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# Ion molecule reactions in the $\text{HBr}^+ + \text{CH}_4$ system: a combined experimental and theoretical study†

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Reactions in the system  $\text{HBr}^+ + \text{CH}_4$  have been investigated inside a guided ion-beam apparatus under single-collision conditions. The  $\text{HBr}^+$  is vibrational and rotational state selected in the electronic  $X^2\Pi_{1/2}$  state created by (2+1)-REMPI. Due to the excitation scheme employed different rotational states of the  $\text{HBr}^+$  are accessible. Four reaction channels have been observed. The cross section,  $\sigma$ , for the exothermic proton transfer channel (PT) decreases with increasing collision energy, steeper than predicted by the Langevin model. The cross section also decreases with increasing rotational energy in the  $\text{HBr}^+$ , with the effect of the rotational energy being stronger than that of translational energy. The cross section for the endothermic charge transfer (CT) increased with increasing collision energy. The energy dependence is well reproduced by a simple line of center (loc) model. Although the bromine transfer (BT) is exothermic the observed cross section increased with increasing collision energy due to an activation barrier on the potential energy surface (PES). Analysis by a modified loc model suggest the relevance of an angle dependence of  $\sigma$ . The cross section for the endothermic hydrogen atom abstraction (HA) exhibits a maximum at 2 eV  $E_{\text{cm}}$ . The measured cross sections are rationalized by means of reaction dynamics simulations which show good agreement with the experimental cross sections. The dynamics simulations are carried out with a machine learning potential that is developed and benchmarked with *ab initio* molecular dynamics simulation. The absolute cross sections predicted by reaction dynamics simulations are well within the same order of magnitude while reproducing the trends over three different collision energies for all four reaction channels. Furthermore, the simulations demonstrate various reaction mechanisms for these reaction channels, including a very interesting  $\text{HBr}^+$  orientation selectivity for the BT reaction channel.

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## Introduction

Methane is an abundant chemical species influencing earth's atmosphere as well as extra-terrestrial atmospheres. Earth's atmosphere contains an amount of methane in the order of 2000 ppb. In the last four decades the methane concentration in the atmosphere increased dramatically.<sup>1,2</sup> Li *et al.* investigated the influence of halogen species on the  $\text{CH}_4$  loss and lifetime of the  $\text{CH}_4$  in the atmosphere by simulations. This led to the conclusion that the rate of  $\text{CH}_4$  loss will decrease and therefore the total lifetime of  $\text{CH}_4$  in the atmosphere will increase until the end of the century.<sup>3</sup> Methane is also detected in the interstellar medium,<sup>4</sup> in the atmosphere of Jupiter,<sup>5</sup>

on the Saturn moon Titan,<sup>5</sup> on Enceladus<sup>6</sup> and Mars.<sup>7</sup> The atmospheres of Uranus and Neptune also contain  $\text{CH}_4$ .<sup>8</sup>  $\text{HBr}$  has been detected in the upper troposphere of Jupiter and Saturn with upper limits of 3 ppb respectively 1.6 ppb.<sup>9</sup>

Since activation barriers in ion-molecule reactions are in general small, these reactions play a major role in the interstellar medium and in planetary ionospheres. Additionally long-range interactions like Coulomb or ion induced dipole interactions favor reactions of this type.<sup>10</sup> Ion-molecule reactions (IMR) were essential in successfully describing the particle densities observed in interstellar clouds.<sup>11</sup> The chemistry of the interstellar medium is characterized by low particle densities and low temperatures ranging from 10 K to 100 K.<sup>12,13</sup> Due to the often barrierless IMRs small changes in the energetics of such systems can influence the outcome of this reaction type sensitively.<sup>12</sup>

IMR also form the basis for chemical ionization (CI) mass spectrometry. Munson and Field exploited the formation of  $\text{CH}_5^+$  from methane and its subsequent proton transfer reactions for analyzing unknown compounds.<sup>14,15</sup> Ultimately, this

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led to the development of the proton transfer reaction mass spectrometry (PTR MS) for on-line trace analysis down to the ppb level.<sup>16</sup>

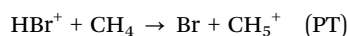
The  $\text{CH}_5^+$  ion is an intriguing chemical species and was subject of interest in numerous studies. Under laboratory conditions  $\text{CH}_5^+$  ions can be formed by radiative association of  $\text{CH}_3^+$  with  $\text{H}_2$  or by hydrogen atom abstraction in the reaction  $\text{CH}_4^+ + \text{H}_2$ .<sup>12,17</sup> Clearly, the  $\text{CH}_5^+$  ion is a rather flexible molecular ion exhibiting a potential energy surface with shallow minima.

In fact, laboratory studies have been vital in reaching the current understanding of interstellar ion chemistry. Many studies aimed at measuring cross sections or rate constants either as a function of the temperature (in thermal ensembles) or as a function of the center of mass collision energy (typically in energy selected ensembles).<sup>18,19</sup>

Rather few studies have focused on the influence of the rotational quantum state of the reactants on the reaction dynamics. As a prominent example we mention the investigation of the reaction  $\text{H}_2^+ (\nu = 0,1, j = 0,4) + \text{H}_2$  with a single and merged beam approach.<sup>20</sup> The observed cross section decreased with increasing vibrational and rotational excitation of the  $\text{H}_2^+$  ions, with the effect of the rotation exceeding that of the vibration.<sup>20</sup> Viggiano *et al.* analyzed the  $\text{Kr}^+ + \text{HCl}$  system in a SIFT apparatus. Here, the increase of the rotational temperature of the neutral target, HCl, increased the rate constant for charge transfer considerably.<sup>21</sup>

The role of ion rotation in IMR has been studied in a number of cases focusing on hydrogen halide ions,  $\text{HX}^+$  with  $x = \text{Cl}$  and  $\text{Br}$ , for which the rotational constants are large allowing to address rotational selectivity in ion preparation. Conceptually, rotational effects may be expected to be large in reactions involving hydrogen halide ions. It has been argued that there is potential relevance of the hydrogen halide ions in the upper atmosphere of earth as well as other astronomical objects.<sup>22</sup> Among the previous reaction systems investigated were the self-reactions of  $\text{HCl}^{23,24}$  and  $\text{HBr}^{25}$ . The authors groups also recently reported a combined experimental and theoretical study of the cross reaction system  $\text{HBr}^+ + \text{HCl}$ .<sup>26</sup>

In the current work the study of rotational effects is extended to the system  $\text{HBr}^+ + \text{CH}_4$ . Here, four reaction channels are accessible, these are namely:



## Experiment and simulation

### Experimental approach

The measured cross sections are analyzed using a guided ion beam setup. This was described in detail in earlier studies.<sup>27</sup>

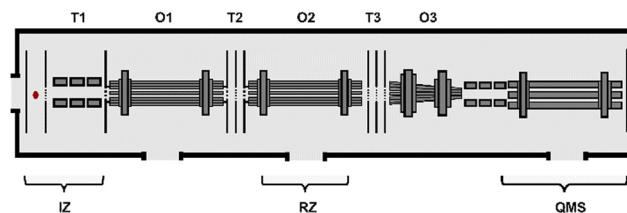


Fig. 1 Guided ion beam setup of the apparatus. Ions are created between the first electrostatic lenses marked in red. O1 and O2 indicate linear octapoles, O3 a conical octupole. T1 T2 and T3 constitute electrostatic lens systems for transfer of the ions. IZ and RZ indicate the ionization zone and the reaction zone respectively.

Here, the apparatus was improved by implementing a second linear octupole stage to inhibit undesired side reactions.<sup>26</sup> The setup is shown in Fig. 1. The ions are created by a Laser as described below, then accelerated and by a focusing stage introduced into the first new linear octupole ion guide. The collisions occur in the second linear octupole ion guide.

Behind the second linear octupole ion guide the ions are transferred into a quadrupole mass spectrometer (QMS) with the help of 2 lens assemblies and a conical octupole ion guide.<sup>28</sup>

$\text{HBr}^+$  was created in the  $X^2\Pi_{1/2}$  electronic state by (2+1) resonance enhanced multiphoton ionization (REMPI) in its vibrational ground state.<sup>29,30</sup> The REMPI transitions for ion creation were addressed with a tunable dye laser (CobraStrech, Sirah) which was pumped by a 20 Hz ND:YAG laser (INDI, Spectra Physics). The ion rotational energy was varied from 3.4 meV up to 46.8 meV. Experiments have been performed on the R(1), R(3), R(4), R(5), R(6) transition. The R(2) transition was not addressed since it overlaps with the S(0) transition. Ultimately, the REMPI excitation scheme allows to prepare  $\text{HBr}^+$  ions with narrow rotational state distribution dominated by few rotational states. The measured rotational distribution of the ions prepared on the pump lines has been reported by Penno *et al.*<sup>31</sup>

The collision energy in the center of mass frame was varied in the range from 0.25 eV up to 3 eV. The neutral reaction partner  $\text{CH}_4$  was introduced at room temperature with a dosing valve. The ions were analyzed by their mass to charge ration ( $m/z$ ) with a Quadrupole Mass Spectrometer (QMS) and detected by a Channeltron. The signals were recorded with a multichannel scaler card (FAST ComTec, P7888). The HBr pressure was set to  $5 \times 10^{-6}$  mbar and the  $\text{CH}_4$  pressure to  $3.5 \times 10^{-5}$  mbar ensuring single collision conditions. The purity of the HBr gas was 3.5, that of the methane 4.5. The kinetic data in this study are based on the analysis of the ion species  $\text{CH}_4^+$ ,  $\text{CH}_5^+$ ,  $\text{HBr}^+$ ,  $\text{H}_2\text{Br}^+$  and  $\text{CH}_4\text{Br}^+$ .

The second-order rate constant  $k_i$ , where i indicates the reaction channel, is given in eqn (1) for the general case.

$$k_i = \frac{k'_{\text{tot}} \cdot f_{\text{aproduct}}}{1 - \exp(-k'_{\text{tot}} \cdot t)} \cdot \frac{1}{[\text{CH}_4]} \quad (1)$$

Here,  $k'_{\text{tot}}$  is the pseudo-first order rate constant of the total reaction,  $f_{\text{aproduct}}$  is the fractional abundance of the respective



product and  $[\text{CH}_4]$  is the particle density of the neutral. Further details have been elaborated in the supplement by Plamper *et al.*<sup>26</sup>

Rate constants can either be transformed into cross sections employing eqn (2) assuming the velocity of the neutral target is negligible compared to that of the ion under the conditions chosen, or directly *via* the approach described by Armentrout.<sup>32</sup> Here, the fact that the neutral target molecules are not at rest but exhibit an isotropic velocity distribution in laboratory space does not affect the value of the center of mass collision energy but its distribution.<sup>33,34</sup> This corresponds to an uncertainty in  $E_{\text{cm}}$  as discussed by Plamper *et al.*<sup>26</sup> As a consequence, reaction barriers may effectively be overcome at an  $E_{\text{cm}}$  nominally below that barrier. In the  $E_{\text{cm}}$  domain this uncertainty is on the order of  $\pm 130$  meV.

$$\sigma = \frac{k}{v_{\text{HBr}^+}} \quad (2)$$

Experimental cross sections are complemented by theoretical data, in part derived from analytical models, but ultimately also from sophisticated molecular dynamics calculations.

For the exothermic reaction channels the experimental data are compared to the Langevin-model. According to the Langevin-model, the cross section of an exothermic ion-molecule reaction is given by<sup>35,36</sup>

$$\sigma_{\text{L}}(E_{\text{cm}}) = \pi \cdot \left( \frac{2 \cdot \alpha \cdot q^2}{E_{\text{cm}}} \right)^{0.5} \quad (3)$$

Here,  $q$  denotes the charge of the ion,  $\alpha$  the polarizability of the neutral molecule. The Langevin cross section  $\sigma_{\text{L}}$  scales with  $E_{\text{cm}}^{-0.5}$  and is considered as an upper limit (Langevin-limit) in the case of a polarizable target. Experimental data smaller than  $\sigma_{\text{L}}$  indicate that not each collision leads to reaction.

For target molecules with non-zero permanent dipole moment Su and Bowers developed a modified Langevin theory, the approximate dipole orientation (ADO) theory.<sup>37</sup> Since the permanent dipole moment of the  $\text{CH}_4$  is very small (approx.  $10^{-6}$  D at room temperature),<sup>38</sup> it is justified to stay with the classical Langevin model of eqn (3). Empirically, the energy dependence of cross sections for exothermic reaction channels often deviates from the  $(1/E_{\text{cm}})^{0.5}$  characteristic. To reflect this, the experimental data are modeled by eqn (4).

$$\sigma_{\text{fit}}(E_{\text{cm}}) = A \cdot \left( \frac{1}{E_{\text{cm}}} \right)^n \quad (4)$$

where  $A$  reflects a system-specific constant and  $n$  reflects the deviation from ideal Langevin behavior ( $n = 0.5$ ). An overview on classical and quantum capture theory models can be found elsewhere.<sup>39</sup>

For endothermic reaction channels, exhibiting an energetic threshold or a barrier to be overcome before reaction can proceed,<sup>40</sup> the cross section can be modeled by eqn (5)<sup>41</sup>

$$\sigma(E) = A \cdot \frac{(E - E_0)^n}{E^m} \quad (5)$$

where  $E_0$  denotes threshold for the reaction and  $A$  is scaling factor. If  $n = m = 1$  this expression simplifies to the classical line of centres model (loc).<sup>40,42–45</sup> The loc model assumes that reaction can only occur if the collision energy along a line connecting the centers of masses is larger than an effective threshold barrier.<sup>40,46</sup>

Throughout this work we will fix the value of  $n$  to  $n = 1$ . The classical loc model would be expected to apply for *e.g.* atom-atom reactions but also to reactions dominated by the center mass of two reactants.

For more complex reactions it may be necessary to account for steric effects. In the simplest case one can define two line of centers and the angle between these two lines. In the reaction system investigated in this work one loc is the  $\text{HBr}^+$  axis, the second loc can be chosen to be the Br-C axis. For such a situation Levine and Bernstein suggested eqn (6) which takes into account this effect of relative orientation in a parameterized form.<sup>40,43,45</sup> Here,  $D$  is the critical separation, which can be smaller than the hard-sphere separation,  $E'_0$  is the negative derivative of the reaction energy profile with respect to the cosine of the angle between the two axis mentioned above.<sup>43</sup> eqn (6) will be applied to the bromine transfer channel.

$$\sigma(E) = \frac{\pi D^2 (E - E_0)^2}{4 \cdot E \cdot E'_0} \quad (6)$$

Alternative models for describing cross sections for endothermic reactions have been elaborated in the literature.<sup>18,19,40,43,45,47</sup>

## Potential energy profile calculation

Although there have been studies on ion-molecule reaction involving  $\text{HBr}^+$ ,<sup>26,48–51</sup> a detailed potential energy profile of the  $\text{CH}_4 + \text{HBr}^+$  reaction has not been reported. The relativistic effects experienced by the core electrons of Br could be accounted for by an appropriate basis set with an effective core potential (ECP),<sup>52</sup> which replaces the explicit treatment of these electrons. Hundreds of combinations of computationally efficient methods (DFT and MP2) and basis sets with different ECPs were performed on a similar reaction ( $\text{HBr}^+ + \text{HCl}$ ), where the frozen core MP2 (fc-MP2)<sup>53</sup> in general is more accurate in representing the benchmark potential energy profile computed at the CCSD(T)/cc-pVDZ//CCSD(T)/CBS level of theory.<sup>48</sup> Therefore, fc-MP2 with five different ECPs for the bromine atoms (pseudopotential (PP),<sup>54</sup> LANL2DZ,<sup>55</sup> LANL2DZdp,<sup>55,56</sup> CRENBL,<sup>57</sup> Stuttgart RLC<sup>58</sup>) and cc-pVTZ<sup>59,60</sup> for carbon and hydrogen atoms have been examined to find an appropriate method for the stationary point geometry search. The heat of potential reactions is summarized in Table 1 and compared with experimental values. The latter are available for the PT, the CT and the HA reaction channels based on the 0 K heat of formation for  $\text{HBr}^+$  ( $^2\Pi_{3/2}$ ) (1097.83 kJ mol<sup>-1</sup>),<sup>61</sup> Br ( $^2P_{3/2}$ ) (117.91 kJ mol<sup>-1</sup>),<sup>61</sup>  $\text{CH}_4$  (−66.55 kJ mol<sup>-1</sup>)  $\text{CH}_5^+$  (921.98 kJ mol<sup>-1</sup>),  $\text{CH}_3$  (149.87 kJ mol<sup>-1</sup>),  $\text{CH}_4^+$  (1150.68 kJ mol<sup>-1</sup>),  $\text{H}_2\text{Br}^+$  (924.20 kJ mol<sup>-1</sup>),  $\text{HBr}$  (−27.85 kJ mol<sup>-1</sup>). It is important to note that neither fc-MP2 nor CCSD(T) accounts for spin-orbit (SO) coupling effect in  $\text{HBr}^+$  or Br, whereas the experimental heat of formation of these



**Table 1** Heat of various reactions. All numbers are given in  $\text{kJ mol}^{-1}$ , numbers in brackets are in eV. Zero-point energy is included and computed at the same level of theory

Method	PT (p1): $\text{CH}_5^+ + \text{Br}$	HA (p2): $\text{CH}_3 + \text{H}_2\text{Br}^+$	CT (p3): $\text{CH}_4^+ + \text{HBr}$	BT (p4): $\text{CH}_4\text{Br}^+ + \text{H}$	RMSE
Experimental at 0 K, SO ground state	8.61 (0.089)	42.79 (0.443)	91.55 (0.949)	—	—
“spin free” experimental	7.09	27.83	75.74	—	—
CCSD(T)-F12/cc-pVDZ-F12	5.08	30.71	86.71	25.75	6.65
fc-MP2/cc-pVTZ-	—	15.63	82.61	8.08	7.44
PP	17.34	26.85	83.49	16.30	6.32
LANL2DZ	67.42	30.74	142.74	37.50	52.08
LANL2DZdp	38.19	38.01	112.20	21.44	28.28
CRENBL	110.40	−10.92	133.10	1.55	71.79
Stuttgart RLC	60.91	32.78	133.64	40.54	45.72

species are measured at ground SO state. Therefore, the SO coupling energies reported by Fujioka *et al.*,<sup>48</sup> are used to calibrate the experimental heat of formation of  $\text{HBr}^+$  ( $^2\Pi_{3/2}$ ) or Br ( $^2P_{3/2}$ ) to obtain the “spin-free” experimental heat of reaction. For  $\text{HBr}^+$ , the four-fold degenerate spin free  $^2\Pi$  state splits into two double-degenerate ( $^2\Pi_{1/2}$  and  $^2\Pi_{3/2}$ ) states, thus the spin free energy state lies halfway between the two SO states. Hence, half of the SO coupling energy ( $31.65 \text{ kJ mol}^{-1}$ )<sup>62,63</sup> is added to the experimental heat of formation of  $\text{HBr}^+$  ( $^2\Pi_{3/2}$ ) to obtain the  $^2\Pi$  spin free energy of  $\text{HBr}^+$ . For Br, the six-fold degenerate SO states split into double degenerate  $^2P_{1/2}$  state and quadruple degenerate  $^2P_{3/2}$  state. The SO states are split in 1:2 ratio and hence, the spin free energy state  $^2P$  is obtained by adding one-thirds of the SO coupling energy ( $43.64 \text{ kJ mol}^{-1}$ ) to the experimental heat of formation of Br ( $^2P_{3/2}$ ). This protocol offers a fair comparison of the heats of reaction obtained between calculations and experiments.<sup>24,48,49</sup> Among the five ECPs tested, only PP gives good agreement (RMSE =  $6.32 \text{ kJ mol}^{-1}$ ) with the experimental heat of the reaction. Note the calculation without any ECP on Br gives a comparable result (RMSE =  $7.44 \text{ kJ mol}^{-1}$ ) as PP, but it is 5 times slower. Therefore, PP is selected as the ECP and fc-MP2/cc-pVTZ-PP is employed to explore the potential energy surface of the reaction. The transition states search is carried out with nudged elastic band (NEB)<sup>64</sup> calculations and their connections to intermediates are confirmed with intrinsic reaction co-ordinate (IRC)<sup>65</sup> calculations. The identity of critical points is confirmed by harmonic frequency calculations with  $3N-6$  ( $N$  is the number of atoms in the system) positive frequencies for the intermediates, and  $3N-7$  positive frequencies for the transition states with one imaginary frequency along the reaction coordinate. The critical points identified at the fc-MP2/cc-pVTZ-PP level of theory is reoptimized with coupled cluster with single and double excitations and perturbative triples with explicitly correlated F12 method (CCSD(T)-F12)<sup>66–68</sup> for better accuracy. As shown in Table 1, the RMSE associated with the CCSD(T)-F12/cc-pVDZ-PP-F12 level of theory is only  $6.65 \text{ kJ mol}^{-1}$ . The CCSD(T)-F12/cc-pVDZ-PP-F12 potential energy profile is used as the benchmark to screen computationally efficient method for dynamics simulations.

### Reaction dynamics simulation

The bimolecular reactions of interest are also studied using *ab initio* molecular dynamics (AIMD) simulations, in which the

trajectories are propagated classically using the energy gradients computed on the fly with the fc-MP2/6-311G(d,p)<sup>53,69</sup> level of theory. fc-MP2/6-311G(d,p) has been shown to accurately represent the dynamics of similar reactions<sup>24,26</sup> and its accuracy is further justified in this reaction system (see Results). Separated by  $8.0 \text{ \AA}$  (center of mass distance) with random orientations,  $\text{HBr}^+$  is fixed at its ground rotational and vibrational state and the rotational and vibrational states of  $\text{CH}_4$  are selected from a Boltzmann distribution at 298 K to mimic the experimental conditions. Three out of the five collision energies studied in the experiments have been simulated with AIMD, *e.g.*, 0.5, 2.0 and 3.0 eV. A chemical dynamics software VENUS<sup>70</sup> is employed to sample the initial conditions and to propagate the trajectory, which is interfaced with NWChem<sup>71</sup> for *ab initio* energy gradients. Velocity verlet<sup>72</sup> with a time step of 0.15 fs is used to propagate the trajectories, and for those having energy jumps greater than  $1 \text{ kcal mol}^{-1}$ , the time step is reduced and restarted with the same initial conditions. The simulation is stopped when the two molecules (either reactive or unreactive) are separated by a center of mass distance of  $12 \text{ \AA}$ . The impact parameter ( $b$ ) is sampled discretely with a fixed stride ( $\Delta b$ ). Firstly,  $b_{\text{max}}$  (maximum impact parameter beyond which no reactive trajectories are observed) is identified by sampling 100 trajectories at each  $b$  with  $\Delta b$  of  $0.5 \text{ \AA}$  from 0 to  $6 \text{ \AA}$ . For collision energies of 0.5 eV, 2.0 and 3.0 eV, the  $b_{\text{max}}$  are  $4.5 \text{ \AA}$ ,  $4 \text{ \AA}$  and  $4 \text{ \AA}$  respectively. After detecting  $b_{\text{max}}$ , 50 (for 0.5 eV collision energy) or 60 (2.0 and 3.0 eV collision energy) AIMD trajectories are carried out at impact parameters separated by  $\Delta b$  of  $0.25 \text{ \AA}$  between 0 and the  $b_{\text{max}}$  at each collision energy, yielding a total of 950, 1020 and 1020 trajectories for collision energies of 0.5, 2.0, and 3.0 eV, respectively.

The AIMD trajectories are further used as the training set to develop a machine learning (ML) potential to carry out simulations at a much faster rate. 171 955 unique geometries (selected by comparing distance matrices, made of the reverse of pairwise distances between all atoms in the system, of configurations from AIMD trajectories with a threshold of  $0.001 \text{ \AA}^{-1}$ ) and their energy and gradients are employed as the initial training (75%) and validation (25%) set. Several iterations of active learning were carried out – a preliminary trained ML-PES was used to propagate MLMD trajectories to potentially obtain novel geometries, which (along with their energy and gradients)





were added to the training set and produce a new ML-PES. Schnetpack<sup>73,74</sup> v1.0 is used for all ML-PES training and predictions. The MLMD trajectories are simulated using ASE's velocity Verlet integrator with a timestep of 0.15 fs and stopped when any two atoms are more than 20 Å apart. The MLMD trajectories are simulated starting from  $b = 0$  with fixed increment  $\Delta b$  of 0.1 Å to  $b_{\max}$ . The estimated  $b_{\max}$  is 4.5, 3.8 and 3.8 Å for 0.5, 2.0 and 3.0 eV collision energies. Trajectories are rejected and restarted if the vibrational energy is lower than the zero-point energy for any species. The number of trajectories simulated at collision energies of 0.5, 2.0, and 3.0 eV, are 10 350, 8200 and 8200, respectively.

## Results

### Experimental results

Experiments have been performed with  $\text{HBr}^+$  prepared in the upper SO state. The question whether the SO energy (0.328 eV<sup>62,63</sup>) is available to the reaction coordinate, will be discussed below.

The analysis of the mass spectra results in the observation of four different reaction channels. These are namely the proton transfer (PT), the hydrogen abstraction (HA), the charge transfer (CT) and the bromine transfer (BT). The mass spectra is provided in the ESI.† In Fig. 2 the cross section of the total reaction and all observable reaction channels is shown as a function of the collision energy for an ion rotational energy of 3.4 meV.

The total cross section decreases with increasing collision energy as does the PT reaction cross section, which dominates the total cross section for collision energies below 2 eV. At collision energies above 2 eV the HA reaction becomes comparable to the PT reaction. The CT and BT reactions are the least efficient reactions and both of the same order of magnitude. Below 1 eV collision energy the latter channels do not proceed

to a measurable extent. The total cross section is significantly below the Langevin prediction indicating that approximately every 4th collision leads to a reactive process.

Tichy *et al.* studied the reaction of  $\text{HBr}^+$  with  $\text{CH}_4$  in a SIFDT apparatus. The cross sections measured by Tichy *et al.* are larger than the numbers measured in this work, but in the same order of magnitude.<sup>75</sup> One difference between the work of Tichy *et al.* and this work concerns the ion preparation: in this work the  $\text{HBr}^+$  is prepared in selected rovibronic states, whereas Tichy *et al.* employed electron impact ionization, presumably leading to a broader distribution of ionic states. In both studies, the PT reaction is the most efficient reaction at low collision energies. At collision energies around 1 to 2 eV center of mass the PT channel becomes comparable to the HA channel. The CT reaction is in both studies the least efficient reaction. In the present study this reaction channel has a threshold of around 0.5 eV, comparable to the earlier study by Tichy *et al.*<sup>75</sup>

In Fig. 3 the collision energy dependence of the PT reaction is presented. The different traces correspond to different ion rotational energies. The cross section decreases with increasing collision energy. Table 1 indicates a slightly positive heat of reaction for the PT channel referenced to the SO ground state of the  $\text{HBr}^+$ . Here, the experimental observation of a cross section significantly decreasing with increasing collision energy suggests that the SO energy of the  $\text{HBr}^+$  ion prepared in the  $X^2\Pi_{1/2}$  electronic state is available to the reaction, turning it effectively into an exothermic channel.

In Table 2 the fit parameters for the PT reaction are assembled. Within the error margins the exponent  $n$  emerges constant. The decrease is much steeper than predicted by the Langevin model. With increasing rotational energy, the cross section decreases significantly, which is recognizable in Fig. 4 and indicated by the parameter  $A$ .

Fig. 4 illustrates  $\sigma_{\text{PT}}$  as a function of the ion rotational energy. The cross section is highly dependent on this degree

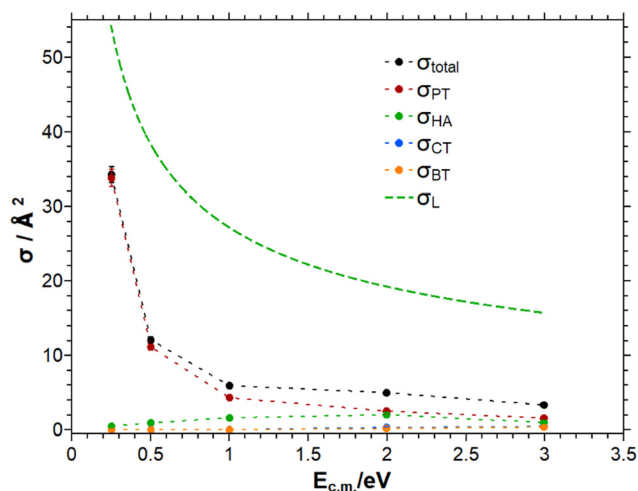


Fig. 2 Cross section of the total reaction and all observable reaction channels as a function of the collision energy  $E_{\text{cm}}$ . The data is provided for the ion rotational energy of 3.4 meV. For comparison the cross section according to the Langevin model  $\sigma_{\text{L}}$  is shown. Note, that the CT data are difficult to distinguish from the BT data plotted in front.

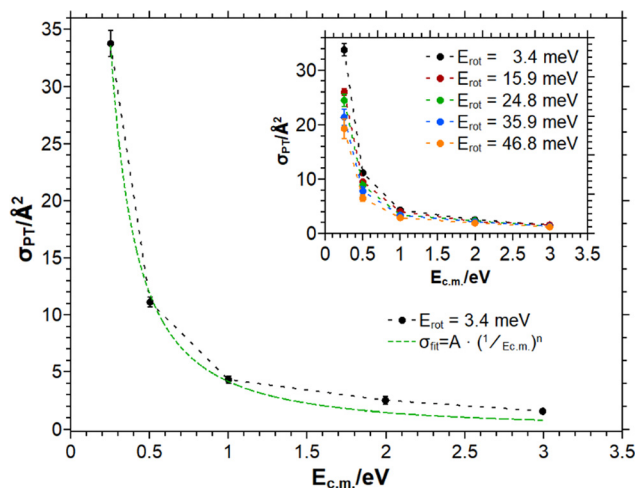
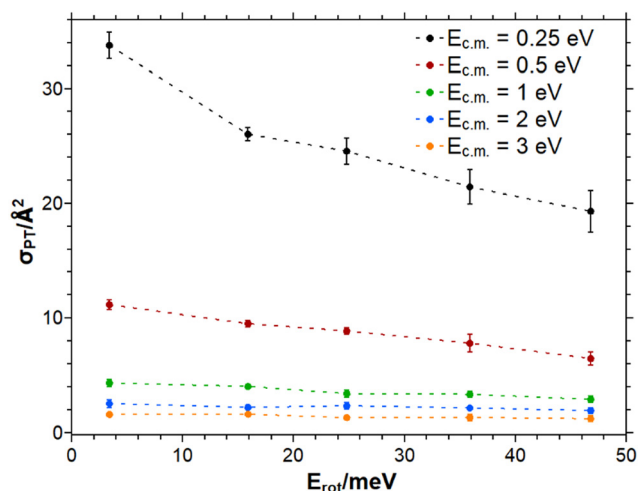


Fig. 3  $\sigma_{\text{PT}}$  as a function of the collision energy  $E_{\text{cm}}$  for different ion rotational energies. The green dotted curve is the Langevin fit to the data for  $E_{\text{rot}} = 3.4$  meV according to eqn (4).



**Table 2** Fit parameter  $A$  and  $n$  according to eqn (4) for the PT reaction

$E_{\text{rot}}/\text{meV}$	$A/(\text{\AA}^2 \cdot \text{eV}^n)$	$n$
3.4	$4.16 \pm 0.47$	$-1.52 \pm 0.09$
15.9	$3.93 \pm 0.38$	$-1.37 \pm 0.07$
24.8	$3.55 \pm 0.39$	$-1.4 \pm 0.09$
35.9	$3.3 \pm 0.39$	$-1.36 \pm 0.09$
46.8	$2.68 \pm 0.43$	$-1.43 \pm 0.12$

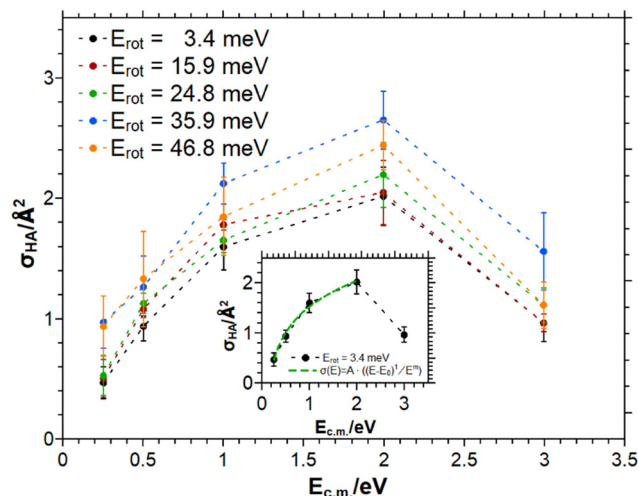
**Fig. 4**  $\sigma_{\text{PT}}$  as a function of  $E_{\text{rot}}$ .

of freedom. By using the Langevin fit for the rotational energy of 3.4 meV the cross section decreases by the same amount in collision energy by  $8.4 \text{ \AA}^2$  over 50 meV, whereas the same amount of rotational energy at 0.25 eV collision energy leads to a decrease of  $13 \text{ \AA}^2$ . Thus, the rotational motion of the ion has a larger influence on the reaction dynamics than the center of mass collision energy and is not only an additive contribution to the total excess energy.

As indicated in Fig. 5 the cross section of the HA reaction increases with increasing collision energy as expected for an endothermic reaction channel. The threshold behavior of  $\sigma_{\text{HA}}$  is modelled by eqn (5) fixing  $n = 1$  in the range from  $E_{\text{cm}} = 0.25 \text{ eV}$  up to 2 eV (*i.e.*, the maximum of  $\sigma_{\text{HA}}$ ). The fit parameters  $A$ ,  $E_0$  and  $m$  are summarized in Table 3.

Note, that the center of mass collisional energy as well as the rotational energy may help in overcoming the chemical threshold for the reaction. This fact is reflected in the observation, that the effective  $E_0$  fitted to the data decreases with increasing rotational energy (*cf.* Table 3). The decrease in  $E_0$  is in fact comparable to the concomitant increase in the rotational energy. The reaction barrier  $E_0$  derived (*ca.* 0.16 eV) matches well the heat of reaction assuming the SO energy of  $\text{HBr}^+$  is available to the reaction (0.443–0.328 eV).

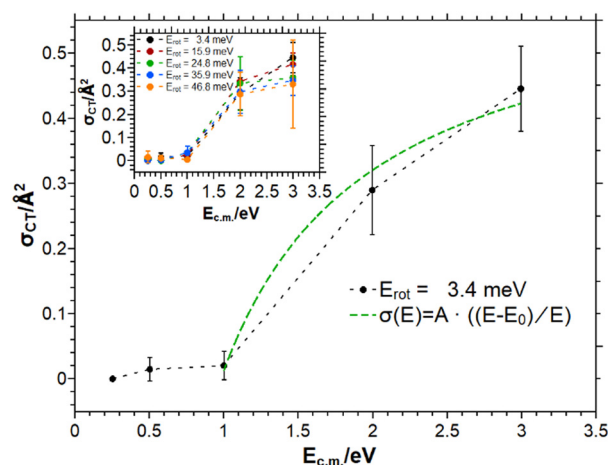
At 2 eV  $E_{\text{cm}}$  the cross section has a distinct maximum. At even higher collision energies the cross section decreases significantly. The increase up to 2 eV can be modelled by the classical loc model suggesting that no angle dependence of the HA reaction is operative. This appears in line with the intuitive expectation, because the transition state for the HA reaction

**Fig. 5**  $\sigma_{\text{HA}}$  as a function of the collision energy shown for the investigated ion rotational energies. The applied fit model is discussed in the text below and summarized in eqn (5).**Table 3** Fit parameter for the HA reaction according to eqn (5), using  $n = 1$ 

$E_{\text{rot}}/\text{meV}$	$A/\text{\AA}^2 \text{ eV}^{m-1}$	$E_0/\text{eV}$	$m$
3.4	$1.81 \pm 0.16$	$0.16 \pm 0.04$	$0.70 \pm 0.12$
15.9	$2.03 \pm 0.19$	$0.18 \pm 0.04$	$0.83 \pm 0.14$
24.8	$1.95 \pm 0.01$	$0.15 \pm 0.01$	$0.72 \pm 0.01$
35.9	$2.11 \pm 0.41$	$0.06 \pm 0.12$	$0.60 \pm 0.23$
46.8	$1.92 \pm 0.04$	$0.09 \pm 0.01$	$0.62 \pm 0.03$

should not involve steric requirements. As complementation, a plot of the cross section for HA as a function of the rotational energy is presented in the ESI.†

In Fig. 6 the collision energy dependence of the CT reaction is presented. The green dotted line is a fit to the data for  $E_{\text{rot}} = 3.4 \text{ meV}$  according to eqn (5) with  $n$  and  $m$  equaling unity and a

**Fig. 6** Collision energy dependence of the CT reaction. Different traces correspond to the different investigated ion rotational energies. The green dotted line is a line of centres model fit as indicated.

**Table 4** Fit parameter for the collision energy dependence of the CT reaction according to the loc model

$E_{\text{rot}}/\text{meV}$	$A/\text{\AA}^2$	$E_0/\text{eV}$
3.4	$0.63 \pm 0.05$	$0.98 \pm 0.06$
15.9	$0.63 \pm 0.03$	$0.96 \pm 0.03$
24.8	$0.55 \pm 0.06$	$0.92 \pm 0.08$
35.9	$0.52 \pm 0.03$	$0.93 \pm 0.05$
46.8	$0.52 \pm 0.04$	$0.98 \pm 0.06$

scaling factor  $A$  which reflects the line of centers (loc) model. All parameters obtained in the analysis of the CT reaction channel are listed in Table 4.

The model fits the experimental data quite well. The threshold of the reaction,  $E_0$ , is found to be  $0.95 \pm 0.03$  eV for all investigated rotational energies. The almost exact agreement between this threshold and the experimental heat of reaction given in Table 1 is fortuitous. In principle the true molecular threshold could be higher than the numbers given in Table 1 due to the smearing out of center of mass collision energies.<sup>34</sup> For a step like model for the cross section this could lead to observing products some 0.25 eV below the true threshold. For the rather shallow increase of  $\sigma$  with  $E_{\text{cm}}$  as operative in the loc model (and also in the modified loc model), convolution with the thermal velocity distribution of the neutral target reveals an effective additional smearing out which is below 50 meV. Given the limited number of data points we would be reluctant to overinterpret the threshold values. On the other hand, it suggests that the SO energy deposited in the  $\text{HBr}^+$  ion upon preparation is not available for the reaction in this channel. Evaluating the PES of the CT reaction (cf. Fig. 8(c)) there is no indication of additional activation barriers. As complementation, a plot of the cross section for CT as a function of the rotational energy is presented in the ESI.†

In Fig. 7 the collision energy dependence of the BT reaction is presented. Overall, the efficiency of the BT reaction is

**Table 5** Fit parameter according to eqn (6) for the BT reaction

$E_{\text{rot}}/\text{meV}$	$E_0/\text{eV}$	$E'_0/\text{eV}$
3.4	$0.78 \pm 0.04$	$22.26 \pm 0.85$
15.9	$0.86 \pm 0.01$	$19.49 \pm 0.2$
24.8	$1.06 \pm 0.08$	$16.11 \pm 1.59$
35.9	$1.16 \pm 0.07$	$15.56 \pm 1.46$
46.8	$0.7 \pm 0.01$	$24.25 \pm 0.21$

comparable to that of the CT reaction. However, the characteristics of the variation of  $\sigma$  with  $E_{\text{cm}}$  is distinctly different.

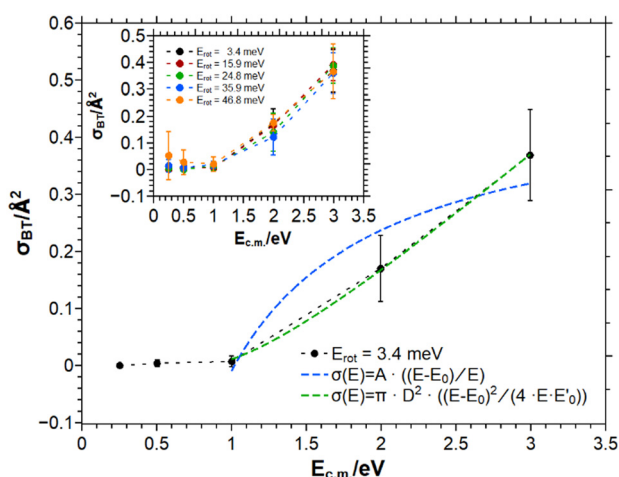
Below 1 eV collision energy no reaction is observable. Above this threshold, the cross section for BT has been fitted both by the simple loc model and the modified loc model. Quite obviously the modified loc model fits significantly better to the experimental data shown in Fig. 7. We conclude that the BT channel must be subject to sterical restriction. Note, that in the modeling, the critical distance  $D$  was chosen to be 2.53 Å using the covalent radii of H, Br and C. An overview over the fit parameter obtained for all rotational energies of the  $\text{HBr}^+$  is given in Table 5. As complementation, a plot of the cross section for BT as a function of the rotational energy is presented in the ESI.†

The data shows the typical behavior of a reaction with a threshold. The *ab initio* potential energy surface (cf. Fig. 8(d)) shows an activation barrier for the spin-free BT reaction channel lying around 0.54 eV. Since the calculation of that PES is based on a spin-free Hamiltonian, the true spin-orbit energies for  $\text{HBr}^+$  in the  $^2\Pi_{3/2}$  and  $^2\Pi_{1/2}$  would correlate with barriers being approximately 0.16 eV higher or lower respectively. The experimental finding of an effective threshold around 1 eV possibly indicates that the spin orbit energy of the  $\text{HBr}^+$  is not available for the BT reaction coordinate, similar to the CT.

As mentioned above the collision energy dependence of CT and BT reaction channels exhibits a characteristic difference. While  $\sigma_{\text{CT}}$  shows a right-curved characteristic above the threshold, well represented by the classical loc model,  $\sigma_{\text{BT}}$  shows a left-curved characteristic above the threshold only represented by the modified loc model. As a consequence, it is concluded that the BT reaction channel is angle-dependent in contrast to the CT reaction channel, where sterical orientation does not appear to play a role.

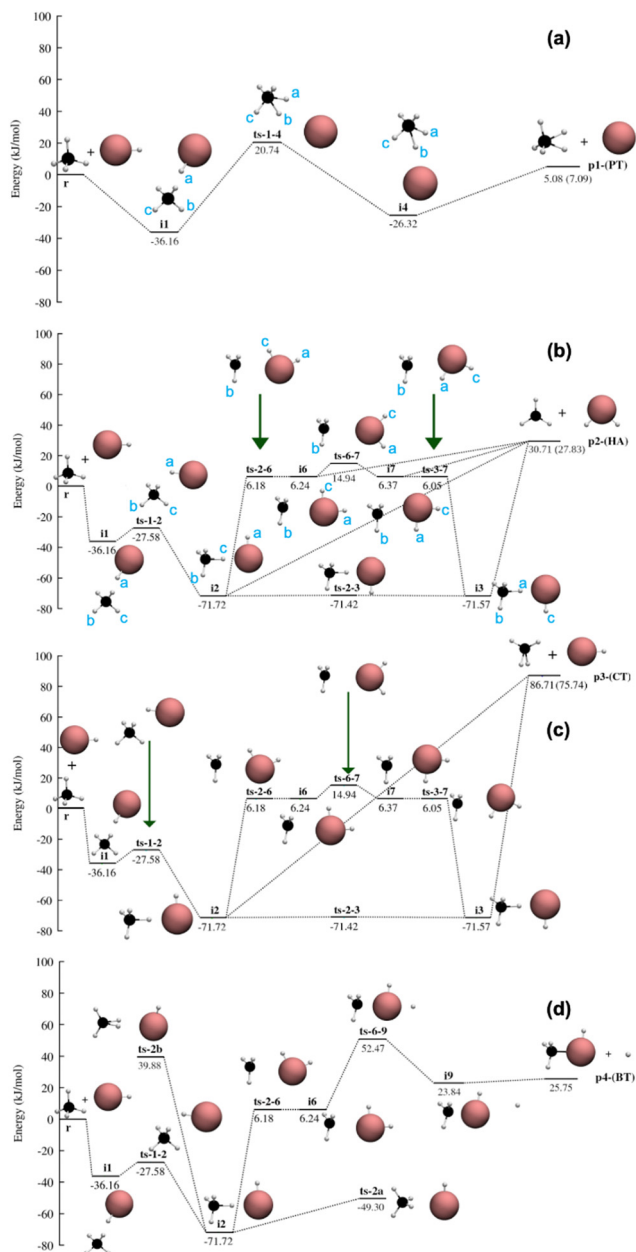
### The potential energy profile

The potential energy profile of the proton transfer (PT) pathway is shown in Fig. 8(a), where the proton from  $\text{HBr}^+$  is transferred to  $\text{CH}_4$  forming  $\text{Br} (^2\text{P})$  atom and  $\text{CH}_5^+$  (carbonium ion). The barrierless association between  $\text{CH}_4$  and  $\text{HBr}^+$  (**r**) forms a van der Waals (vdW) complex **i1** ( $-36.16$  kJ mol $^{-1}$  with respect to separated reactant, **r**) where the proton from  $\text{HBr}^+$  ( $\text{H}_a$ ) is pointing towards the  $\text{CH}_4$  molecule. **i1** isomerizes to another vdW complex **i4** ( $-26.32$  kJ mol $^{-1}$ ) via a transition state **ts-1-4** that is 20.74 kJ mol $^{-1}$  above **r**. Following the IRC of **ts-1-4**, Br pivots around  $\text{CH}_5^+$  and moves from coordinating with  $\text{H}_a$  in **i1** to  $\text{H}_b$  ( $\angle \text{C-H}_b\text{-Br} = 180^\circ$ ) in **i4**. This pivoting mechanism is a result of the 3 centered 2 electron bond of  $\text{H}_a\text{-C-H}_b$  where  $\text{H}_a$



**Fig. 7** Experimental cross section of the BT reaction. The main graph shows the  $E_{\text{rot}} = 3.4$  meV data together with two fits. The blue dotted line is a fit according to the loc model, whereas the green dotted line originates from the improved loc model. The inset shows traces corresponding to additional rotational energies.





**Fig. 8** Potential energy profile of PT (a), HA (b), CT (c) and BT (d) reaction channels at CCSD(T)-F12/cc-pVDZ-PP-F12 level of theory with ZPE included. The atoms are represented as black (C), maroon (Br) and white (H). The energies in parentheses are experimental heats of reaction. The coordinates of these stationary points are given in the ESI†

and  $H_b$  possess most of the partial positive charges.  $C_s$  symmetry is maintained throughout the path where  $Br-H_a-C-H_b-H_c$  are in the same plane. **i4** can dissociate without a transition state to form **p1** ( $Br(^2P) + CH_5^+$ ). The PT reaction is endothermic by  $5.08 \text{ kJ mol}^{-1}$  with an overall barrier of  $20.74 \text{ kJ mol}^{-1}$  (**ts-1-4**). The structure and reactivity of  $CH_5^+$  has been extensively studied in the literature<sup>76–86</sup> since its discovery in the 1950s which show that  $CH_5^+$  is highly fluxional with many different local minimum structures.<sup>87</sup> But the global minimum among them is the  $C_s(I)$  structure<sup>88</sup> as depicted in

the Fig. 8(a). It is important to note that experimental and previous dynamics study of  $CH_5^+$  have shown its tendency to dissociate into  $CH_3^+$  and  $H_2$  molecule,<sup>77</sup> which is out of the scope of the present work.

The potential energy profile of the hydrogen abstraction (HA) pathway is shown in Fig. 8(b), where  $HBr^+$  abstracts one hydrogen atom from  $CH_4$  to form planar  $CH_3$  radical ( $D_{3h}$ ) and  $H_2Br^+$  ( $C_{2v}$ ). The vdW complex **i1** ( $-36.16 \text{ kJ mol}^{-1}$ , see the PT pathway) is connected to a submerged barrier **ts-1-2** ( $-27.58 \text{ kJ mol}^{-1}$ ), where  $HBr^+$  (instead of just Br as seen in the PT pathway) pivots around  $CH_4$  to form **i2** ( $-71.72 \text{ kJ mol}^{-1}$ ). **i2**, stabilized by the hydrogen bond between  $H_c$  and Br, possesses a ‘staggered’ conformation where the dihedral angle of  $H_a-Br-C-H_b$  is  $180^\circ$ . **ts-2a** ( $-49.30 \text{ kJ mol}^{-1}$ ) (Fig. 8(d)) is a self-isomerization transition state of **i2**, where  $CH_4$  tumbles, but does not lead to the products.  $CH_4$  in **i2** could also rotate with respect to  $C-H_c-Br$  axis to form the ‘eclipsed’ conformer **i3** ( $-71.57 \text{ kJ mol}^{-1}$ ), where the dihedral angle of  $H_a-Br-C-H_b$  is  $0^\circ$ . The corresponding transition state of this rotation, **ts-2-3** ( $-71.42 \text{ kJ mol}^{-1}$ ), is well less than  $1 \text{ kJ mol}^{-1}$  compared to **i2** and **i3**. The H atom in the  $CH_4$  group of **i2** and **i3** can transfer to Br, forming **p2** without a transition state. **p2** could also be formed without a transition state *via* vdW complexes **i6** ( $6.24 \text{ kJ mol}^{-1}$ ) and **i7** ( $6.37 \text{ kJ mol}^{-1}$ ), where the H has already transferred from  $CH_4$  to  $HBr$ , but the newly formed  $H_2Br^+$  has not dissociated. **i6** (‘staggered’) and **i7** (‘eclipsed’) are roaming complexes formed from its corresponding H-bond complex **i2** and **i3**, which can also isomerize to one another *via* transition state **ts-6-7** ( $14.94 \text{ kJ mol}^{-1}$ ). The C–Br distance changes from  $2.92 \text{ \AA}$  (**i6**)  $\rightarrow 3.21 \text{ \AA}$  (**ts-6-7**)  $\rightarrow 2.92 \text{ \AA}$  (**i7**) in this process on a relative flat potential energy profile. The HA reaction is endothermic by  $30.71 \text{ kJ mol}^{-1}$ .

The potential energy profile of the charge transfer (CT) pathway is shown in Fig. 8(c), where an electron is transferred from  $CH_4$  to  $HBr^+$ . The CT reaction pathway is very similar to the HA pathway, except **p3** is only formed *via* a barrierless dissociation of **i2** and **i3** (not **i6** and **i7**).  $CH_4$  changes from  $T_d$  point group to  $C_{2v}$  point group after losing an electron, while the H–Br bond length decreased from  $1.43 \text{ \AA}$  to  $1.40 \text{ \AA}$  after gaining an electron. The CT reaction is the most endothermic ( $86.71 \text{ kJ mol}^{-1}$ ) among all the reaction pathways.

The potential energy profile of the bromine transfer (BT) is shown in Fig. 8(d), which forms  $CH_4Br^+$  ( $C_s$ ) and H. As noted in the method section, although the experimental heat of formation of  $CH_4Br^+$  is not known to date, there is one ion-beam experiment tentatively speculating its formation.<sup>89</sup> Theoretical investigation by Chistyakov *et al.*<sup>90</sup> reported the geometries and energies of  $CH_4Br^+$  as intermediates of the  $CH_4 + Br^+ \rightarrow BrH + CH_3^+$  reaction. While the level of the theory (MNDO/PM3) in Chistyakov *et al.* is not considered as state of the art anymore, its reported structure (Fig. 8(d)) agrees with CCSD(T)-F12/cc-pVDZ-PP-F12 geometry optimization in this study. Electron density analysis shows that the net positive charge is mostly concentrated on Br. The BT reaction pathway follows the reaction pathways of HA and CT until **i6**. The  $H_2Br$  in **i6** could recombine with  $CH_3$  and form a vdW complex, **i9** ( $23.84 \text{ kJ mol}^{-1}$ ), after crossing a barrier (**ts-6-9**) of  $52.74 \text{ kJ mol}^{-1}$ . According to





fc-MP2/cc-pVTZ-PP, several vdW complexes similar to **i9** have been identified with the H atoms at different positions with respect to  $\text{CH}_4\text{Br}^+$ , suggesting a roaming region in the potential energy surface. However, these stationary points could not be confirmed with CCSD(T)-F12/cc-pVDZ-PP-F12 level of theory, thus they are not reported in Fig. 8. Further **i9** dissociates to **p4** without a transition state. The BT reaction is endothermic ( $25.75 \text{ kJ mol}^{-1}$ ) with an overall barrier of  $52.47 \text{ kJ mol}^{-1}$  (**ts-6-9**).

### Computationally efficient method for AIMD simulations

The potential energy profile is informative for a conceptual understanding of the mechanism of the reaction, but it relies on the assumptions that the reaction behaves statistically (sufficient lifetime of each intermediate) and strictly follows the IRC. Numerous examples have shown that these assumptions are not necessarily true in bimolecular reactions,<sup>24,26,49,91–94</sup> thus *ab initio* molecular dynamics (AIMD) simulations are carried out. In AIMD, the positions of the atoms are propagated by the classical equations of motion with the potential energy gradients computed using quantum chemistry on the fly. AIMD demands an enormous number of gradient calculations, often in the order of millions to sample an ensemble of trajectories (of different orientations, impact parameters, *etc.*) that represent the experimental conditions. Therefore, it is imperative to screen different computationally efficient methods for one that can accurately characterize the potential energy profile. In the current study of  $\text{CH}_4 + \text{HBr}^+$  bimolecular reaction, the collision energies in the experiments range from  $48.25 \text{ kJ mol}^{-1}$  (0.5 eV) to  $289.46 \text{ kJ mol}^{-1}$  (3.0 eV). According to the CCSD(T)-F12/cc-pVDZ-PP-F12 potential energy profile, all stationary points reported in Fig. 8 are within the energy range thus should be included in selecting the quantum chemistry method for AIMD.

Both frozen core and non-frozen core MP2 has been screened in this study due to our previous experiences with similar reaction systems.<sup>26,49</sup> 15 different basis sets, including 6-311G(d,p),<sup>95,96</sup> aug-cc-pVTZ-PP,<sup>59,60,97</sup> aug-cc-pVTZ,<sup>59,60,97</sup> pc-1,<sup>98,99</sup> pc-2,<sup>98,99</sup> aug-pc-1,<sup>98,99</sup> aug-pc-2,<sup>98,99</sup> cc-pVDZ,<sup>59,60</sup> cc-pVDZ-PP,<sup>59,60</sup> cc-pVTZ,<sup>59,60</sup> cc-pVTZ-PP,<sup>59,60</sup> def2-SVP,<sup>100</sup> def2-SVPD,<sup>100</sup> def2-TZVP<sup>100</sup> and def2-TZVPD,<sup>100</sup> are screened. Each method/basis set attempts to identify the stationary points found by CCSD(T)-F12/cc-pVDZ-PP-F12. An appropriate method/basis set for AIMD simulation should be able to identify all stationary points in Fig. 8 and have a small root mean square deviation (RMSD) with the benchmark PES. The RMSD of a candidate method/basis set (A) is computed as:

$$\text{RMSD}(\text{A}, \text{ref}) = \sqrt{\frac{1}{K} \sum_{i=1}^K (E_i^{\text{A}} - E_i^{\text{ref}} - \Delta E(\text{A}, \text{ref}))^2} \quad (7)$$

$$\begin{aligned} \Delta E(\text{A}, \text{ref}) &= \arg \min_{\Delta E} \left( \frac{1}{K} \sum_{i=1}^K (E_i^{\text{A}} - E_i^{\text{ref}} - \Delta E)^2 \right) \\ &= \overline{E_{\text{A}}} - \overline{E_{\text{ref}}} \end{aligned} \quad (8)$$

**Table 6** RMSD ( $\text{kJ mol}^{-1}$ ) of each candidate method with respect to benchmark method. n/a indicates at least one of the optimal structure in Fig. 8 could not be optimized

fc-MP2	RMSD ( $\text{kJ mol}^{-1}$ )	MP2	RMSD ( $\text{kJ mol}^{-1}$ )
6-311G(d,p)	10.7	6-311G(d,p)	11.2
aug-cc-pVTZ	9.9	aug-cc-pVTZ	n/a
aug-cc-pVTZ-PP	10.5	aug-cc-pVTZ-PP	n/a
aug-pc-1	15.1	aug-pc-1	15.1
aug-pc-2	10.3	aug-pc-2	10.9
cc-pVDZ	11.4	cc-pVDZ	11.0
cc-pVDZ-PP	10.8	cc-pVDZ-PP	10.9
cc-pVTZ	9.4	cc-pVTZ	n/a
cc-pVTZ-PP	9.1	cc-pVTZ-PP	9.3
pc-1	15.6	pc-1	16.1
pc-2	12.4	pc-2	13.5
def2-SVP	12.4	def2-SVP	13.9
def2-SVPD	n/a	def2-SVPD	10.4
def2-TZVP	11.2	def2-TZVP	13.0
def2-TZVPD	11.5	def2-TZVPD	11.2

$K$  ( $K = 20$ ) is the number of stationary points (including reactants and products). The energy shift  $\Delta E(\text{A}, \text{ref})$  is difference between the average potential energy computed from candidate method A ( $\overline{E_{\text{A}}}$ ) and CCSD(T)-F12/cc-pVTZ-PP-F12 ( $\overline{E_{\text{ref}}}$ ).  $i$  is the index of stationary points. Table 6 contains the RMSD of the screened candidate method/basis set for AIMD simulations. It is important to note that Table 6 only assesses the performance of these methods on the  $\text{CH}_4 + \text{HBr}^+$  bimolecular collision and should not be taken as a comparison of their general performance. The same convergence criteria such as maximum ( $1.5 \times 10^{-5}$  hartree bohr $^{-1}$ ) and RMSD ( $1.0 \times 10^{-5}$  hartree bohr $^{-1}$ ) change in energy gradient, maximum ( $6.0 \times 10^{-5}$  bohr) and RMSD ( $4.0 \times 10^{-5}$  bohr) change in coordinates are applied to all candidate methods. fc-MP2/def2-SVPD, MP2/aug-cc-pVTZ, MP2/aug-cc-pVTZ-PP, and MP2/cc-pVTZ fail to optimize **i6**, **i7**, and **i9**, hence their RMSDs are marked as **n/a** and are not considered further. The results show that both fc-MP2 and MP2 have fairly low RMSD with all tested basis set, with the lowest ( $9.1 \text{ kJ mol}^{-1}$ ) and largest ( $16.1 \text{ kJ mol}^{-1}$ ) RMSD found in fc-MP2/cc-pVTZ-PP and MP2/pc-1, respectively. Considering the cost of MP2 method scales as  $N^{5.48}$  where  $N$  is the number of basis functions which ranges between 52 (fc-MP2/cc-pVDZ-PP) and 220 (MP2/aug-pc-2), the cost of these candidate method/basis sets varies dramatically. Generally speaking, the level of theory with an RMSE of  $\sim 10 \text{ kJ mol}^{-1}$  or smaller could be used for trial runs, where the energy conservation of the trajectory, the stability of molecular orbital, and the converging speed will be used to further select a quantum chemistry method for AIMD simulations.

### Simulation results

All four reaction channels observed in experiments are detected in simulations and their cross sections are compared in Fig. 9. First, it is interesting to note that trace amount of hydrogen exchange (HE, hydrogen from  $\text{HBr}^+$  ion is exchanged with one of the hydrogens from neutral  $\text{CH}_4$  molecule) reactions is detected in the simulation (*e.g.*, cross section  $\sim 0.01 \text{ \AA}^2$ ), which cannot be distinguished from the non-reactive collisions in the



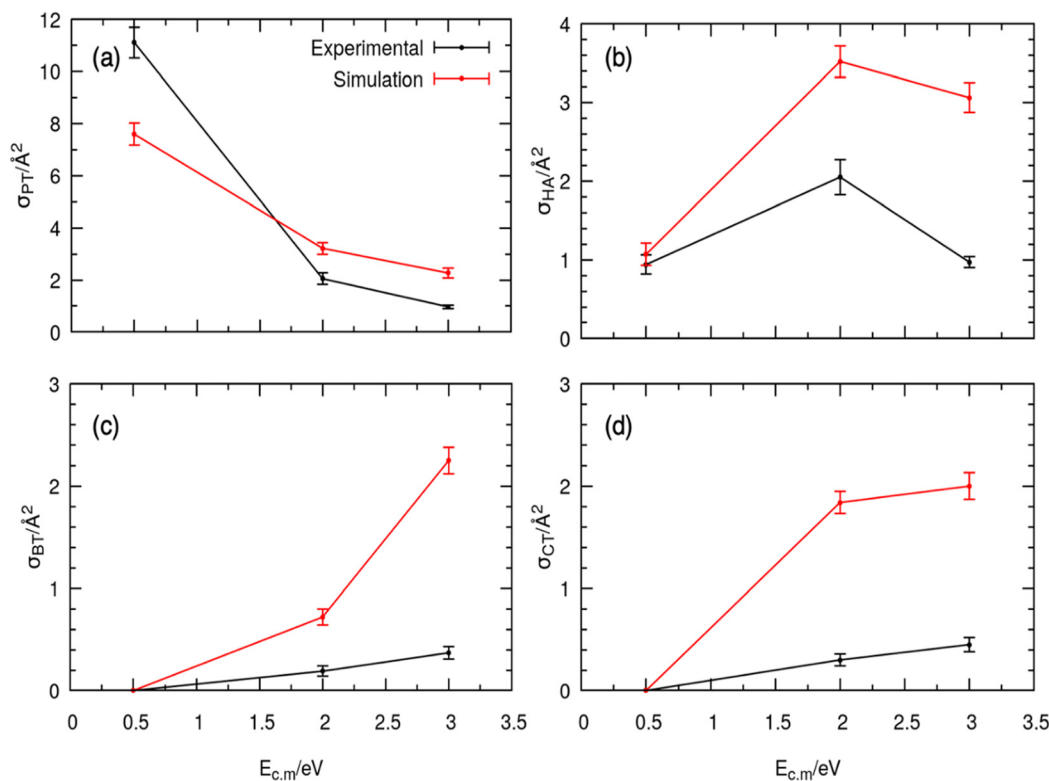


Fig. 9 Reactive cross sections of the four product channels *i.e.*, PT (a), HA (b), BT (c), and CT (d) measured from the experiments (black) and reaction dynamics simulations (red) at three collision energies.

guided-ion beam experiments. Second, for the PT (proton from  $\text{HBr}^+$  ion is transferred to  $\text{CH}_4$  molecule, forming neutral Br atom and  $\text{CH}_5^+$  carbonium ion) reaction, the cross section obtained from the simulation agrees well with the experiment. While the simulations in general overestimate the cross section of HA (hydrogen from  $\text{CH}_4$  is transferred to  $\text{HBr}^+$  ion, forming  $\text{H}_2\text{Br}^+$  ion and neutral  $\text{CH}_3$  radical), BT (the Br from  $\text{HBr}^+$  is transferred to  $\text{CH}_4$  molecule, forming  $\text{CH}_4\text{Br}^+$  ion and hydrogen atom), and CT (single electron is transferred from neutral  $\text{CH}_4$  molecule to  $\text{HBr}^+$  ion, forming neutral HBr molecule and  $\text{CH}_4^+$  ion) reactions, they qualitatively reproduce the trend observed in the experiment, including the local maximum observed in the HA reaction at 2.0 eV collision energy. The simulations also reproduce the relative branching ratios of the products, for example, at 0.5 eV collision energy, nearly  $88 \pm 10\%$  of the reactive trajectories yield PT products and the remaining  $12 \pm 2\%$  are HA products; no CT or BT products are observed. This is in good agreement with the experiment where the reaction cross section of CT and BT products are negligible, while the cross section of HA is about one order of magnitude smaller than the PT. At higher collision energies (*i.e.*, 2.0 eV and 3.0 eV), the agreement becomes only qualitative due to the overestimate of the cross section for HA, BT, and CT reactions. Nonetheless, the simulations agree with the experiments that PT is the most predominant reaction, followed by HA.

Ion-molecule collisions yield products *via* direct and indirect mechanism<sup>26,48,49,93,94,101–105</sup> with their scattering angle

measured according to the illustration in Fig. 10. Reactive trajectories which do not form long-lived intermediates are classified as direct reactions. Following the convention of other ion-molecule reactions, direct reactions are classified as direct rebound (DR) and direct stripping (DS), where DR is mostly observed at small impact parameters and direct stripping (DS) is mostly observed at large impact parameters. The scattering angle distribution of direct reactions of each reaction will be discussed in detail later in the manuscript. Reactive trajectories with significant lifetime of the collision complex are classified as indirect reactions, whose collision complex is long-lived (*e.g.*, longer than the time for intramolecular vibrational energy redistribution) before dissociating into products, and as a result, yielding a near isotropic scattering angle distribution.

Snapshots of representative trajectories of different reaction mechanisms in all pathways are provided in Fig. 10. Taking the dynamics of the reaction in the case of 2.0 eV collision energy as an example, a strong correlation between the reaction pathway and the scattering angle is observed. Fig. 11 shows the scattering angle distributions for all four reaction pathways. As noted earlier, PT and HA are the predominant reactions. The PT reaction shows large scattering angles, where the product ion leaves in the opposite direction as the reactant ion, indicating the dominance of the DS mechanism (Fig. S6(b), ESI†). The DS mechanism is also the dominating mechanism for the HA reaction (Fig. S6(c), ESI†), but in this case, resulting in small scattering angle, where the product ion leaves in the same



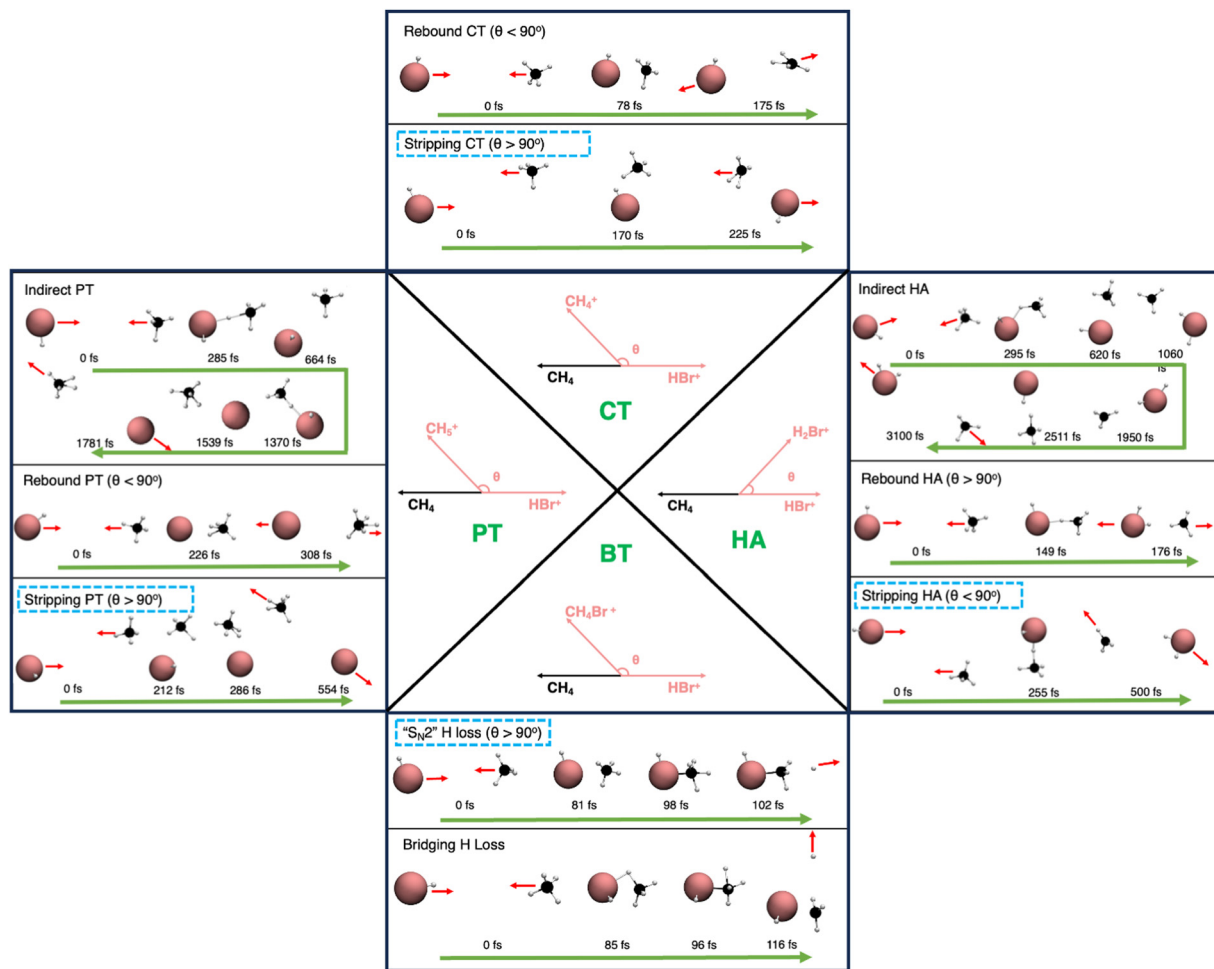


Fig. 10 Illustration of the definition of scattering angle  $\theta$ , which is defined as the angle between the velocities of the reactant and product ions (pink vectors).  $\bar{v}_i$  and  $\bar{v}_f$  denote the velocities before and after collision. Snapshots from representative trajectories of different reaction mechanisms are provided in the box. Blue dotted box denotes the dominant mechanism for each reaction channel.

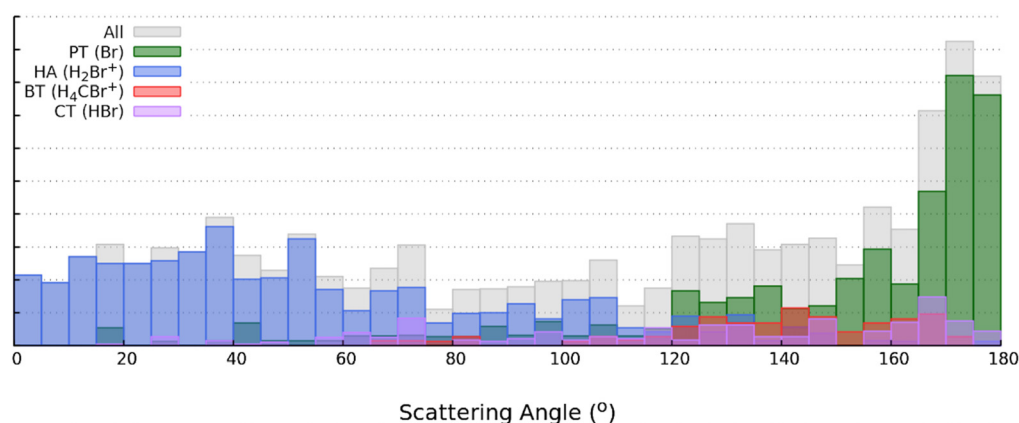


Fig. 11 The scattering angle distribution (overall, gray; PT, green; HA, blue; BT, red; and pink, CT) from the simulation for 2.0 eV.

direction as the reactant ion. Overall, the dynamics of the PT and HA reactants are in accordance with what have been reported in similar ion–molecule bimolecular collisions, e.g.,  $\text{HBr}^+ + \text{HCl}$  and  $\text{HCl}^+ + \text{HCl}$ .<sup>24,26</sup>

CT and BT are two minor reaction pathways observed in this reaction (Fig. 9). CT reaction takes place only *via* direct mechanism across all impact parameters. This result is similar to what Luo *et al.*<sup>24</sup> reported in the study of the  $\text{HCl}^+ + \text{HCl}$



bimolecular collision, although the strong selectivity of the entrance channel complex (*e.g.*, only those trajectories where chlorine collides with chlorine result in CT) is absent in the current system. More than 70% of the CT trajectories follow the DS mechanism (Fig. S6(a), ESI<sup>†</sup>), leading to large scattering angles. Similar to CT, all the BT products are formed *via* direct mechanism and the initial contact determines the reaction mechanism (Fig. 10): (1) the bridging H loss: if the hydrogen in CH<sub>4</sub> is directly colliding onto the bromine of HBr<sup>+</sup>, it acts as a bridging atom between the C and Br, which is squeezed out immediately by these two heavy atoms to form the C–Br bond in CH<sub>4</sub>Br<sup>+</sup>. In this case, the hydrogen atom (and the accompanying CH<sub>4</sub>Br<sup>+</sup>) traverses perpendicular to the C–Br axis, resulting in a scattering angle of near 90 degrees. This is evident from the scattering angle distribution in Fig. S6(d) (ESI<sup>†</sup>). (2) the “S<sub>N</sub>2” H loss: if the CH<sub>4</sub> is orientated in a direction that allows for the bromine to directly form a bond with carbon, the H atom of CH<sub>4</sub> on the opposite side of the bromine will pop away. In this case, the hydrogen atom (and the accompanying CH<sub>4</sub>Br<sup>+</sup>) traverses parallel along the C–Br axis, resulting in a near 180-degree scattering angle Fig. S6(d) (ESI<sup>†</sup>). Combining the scattering angles from all reactions, the overall scattering angle of the HBr<sup>+</sup> + CH<sub>4</sub> is shown in Fig. 11.

## Discussion

In this section, the results presented are put into the context of previous work. Four different reaction channels have been observed for the reaction system HBr<sup>+</sup> + CH<sub>4</sub>, proton transfer (PT), hydrogen atom abstraction (HA), charge transfer (CT) and bromine cation transfer (BT).

The PT reaction shows a monotonically decreasing cross section with increasing collision energies implying that no significant barrier is operative on that reaction coordinate. The SO energy seems to be available to the reaction coordinate. The cross section for PT also decreases with increasing rotational energy. A similar trend was observed in earlier studies HBr<sup>+</sup> + HBr<sup>25</sup> and HBr<sup>+</sup> + HCl.<sup>26</sup> In the reaction system HBr<sup>+</sup> + HCl the influence of the rotational energy on the PT cross section was more pronounced than that of collision energy.<sup>26</sup> The data presented in this work exhibit the same trend.

The cross section for the endothermic hydrogen abstraction can be fitted to the simple loc model up to  $E_{\text{cm}} = 2$  eV. Beyond this collision energy the cross section decreases significantly. This can be rationalized by the switching-on of competing reactions, in particular the CT and the BT channel, which is observed also in the AIMD simulations. The PES prompt similar reaction pathways for the HA and BT channels with identical transition state followed by splitting up into different pathways. In the experiment the BT pathway appears significantly enhanced at the largest collision energies employed, while the HA channel appears suppressed at the largest collision energies. This observation comes along with the finding that the BT channel is the only channel exhibiting a quadratic increase of the cross section with increasing  $E_{\text{cm}}$ , which can

be modelled by the modified loc model suggesting an angle-dependence of the reaction, which is in line with the simulation results qualitatively.

In contrast, the cross section for CT can be fitted by the simple loc model which implies no angle dependence. The thermochemical threshold for the CT reaction pathway, as obtained from the calculated PES, is higher than the corresponding activation barrier of the BT reaction. This observation is consistent with experimental results, which also indicate a lower threshold for the BT reaction channel.

The cross sections for BT as well as CT are basically independent of the rotational energy of the ion, the cross section for HA has only a minor dependence on the ion rotation. In contrast, the cross section for PT markedly decreases with rotational energy of the ion, at least for the smallest  $E_{\text{cm}}$  investigated. To be effective, the PT channel requires the hydrogen atom pointing in the direction of the CH<sub>4</sub>. A higher rotational velocity will likely disfavor the passage through the transition state geometry.

For the HA and the CT reaction orientational requirements do not appear to pose a major restriction to the efficiency of those reaction channels. Consequently, the cross sections appear less affected by the rotational motion. However, the BT channel requires the Br atom of HBr<sup>+</sup> ion oriented towards CH<sub>4</sub> for the reaction to proceed.

Finally, the threshold for the respective reaction channels suggests that the spin-orbit energy of HBr<sup>+</sup> employed in the experiment may not automatically be available to the reaction. The SO energy in the HBr<sup>+</sup> ion appears to be available for the reaction for the PT and the HA channel, but not for the CT channel. We note, that earlier studies by Paetow *et al.* clearly showed that the spin orbit energy of the X<sup>2</sup>Π<sub>1/2</sub> state is also available for the PT reaction in HBr<sup>+</sup> + CO<sub>2</sub>.<sup>27,106</sup>

It is of interest to note the behavior of the cross section of the PT reaction in AIMD simulations, which is slightly endothermic (5.08 kJ mol<sup>−1</sup>) and has a non-negligible barrier (20.74 kJ mol<sup>−1</sup>). Normally one would expect its cross section to increase as the collision energy increases but the simulation shows that the cross section decreases monotonically from 0.5 eV to 3.0 eV. We currently do not have a thorough explanation to this phenomenon, but we note the previous statement relies on maintaining a statistical ensemble that follows the intrinsic reaction coordinate. In the current system, the excess energy overwhelms the barrier and the heat of the reaction – the lowest collision energy simulated is 48.24 kJ mol<sup>−1</sup> (0.5 eV). As a result, 47% percent of PT and 7% of HA trajectories are direct, as they simply glide over the intermediates and barrier reported in the potential energy profile (Fig. 8) and directly form the product (*cf.* Table 7). The ratio of direct reaction increases to over 90% when the collision energy is 289.44 kJ mol<sup>−1</sup> (3.0 eV). In these cases, an increase in the collision energy results in the reactants having even less time to interact with each other, thus the reaction probability decreases. A thought experiment can be laid out to make the point – even for an exothermic reaction, if the collision energy is infinite, the molecules would simply be passing through each other and no reaction can be observed.





**Table 7** Percentage of trajectories in the AIMD simulations of mechanisms indicated

Collision energy (eV)	Direct PT trajectories	Direct HA trajectories
0.5	47%	7%
2.0	84%	77%
3.0	87%	91%

We note, that a similar observation has been arrived at with the  $\text{HBr}^+ + \text{CO}_2$  reaction system.<sup>49</sup> Considering a well-benchmarked ML potential has been developed in this work, more AIMD simulations below 0.5 eV will be conducted to verify the impact of the collision energy when it is below the barrier of the reaction and detect the turning point after which the cross section decreases with the increase of collision energy.

The agreement between the simulations and experiments is qualitative, as shown in Fig. 9. The disagreement can be attributed to the lack of SO-coupling effect in the simulations and the differences between the SO-free PES used in the simulation and the true SO-free PES. However, it is important to realize that (1) the true SO-free PES is not accessible except for the heat of the reaction and (2) the PES for the simulations is selected from the benchmark, which only mimics the true PES. As shown in Table 6, there is a finite difference between the PES of the simulation and the benchmark thus only qualitative agreement can be expected. Nonetheless, it is our opinion that the level of agreement reported in this manuscript is better than other AIMD simulations of similar reactions, where only the trend of the cross section (*e.g.*, normalized cross section) *vs.* collision energy is compared to the experiment.<sup>24,26,49,107,108</sup> In other cases where the absolute cross sections are reported, they are off by one order of magnitude from the experiment.<sup>109,110</sup> In particular there is almost quantitative agreement between the experimental and AIMD calculated cross sections for the dominating PT channel. The fact that both are lower by a factor of 3 compared to Langevin theory consistently indicates that on the average every third collision is reactive.

## Summary

Four reaction channels in the system  $\text{HBr}^+ + \text{CH}_4$  were investigated experimentally and analyzed. The PT exhibits characteristics of an exothermic reaction taking into account the SO energy in the  $\text{HBr}^+$ . The HA and the CT are endothermic reaction with no dominant activation barriers observed in the PES. The BT pathway is dominated by an intermediate barrier. All measured cross sections are below the Langevin limit. The absolute values are observed between  $34 \text{ \AA}^2$  and  $0.1 \text{ \AA}^2$ .

The cross section of the PT reaction decreases with increasing collision energy as expected but steeper than predicted by the Langevin model. The monotonic decrease of  $\sigma_{\text{PT}}$  suggests that no effective barrier is operative in the PT reaction.  $\sigma_{\text{PT}}$  decreases with increasing rotational energy.

The HA cross section exhibits a maximum at 2 eV collision energy and decreases beyond this to the primal cross section value. The HA cross section is independent of the ion rotation with the exception at the point of similar angular speed of the reactants, where there is a maximum.

The CT reaction exhibits characteristics of a typical endothermic reaction. Experimentally the thermodynamic threshold was determined to be  $0.95 \pm 0.03 \text{ eV}$ .

The cross section of the BT reaction fit quite well with a modified loc model, suggesting an angle-dependence to be operative. In contrast no angle-dependence appears operative for the CT reaction. For both reaction channels the cross sections are independent of the ion rotational motion in the range of collision energies investigated.

A machine learning potential for the title reaction system has been devised, which allowed the successful rationalization of experimentally measured cross sections as well as prediction of mechanistic aspects not directly accessible to the experiment.

## Associated content

There is ESI† available which contains the discussion of single collision conditions, the mass spectra and the data treatment.

## Author contributions

The experiments discussed have been conducted by D. P., the AIMD calculations and machine-learning potential have been worked out by K. F. and A. V. The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

## Conflicts of interest

There are no conflicts to declare.

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