

# Physical, Chemical and Morphological Evolution of Incipient Soot Obtained from Molecular Dynamics Simulation of Acetylene Pyrolysis

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## Abstract

Incipient soot particles obtained from a series of reactive molecular dynamics simulations were studied to understand the evolution of physical, chemical, and morphological properties of incipient soot. Reactive molecular dynamics simulations of acetylene pyrolysis were performed using ReaxFF potential at 1350, 1500, 1650, and 1800 K. A total of 3324 incipient soot particles were extracted from the simulations at various stages of development. Features such as the number of carbon and hydrogen atoms, number of ring structures, mass, C/H ratio, radius of gyration, surface area, volume, atomic fractal dimension, and density were calculated for each particle. The calculated values

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of density and C/H ratio matched well with experimental values reported in the literature. Based on the calculated features, the particles were classified in two types: type 1 and type 2 particles. It was found that type 1 particles show significant morphological evolution while type 2 particles undergo chemical restructuring without any significant morphological change. The particle volume was found to be well-correlated with the number of carbon atoms in both type 1 and type 2 particle, whereas surface area was found to be correlated with the number of carbon atoms only for type 1 particles. A correlation matrix comparing the level of correlation between any two features for both type 1 and type 2 particle was created. Finally, based on the calculated statistics, a set of correlations among various physical and morphological parameters of incipient soot was proposed.

*Keywords:* Soot, Molecular Dynamics, Radius of gyration, C/H Ratio, Surface Area

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## 1. Introduction

Soot, also known as black carbon, is a particulate matter that is an unwanted byproduct of incomplete combustion of hydrocarbon fuels [1]. It greatly influences the radiative energy balance of the atmosphere and is a major forcing factor behind climate change [2, 3]. It also impacts public health and welfare and is one of the leading causes of mortality worldwide [4]. Exposure to soot or black carbon can lead to serious health issues such as cancer [5] and cardiovascular diseases [6]. Due to the ubiquitous presence

9 of combustion events – both natural and anthropogenic – it is essential to  
10 understand the formation and evolution of soot particles in order to regulate  
11 and control their detrimental effects [7].

12 The precise mechanism underlying the formation of soot particulates from  
13 gaseous species remains uncertain, primarily due to the intricate chemical  
14 composition of the hydrocarbon system, the multiphysics interplay, and the  
15 multiscale nature of the soot formation process. The soot formation and  
16 growth involve a series of complex physical and chemical processes [8, 9].  
17 These include the generation of gaseous precursor molecules such as poly-  
18 cyclic aromatic hydrocarbons (PAHs)[10, 11, 12], the inception of the incipi-  
19 ent soot particles through the physical and chemical interactions among these  
20 precursor molecules [1, 13], the aging of these particles via surface growth due  
21 to dehydrogenation and carbon-addition from the gas phase and due to ag-  
22 gregation via coagulation and coalescence [1, 14, 15], and the fragmentation  
23 and oxidation of soot particles [1, 13, 15, 16].

24 Due to the complex physicochemical interactions, soot undergoes signif-  
25 icant alterations in its internal structure and physical properties during its  
26 evolution. These modifications occur as the particles progress from the ini-  
27 tial stage of incipient soot to the intermediate stage of young soot, ultimately  
28 culminating in the final stage of mature soot [1]. Initially, clusters of gaseous  
29 PAHs come together to form the first incipient soot particles. During the  
30 later stages of formation, the incipient soot undergoes surface chemical reac-  
31 tions and surface condensation of PAHs, resulting in the transformation of

incipient soot into young soot. The properties of young soot can be described as having a liquid-like structure and a relatively low level of graphitization [1, 17, 18]. Mature soot exhibits a highly organized graphitic structure that possesses a minimal level of curvature [17, 18].

The C/H ratio of soot particles increases as the particles get matured. For example, the C/H ratio of freshly formed soot particles is less than 2.0 [19] while the young soot particles can attain a C/H ratio ranging from 2.0 to 4.5 [20]. Mature soot particles usually have a C/H ratio of 4.5 or higher [20]. The average C/H ratio of soot particles from a premixed ethylene flame was also reported by Schulz et al. [19] to be around 2.33. The density of the soot particles also changes as the particles go through maturation. The empirical density of young and mature soot particle is measured to be 1.5 g/cm<sup>3</sup> [21] and 1.7-1.9 g/cm<sup>3</sup> [22], respectively. The values reported or assumed in multiple other studies [23, 24, 25, 14] are comparable to this.

The internal structure of soot consists of both aromatic and aliphatic carbon atoms. The presence of 5- and 6-member ring structures have been identified as an important feature of the soot core [14, 26, 27, 28], which influences mechanical properties of soot [29]. The physicochemical properties of mature soot particle that come out of a combustion system is strongly dependent on the internal structure of particles, which in turn depend on the physicochemical evolution process that the particle has gone through since its formation. [1].

In recent years, there have been remarkable experimental advances into

55 understanding the internal structure of soot. Almost all of these recent exper-  
 56 imental findings show the importance of ring structures in various stages of  
 57 soot. For example, Schulz et al. [19] observed multiple aromatic compounds  
 58 with aliphatic side chains; Gleason et al. [30] showed that soot nuclei can  
 59 form from aromatic compounds with only one or two rings; Cheng et al. [31]  
 60 observed structural changes such as onset of micropores and graphitic micro-  
 61 crystals of carbon black and soot particles during their evolution; Carbone  
 62 et al. [32] found that the optical properties of soot change as soot graphitizes  
 63 during its evolution; Jacobson et al. [33] explored the molecular structure of  
 64 soot and concentration of PAH in soot; Commoco et al. provided insights  
 65 of the importance of  $sp^3$  carbon and advanced graphitic structure [34] and  
 66 aliphatic pentagonal rings [35] in the early stages of soot formation. When  
 67 analyzing the radiation scattering by soot particles using refractive index,  
 68 discrete element modeling with discrete dipole approximation simulations  
 69 showed that the mass absorption coefficient of soot increases by up to 75%  
 70 with increasing residence duration in premixed fires of low equivalency ratio  
 71 [36]. Increased soot maturity is the cause of this, which is in great agreement  
 72 with evidence obtained from laser induced incandescence in ethylene flames  
 73 [37] and premixed methane [38].

74 However, despite these recent findings, our knowledge about the evolu-  
 75 tion of internal and physicochemical properties of soot is still incomplete.  
 76 Since the exact physical and chemical pathways behind the formation and  
 77 evolution of soot particles from incipient to mature are still not fully known,

78 there is considerable uncertainty in the estimation of the physical, chem-  
 79 ical, and morphological properties of soot at various stages. This poses  
 80 difficulty down the line in engineering-scale modeling, where the goal is of-  
 81 ten to model soot emissions from combustion systems at a scale relevant  
 82 to real-world devices. Engineering-scale reactive CFD models are compu-  
 83 tational models that operate at the continuum scale and are designed to  
 84 capture the continuum-scale dynamics of reactive flow. These models are ca-  
 85 pable of replicating the combustion behavior of real-world systems, including  
 86 laboratory-scale flames, internal combustion engines, and fires, and can pro-  
 87 vide estimations of both local and global characteristics of the reactive flow  
 88 field. Because of the inherent complexity involved in combustion modeling  
 89 and the vast difference in scales, it is impractical for engineering-scale models  
 90 to keep track of the evolution of the internal atomic structures of the parti-  
 91 cle. Therefore, engineering-scale models of soot formation often depend on  
 92 approximations. Notable numerical soot models such as the semi-empirical  
 93 two-equation model [39], method of moments [40, 41, 42, 43, 44], stochastic  
 94 soot model [45], discrete sectional model [46, 47, 48, 49, 50], etc. all con-  
 95 tain several approximations and/or hypotheses to simplify the inception and  
 96 growth of soot. These approximations, which include, but are not limited to,  
 97 inception due to dimerization of soot precursor [40, 41], the spherical shape  
 98 of particles [40, 39], constant density [45], etc. exist partly due to our incom-  
 99 plete knowledge of underlying soot-related processes and partly due to the  
 100 complexity of combustion modeling.

101 In this work, we attempt to mitigate some of these shortcomings of  
102 engineering-scale soot models by providing an improved estimation – by way  
103 of reactive molecular dynamics simulation – of various soot properties as soot  
104 evolves in combustion systems. We extend our previous work on acetylene  
105 pyrolysis using reactive molecular dynamics (RMD) at four different process  
106 temperatures [51] to investigate how physical, chemical, and morphological  
107 properties of incipient soot evolve and how are they correlated with one an-  
108 other.

109 Reactive molecular dynamics allows for modeling the chemical evolution  
110 in a reacting system by tracking bond breakage and bond formation among  
111 atoms. This provides an unprecedented view of physicochemical transforma-  
112 tions that take place during soot inception [52, 53, 54, 55]. One of the most  
113 common tools for modeling reactive hydrocarbon systems in RMD is the  
114 reactive force field (ReaxFF) [56] for carbon, hydrogen, and oxygen chem-  
115 istry [57, 58]. RMD has been used to explore pyrene dimerization [52], which  
116 is often treated as a key step in soot nucleation. RMD has also been utilized  
117 to look at other mechanism of soot nanoparticle formation [54], the inception  
118 of soot from different PAHs such as naphthalene, pyrene, coronene, ovalene  
119 and circumcoronene [53]. Recently, the effect of oxygenated additives on  
120 diesel soot was also explored via RMD [55]. RMD also allows for a detailed  
121 atomic exploration of the internal structure of soot [29, 51]. For example,  
122 the amount of cross-linking in the core and shell structure of developing and  
123 mature soot particles were explored in [29]. In our previous study, we also

124 identified the presence of a denser core with the existence of ring structures  
125 at the center of larger incipient soot particles [51].

126 Molecular dynamics simulations, while providing atomistic insights, are  
127 computationally demanding. To optimize these simulations while ensuring  
128 realistic outcomes, it is standard practice to select higher temperatures and  
129 molecular concentration. At such conditions, particle inception and growth  
130 take place within a few microseconds and can be elucidated by reactive molec-  
131 ular dynamics [55, 59, 60]. At the same time, the impact of temperature on  
132 soot-related processes can be significant. Elevated temperatures have been  
133 shown to accelerate the graphitization process, transforming the structure of  
134 soot particles to become more spherical and mature [61]. This structural  
135 transformation also affects the surface functional groups (SFGs) associated  
136 with soot particles, altering their reactivity and physical characteristics. Such  
137 findings are supported by Pathak et al., who documented the temperature-  
138 dependent graphitization in candle soot [61]. Liu et al. have discussed how  
139 these transformations influence the key characteristics of soot particles, such  
140 as reactivity and fractal dimension [62]. Furthermore, it has been reported  
141 that below 1500 K, acetylene pyrolysis is primarily driven by a radical mech-  
142 anism that leads to polymerization reactions [63]. Above this temperature  
143 threshold, the dominant process shifts to the homolytic fission of C-H bonds,  
144 indicating a fundamental change in the chemical pathways [64]. Addition-  
145 ally, the research by Wittig et al. [65] has highlighted that soot formation  
146 reaches its peak at around 1850 K. Considering these findings in the liter-

147 ature and typical temperature range seen in real-world combustion systems  
148 [66, 67, 32], we selected four different process temperatures – 1350, 1500,  
149 1650, and 1800 K – in our study. By doing so, we ensure that the simula-  
150 tions not only reflect the true nature of soot formation but also adhere to  
151 the realistic conditions under which these particles are typically formed.

152 The RMD simulations at the four temperatures yield numerous incipient  
153 soot particles at different stages of growth. The physicochemical characteris-  
154 tics of the soot particles are subsequently examined to explore the statistical  
155 measures that can be used to describe the development of the initial soot  
156 particle. The main objective of this article is to provide insights into the  
157 physicochemical and morphological characteristics of early-stage soot par-  
158 ticles acquired through RMD simulations and to explore possible correla-  
159 tions among various properties which can potentially be used to improve  
160 engineering-scale soot models.

## 161 **2. Numerical Methodology**

### 162 *2.1. Simulation configurations*

163 The RMD approach taken in this study has been reported in [68], and the  
164 exact simulation configurations for this study have been previously described  
165 in [51]. Therefore, we only provide a brief summary here. 1000 acetylene  
166 molecules are randomly distributed within a  $75\text{\AA} \times 75\text{\AA} \times 75\text{\AA}$  cubic domain  
167 at four different temperatures: 1350, 1500, 1650, and 1800 K. This tem-  
168 perature range is consistent with those used in laminar flames [69] or flow

169 reactors [70]. Each configuration was simulated multiple times with different  
 170 randomization. The simulations were done in Large-scale Atomic/Molecular  
 171 Massively Parallel Simulator (LAMMPS) software [71] using the ReaxFF  
 172 potential [56, 72] with a timestep of 0.25 fs following Mao et al. [53]. The  
 173 simulations are conducted using the NVT (constant number, volume, and  
 174 temperature) ensemble using the velocity-Verlet algorithm [73] along with  
 175 the Nose-Hoover thermostat [74]. The simulation results are examined at  
 176 intervals of 0.05 ns, and large hydrocarbon clusters are identified, organized,  
 177 and analyzed using a variety of tools including MSMS [75], MAFIA-MD [76],  
 178 and OVITO [77].

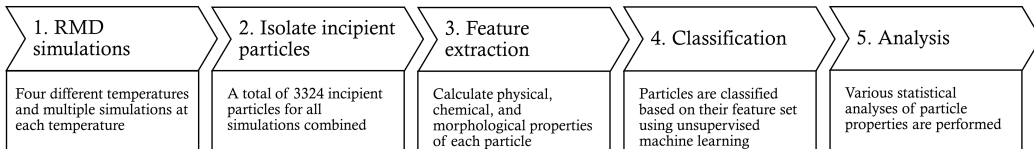


Figure 1: Overview of the workflow employed in this study. The blocks numbered (1) to (4) have been discussed in more detail in our companion work [51]. This work focuses on the block (5).

179 The overall workflow for this work is depicted in Fig. 1. A total of 24  
 180 RMD simulations are performed at four different temperatures (Block 1 in  
 181 Fig. 1). The simulation details have been reported in [51] and are mentioned  
 182 earlier in this section. From each simulation, the large molecular clusters are  
 183 identified as potential incipient soot at every 0.05 ns (Block 2 in Fig. 1).  
 184 These clusters are molecules having more than 20 carbon atoms and at least  
 185 one 5-, 6-, or 7-member ring structure (indicating the possible presence of  
 186 an aromatic component). These criteria are based on previous findings [78].

187 Incidentally, in our simulations, the smallest molecular cluster matching these  
188 criteria was found to have 65 carbon atoms. A total of 3324 soot particles  
189 are identified at various stages of their development from the 24 simulations.  
190 Then a variety of physical (e.g., density and mass), chemical (e.g., number  
191 of rings), and morphological (e.g., volume and surface area) features of each  
192 particle are quantified (Block 3 in Fig. 1). These features are described  
193 in Sec. 2.2. Following this feature extraction, the particles are classified  
194 using two unsupervised machine-learning techniques: k-means clustering [79]  
195 and t-distributed stochastic neighbor embedding (t-SNE) [80] (Block 4 in  
196 Fig. 1). As discussed in our previous work [51], this classification results in  
197 two distinct classes of incipient particles, referred to as Type 1 and Type 2  
198 incipient particles.

199 In this study, Kendall’s Tau [81], a non-parametric test, was employed to  
200 evaluate the correlations between various properties of soot particles. This  
201 statistical method is robust against non-normal distributions of data and  
202 sensitive to ordinal relations between data points. Kendall’s Tau measures  
203 the strength and direction of association between two variables, producing a  
204 correlation coefficient that ranges from -1 to +1. A coefficient of +1 indicates  
205 perfect agreement, 0 indicates no correlation, and -1 signifies perfect disagree-  
206 ment. It also provides a p-value that indicates the statistical significance of  
207 the correlation.

208 The choice of Kendall’s Tau was driven by its effectiveness in handling the  
209 skewed data distributions commonly encountered in complex physicochemical

210 systems, such as soot formation. Its ability to account for ties in data ranks  
211 enhances its suitability for the datasets generated in our molecular dynamics  
212 simulations, where property values can recur, reflecting the repetitive nature  
213 of molecular structures.

214 Furthermore, the use of Kendall’s Tau allows for a nuanced understanding  
215 of how various properties of soot interact under different experimental condi-  
216 tions, providing critical insights that aid the interpretation of our simulation  
217 results. For a more detailed discussion on the application and significance of  
218 Kendall’s Tau in statistical analysis, especially in regression contexts, readers  
219 are referred to the comprehensive overview by Ghosh and Sen [82] on the use  
220 of Kendall’s Tau for sequential confidence intervals in regressions analysis  
221 and its robust application across various data types.

## 222 2.2. Extraction of physicochemical properties

223 Once the soot particles are identified and isolated using the cluster analy-  
224 sis tool from the OVITO python module [77], the physicochemical properties  
225 of each identified soot particle are evaluated using in-house Python script  
226 and other tools such as MSMS [75] and MAFIA-MD [76]. Key features such  
227 as number of atoms ( $N$ ), carbon to hydrogen ratio ( $\Theta_{c/H}$ ), and particle mass  
228 ( $M_p$ ) can be obtained directly from the output log of RMD simulation (a tra-  
229 jectory file). The solvent-excluded volume ( $V$ ) and solvent-excluded surface  
230 area ( $A$ ) are calculated using MSMS [75] using a probe radius of 1.5Å. Some  
231 other features are calculated by simple algebraic, or geometric analysis or by

232 using correlations proposed in the literature as discussed below.

233 The radius of gyration ( $R_g$ ) is calculated geometrically using the atomic  
 234 coordinates extracted from the trajectory files using Eqn. 1:

$$R_g = \sqrt{\frac{\sum_{i=1}^N m_{p,i} r_i^2}{\sum_{i=1}^N m_{p,i}}}, \quad (1)$$

235 where  $r_i$  is the distance of the  $i^{\text{th}}$  atom from the center of mass of the molec-  
 236 ular cluster,  $m_{p,i}$  is the mass of  $i^{\text{th}}$  atom, and  $N$  is the total number of atoms  
 237 in the cluster. In engineering-scale soot models, it is often difficult to capture  
 238 the radius of gyration of incipient particles due to the lack of information on  
 239 particle morphology and size distribution. However, the mass and volume  
 240 of the particles are comparatively easier to obtain. Using these, the volume-  
 241 equivalent radius ( $R_{eq}$ ) can be calculated directly from particle volume from  
 242 Eqn. 2:

$$R_{eq} = \left( \frac{3V}{4\pi} \right)^{1/3}. \quad (2)$$

243 The atomic fractal dimension ( $D_f$ ) is calculated using the sandbox method  
 244 [83, 84] using Eqn. 3.

$$D_f = \frac{\log M_p(r)}{\log r}, \quad (3)$$

245 where  $M_p(r)$  is the mass of atoms in the cluster as a function of radial distance  
 246 from center of mass ( $r$ ). Atomic fractal dimension ( $D_f$ ) is, therefore, the  
 247 slope of the log-log plot of  $M_p(r)$  vs.  $r$ . As discussed in [68], here the fractal  
 248 dimension is calculated using the existing atoms in an incipient particle.

249 Hence, the term “atomic” fractal dimension is used to remove any confusion  
 250 with the fractal dimension of aggregates which is often used to calculate the  
 251 level of geometric self-similarity in soot aggregates [85, 86, 87]. An atomic  
 252 fractal dimension of 1 represents a linear structure while a value of 3 indicates  
 253 a perfectly spherical shape [86].

254 The simulated primary particle density (shortened as simulated density,  
 255 or  $\rho_s$ ) of the incipient soot particles is obtained from the mass and volume  
 256 of the incipient particle (Eqn. 4):

$$\rho_s = \frac{M_p}{V} \quad (4)$$

257 We also calculate a widely used metric – empirical density ( $\rho_e$ ) also referred to  
 258 as bulk density in the contemporary literatures, which can convey additional  
 259 information about the maturity of the incipient particles. Empirical density  
 260 of an incipient particle changes with the level of maturity of the particle and  
 261 is calculated using Eqn. 5 [14, 88]:

$$\rho_e = (0.260884a^2c)^{-1} \left( \frac{w_C \Theta_{C/H} + w_H}{\Theta_{C/H} + 1} \right), \quad (5)$$

262 where  $w_C$  is the weight of carbon atoms (12.011 g/mol),  $w_H$  is the weight  
 263 of hydrogen atoms (1.008 g/mol),  $a$  is the length of the graphite unit cell in  
 264 the basal plane (2.46 Å),  $c$  is the interlayer spacing in Angstroms (3.50 Å for  
 265 soot), and  $\Theta_{C/H}$  represents the carbon to hydrogen ratio of the cluster.

266 Finally, **MAFIA-MD** [76] code is used to identify 5- /6- /7-membered ring

267 structures in a molecular cluster. As discussed in detail in [76], **MAFIA-MD**  
 268 does not strictly check for Huckel’s rules of aromaticity, and hence, to remove  
 269 any confusion, we will use the terms “ring” or “cyclic” in this manuscript  
 270 instead of aromatic when discussing these internal structures in the soot  
 271 clusters. The number of 5- /6- /7-membered rings are denoted as  $N_5$ ,  $N_6$ ,  
 272  $N_7$ , respectively, and the total number of rings is denoted as  $N_{\odot}$ . Similarly,  
 273 number of carbons in rings are denoted as  $N_{\odot}$  and the number of non-cyclic  
 274 carbons in a particle is denoted as  $N_{\Phi}$ .

### 275 **3. Results and Discussion**

#### 276 *3.1. Inception of soot and classification of incipient soot particles*

277 The general sequence of events as seen from the RMD simulations lead-  
 278 ing up to the inception events have been discussed in detail in our earlier  
 279 works [78, 51]. Initially, the acetylene molecules combine to form small linear  
 280 chains. Subsequently, these linear chains undergo cyclization, transforming  
 281 into cyclic structures. Following the process of cyclization, the small clusters  
 282 start to grow through surface reactions that involve bond formation, as well  
 283 as internal reorganization leading to incipient soot particles [78, 51]. A sim-  
 284 ilar process has been also been reported by Zhang et al. [89] and Sharma et  
 285 al. [68].

286 In the present study, being consistent with the current understanding  
 287 of soot particles, an incipient soot particle is identified as a molecular clus-  
 288 ter with more than 20 carbon atoms and with at least one ring structure

289 (5-, 6-, or 7-member rings) [78]. The first such particle in our simulation  
 290 was found to have 65 carbon atoms. A total of 3324 incipient soot parti-  
 291 cles, with carbon atoms ranging from 65 to 1503, were extracted at various  
 292 stages of evolution from all the simulations at four temperatures. These  
 293 particles showed significant variation in their physicochemical features and  
 294 were therefore classified into two classes based on all the extracted features  
 295 using unsupervised machine learning techniques (k-means clustering and t-  
 296 SNE diagram) as discussed in [51]. For easier identification, the two classes  
 297 of particles are denoted as “Type 1” and “Type 2” particles (see also Fig. 2).  
 298 Type 1 particles exhibit a lower number of carbon atoms ( $65 - 818$ ), whereas,  
 299 in Type 2 particles, the number of carbon atoms is higher ( $759 - 1503$ ).  
 300 This observation highlights the fact that the physicochemical properties of  
 301 the incipient particles undergo a transition once a certain level of growth  
 302 is reached [51]. It should be emphasized that the number of carbon atoms  
 303 is not a unique or absolute identifier for particle classification. Although  
 304 it serves as an approximate and practical marker, classification relies on a  
 305 holistic analysis of multiple features, including size, surface area, and chem-  
 306 ical composition. A detailed description of this classification methodology  
 307 is available in [51]. Some small type 2 particles may have a lower number  
 308 of carbon atoms than large type 1 particles (there is a slight overlap in the  
 309 range of the number of atoms between the two types). In our simulation, we  
 310 identified a total of 670 type 1 and 2654 type 2 incipient particles. Figure 2  
 311 shows one sample Type 1 and one sample Type 2 particle. In this repre-

312 sentation, the non-cyclic carbon atom structures are denoted by blue dots,  
 313 while the cyclic structures are denoted by black dots.

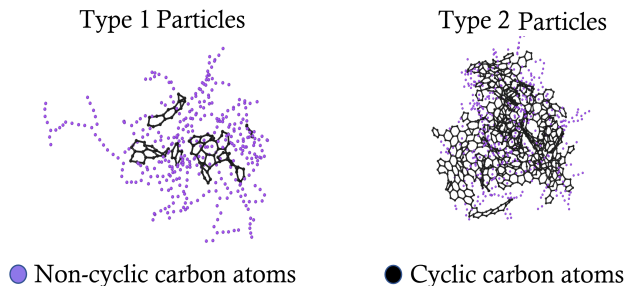


Figure 2: One example particle from each class obtained from RMD simulations.

314        It can be observed in Fig. 2 that there are discernible differences in the  
 315 internal structure between type 1 and type 2 particles. Type 1 particles pos-  
 316 sess numerous small aromatic islands embedded within a plentiful network of  
 317 aliphatic compounds. As the particles transitions from type 1 to type 2, the  
 318 smaller islands amalgamate into larger aromatic islands situated in the cen-  
 319 tral region of the particles (growth centers [1]), resulting in a decrease in the  
 320 proportion of aliphatics. In this manner, the liquid-like or young soot par-  
 321 ticles that are rich in aliphatic compounds (i.e., type 1 particles) transform  
 322 and develop into partially graphitized soot particles (i.e., type 2 particles)  
 323 with higher fraction of aromatic components. During this transformation,  
 324 the soot particles acquire well-defined growth centers. Therefore, it is ex-  
 325 pected that the intercorrelations among various physicochemical properties  
 326 will change as the particle transitions from type 1 to type 2.

### 3.2. *Physicochemical features of incipient particles*

The physicochemical features of soot particles investigated include mass, number of atoms, atomic fractal dimension, volume, surface area, density, particle radius, and statistics of cyclic structures. The physical properties (for example, mass, volume, density, etc.) are often the features that are used in engineering-scale soot models for reactive CFD as well as in discrete element modeling [90] and dipole approximation [91, 36]. A better understanding of these features and their inter-correlation will help improve these engineering-scale soot models. The chemical properties such as the number of atoms, C/H ratio and statistics of cyclic/non-cyclic structures are important metrics by which the evolution and maturity of soot particles can be tracked. The evolution of the soot C/H ratio is essential to estimate the evolution of its optical properties [92] and assist its detection by laser diagnostics [92, 93].

In this work, we focused on the analysis for a set of select physical (mass, radius, surface area, and volume) and chemical (statistics of ring structures) features as the particle grows. As mentioned in Sec. 3.1, as the particle grows, it transitions from type 1 to type 2. Since the demarcation of these types can be very closely tracked by the number of carbon atoms in the particle, which correlates very well with the mass and size of the particle, we track the growth of a particle via either the total number of carbon atoms or the particle mass or the particle radius. The Kendall’s Tau [81] statistical test is performed to determine the level of correlation between the different properties. The correlation coefficients ( $\tau$ ) of the Kendall’s Tau statistical test are reported in

each figure. It was found that whenever a good correlation (i.e.,  $|\tau| \gg 0$ ) was found between two variables, the test yielded a very small p-value (almost zero), indicating a high statistical significance. Therefore, the p-value is not reported in the figures for brevity. We visualize the data using a joint plot of scatter plot and histogram/distribution using the python package `seaborn` [94].

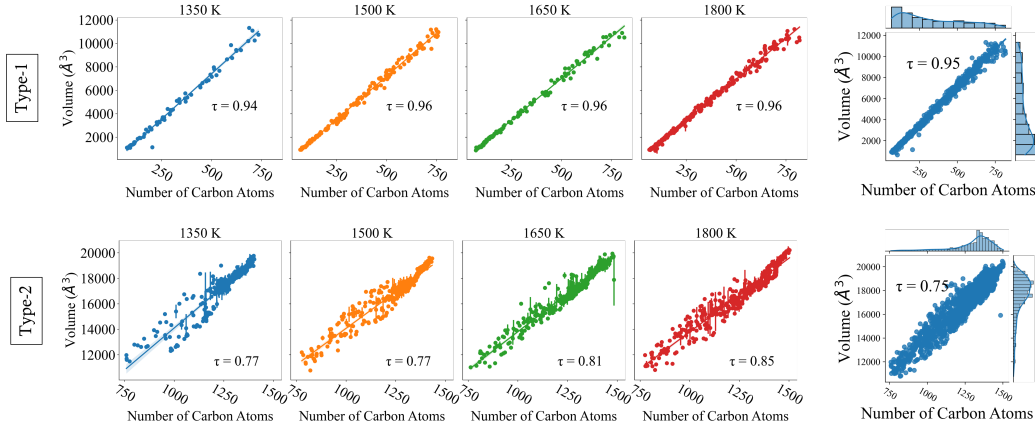


Figure 3: Evolution of particle volume with the number of carbon atoms at different temperatures. Top row: Type 1 particles, bottom row: Type 2 particles.

The evolution of particle volume and surface area is presented in Figs. 3 and 4 for both type 1 (top row) and type 2 particles (bottom row) as a function of the number of carbon atoms in the particles. The first four columns of plots correspond to simulation temperatures of 1350, 1500, 1650, and 1800 K, whereas the rightmost column combines all the temperatures together. A trendline is also shown on the scatter plots for each temperature. From Fig. 3, we see that both type 1 and type 2 particles have an excellent correlation between the particle volume and the number of carbon atoms in the

364 particles across all temperatures. The correlation coefficient ( $\tau$ ) is very close  
 365 to 1 for type 1 particles, representing an almost perfect correlation between  
 366 the variables. For type 2 particles, the correlation coefficient ( $\tau$ ) is lower, but  
 367 still close to 1. This indicates that the particle volume is well correlated with  
 368 the number of carbon atoms in both type 1 and type 2 particles. Another im-  
 369 portant observation is that the particle volume and number of carbon atoms  
 370 seem to be correlated in the same way for all simulation temperatures. The  
 371 slopes of the lines that provide linear fit between the volume and the number  
 372 of carbon atoms do not vary much with temperature (discussed further later  
 373 in Table 1). This shows that the relationship between particle volume and  
 374 number of carbon atoms is not affected by the temperature.

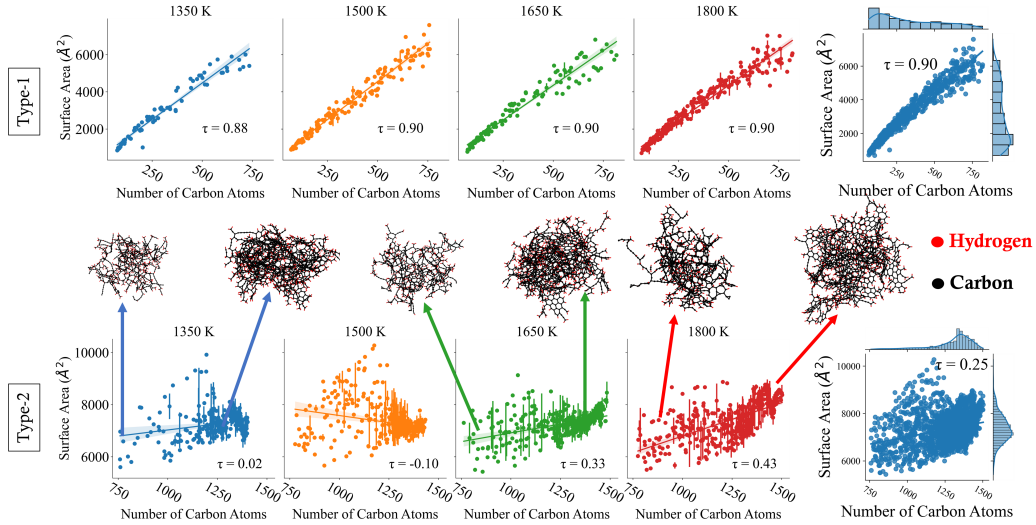


Figure 4: Evolution of particle surface area with the number of carbon atoms at different temperatures. Top row: Type 1 particles, bottom row: Type 2 particles.

375 For type 1 particles, a similar conclusion can also be drawn from Fig. 4

376 for the surface area: a very good correlation is observed with the number of  
 377 carbon atoms. But for the type 2 particles, the surface area does not seem to  
 378 be correlated with the number of carbon atoms. As the particle transitions  
 379 from type 1 to type 2, a change from the initial linear growth to the extensive  
 380 reorganization of the surface is observed. This is shown using some actual  
 381 particles at the two extremes of the number of carbon atoms for 1350, 1650  
 382 and 1800 K in the insets of Fig. 4. As can be seen, while the topology  
 383 of the surface shows significant difference between a small type 2 particle  
 384 ( $N_C \sim 800$ ) and a large type 2 particle ( $N_C \sim 1400$ ), the actual difference in  
 385 surface area is small. It shows that the soot surface goes through extensive  
 386 rearrangement in type 2 particles, which makes the surface area hard to  
 387 correlate with the number of carbon atoms. The rearrangement of the surface  
 388 area occurs mostly because of graphitization of the surface as discussed in  
 389 the internal structure of type 2 particles in [51]. The graphitization of the  
 390 surface is a very complex process and is not well understood. However, it  
 391 is known that the graphitization of the surface is a slow process, and it  
 392 depends on the size of the primary particle itself [95]. We can also note  
 393 that there is a lower number of ring structures in the similar-sized small  
 394 type 2 particles ( $N_C \sim 800 - 1000$ ) in 1800 K than in 1350 K. Temperature  
 395 can accelerate surface graphitization [96] and, therefore, while comparing  
 396 the small type 2 particles ( $N_C \sim 800 - 1000$ ) we observe the formation  
 397 of graphitized particles (indicated by a large presence of cyclic structures)  
 398 earlier in 1800 K simulation than in 1350 K simulation. The fraction of

399 cyclic carbon atoms is plotted against molar mass in Fig. 5. For type 1  
 400 particles, the fraction of cyclic carbon atoms is mostly insensitive to the  
 401 particle mass. However, for type 2 particles, the fraction of cyclic carbon  
 402 atoms increases rapidly with molar mass. This further supports the inference  
 403 regarding the extensive reorganization of the surface in type 2 particles due to  
 404 graphitization. This is consistent with results reported by Liu et al. [97] where  
 405 it is shown that smaller soot particles take longer to graphitize compared  
 406 to the larger ones. This lack of graphitization leads to a good correlation  
 407 between surface area and the number of atoms in type 1 particles, which are  
 408 primarily seen at the early stage of soot formation. Furthermore, the process  
 409 temperature does not seem to affect the quality of correlation or lack thereof.

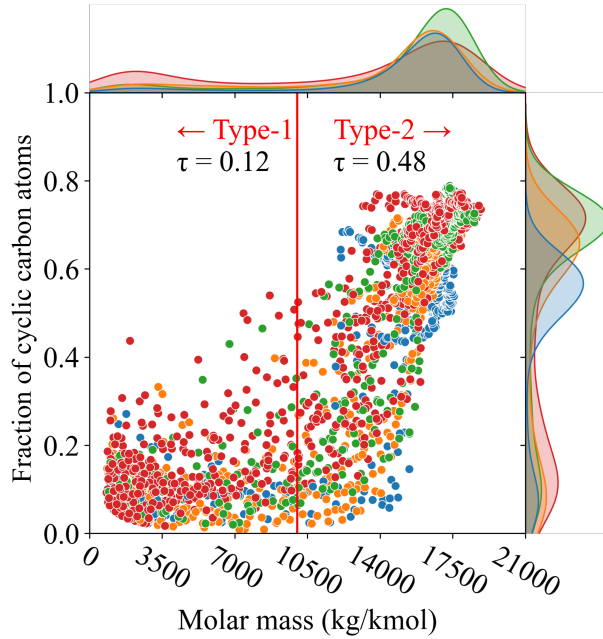


Figure 5: Evolution of fraction of carbon atoms in ring structures ( $N_{@}/N_C$ ) with molar mass.

From Figs. 3 and 4, linear trends with the number of carbon atoms are observed for particle volume (type 1 and type 2) and surface area (type 1). A set of linear equations were fitted between particle volume and surface area with the number of carbon atoms for different temperatures and presented in Table 1. For particle volume, both type 1 and type 2 particles show a very good linear relationship with the number of carbon atoms ( $N_C$ ) as indicated by high  $R^2$  values across different temperatures and classes of particles. The  $R^2$ , or the coefficient of determination ( $R^2 \in [0, 1]$ ) is a statistical measure of how close the data are to the fitted regression line. As discussed previously, for surface area, a good correlation is only observed for type 1 particles and therefore, no correlation for surface area for type 2 particles is presented in Table 1. The slope of these linear correlations are very close to one another supporting the observation of the lack of influence of temperature on the quality of the correlation between these quantities. Therefore, we constructed a set of temperature-independent correlations for volume and surface area by aggregating data from all the temperature in Correlation Set 1.

Table 1: Equation of linear curves fitted to the data for different temperatures shown in Figs. 3 and 4.  $V$  is the particle volume in  $\text{\AA}^3$ ,  $A$  is the particle surface area in  $\text{\AA}^2$ , and  $N_C$  is the total number of carbon atoms.

| Temperature | Particle Volume (V)                       |                                            | Surface Area (A)                         |                                 |
|-------------|-------------------------------------------|--------------------------------------------|------------------------------------------|---------------------------------|
|             | Type 1                                    | Type 2                                     | Type 1                                   | Type 2                          |
| 1350 K      | $V=15.405 N_C - 297.596$<br>$R^2 = 0.987$ | $V=13.172 N_C + 930.663$<br>$R^2 = 0.883$  | $A=7.842 N_C + 551.652$<br>$R^2 = 0.944$ | No<br>meaningful<br>correlation |
| 1500 K      | $V=15.405 N_C - 297.596$<br>$R^2 = 0.987$ | $V=11.41 N_C + 2663.046$<br>$R^2 = 0.913$  | $A=8.171 N_C + 464.281$<br>$R^2 = 0.960$ |                                 |
| 1650 K      | $V=14.207 N_C - 113.638$<br>$R^2 = 0.994$ | $V=12.028 N_C + 1784.325$<br>$R^2 = 0.934$ | $A=7.459 N_C + 614.673$<br>$R^2 = 0.944$ |                                 |
| 1800 K      | $V=14.014 N_C - 65.388$<br>$R^2 = 0.994$  | $V=11.564 N_C + 2228.574$<br>$R^2 = 0.926$ | $A=7.583 N_C + 560.486$<br>$R^2 = 0.953$ |                                 |

**Correlation Set 1:** Equation of curves fitted to the temperature-aggregated data shown in Figs. 3 and 4.  $V$  is the particle volume in  $\text{\AA}^3$ ,  $A$  is the particle surface area in  $\text{\AA}^2$ , and  $N_C$  is the total number of carbon atoms.

**Type 1 particles:**

$$V = 14.353N_C - 119.071, \quad R^2 = 0.992 \quad (6)$$

$$A = 7.733N_C + 547.914, \quad R^2 = 0.951 \quad (7)$$

**Type 2 particles:**

$$V = 11.825N_C + 2151.314, \quad R^2 = 0.897 \quad (8)$$

While we only show the results for particle volume and surface area, a similar conclusion about the effect of temperature can be drawn from the evolution of other morphological features, i.e. radius of gyration, volume equivalent radius, number/fraction of cyclic structures, etc. as well. Discussion on these are omitted in this work for brevity.

Most engineering-scale soot models track the evolution of the soot population via the mass or size of soot particles. Therefore, the correlations of particle volume, surface area, and number of rings are shown with molar mass in Fig. 6 and with the radius of gyration in Fig. 7. The results are presented in the form of joint plots which show the distribution of the data points in the form of a scatter plot and the distribution of the individual

438 properties in the form of a density plot along with the temperature markers.  
 439 The vertical red line in each plot indicates the boundary between type 1 and  
 440 type 2 particles and the correlation coefficients ( $\tau$ ) are reported separately  
 441 for both types of particles on their respective zones. The transition of a par-  
 442 ticle from type 1 to type 2 occurs around a molar mass of 10050 kg/kmol or  
 443 a radius of gyration of 13.8 Å, and the vertical red lines are drawn at those  
 444 locations in these plots. The type 1 particles are on the left of this line and  
 445 type 2 is on the right.

446 The volume, surface area, and radius of gyration of the type 1 particle are  
 447 well correlated with the molar mass of the particles as seen in Fig. 6. For type  
 448 1 particles, volume and surface area show a linear correlation, while the radius  
 449 of gyration shows a nonlinear correlation with the mass of the particles. For  
 450 the total number of ring structures, however, the correlation is not as good as  
 451 the other three properties. The nature of the correlations between variables  
 452 remains unaffected by the temperature. The most important observation  
 453 from Fig. 6 is the difference in the nature of the correlations between type  
 454 1 and type 2. In all cases, the data points become more clustered and the  
 455 correlations become weaker except for the total number of ring structures in  
 456 type 2 particles. A very sharp increase in the total number of ring structures  
 457 is observed as the particles transition to type 2 and grow in mass. The total  
 458 number of rings is also affected by temperature, even though temperature  
 459 does not affect the other morphological features. A higher number of cyclic  
 460 structures is observed with the increase in temperature as we can see from

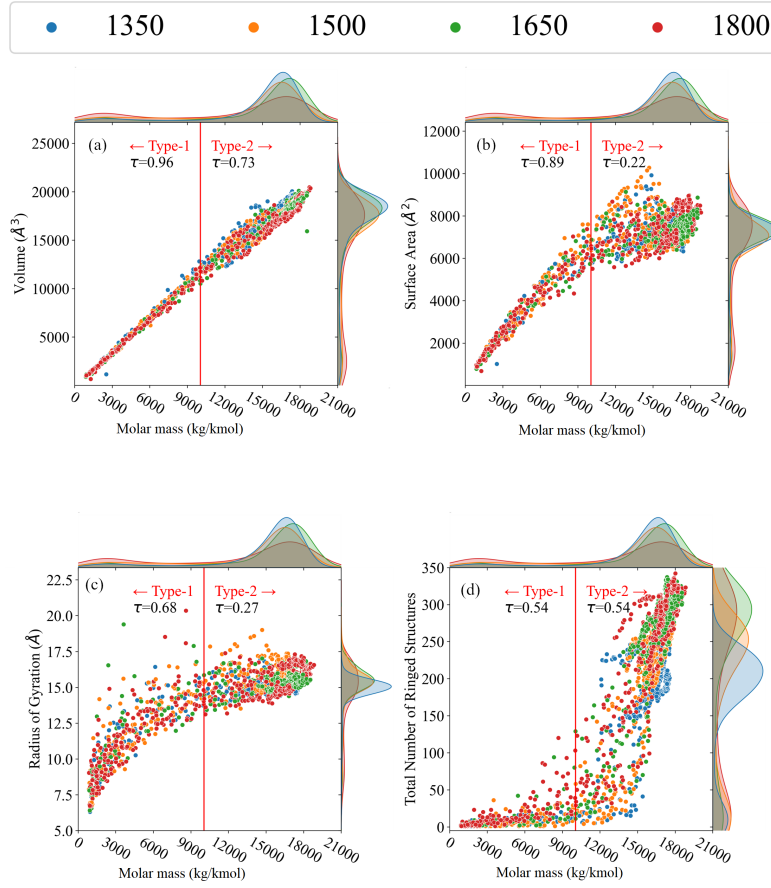


Figure 6: Relationship between molar mass and (a) volume, (b) surface area, (c) radius of gyration, and (d) total number of rings in incipient soot particles

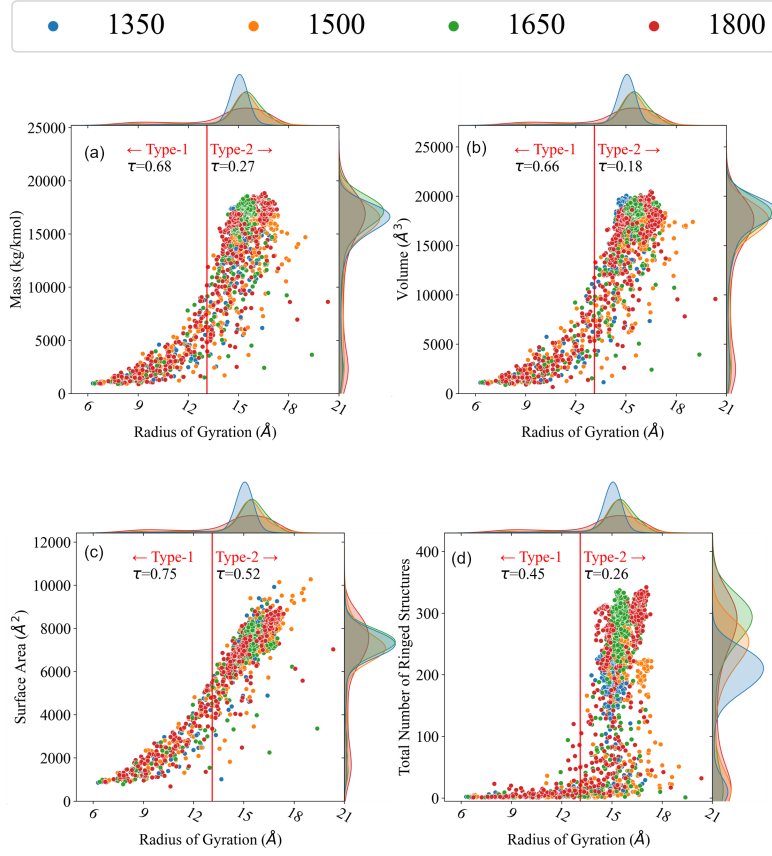


Figure 7: Relationship between radius of gyration and (a) mass, (b) volume, (c) surface area, and (d) total number of rings in incipient soot particles.

461 the temperature markers and density plots on the right side of the plot. A set  
462 of correlation equations by curve-fitting the data shown in Fig. 6 is presented  
463 in Corr. Set 2.

464 Similar conclusions can be drawn using the radius of gyration as the  
465 independent variable as shown in Fig. 7. The volume and surface area,  
466 and mass all show a good correlation for type 1 particles. For the total  
467 number of ring structures, however, the correlation is not as good as the other  
468 three properties. The nature of the correlations between features remain  
469 unaffected by the temperature. Similar to Fig. 6, the type 2 particles show  
470 comparatively weaker correlations with the radius of gyration compared to  
471 type 1 particles. A set of correlation equations obtained by curve-fitting the  
472 data shown in Fig. 7 is presented in Corr. Set 3.

473 The nature of the physical and chemical properties of incipient soot  
474 changes as the particle grows from type 1 to type 2. Identification of this  
475 transition from type 1 and 2 particles is valuable in the context of engineering-  
476 scale soot models as it will allow for updating of property correlation in the  
477 soot model without analyzing the internal structure. This may lead to a more  
478 comprehensive understanding of soot evolution, including the morphology of  
479 primary particles. This is further evident in the discussion of ring structures  
480 presented in Sec. 3.3.

**Correlation Set 2:** Equation of curves fitted to the data shown in Fig. 6.  $M$  is the molar mass of the particle in kg/kmol,  $V$  is the particle volume in  $\text{\AA}^3$ ,  $A$  is the particle surface area in  $\text{\AA}^2$ ,  $R_g$  is the radius of gyration in  $\text{\AA}$ , and  $N_{\text{O}}$  is the total number of ring structures in the particle.

**Type 1 particles:**

$$V = 1.160M - 124.597, \quad R^2 = 0.993, \quad (9)$$

$$A = 0.625M - 545.410, \quad R^2 = 0.952, \quad (10)$$

$$R_g = 2.947 \ln(M) - 12.487, \quad R^2 = 0.717, \quad (11)$$

$$N_{\text{O}} = 0.004M - 5.964, \quad R^2 = 0.372. \quad (12)$$

481

**Type 2 particles:**

$$V = 0.935M - 2375.685, \quad R^2 = 0.905, \quad (13)$$

$$A = 0.098M - 5783.961, \quad R^2 = 0.090, \quad (14)$$

$$R_g = 1.933 \ln(M) - 3.293, \quad R^2 = 0.114, \quad (15)$$

$$N_{\text{O}} = 0.036M - 342.906, \quad R^2 = 0.704. \quad (16)$$

**Correlation Set 3:** Equation of curves fitted to the data shown in Fig. 6.  $V$  is the particle volume in  $\text{\AA}^3$ ,  $A$  is the particle surface area in  $\text{\AA}^2$ ,  $R_g$  is the radius of gyration in  $\text{\AA}$ , and  $N_{\text{O}}$  is the total number of ring structures in the particle.

**Type 1 particles:**

$$V = 995.677R_g - 6699.483, \quad R^2 = 0.647, \quad (17)$$

$$A = 596.486R_g - 3678.870, \quad R^2 = 0.767, \quad (18)$$

$$N_{\text{O}} = 2.945R_g - 22.272, \quad R^2 = 0.162. \quad (19)$$

482

**Type 2 particles:**

$$V = 807.096R_g + 4944.945, \quad R^2 = 0.106, \quad (20)$$

$$A = 608.281R_g + 2042.065, \quad R^2 = 0.541, \quad (21)$$

$$N_{\text{O}} = 25.862R_g - 169.784, \quad R^2 = 0.059. \quad (22)$$

483 Fig. 8 shows the comparison between the molar mass and the atomic  
 484 fractal dimension ( $D_f$ ) in the form of a joint scatter plot. As discussed in  
 485 Eq. 3, the atomic fractal dimension is calculated using box counting method  
 486 for individual incipient particles, not for an aggregate. The value of atomic  
 487 fractal dimension ( $D_f$ ) is an indication of the shape of the incipient primary  
 488 particles. A value of  $D_f$  close to 3 indicates a spherical shape, while a value  
 489 of  $D_f$  close to 1 indicates a linear shape. Contemporary engineering-scale  
 490 soot models often assume spherical incipient particles [98, 40, 12].

491 For both type 1 and type 2 particles, we do not observe any specific  
 492 correlation between molar mass and atomic fractal dimension as indicated  
 493 by the low  $\tau$  value in Fig. 8. As the molar mass increases, the atomic  
 494 fractal dimension increases and approaches 3. This is because as the incipient  
 495 particles grow, the shape of the particles becomes more spherical. The value  
 496 of  $D_f$  captures the evolution of the shape of a single incipient particle before  
 497 coalescence. In the inset of Fig. 8, some representative incipient particles are  
 498 shown at various stages of their evolution.

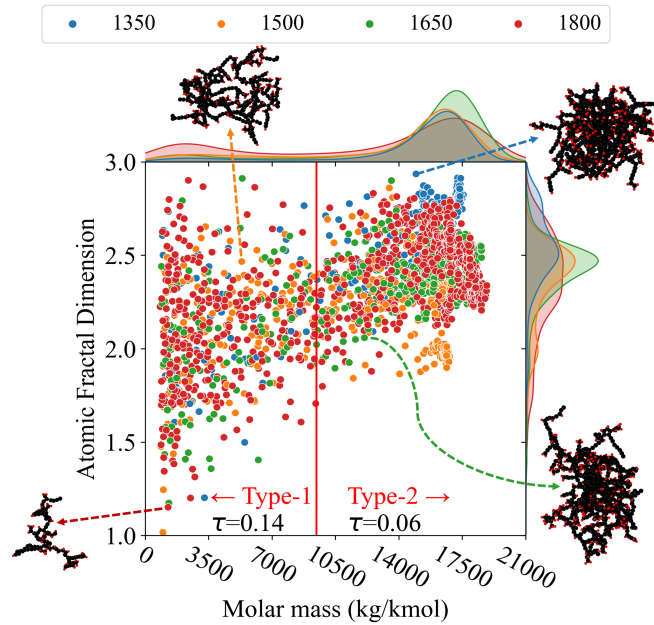


Figure 8: Evolution of atomic fractal dimension ( $D_f$ ) with molar mass

499 The correlation between the volume equivalent radius and the radius of  
 500 gyration is shown in Fig. 9(a). The transition from type 1 to type 2 particles  
 501 occurs around a volume equivalent radius of 13.8 Å corresponding to the

502 red vertical line in Fig. 9(a). An overall good correlation is observed between  
 503 the two quantities for type 1 particles. Like the other morphological features,  
 504 the type 2 particles show a comparatively weaker correlation compared to the  
 505 type 1 particles. Since the particles tend to become spherical as they evolve  
 506 (Fig. 8), the volume equivalent radius can be a good approximation for  
 507 the radius of gyration. It should be noted here that although the particles  
 508 become more spherical, they are not solid spheres, therefore relationships  
 509 between the volume-equivalent radius and radius of gyration do not follow  
 510 the classical  $\sqrt{3/5}$  scaling (black solid line). Rather they closely follow the  
 511  $R_g = R_{eq}$  scaling (blue dashed line) as shown in Fig. 9(a).

512 This becomes more evident if we look at the evolution of the ratio of radius  
 513 of gyration and volume-equivalent radius ( $R_g/R_{eq}$ ) as the particles grow in size.  
 514 Figure 9(b) and 9(c) depict  $R_g/R_{eq}$  vs. the number of carbon atoms ( $N_c$ ) for  
 515 type 1 and type 2 particles respectively. For small type 1 particles, the ratio  
 516  $R_g/R_{eq}$  shows a wide range of values ranging from 1.0 to 2.1. But within the  
 517 increase in particle size, i.e., increase in the number of carbon atoms ( $N_c$ ) in  
 518 the particle, the spread of the ratio  $R_g/R_{eq}$  becomes narrower and approaches  
 519 unity as seen from Fig. 9(b). This is because the particles become more  
 520 spherical and compact as they grow in size. For type 2 particles, the ratio  
 521  $R_g/R_{eq}$  steadily hovers near 1.0 with very little spread in the data as observed  
 522 from Fig. 9(c). This is because the type 2 particles are more graphitized and  
 523 have a more compact structure compared to type 1 particles.

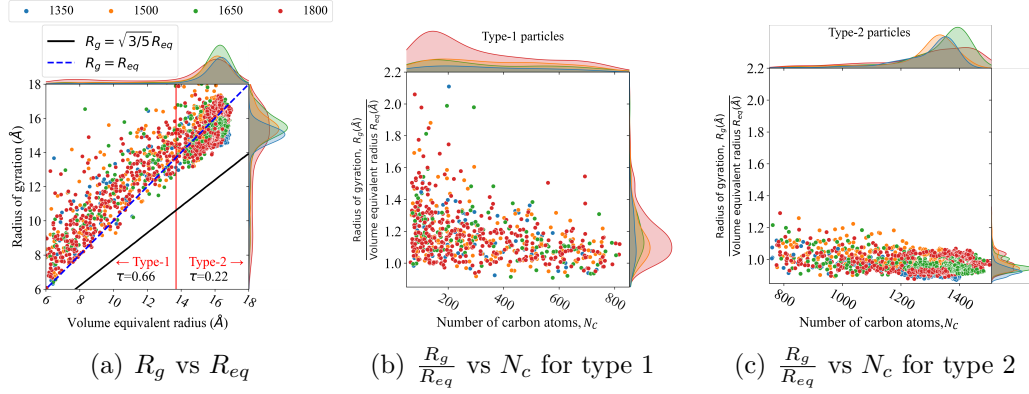


Figure 9: Evolution of radius of gyration ( $R_g$ ) and volume equivalent radius ( $R_{eq}$ ): Comparison between volume equivalent radius and radius of gyration for all particles (a); ratio of radius of gyration and volume equivalent radius vs number of carbon atoms for type 1 particles (b) and for type 2 particles (c).

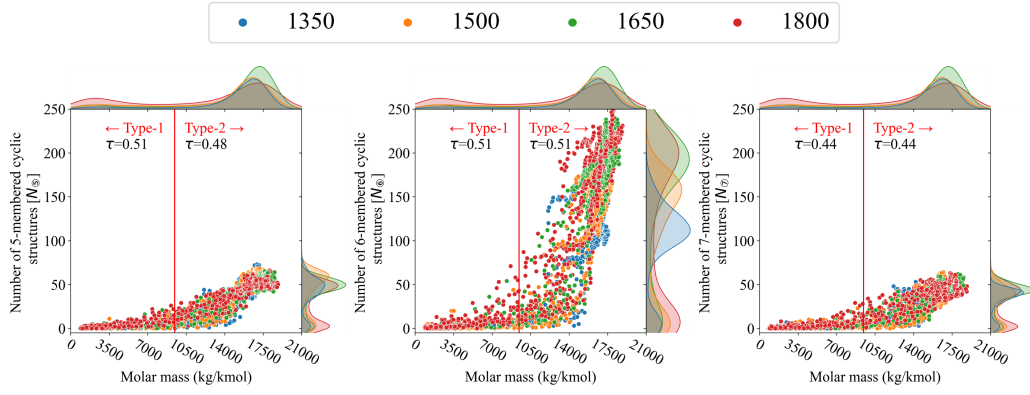
### 3.3. Evolution of ring structures in incipient soot particles

The ring structures in soot particle play an important role in their evolution and impact their physical and chemical properties [99]. As seen in Figs. 6 and 7, the number of rings in incipient soot particles evolve differently from the morphological features. Therefore, we looked into the evolution of 5-/6-/7-membered rings more closely in this section. Fig. 10 shows the evolution of the total number of 5-/6-/7-membered rings ( $N_5$ ,  $N_6$ ,  $N_7$ ) in the top row and their fraction with respect to the total number of rings ( $N_5/N_O$ ,  $N_6/N_O$ ,  $N_7/N_O$ ) in the bottom row as a function of the molar mass of the incipient particles. The red vertical line indicates the threshold between type 1 and type 2 particles. The type 1 particles are on the left of the line and type 2 particles are on the right. The Kendall's correlation coefficient ( $\tau$ ) between the ring structures with particle mass are reported for each type on their

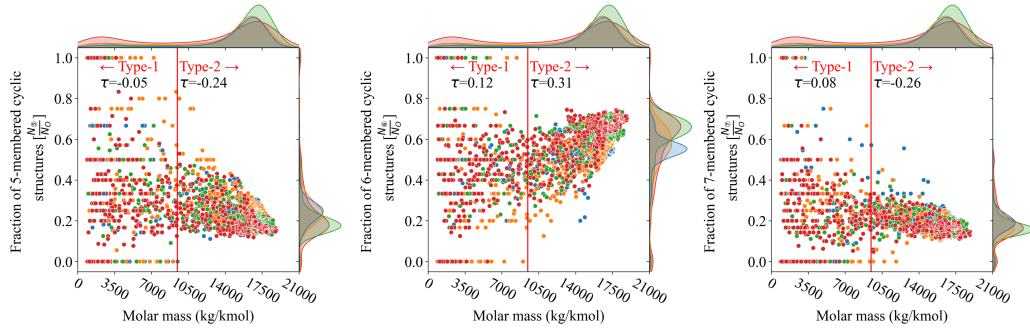
537 respective zones.

538     The total number of 5-/6-/7-membered rings in type 1 particles increases  
539 only slightly with molar mass and no distinct difference is observed between  
540 different ring structures. However, in the type 2 regime, a rapid increase in  
541 the total number of rings is observed with mass. This increase is most promi-  
542 nent for the 6-membered rings. The 5- and 7-membered rings also increase  
543 with mass but at a much slower rate. A higher number of 6-membered rings  
544 is observed with increasing temperature in the type 2 regime as seen from  
545 the temperature markers and density plots on the right side of top middle  
546 plot of Fig 10(a).

547     Figure 10(b) shows the fraction of 5-/6-/7-membered rings in individual  
548 incipient particles and provides insights into how different rings interact and  
549 change during the evolution of incipient soot particles. In the type 1 regime  
550 of Fig. 10, the fraction of 5-/ 6-/ 7-membered rings does not show any order  
551 or correlation. Throughout the simulation domain, 5-, 6-, and 7-membered  
552 rings form independently due to the chemical interactions between small  
553 aliphatics without the influence of other cyclic structures. Once the particles  
554 grow enough to transition to type 2, the fractions of 5-/ 6-/ 7-membered rings  
555 start to change in an orderly manner. The fractions of 5- and 7-membered  
556 rings decrease with mass while the fraction of 6-membered rings increases.  
557 This is because the 6-membered rings are the most stable ring structures  
558 and as the particle grows, the 5- and 7-membered rings are more likely to  
559 break and form 6-membered rings. The fraction of rings is also affected



(a) Number of 5-/6-/7-membered cyclic structures



(b) Fraction of 5-/6-/7-membered cyclic structures

Figure 10: Evolution of cyclic structures in incipient soot particles.

by temperature. A higher fraction of 6-membered rings is observed with increasing temperature in the type 2 regime as seen from the temperature markers and density plots on the right side of the center plot of Fig. 10(b). The fraction of 5- and 7-membered cyclic structures, on the other hand, decreases slightly with increasing temperature.

### 3.4. *Physicochemical correlations*

As discussed in previous sections, in type 1 particles, we observe strong linear correlations between morphological features (such as volume, surface area, and radius of gyration) and particle size. This size is quantitatively expressed in terms of molar mass and the number of carbon atoms. The correlations are presented in Correlation Sets 1, 2, and 3. These correlations suggest that during the initial phase of inception (i.e., in type 1 particles), particle growth predominantly results from uniform mass accretion, proportionally increasing the volume and surface area. Importantly, these morphological evolutions seem to be independent of temperature, as shown in Table 1, suggesting that the structural changes are intrinsic to the mass addition process rather than thermally driven.

As these particles transition to type 2, the previously observed linear correlations begin to weaken. This weakening signals a shift in growth dynamics from simple mass addition to more complex processes involving structural reorganization and increased graphitization. This shift also marks significant changes in chemical composition, notably a rise in the stability and predomi-

nance of 6-membered rings with increasing temperature. The transformation from less stable 5- and 7-membered rings to more stable 6-membered configurations is more dependent on the process temperature. This points to a thermally facilitated stabilization process during the chemical evolution of the particle.

The shift from type 1 to type 2 particles also reflects a broader spectrum of physicochemical transformations. In type 1, the particle growth and properties are predictable based on simple linear models. However, in type 2, the growth becomes non-linear, emphasizing complex internal restructuring that does not directly impact the external dimensions such as surface area and volume. This complex behavior highlights the need for advanced modeling techniques that can account for internal chemical changes and their impact on particle morphology.

### 3.5. Summary statistics

The summary of the statistics is presented in Table 2 in terms of mean, standard error to the mean (**SEM**) and standard deviation (**SD**) of the extracted features. These values can be useful in determining model parameters and model constants for engineering-scale soot model. The statistics are also separated by the type of the particles. It can be seen that the variation in physical features such as simulated density, radius of gyration, volume, and surface area is much smaller in type 2 particles than in type 1 particles. This indicates that in type 1 regime, particles go through a strong physical and

604 morphological evolution, but in type 2 regime, they go through a chemical  
 605 restructuring. Due to these changes, from type 1 to type 2, the atomic fractal  
 606 dimension increases from 2.1 to 2.5 (more spherical). The proportion of 6-  
 607 membered rings increases significantly while the fractions of 5-/7-membered  
 608 rings decrease as they restructured into the more stable 6-membered rings.

609 The calculated statistics provide a great validation for the RMD when  
 610 compared with experimental data reported in the literature. Schulz et. al  
 611 [19] reported that the average C/H ratio of soot particles from a premixed  
 612 ethylene flame was  $2.33 \pm 0.16$ , which matches very well with the mean C/H  
 613 ratio of 2.36 with a standard deviation of 0.37 for the simulated particles  
 614 in our study. It should be noted that, we do see a reduction in the C/H  
 615 ratio as the particles transition from type 1 to type 2 particles. This can  
 616 be explained by the internal structure of the incipient particles where the  
 617 type 2 particles have a larger shell region consisting of mostly non-cyclic  
 618 aliphatic chains compared to type 1 particles [51]. The average simulated  
 619 density of the soot particle in our study is in the range of 1.50 (type 1) – 1.53  
 620 g/cm<sup>3</sup> (type 2). This is very similar to values reported or assumed in several  
 621 other studies [23, 24, 25]. Furthermore, Johansson et al. [14] and [21] found  
 622 a empirical density of about 1.5 g/cm<sup>3</sup> for incipient soot particles in their  
 623 experiments. For PAHs with C/H ratio of 1.0-2.4, Minutolo et. al. [100] found  
 624 the average density of soot to be 1.5 gm/cm<sup>3</sup> using relationships from [101].

625 Finally, a summary correlation matrix between each pair of features for  
 626 both type 1 and type 2 incipient particles are presented in Fig. 11. The corre-

Table 2: Mean, Standard Error of the Mean (SEM), and Standard Deviation (SD) of the physicochemical features of soot clusters.

| Property                                                  | Unit              | Type 1 |   |       |        | Type 2  |   |       |        |
|-----------------------------------------------------------|-------------------|--------|---|-------|--------|---------|---|-------|--------|
|                                                           |                   | Mean   | ± | SEM   | SD     | Mean    | ± | SEM   | SD     |
| Simulated Density                                         | g/cm <sup>3</sup> | 1.502  | ± | 0.005 | 0.139  | 1.533   | ± | 0.001 | 0.060  |
| Radius of gyration                                        | Å                 | 11.349 | ± | 0.094 | 2.430  | 15.472  | ± | 0.014 | 0.741  |
| Volume equivalent radius                                  | Å                 | 9.793  | ± | 0.090 | 2.318  | 16.063  | ± | 0.012 | 0.597  |
| Ratio of radius of gyration over volume equivalent radius | –                 | 1.176  | ± | 0.007 | 0.171  | 0.964   | ± | 0.001 | 0.05   |
| Molar mass                                                | kg/kmol           | 4073.8 | ± | 99.9  | 2584.0 | 16104.5 | ± | 36.2  | 1866.3 |
| Volume                                                    | Å <sup>3</sup>    | 4600.3 | ± | 116.3 | 3008.3 | 17432.3 | ± | 35.6  | 1834.6 |
| Surface area                                              | Å <sup>2</sup>    | 3090.6 | ± | 64.0  | 1654.9 | 7369.2  | ± | 11.9  | 612.2  |
| Atomic fractal dimension                                  | –                 | 2.093  | ± | 0.013 | 0.340  | 2.460   | ± | 0.003 | 0.169  |
| Fraction of 5-membered rings                              |                   | 0.374  | ± | 0.011 | 0.294  | 0.218   | ± | 0.001 | 0.063  |
| Fraction of 6-membered rings                              |                   | 0.399  | ± | 0.010 | 0.258  | 0.605   | ± | 0.002 | 0.084  |
| Fraction of 7-membered rings                              |                   | 0.227  | ± | 0.009 | 0.221  | 0.177   | ± | 0.001 | 0.041  |

627 lation matrix is a square matrix with the number of rows and columns equal  
628 to the number of properties. The diagonal elements of the matrix are always  
629 1, and the off-diagonal elements are the correlation coefficients between the  
630 corresponding properties. The correlation coefficients are calculated using  
631 Kendall’s Tau test. The correlation coefficients are presented in the form of  
632 a heat map in Fig. 11, where the color intensity is proportional to the value of  
633 the correlation coefficient. Both type 1 and type 2 correlations are presented  
634 in the square correlation matrix. The lower triangular region represents type  
635 1 particles and the upper triangular region represents type 2 particles. For  
636 simplicity, the correlation matrix is presented only for a subset of features  
637 explored.

638 If the nature of correlations were to be the same between the types of par-  
639 ticles, the lower and upper triangular portions would be symmetric about the  
640 diagonal. However, as seen in Fig 11, the quality and trends of correlations  
641 change significantly between the types of particles. For example, the mass

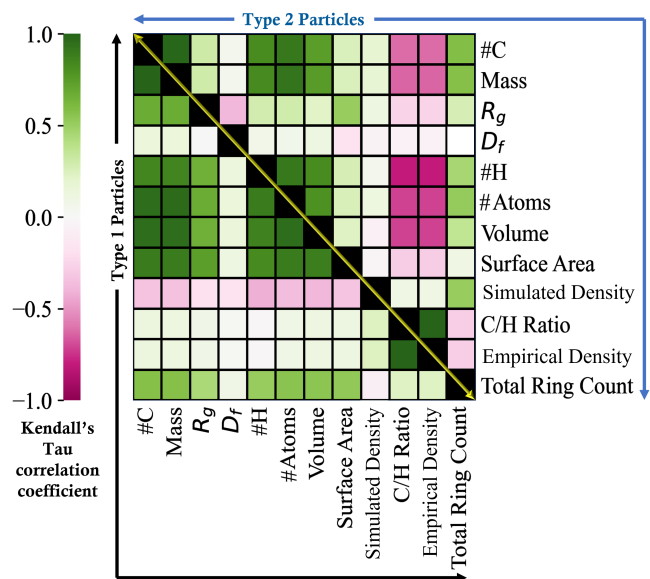


Figure 11: Kendall's rank correlation coefficient between different physicochemical features of type 1 (lower-left triangular matrix) and type 2 (upper-right triangular matrix) incipient soot particles.

642 and empirical density is negatively correlated in type 2 particles whereas they  
 643 are almost uncorrelated in type 1 particles. A correlation matrix like this can  
 644 be useful in creating a reduced-order soot model in the future.

#### 645 4. Conclusion

646 A series of molecular dynamics simulations was performed to study the  
 647 evolution of incipient soot particles during acetylene pyrolysis at four differ-  
 648 ent temperatures. The evolution of the incipient soot particles was studied  
 649 via their physicochemical characteristics such as mass, volume, surface area,  
 650 radius of gyration, density, and the number of 5-/6-/7-membered rings. Us-  
 651 ing unsupervised machine learning techniques, the incipient soot particles are

652 classified into two types – type 1 and type 2 – based on their morphological  
653 and chemical features. This classification was very well predicted by the num-  
654 ber of carbon atoms in the particles, indicating the two types corresponding  
655 to early and late stages of incipient soot. The RMD-derived incipient soot  
656 particle density and C/H ratio shows excellent agreement with experimental  
657 data.

658 The following conclusions were drawn from the study.

- 659 1. Morphological features of incipient particles are often well correlated  
660 with each other and with the size of the particle (indicated by the molar  
661 mass, number of atoms, or radius of gyration). However, the quality  
662 and nature of their correlations are different between different types of  
663 particles.
- 664 2. Type 1 particles usually show stronger correlations between different  
665 morphological features and size than type 2 particles. Morphological  
666 features in type 2 particles show much smaller variation than type 1  
667 particles.
- 668 3. Morphological features of incipient particles, e.g., volume, surface area,  
669 radius of gyration etc. are not affected by temperature. However, the  
670 chemical characteristics, e.g., number of cyclic structure and 5-,6-,7-  
671 membered rings of incipient particles are affected by temperature.
- 672 4. At the early stage of incipient soot (type 1), 5-, 6-, and 7-membered  
673 rings are formed independently from one another. However, at the later  
674 stage (type 2), the 5- and 7-membered rings are more likely to break

675 and form 6-membered rings.

676 5. The incipient particles evolve into a more spherical shape as they tran-  
677 sition from type 1 to type 2.

678 6. Overall, type 1 particles show a more prominent morphological evo-  
679 lution (i.e. volume, surface area and radius of gyration) than type 2  
680 particles with increasing particle mass. On the other hand, type 2 par-  
681 ticles go through a more prominent chemical evolution (i.e. evolution  
682 of 5-,6-, and 7-memebered cyclic structures) than type 1 particles.

683 The estimation of various quantitative properties and their correlation in  
684 incipient soot reported in this work can improve engineering-scale models for  
685 soot inception and growth. We believe that one would be able to interface the  
686 correlation derived here by reactive molecular dynamics with a soot model  
687 that can be used in reactive flow simulation using the conventional reactive  
688 computational fluid dynamics (CFD) framework. Such a soot model can be  
689 used to predict (and, thereby, validate) specific experiments.

690 It must be noted here that this study focuses on acetylene pyrolysis at four  
691 different temperatures. Acetylene is a common fuel used to study soot, and  
692 the literature suggests that the soot formation pathways are similar across  
693 different hydrocarbon fuels [102]. Still, the generalizability of our findings to  
694 other fuels and combustion configurations should be verified in future studies.

## 695 5. Acknowledgments

696 The research benefited from computational resources provided through  
697 the NCMAS, supported by the Australian Government, The University of  
698 Melbourne’s Research Computing Services and the Petascale Campus Ini-  
699 tiative. K.M.M. and S.P.R. acknowledge funding support from the National  
700 Science Foundation as some of this material is based upon work supported  
701 by the National Science Foundation under Grant No. 2144290.

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