i^2 + \langle\beta_1\rangle^2 \delta x_i^2)}} / \sqrt{2\pi(\delta y_i^2 + \langle\beta_1\rangle^2 \delta x_i^2)}, \quad (30)$$

195 We see that this probability follows a standard normal distribution with respect to the parameter  $r_i = \frac{\langle y_i \rangle - \langle\beta_0\rangle - \langle\beta_1\rangle \langle x_i \rangle}{\sqrt{\delta y_i^2 + \langle\beta_1\rangle^2 \delta x_i^2}}$ . If our assumptions are consistent, and notably the assumption that a linear relation exists be-  
196 tween  $y_i$  and  $x_i$  is correct, then the distribution of  $r_i$  over all the measurements should be close to a standard normal  
197 distribution. To assess this, we performed a Kolmogorov-Smirnov test **at the 5% significance level**. We concluded  
198 that, in the case of the master curve, the distribution of data around the fit can be explained by the uncertainty on  
199 the estimates, and that the data are compatible with the hypothesis of a linear and deterministic relation between  
200  $\Gamma_t$  and  $\Delta t/\tau_t$ , while we could not draw the same conclusions for any of the other pairwise trends. **The p-values of**  
201 **the Kolmogorov-Smirnov test for the residuals of the linear fits of all the plots of Fig. 6. of the main are given in the**  
202 **table below.**

Plot	p-value
$\Gamma_t$ vs $\bar{G}_t$	$2.2 \cdot 10^{-4}$
$\alpha_t$ vs $\bar{G}_t$	$4.3 \cdot 10^{-2}$
$\Delta G_t/\bar{G}_t$ vs $\bar{G}_t$	$3.3 \cdot 10^{-7}$
$\Gamma_t$ vs $\alpha_t$	$2.0 \cdot 10^{-2}$
$\Gamma_t$ vs $\Delta G_t/\bar{G}_t$	$8.7 \cdot 10^{-3}$
$\alpha_t$ vs $\Delta G_t/\bar{G}_t$	$1.6 \cdot 10^{-5}$
$\Gamma_t$ vs $\Delta t G_t / (2(1 - \alpha_t))$	2.5

TABLE I. p-value for the Kolmogorov-Smirnov test of the residuals of the linear fits of all the plots in Fig. 6.

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