

# Almost All Carbon/Oxygen White Dwarfs Can Host Double Detonations

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## ABSTRACT

Double detonations of sub-Chandrasekhar-mass white dwarfs (WDs) in unstably mass-transferring double WD binaries have become one of the leading contenders to explain most Type Ia supernovae. However, past theoretical studies of the explosion process have assumed relatively ad hoc initial conditions for the helium shells in which the double detonations begin. In this work, we construct realistic C/O WDs to use as the starting points for multidimensional double detonation simulations. We supplement these with simplified one-dimensional detonation calculations to gain a physical understanding of the conditions under which shell detonations can propagate successfully. We find that C/O WDs  $\lesssim 1.0 M_{\odot}$ , which make up the majority of C/O WDs, are born with structures that can support double detonations. More massive C/O WDs require  $\sim 10^{-3} M_{\odot}$  of accretion before detonations can successfully propagate in their shells, but such accretion may be common in the double WD binaries that host massive WDs. Our findings strongly suggest that if the direct impact accretion stream reaches high enough temperatures and densities during mass transfer from one WD to another, the accreting WD will undergo a double detonation. Furthermore, if the companion is also a C/O WD  $\lesssim 1.0 M_{\odot}$ , it will undergo its own double detonation when impacted by the ejecta from the first explosion. Exceptions to this outcome may explain the newly discovered class of hypervelocity supernova survivors.

## 1. INTRODUCTION

The identity of Type Ia supernova (SN Ia) progenitors remains an unsolved mystery (see, e.g., Liu et al. 2023 for a recent review), but recent work appears to be converging towards a solution. Many theoretical SN Ia explosion mechanisms fall into two categories: deflagrations and/or detonations ignited close to the center of near-Chandrasekhar-mass white dwarfs (WDs; e.g., Whelan & Iben 1973; Iben & Tutukov 1984; Nomoto et al. 1984; Webbink 1984) and double detonations of sub-Chandrasekhar-mass WDs (e.g., Nomoto 1982; Woosley et al. 1986; Livne 1990), in which a helium shell detonation triggers a subsequent carbon/oxygen core detonation. Double detonations were initially envisioned as occurring due to helium-rich accretion from non-degenerate donors. However, such systems lead to relatively massive helium shells  $\sim 0.1 M_{\odot}$ , and the ashes of these thick shell detonations result in discrepancies when compared to observations of SNe Ia (Höflich & Khokhlov 1996; Nugent et al. 1997). Recent theoretical

work has explored the alternative possibility of degenerate donors leading to double detonations, either via stable (Bildsten et al. 2007; Fink et al. 2007; Shen & Bildsten 2009; Shen et al. 2010; Fink et al. 2010) or unstable (Guillochon et al. 2010; Dan et al. 2011, 2012; Raskin et al. 2012; Pakmor et al. 2013; Moll et al. 2014; Tanikawa et al. 2018, 2019; Pakmor et al. 2021, 2022) mass transfer. The helium shells at the time of explosion in these systems are much less massive, and thus better matches to observations can be achieved.

There is now mounting evidence that the core spectral subclasses of SNe Ia, from subluminous SN 1991bg-likes to overluminous SN 1991T-likes and SN 2003fg-likes,<sup>1</sup> are the results of detonations of sub-Chandrasekhar-mass WDs in double WD systems. The growing support includes the lack of bright non-degenerate surviving companions within SN remnants (Schaefer & Pagnotta

<sup>1</sup> Recent discoveries have uncovered classes of transients that share some spectroscopic similarities to the core spectral subgroups of SNe Ia, including SNe Iax or SN 2002cx-likes, SN 2002es-likes, and calcium-strong transients. While these explosions are likely thermonuclear in origin, it is widely believed that they arise from different progenitors than the main subclasses of SNe Ia discussed here (e.g., Taubenberger 2017).

2012; Kerzendorf et al. 2012, 2013, 2014), the prediction and discovery of a growing number of hypervelocity surviving companion WDs (Shen et al. 2018b; El-Badry et al. 2023), and explosion simulations and radiative transfer calculations that broadly match observed features of SNe Ia, with calculations that include more accurate physics better reproducing observables (Fink et al. 2007, 2010; Guillochon et al. 2010; Kromer et al. 2010; Sim et al. 2010; Townsley et al. 2012; Moore et al. 2013; Pakmor et al. 2013; Shen & Moore 2014; Shen et al. 2018a; Tanikawa et al. 2018; Polin et al. 2019; Tanikawa et al. 2019; Townsley et al. 2019; Gronow et al. 2020, 2021a; Shen et al. 2021a,b; Boos et al. 2021; Pakmor et al. 2022; Roy et al. 2022; Burmester et al. 2023; Boos et al. 2024).

Past studies that have included helium shells have assumed ad hoc masses and/or compositions, often appealing to a previous phase of accretion before the explosion. However, in the case of double WD mergers, the amount of mass transferred in the lead-up to the exponential increase in accretion rate is minimal, and furthermore, the mass that is transferred passes through an accretion shock and is thus much hotter and less dense than assumed. The true masses of the helium layers in double WD binaries at the time of explosion should in fact be much smaller than assumed in these studies, by orders of magnitude in some cases.

In this paper, we improve upon previous work by constructing realistic C/O WDs and using these as the starting points for two-dimensional double detonation calculations. We find that C/O WDs  $\lesssim 1.0 M_{\odot}$ , which make up the majority of C/O WDs, are born with composition and density profiles that support helium shell detonations without the need for any added mass, and that these shell detonations robustly trigger core detonations. WDs that are more massive than  $\sim 1.0 M_{\odot}$  require the addition of  $\sim 10^{-3} M_{\odot}$  of material before they can support a shell detonation, but such accretion prior to the formation of the double WD binary may be fairly common for these masses.

In Section 2, we describe the stellar evolution calculations that produce the C/O WDs we use as initial conditions for one-dimensional detonation calculations, described in Section 3, and multidimensional detonation simulations, detailed in Section 4. We discuss implications of our results in Section 5 and conclude in Section 6.

## 2. CONSTRUCTING C/O WHITE DWARFS WITH REALISTIC COMPOSITION PROFILES

To set the stage for the detonation calculations that we discuss in later sections, we first create C/O WD

models with realistic composition profiles using the stellar evolution code **MESA** (Paxton et al. 2011, 2013, 2015, 2018, 2019).<sup>2</sup> We follow a similar recipe as in Shen et al. (2023) to construct our models; see their appendix for sample inlists.<sup>3</sup> We begin with stars of pure  $^4\text{He}$  and  $^{14}\text{N}$  with mass fractions of  $X_{^4\text{He}} = 0.99$  and  $X_{^{14}\text{N}} = 0.01$ , as appropriate for stars that have undergone CNO-burning, with masses of 0.5, 0.6, 0.7, 0.8, 0.9, and  $1.0 M_{\odot}$ . Semiconvection, thermohaline mixing, and diffusion are turned off during this first stage, and the **mesa\_45.net** nuclear network is used. The models are evolved through the core- and shell-burning phases until the remaining helium-burning shell is too small to support a stable steady-state solution. This minimum-mass stably burning helium shell is a robust feature and only depends on the underlying core mass (Shen & Bildsten 2007; Kippenhahn et al. 2013), thus justifying our initial conditions, which skip over the intricacies of binary stellar evolution.

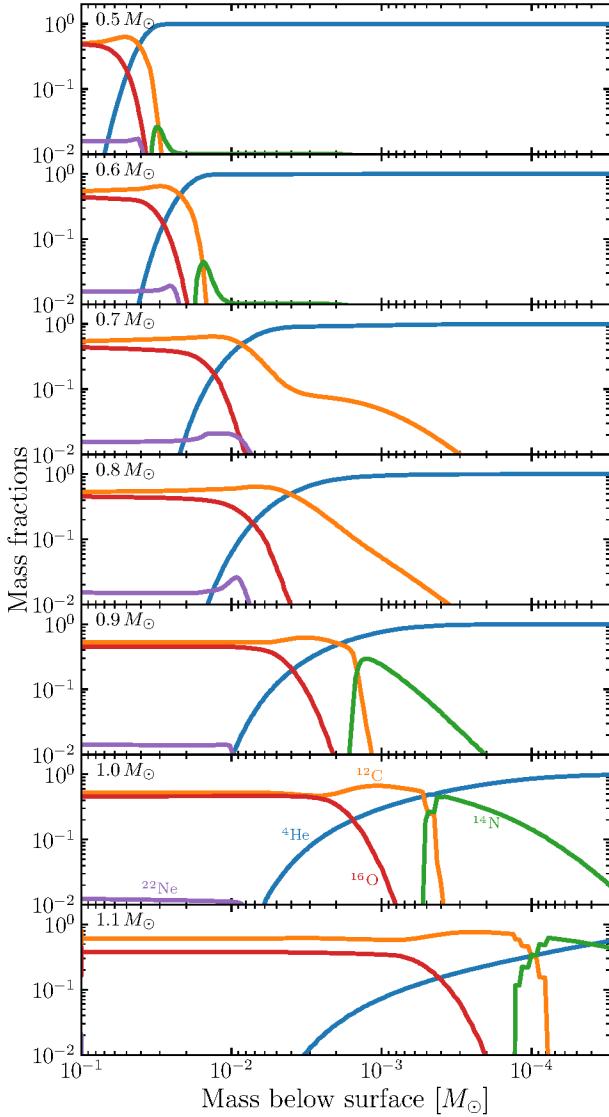
After shell-burning quenches, the stars contract and reach a maximum effective temperature and then begin to evolve down the WD cooling track. At the time of maximum effective temperature, we turn on semiconvection and thermohaline mixing along with diffusion. Finally, we stop the models after they reach 1 Gyr of age.

We also consider a C/O WD model of  $1.1 M_{\odot}$ . If created during single stellar evolution, such a massive core will ignite carbon-burning on the asymptotic giant branch and thus become an O/Ne WD (e.g., Murai et al. 1968; Doherty et al. 2015). However, a C/O WD of this mass can be created if  $\sim 0.1 M_{\odot}$  of helium is accreted onto a lower-mass C/O WD and is burned to C/O stably (Wu et al. 2022; Shen et al. 2023) without igniting carbon-burning. Thus, we construct a  $1.1 M_{\odot}$  C/O WD by accreting helium-rich material ( $X_{^4\text{He}} = 0.99$  and  $X_{^{14}\text{N}} = 0.01$ ) onto our  $1.0 M_{\odot}$  C/O WD model at a rate of  $2 \times 10^{-6} M_{\odot} \text{ yr}^{-1}$ , which yields a stable-burning envelope (Shen & Bildsten 2007; Piersanti et al. 2014; Brooks et al. 2016). Mixing and diffusion are turned off during this phase. Once the total mass reaches  $1.1 M_{\odot}$ , the star is allowed to cool down (with mixing and diffusion reactivated at the time of maximum effective temperature) and become a WD. The model only cools for  $6 \times 10^8 \text{ yr}$  before convergence issues halt further evolution, but we deem this age to be adequate for our purposes.

Figures 1 and 2 show mass fractions for our seven WD models as a function of mass and distance below

<sup>2</sup> <https://docs.mesastar.org>, version 15140.

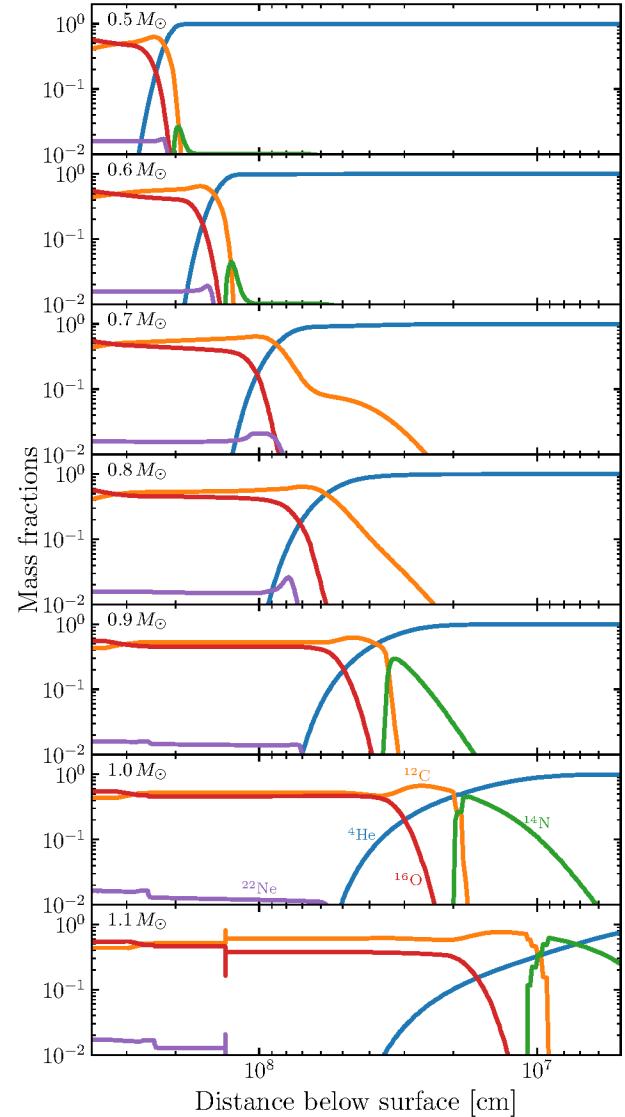
<sup>3</sup> See also the materials associated with Shen’s 2015 **MESA** summer school lectures: <https://doi.org/10.5281/zenodo.2603640>.



**Figure 1.** Composition profiles vs. mass below the surface of our WD models with total masses given in the upper left corner of each panel. Mass fractions are as labeled in the  $1.0 M_{\odot}$  panel.

the surface, respectively. The helium-rich envelope is a significant fraction of lower-mass WDs, making up almost 10% of a  $0.5 M_{\odot}$  WD's mass. The helium fraction decreases as the WD mass increases and makes up only  $\sim 10^{-4}$  of a  $1.1 M_{\odot}$  WD (although the tail of the helium distribution reaches much farther into the core).

Figure 3 shows the total  $^4\text{He}$  mass,  $M_{\text{He,tot}}$ , and the mass above the radius where the  $^4\text{He}$  mass fraction equals that of  $^{12}\text{C}$ ,  $M_{\text{He,transition}}$ , vs. WD mass. The two quantities are quite close in value for most WDs, but as the WD mass increases, the total helium mass becomes several times larger than the mass above the

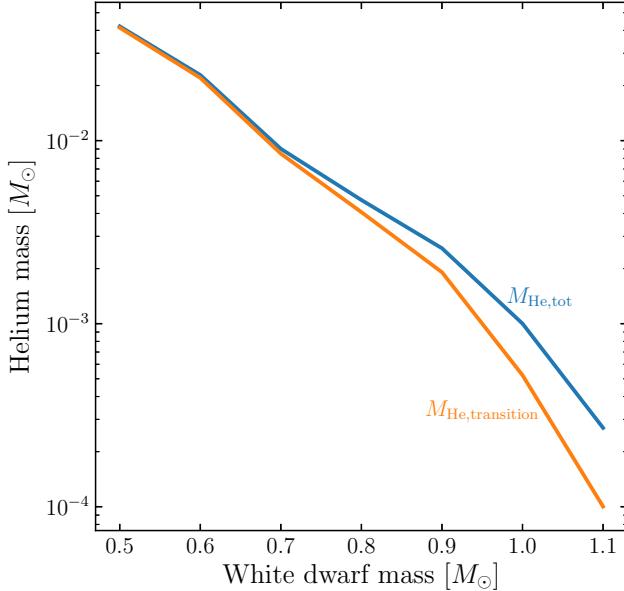


**Figure 2.** Same as Fig. 1 but vs. distance below the surface.

transition radius. This is due to the aforementioned significant helium tail that extends into the WD core.

Zenati et al. (2019) also emphasized the importance of the surface helium layers on C/O WDs by constructing models with `MESA`. Within our region of overlap ( $0.5 - 0.7 M_{\odot}$ ), our higher-mass models are in rough agreement, but we obtain significantly smaller helium masses at the lower-mass end; e.g., our  $0.5 M_{\odot}$  model has 50% less helium than obtained by Zenati et al. (2019). The reasons for this discrepancy are unclear.

With our realistic C/O WD models in hand, we are ready to construct two-dimensional detonation simulations, which we perform in Section 4. But first, we build our physical understanding with simplified one-



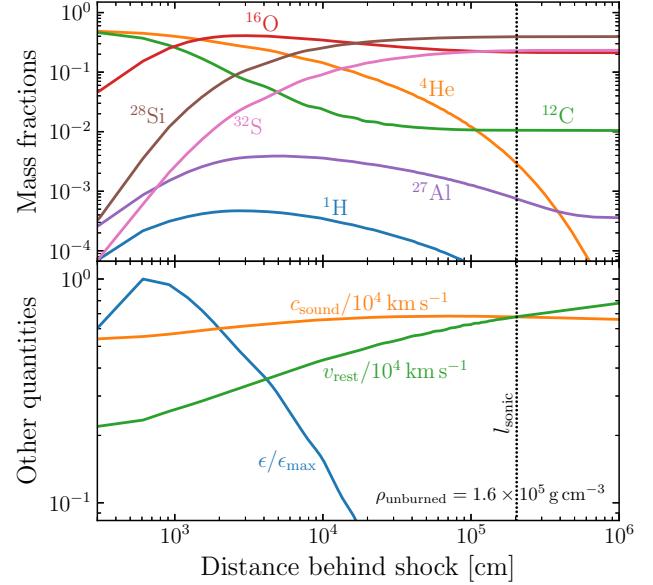
**Figure 3.** Total mass of  $^4\text{He}$  ( $M_{\text{He,tot}}$ ) and mass above the transition layer ( $M_{\text{He,transition}}$ ) vs. WD mass.

dimensional detonation calculations, which we now describe.

### 3. ONE-DIMENSIONAL HE/C DETONATIONS

In this section, we examine the propagation of one-dimensional detonations in material with equal mass fractions of  $^4\text{He}$  and  $^{12}\text{C}$ . This choice is motivated by the two-dimensional detonations discussed in the next section, which propagate in the transition region between the helium-rich surface layer and the carbon-rich core. Here, we calculate whether or not detonations can propagate at various densities, their associated lengthscales, and the effects of resolution on these results.

Our one-dimensional detonation simulations are performed using the reactive hydrodynamics code **FLASH** (Fryxell et al. 2000; Dubey et al. 2009),<sup>4</sup> modified to use nuclear networks and tabulated reaction rates from **MESA** (Shen et al. 2018a; Townsley et al. 2019; Boos et al. 2021, 2024). We use a 56-isotope nuclear network for all of the simulations discussed in this paper, composed of neutrons,  $^1\text{H}$ ,  $^4\text{He}$ ,  $^{11}\text{B}$ ,  $^{12-13}\text{C}$ ,  $^{13-15}\text{N}$ ,  $^{15-17}\text{O}$ ,  $^{18-19}\text{F}$ ,  $^{19-22}\text{Ne}$ ,  $^{22-23}\text{Na}$ ,  $^{23-26}\text{Mg}$ ,  $^{25-27}\text{Al}$ ,  $^{28-30}\text{Si}$ ,  $^{29-31}\text{P}$ ,  $^{31-33}\text{S}$ ,  $^{33-35}\text{Cl}$ ,  $^{36-39}\text{Ar}$ ,  $^{39}\text{K}$ ,  $^{40}\text{Ca}$ ,  $^{43}\text{Sc}$ ,  $^{44}\text{Ti}$ ,  $^{47}\text{V}$ ,  $^{48}\text{Cr}$ ,  $^{51}\text{Mn}$ ,  $^{52,56}\text{Fe}$ ,  $^{55}\text{Co}$ , and  $^{56,58-59}\text{Ni}$ ; this network is the same as that used in Townsley et al. (2019) and Boos et al. (2021, 2024), with the addition of the isotope  $^{19}\text{F}$  for completeness, although it does not appear to have an effect on our results. Detonations are initi-



**Figure 4.** Profiles vs. distance behind the shock front of a steady-state detonation. The upstream unburned fuel has equal mass fractions of  $^4\text{He}$  and  $^{12}\text{C}$  and a density of  $1.6 \times 10^5 \text{ g cm}^{-3}$ . The top panel shows mass fractions of selected isotopes, and the bottom panel shows the sound speed and rest frame fluid velocity (in units of  $10^4 \text{ km s}^{-1}$ ) and the energy generation rate normalized to the maximum value,  $\epsilon/\epsilon_{\text{max}}$ . The dotted line shows the location where the rest frame fluid velocity is equal to the sound speed.

ated in spherical symmetry via a hotspot in a uniform medium with a temperature of  $2 \times 10^9 \text{ K}$  at the center that decreases linearly to the edge of the hotspot to a value of  $10^6 \text{ K}$ , matching the temperature of the unperturbed material. The size of the hotspot is chosen to be approximately the smallest size that results in a successful detonation that continues to propagate for at least 10 hotspot radii or 100 sonic lengthscales, as defined below. Burning is turned off within the shock, and no reaction limiter is used (Kushnir et al. 2013; Shen et al. 2018a; Kushnir & Katz 2020; Boos et al. 2021, 2024), although both choices are moot for our highest resolution cases because the burning structure is resolved. Electron screening is implemented following Chugunov et al. (2007), and neutrino losses are neglected given the high temperatures achieved in the detonations.

Figure 4 shows the results for our fiducial case with an initial unburned fuel density of  $1.6 \times 10^5 \text{ g cm}^{-3}$  and a minimum cell size of  $300 \text{ cm}$ . The initial composition is equal mass fractions of  $^4\text{He}$  and  $^{12}\text{C}$ , as with all of the calculations discussed in this section. The top panel shows the steady-state post-shock profiles of mass fractions for selected isotopes, and the bottom panel shows the energy generation rate, normalized to its maximum

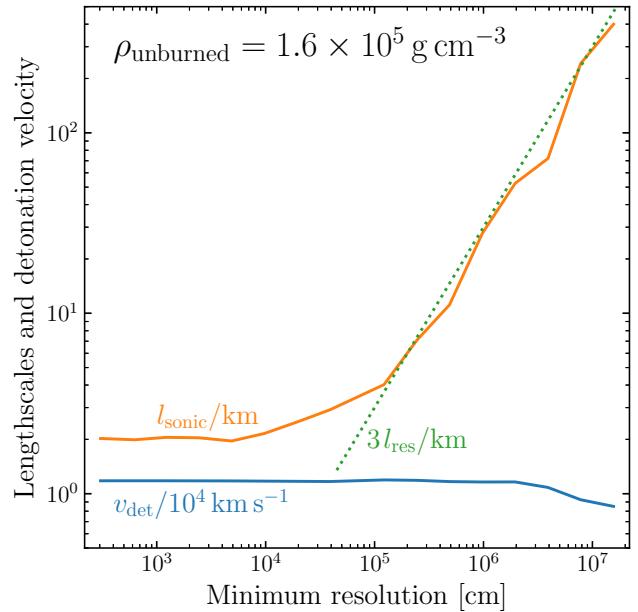
<sup>4</sup> <https://flash.rochester.edu/site/flashcode>, version 4.3.

value ( $\epsilon/\epsilon_{\max}$ ) as well as the sound speed ( $c_{\text{sound}}$ ) and the fluid velocity in the rest frame of the shock ( $v_{\text{rest}}$ ), both in units of  $10^4 \text{ km s}^{-1}$ .

The primary products of this detonation are  $^{28}\text{Si}$ ,  $^{32}\text{S}$ , and  $^{16}\text{O}$ , with a smaller amount of  $^{24}\text{Mg}$ ,  $^{20}\text{Ne}$ ,  $^{36}\text{Ar}$  (not shown in Fig. 4) and unburnt  $^{12}\text{C}$ . Essentially no iron-group elements are produced; the heaviest isotope that reaches a mass fraction  $> 10^{-3}$  is  $^{40}\text{Ca}$ . Crucially, a small amount of hydrogen is generated, as can be seen in the top panel, peaking at a mass fraction of  $5 \times 10^{-4}$ . These protons are produced via  $^{24}\text{Mg}(\alpha, p)^{27}\text{Al}$  and, to a lesser extent,  $^{20}\text{Ne}(\alpha, p)^{23}\text{Na}$ , reactions; the small number of  $^{20}\text{Ne}$  and  $^{24}\text{Mg}$  seeds are generated via direct  $\alpha$ -captures starting from  $^{12}\text{C}$ . We note that while Shen & Moore (2014) emphasized the importance of  $^{14}\text{N}$  as a source of protons via the  $^{14}\text{N}(\alpha, p)^{17}\text{O}$  reaction, our calculations show that free protons can be generated even if no  $^{14}\text{N}$  is available.

As discussed by Weinberg et al. (2006) in the context of Type I X-ray bursts and by Shen & Moore (2014) for helium shell detonations on WDs, these protons greatly accelerate helium-burning by allowing for the  $^{12}\text{C}(p, \gamma)^{13}\text{N}(\alpha, p)^{16}\text{O}$  pathway, shortcutting the relatively slow direct  $\alpha$ -capture on  $^{12}\text{C}$ . Shen & Moore (2014) noted that this can reduce the helium-burning timescale by a factor of  $\sim 5000$  at a density of  $10^5 \text{ g cm}^{-3}$  when compared to the triple- $\alpha$  reaction (see their Fig. 1), but this was for an assumed composition of  $X_{12\text{C}} = 0.05$  and  $X_{\text{H}} = 10^{-4}$ . In the transition region between the helium-rich shell and the carbon-rich core, the carbon mass fraction is a factor of 10 higher and the hydrogen mass fraction grows to a factor of  $\sim 5$  larger as well, reducing the burning time to just  $\sim 3 \times 10^{-6}$  of the triple- $\alpha$  timescale. It is thus vital that any studies of helium detonations, especially those occurring in thin shells, use large nuclear reaction networks; nuclear networks that shortcut  $\alpha$ -chain burning and only assume direct  $\alpha$ -captures and  $(\alpha, p)(p, \gamma)$  reactions yield qualitatively different and incorrect results in this regime.

The bottom panel of Figure 4 shows that the fluid velocity in the shock's rest frame reaches the local sound speed at a distance behind the shock front that we label the sonic lengthscale,  $l_{\text{sonic}}$ . In a standard Chapman-Jouguet (C-J) detonation, this lengthscale coincides with the complete conversion of fuel to ash (Fickett & Davis 1979). In our case, a small amount of burning continues beyond this point (as evidenced by the decreasing  $^4\text{He}$  mass fraction), but this region is out of sonic contact with the shock front, and the energy release does not contribute to its propagation. This lengthscale is thus closely related to the C-J lengthscale, but we label it  $l_{\text{sonic}}$  to avoid any confusion.



**Figure 5.** Resolution study for a detonation with the same initial conditions as for the calculation shown in Figure 4. The detonation velocity in units of  $10^4 \text{ km s}^{-1}$  is shown in blue, and the sonic lengthscale in km is shown in orange. The green dotted line is three times the minimum cell size in km.

Figure 5 shows the results of a resolution study for our fiducial one-dimensional detonation calculation ( $\rho_{\text{unburned}} = 1.6 \times 10^5 \text{ g cm}^{-3}$ , initial  $X_{4\text{He}} = X_{12\text{C}} = 0.5$ ). As the minimum resolution,  $l_{\text{res}}$ , coarsens and the sonic lengthscale is no longer resolved,  $l_{\text{sonic}}$  becomes  $\sim 3 \times l_{\text{res}}$ . That is to say, the energy release that powers the detonation occurs over just three zones in unresolved helium detonations.

The total energy release and the commensurate detonation velocity remain close to the actual, physical value even for grossly unresolved simulations: e.g., when the minimum resolution is 10 times larger than the resolved sonic lengthscale, the detonation velocity is still 99% of the converged result. Even at a minimum resolution of 100 times the true value of  $l_{\text{sonic}}$ , the velocity is 70% of the converged value.

We do not find any cases in which a detonation that successfully propagates at a coarse resolution fails to propagate at a finer resolution. Our resolution studies show that, for simulations that do not resolve the true sonic lengthscale, going to higher resolutions increases the detonation velocity and decreases the sonic lengthscale.

Previous studies have probed the success and failure of helium shell detonations, pointing out the importance of post-shock radial expansion as a mechanism for quench-

ing the burning and causing a detonation to fail (Townsley et al. 2012; Moore et al. 2013; Shen & Moore 2014). If radial expansion occurs within sonic communication of the detonation front, it can act as an additional energy sink that weakens and ultimately quenches the propagating detonation.

For a strong shock, as appropriate for the detonations we consider, the jump conditions yield a pressure in the burned ash of  $P_{\text{burn}} = \rho_{\text{unburned}} v_{\text{det}}^2 / (\gamma_{\text{burn}} + 1)$ , where  $\gamma_{\text{burn}}$  is the equation of state adiabatic exponent,  $\gamma = 1 + P/(u\rho)$ , evaluated in the ash. The over-pressured ash expands radially with an acceleration of  $gP_{\text{burn}}/P_{\text{unburned}}$ , where  $g$  is the gravitational acceleration at the interface and  $P_{\text{unburned}}$  is the unperturbed pressure. Thus, the ash will expand a pressure scale height ( $H_P = P_{\text{unburned}}/\rho_{\text{unburned}}g$ ) in a timescale

$$t_{\text{expand}} \sim \sqrt{\frac{2H_P P_{\text{unburned}}}{P_{\text{burn}} g}} \sim \sqrt{2(\gamma_{\text{burn}} + 1)} \frac{H_P}{v_{\text{det}}}, \quad (1)$$

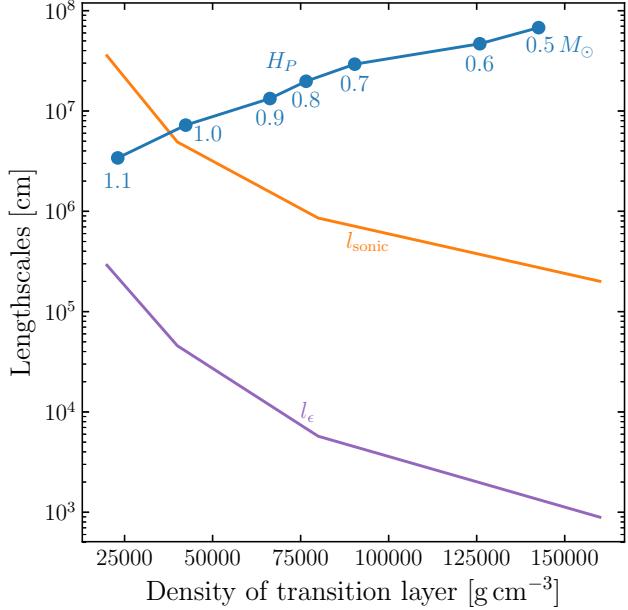
and so the lengthscale that the detonation traverses in the time that the overpressure causes significant radial expansion is

$$l_{\text{expand}} \sim \sqrt{2(\gamma_{\text{burn}} + 1)} H_P. \quad (2)$$

Thus, for a shell detonation to successfully propagate, it must complete (or nearly complete) its burning before the detonation has moved a lengthscale equivalent to the pressure scale height in the unburned medium: that is, a successful shell detonation requires  $l_{\text{sonic}} \lesssim H_P$ .

Figure 6 shows the detonation lengthscales  $l_{\text{sonic}}$  and  $l_\epsilon$  (the post-shock distance to the location of maximum energy generation rate) and the scale height at the transition layer for the WD models discussed in Section 2 as a function of the density of the unburned fuel in the case of the detonation lengthscales and the density of the transition layers for the WD models. We see that lower-mass WDs  $\lesssim 1.0 M_\odot$  are born with helium shells for which the transition regions have relatively large scale heights. If a detonation can be initiated in such a transition region, it should successfully propagate without being affected by the radial expansion caused by the shock's overpressure. Conversely, for higher-mass WDs  $\gtrsim 1.0 M_\odot$ , the radial blowout will quench the burning, and no detonation is possible unless more mass is added to the shell, which both decreases  $l_{\text{sonic}}$  and increases the scale height.

#### 4. TWO-DIMENSIONAL DETONATIONS IN REALISTIC C/O WDS

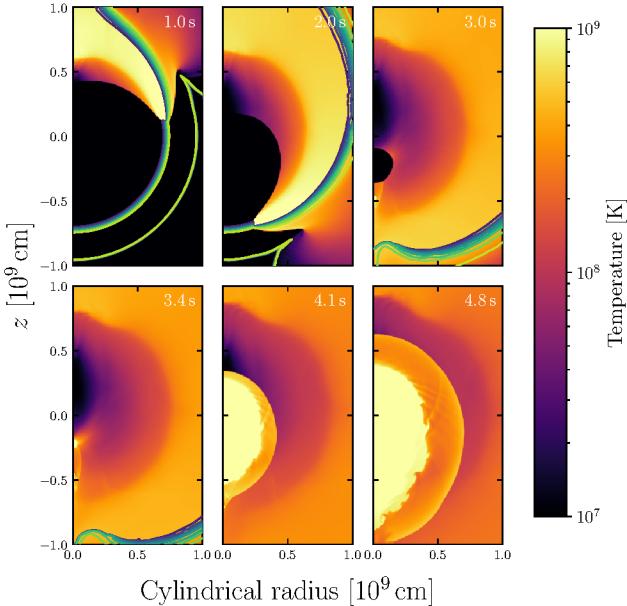


**Figure 6.** Various lengthscales vs. the density of the transition layer for the WD models discussed in Section 2. The pressure scale height is shown in blue, with each mass as labeled. The orange line shows the sonic lengthscale assuming equal mass fractions of  $^4\text{He}$  and  $^{12}\text{C}$ , and the purple line shows the lengthscale between the shock and the location of maximal energy generation.

In this section, we test the intuition gained from our one-dimensional toy calculations with two-dimensional axisymmetric simulations performed with FLASH. We use the same 56-isotope nuclear network as in our one-dimensional calculations. We do not use tracer particles (Shen et al. 2018a; Boos et al. 2021, 2024), as we do not attempt to track detailed nucleosynthesis in this work. The composition, density, and temperature profiles calculated with MESA, described in Section 2, are mapped onto grids with domain sizes  $\sim 1.2$  times larger than the WD radii. The shell detonations are initiated by perturbing stellar material within hotspots centered on the symmetry axis at the transition layer. The hotspots have radii of  $4 \times 10^7$  cm, maximal temperatures at the center of  $2 \times 10^9$  K, linear temperature gradients, and densities equal to four times the local density. These hotspot conditions are extreme, but the present work focuses only on the success or failure of the shell detonation's propagation and the shock's convergence within the core. We leave a proper examination of the initiation of the detonation to other complementary studies.

##### 4.1. Simulations of models with natal profiles

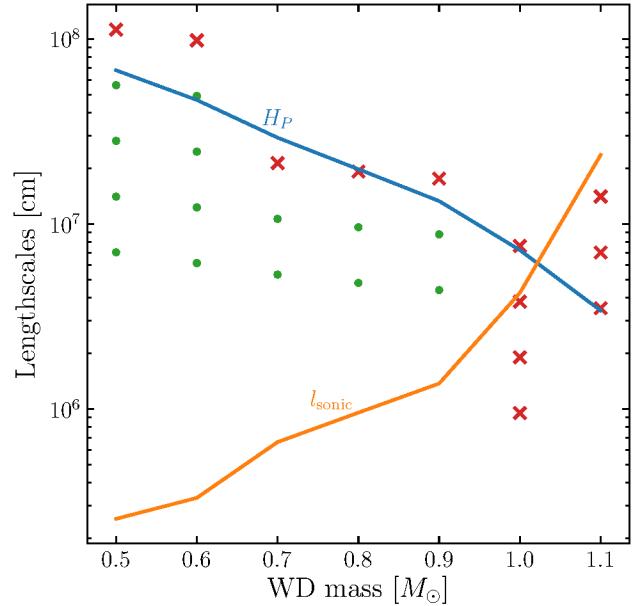
Figure 7 shows multiple snapshots of the temperature for our  $0.5 M_\odot$  model with a minimum cell size of 23 km. The nine contours show linearly increasing constant he-



**Figure 7.** Temperatures (colors) and helium mass fractions (green contours) for six snapshots of a  $0.5 M_{\odot}$  double detonation simulation. Helium mass fraction contours increase linearly from a value of 0.1 to 0.9 from dark to light.

lum mass fractions of  $0.1 - 0.9$  from dark to light colors. In the first two panels (1.0 and 2.0 s after the simulation begins), the shell detonation can be seen to propagate successfully, led by a front in the transition layer where  ${}^4\text{He}$  and  ${}^{12}\text{C}$  have roughly equal mass fractions. Our goal is not to calculate detailed nucleosynthesis in these simulations, but we note that the shell detonation primarily produces  ${}^{16}\text{O}$ ,  ${}^{28}\text{Si}$ , and  ${}^{32}\text{S}$  with essentially no iron-group elements, matching the expectations from our one-dimensional calculations. By 3.0 s, the shell detonation has completed its journey and the shock wave it sent into the core focuses towards a convergence region. The converging shock ignites a core detonation just before 3.4 s. In the final two panels (4.1 and 4.8 s), the core detonation has extinguished due to the relatively low densities in this low-mass model and has become an outwardly propagating shock wave, as evidenced by the  $> 10^9 \text{ K}$  central ash surrounded by an expanding shell of just-shocked, but non-burned, core material at a temperature of  $\sim 3 \times 10^8 \text{ K}$ .

Table 1 and Figure 8 summarize the results of our two-dimensional simulations. In Figure 8, the pressure scale height at the transition layer for each WD model is shown in blue, and the orange line shows the sonic lengthscale for a detonation at the transition layer density. Crosses and circles show three times the minimum cell size – approximately the sonic lengthscale for un-



**Figure 8.** Various lengthscales vs. total WD mass. The blue line shows the pressure scale height measured at the transition layer. The sonic lengthscale of a detonation powered by helium/carbon fuel at the transition layer density is shown in orange. Crosses and circles show three times the minimum cell size for two-dimensional simulations with failed and successful detonations, respectively.

resolved detonations – for failed and successful simulations, respectively.

As expected from our previous discussion, we find that lower-mass models  $\lesssim 1.0 M_{\odot}$  can support successful shell detonations with their natal compositional profiles, given sufficient resolution such that  $l_{\text{sonic}} \lesssim H_P$ , where  $l_{\text{sonic}} \sim 3 \times l_{\text{res}}$  for unresolved detonations. Conversely, higher-mass models  $\gtrsim 1.0 M_{\odot}$  cannot have successful shell detonations at birth because the scale height at the transition layer is shorter than the sonic lengthscale of a detonation at that density, and the post-shock radial expansion extinguishes the burning. Table 1 also demonstrates that, for cases where the shell detonates, the converging shock always ignites a core detonation. For some models, achieving the core detonation requires decreasing the minimum cell size prior to shock convergence (see, e.g., Boos et al. 2021 and Rivas et al. 2022), as denoted in the table, but, for a sufficient resolution, a shell detonation implies a core detonation (Shen & Bildsten 2014; Ghosh & Kushnir 2022). We note that in some previous studies (Pakmor et al. 2013, 2021, 2022; Roy et al. 2022), a successful shell detonation failed to trigger a converging core detonation. However, the minimum spatial resolutions in these studies range from  $10 - 30 \text{ km}$ , whereas Table 1 shows that achieving core

**Table 1.** Results of multi-dimensional simulations

Total mass [ $M_{\odot}$ ]	Mass above transition layer [ $M_{\odot}$ ]	Transition layer density [ $\text{g cm}^{-3}$ ]	Minimum resolution [km]	Shell detonation? N: No, Y: Yes	Average shell detonation velocity [ $1000 \text{ km s}^{-1}$ ]	<i>z</i> -coordinate of core convergence [1000 km]	Core detonation? —: No, Y: Yes
0.5	$4.138 \times 10^{-2}$	$1.426 \times 10^5$	375	N	—	—	—
			188	Y	8.166	-2.69	Y (with 47 km min. res.)
			93.8	Y	8.924	-2.45	Y (with 47 km min. res.)
			46.9	Y	9.636	-2.32	Y
			23.4	Y	10.39	-2.18	Y
			—	—	—	—	—
0.6	$2.214 \times 10^{-2}$	$1.259 \times 10^5$	328	N	—	—	—
			164	Y	8.100	-2.85	Y (with 41 km min. res.)
			82.0	Y	8.816	-2.61	Y (with 41 km min. res.)
			41.0	Y	9.451	-2.44	Y
			20.5	Y	10.14	-2.32	Y
0.7	$8.469 \times 10^{-3}$	$9.036 \times 10^4$	71.1	N	—	—	—
			35.6	Y	8.938	-2.56	Y (with 18 km min. res.)
			17.8	Y	9.856	-2.42	Y
0.8	$4.070 \times 10^{-3}$	$7.656 \times 10^4$	64.1	N	—	—	—
			32.0	Y	8.708	-2.54	Y (with 8.0 km min. res.)
			16.0	Y	9.685	-2.40	Y (with 8.0 km min. res.)
0.9	$1.900 \times 10^{-3}$	$6.629 \times 10^4$	58.6	N	—	—	—
			29.3	Y	8.531	-2.53	Y (with 3.7 km min. res.)
			14.7	Y	9.408	-2.37	Y (with 3.7 km min. res.)
1.0	$5.232 \times 10^{-4}$	$4.237 \times 10^4$	25.4	N	—	—	—
			12.7	N	—	—	—
			6.35	N	—	—	—
			3.17	N	—	—	—
1.0 + 0.001	$1.504 \times 10^{-3}$	$8.337 \times 10^4$	54.7	N	—	—	—
			27.3	Y	7.580	-2.54	Y (with 3.4 km min. res.)
			13.7	Y	8.333	-2.40	Y (with 3.4 km min. res.)
1.1	$9.412 \times 10^{-5}$	$2.307 \times 10^4$	46.9	N	—	—	—
			23.4	N	—	—	—
			11.7	N	—	—	—
1.1 + 0.001	$1.099 \times 10^{-3}$	$1.031 \times 10^5$	39.1	N	—	—	—
			19.5	N	—	—	—
			9.77	N	—	—	—
1.1 + 0.002	$2.110 \times 10^{-3}$	$1.582 \times 10^5$	4.88	N	—	—	—
			23.4	N	—	—	—
			11.7	Y	7.789	-2.25	Y (with 1.5 km min. res.)
1.1 + 0.003	$3.126 \times 10^{-3}$	$2.065 \times 10^5$	93.8	N	—	—	—
			46.9	Y	7.624	-2.29	Y (with 3.0 km min. res.)
			23.4	Y	8.123	-2.21	Y (with 3.0 km min. res.)
			11.7	Y	8.676	-2.13	Y (with 3.0 km min. res.)

detonations can require resolutions of  $\sim 3$  km. Thus, the lack of core detonations in these previous studies is likely due to insufficient resolution, as speculated by Pakmor et al.

We also note that, for simulations with successful detonations, higher resolutions imply more complete shell burning and faster detonation velocities (column 6 of Table 1). This is in line with the resolution study described in Section 3 and Figure 5. The shorter time for the shell detonation to completely encircle the WD core also implies a convergence point closer to the WD’s center (column 7 of Table 1), which will have implications for the ejecta structure of the resulting explosion, affecting, for example, the asymmetries in spectral velocities from opposing lines of sight.

We find successful detonations for significantly smaller shell masses than the minimum detonatable masses presented by Shen & Moore (2014). Our  $0.9 M_{\odot}$  model, with  $M_{\text{He,tot}} = 0.0026 M_{\odot}$  and  $M_{\text{He,transition}} = 0.0019 M_{\odot}$ , successfully detonates while Shen & Moore (2014) find a minimum critical shell mass of  $0.007 M_{\odot}$  for this core mass. This is due to the different composition of the detonating layer: Shen & Moore (2014) assumed a composition of  $X_{4\text{He}} = 0.891$ ,  $X_{12\text{C}} = X_{16\text{O}} = 0.05$ , and  $X_{14\text{N}} = 0.009$ , whereas in our realistic WD models, the detonation propagates within a layer of nearly equal  ${}^4\text{He}$  and  ${}^{12}\text{C}$  mass fractions. Even without  ${}^{14}\text{N}$ , sufficient protons are still produced to allow the  ${}^{12}\text{C}(p, \gamma)(\alpha, p){}^{16}\text{O}$  to occur, and the higher initial mass fraction of  ${}^{12}\text{C}$  allows for more complete consumption of the  ${}^4\text{He}$  at lower densities, thus powering a successful detonation.

The  $0.5$  and  $0.6 M_{\odot}$  core detonations produce  $1.2 \times 10^{-4}$  and  $1.3 \times 10^{-3} M_{\odot}$  of  ${}^{56}\text{Ni}$ , respectively. Although our simulations are not designed to calculate detailed nucleosynthesis,<sup>5</sup> our findings of very small  ${}^{56}\text{Ni}$  masses for low-mass core detonations are likely robust, given the low densities  $< 10^7 \text{ g cm}^{-3}$  (Seitenzahl & Townsley 2017). However, these yields will be boosted if the low-mass core is the companion WD in a double WD binary in which the primary explodes. The impact of the first explosion’s ejecta may both initiate a shell detonation of the secondary and send a strong shock into the core that increases its density prior to the ignition of the core detonation. This explains why Shen et al. (2018a)

<sup>5</sup> Our simulations are not followed all the way to homologous expansion, nor do we include tracer particles for post-processing with a large reaction network. We refer the interested reader to previous work focused on nucleosynthesis of exploding sub-Chandrasekhar-mass WDs, such as Shen et al. (2018a), Gronow et al. (2021b), Boos et al. (2021, 2024), and Keegans et al. (2023).

find a  ${}^{56}\text{Ni}$  mass of  $0.02 M_{\odot}$  for their  $0.8 M_{\odot}$  WD detonation whereas Boos et al. (2024)’s  $0.8 M_{\odot}$  secondary WD, ignited after the impact of a primary WD’s ejecta, produces  $0.15 M_{\odot}$  of  ${}^{56}\text{Ni}$ .

#### 4.2. High-mass models with added mass

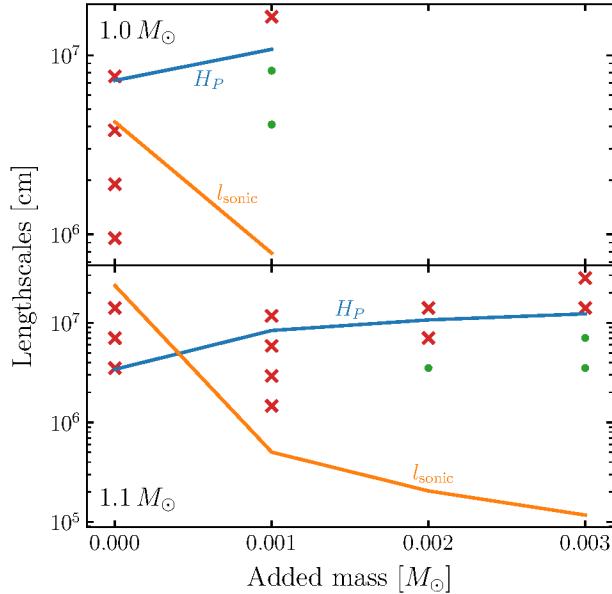
We supplement the  $1.0$  and  $1.1 M_{\odot}$  calculations with additional models in which we add a small amount of helium-rich mass ( $X_{4\text{He}} = 0.99$ ,  $X_{14\text{N}} = 0.01$ ) and then allow the resulting stars to relax back to their initial central temperatures with mixing and diffusion active. Such stars may arise in binaries where the companion is a helium-burning star that transfers material when it expands and crosses the helium-burning equivalent of the Hertzsprung gap (Yoon & Langer 2003; Ruiter et al. 2013). The first phase of this mass transfer may result in stable helium-burning, growing the WD accretor by  $\sim 0.1 M_{\odot}$  (Piersanti et al. 2014; Brooks et al. 2016). However, as mass transfer continues, the accretion rate declines, stable helium-burning ends, and unstable helium novae will result.<sup>6</sup> Eventually, mass transfer ceases, and the resulting helium layer on the WD’s surface will be, on average, several  $10^{-3} M_{\odot}$  larger than the minimum mass for stable helium-burning (Iben & Tutukov 1989; Bildsten et al. 2007) that the WDs initially possessed at birth.

The additional mass increases the density of the transition layer, which increases the scale height and decreases the detonation’s sonic lengthscale, both of which help to make shell detonations more successful. Table 1 and Figure 9 summarize the results of these additional simulations. Adding  $10^{-3} M_{\odot}$  to the  $1.0 M_{\odot}$  model allows for a successful shell detonation (and subsequent core detonation). For reasons that are unclear, an additional  $\geq 2 \times 10^{-3} M_{\odot}$  is required for a shell and core detonation for the  $1.1 M_{\odot}$  model, even though  $l_{\text{sonic}} < H_P$  is achieved for the  $1.1 + 10^{-3} M_{\odot}$  case. Further investigation is required to understand why a detonation does not propagate in this case.

## 5. DISCUSSION

Our results show that most C/O WDs are born with structures that allow for successful double detonations if a helium shell detonation can be initiated. Only massive C/O WDs  $\gtrsim 1.0 M_{\odot}$  do not possess sufficiently dense transition regions for successful shell detonations at birth. However, some of these massive WDs will ac-

<sup>6</sup> We assume that these novae do not result in the merger of the helium star and WD, whereas this may be the case for novae in double WD systems due to orbital angular momentum loss during the nova (Shen 2015; Nelemans et al. 2016; Schreiber et al. 2016; Shen & Quataert 2022).



**Figure 9.** Lengthscales vs. added mass for 1.0 (top panel) and  $1.1 M_{\odot}$  (bottom panel) WDs. The pressure scale heights at the transition radius are shown as blue lines, and the orange lines demarcate the sonic lengthscale at the transition radius’s density. Crosses and circles represent three times the minimum cell size for simulations with failed and successful detonations, respectively.

crete enough helium after they are first formed and prior to the formation of the double WD binary to allow for successful shell and core detonations during the merging process.

Thus, the crucial issue determining the success of a double detonation and subsequent SN Ia is reduced to: does the unstable mass transfer during a double WD merger reach conditions to initiate a shell detonation? Explorations of detonation ignition during double WD mergers have been performed (Guillochon et al. 2010; Dan et al. 2012; Pakmor et al. 2013; Shen & Moore 2014; Dan et al. 2015; Iwata & Maeda 2022; Pakmor et al. 2022; Roy et al. 2022) and are still ongoing (Rajavel et al. submitted). Further work needs to be carried out, including the possible ignition of a subsonic deflagration prior to the onset of the detonation, but some broad trends can be inferred. For one, a more massive accretor will yield a hotter and denser region surrounding the impacting accretion stream. This is due to the fact that a more massive WD has a deeper gravitational potential, so the virial temperature and the ram pressure, and thus the depth and density the stream reaches, will be higher. Additionally, binaries with higher mass ratios yield accretion streams that impact the accretor’s surface more perpendicularly and thus plunge more deeply.

Thus, the hottest and densest hotspots with the greatest likelihood to ignite detonations will be generated in binaries with the highest-mass accretors and donors. This may be the reason that there do not appear to be more subluminous SNe Ia (Li et al. 2011; Ghosh & Kushnir 2022; Sharon & Kushnir 2022), which likely occur in binaries with primary WD masses  $\sim 0.85 M_{\odot}$  (Blondin et al. 2017; Shen et al. 2018a, 2021a,b), which should outnumber binaries with more massive WDs. Even though we have found that double detonations can propagate in all C/O WDs  $\lesssim 1.0 M_{\odot}$ , the ignition of such a detonation in a low-mass WD via an accretion stream may require a mass ratio close to unity or may even be entirely impossible for a low-enough primary mass (although see Morán-Fraile et al. 2024 for a counter-example).

If the primary WD does explode, our results suggest that if the impacting ejecta can ignite a helium detonation in the companion’s helium shell (which seems plausible given the outer ejecta velocities  $> 10^4 \text{ km s}^{-1}$ ), the detonation will successfully propagate in the companion’s natal transition layer and lead to a double detonation of the companion, resulting in a two-star explosion (Tanikawa et al. 2019; Pakmor et al. 2022; Boos et al. 2024). If this occurs most of the time, and thus most SNe Ia leave no companion behind, then historical SN remnants will contain no surviving companion WDs, which appears to be the case for the remnants of SN 1006 (Kerzendorf et al. 2018; Shields et al. 2022) and SNR 0509-67.5 (Shields et al. 2023). Exceptions to this outcome are if the donor is a low-mass helium core WD (for which densities are relatively low and  $^{12}\text{C}$  is not present to accelerate helium-burning<sup>7</sup>) or a high-mass C/O WD  $\gtrsim 1.0 M_{\odot}$ . One other exception is if the primary WD is  $\gtrsim 1.0 M_{\odot}$  and did not undergo an additional phase of helium accretion prior to the merger. In this case, a direct carbon ignition might be triggered (Pakmor et al. 2010, 2011, 2012) but would require a significant amount of mass transfer from the companion, possibly removing the helium-rich layers and thus preventing a double detonation when the primary’s ejecta impacts the companion (if the companion has not been completely tidally disrupted at the time of explosion). The interaction of the ejecta with the excess C/O-rich

<sup>7</sup> Several studies (Papish et al. 2015; Tanikawa et al. 2019; Boos et al. 2024) have suggested the possibility that the primary WD’s impacting ejecta can indeed ignite a detonation in a helium-core WD companion. However, in all three studies, ignition was only achieved at artificially reduced separations between the two WDs. Further study is necessary to examine this possibility, which perhaps exists for the highest-mass helium-core WDs but likely does not for lower-mass cases.

companion material surrounding the exploding primary WD will increase the SN luminosity and possibly form dust at late times (Taubenberger et al. 2013; Siebert et al. 2024) and may be the explanation for the rare class of “super-Chandrasekhar-mass” SN 2003fg-like SNe Ia (Howell et al. 2006; Taubenberger et al. 2013; Raskin et al. 2014; Noebauer et al. 2016; Fitz Axen & Nugent 2023).

These three cases of exceptions may explain the class of seven recently discovered hypervelocity SN survivors (Shen et al. 2018b; Bauer et al. 2021; Chandra et al. 2022; El-Badry et al. 2023; Werner et al. 2024). The relatively low-velocity ( $1050 \text{ km s}^{-1}$ ), possibly helium-rich (Chandra et al. 2022) hypervelocity star D6-2 (Shen et al. 2018b) may have been a helium-core WD donor. Meanwhile, the four higher-velocity ( $\sim 2000 \text{ km s}^{-1}$ ) hot ( $> 2 \times 10^4 \text{ K}$ ) candidates discovered by El-Badry et al. (2023) may have been high-mass donors with insufficient helium layers to undergo a double detonation upon impact. Finally, D6-1 and D6-3 (Shen et al. 2018b), which are both cooler like D6-2 ( $< 10^4 \text{ K}$ ) but have much higher velocities ( $\sim 2000 \text{ km s}^{-1}$ ), may be formerly high-mass companions that lost significant mass while triggering direct carbon ignition of their primaries, leading to 2003fg-like SNe Ia; indeed, the late-time spectra of the SN 2003fg-like SN 2020hvf have been interpreted as evidence for a wind from a surviving star (Shen & Schwab 2017; Siebert et al. 2023). Further studies are necessary to explore all of these possible outcomes.

## 6. CONCLUSIONS

In this paper, we have calculated realistic models of C/O WDs for a range of masses and then conducted one- and two-dimensional detonation simulations based on these results. We have found that:

- Most C/O WDs are born with composition and density profiles that can support a detonation in the transition layer between the helium-rich shell and carbon-rich core. If such a shell detonation can be triggered, we find that it will, in turn, trigger a core detonation. No additional accretion after the formation of the WD is necessary for these detonations to propagate.
- Large nuclear reaction networks and realistic compositional profiles are crucial for capturing the propagation of these relatively low-density detonations in hydrodynamic codes.
- Only higher-mass C/O WDs  $\gtrsim 1.0 M_\odot$  cannot support shell detonations at birth. However,  $\sim 10^{-3} M_\odot$  of material accreted prior to the formation of the double WD binary, which is expected

for some systems, including all of those with primary C/O WDs  $> 1.05 M_\odot$ , is enough to allow for successful shell detonations when the double WDs begin to merge.

- If a companion C/O WD  $\lesssim 1.0 M_\odot$  is impacted with sufficient strength by the primary WD’s ejecta and has not transferred substantial mass prior to the explosion, it will undergo its own double detonation, leading to a two-star SN Ia.
- The detonations of natal low-mass helium shells do not produce significant amounts of iron-group elements. The detonations of low-mass C/O cores also do not produce a significant amount of  $^{56}\text{Ni}$ , but the yield will be increased if the core detonation is preceded by a strong shock from the impact of a primary WD explosion.

Combined with the extensive existing literature comparing observations to predicted observables of thin-shell sub-Chandrasekhar-mass WD explosions (Fink et al. 2007, 2010; Kromer et al. 2010; Sim et al. 2010; Blondin et al. 2017; Shen et al. 2018a; Polin et al. 2019; Townsley et al. 2019; Gronow et al. 2020, 2021a; Shen et al. 2021a,b; Boos et al. 2021; Pakmor et al. 2022; Boos et al. 2024), our work suggests that a majority of SNe Ia, ranging from subluminous SN 1991bg-likes to overluminous SN 1991T-likes and SN 2003fg-likes, may arise from the double detonations of both WDs in a merging double WD binary. A smaller fraction of SNe Ia may result from the explosion of only the more massive WD, leaving behind surviving hypervelocity companion WDs.

Our present study has several limitations, including the two-dimensional nature of our explosion simulations and our assumption that a detonation can be initiated in the shell-core transition layer by mass transfer from a companion WD. The interaction of the accretion stream with the accretor’s surface layers is a three-dimensional, turbulent, and complex process, which we do not attempt to capture in this paper. The propagation of the detonations we model may be influenced by these fluctuations, including compositional inhomogeneities mixing the core and surface material. Deflagrations or failed detonations may also alter the structure of the transition layer prior to the onset of a successful detonation. Future work should include an examination of detonation ignition conditions during mass transfer and during the interaction of the primary WD’s ejecta with the companion; two-dimensional and three-dimensional explosion modeling and radiative transfer of two-star explosions, including non-local thermodynamic equilibrium and early- and late-time calculations; simulations

of primary WD explosions within transferred companion material, possibly appropriate for 2003fg-like “super-Chandrasekhar-mass” SNe Ia; and stellar evolution calculations of hypervelocity survivors. These and other studies remain to be done, but it appears hopeful that the resolution to the SN Ia progenitor question is close at hand.

*Software:* `matplotlib` (Hunter 2007), `MESA` (Paxton et al. 2011, 2013, 2015, 2018, 2019), `FLASH` (Fryxell et al. 2000; Dubey et al. 2009)

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