

Fast SMBH growth in the SPT2349–56 protocluster at $z = 4.3$

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ABSTRACT

Context. Environment is one of the main physical drivers of galaxy evolution. The densest regions at high-redshift, i.e. $z > 2$ protoclusters, are gas-rich regions characterized by high star-formation activity. The same physical properties that enhance star formation in protoclusters are also thought to boost the growth of supermassive black holes (SMBHs), likely in heavily obscured conditions.

Aims. We aim to test this scenario by probing the active galactic nucleus (AGN) content of SPT2349–56, a massive, gas-rich, and highly star-forming protocluster core at $z = 4.3$ discovered as an overdensity of dusty star-forming galaxies (DSFGs), and comparing the results with the field environment and other protoclusters.

Methods. We observed SPT2349–56 with *Chandra* (200 ks), and search for X-ray emission from the known galaxy members. We also perform a spectral energy distribution fitting procedure to derive the physical properties of the discovered AGN.

Results. We detected in the X-ray band two protocluster members, namely C1 and C6, corresponding to an AGN fraction among DSFGs in the structure of $\approx 10\%$. This value is consistent with other protoclusters at $z = 2 - 4$, but higher than the AGN incidence among DSFGs in the field environment. Both AGN are heavily obscured sources, hosted in star-forming galaxies with $\approx 3 \times 10^{10} M_{\odot}$ stellar masses. We estimate that the intergalactic medium in the host galaxies contributes to a significant fraction, or even totally, to the nuclear obscuration. C1, in particular, is a highly luminous ($L_X = 2 \times 10^{45} \text{ erg s}^{-1}$) and Compton-thick ($N_H = 2 \times 10^{24} \text{ cm}^{-2}$) AGN, likely powered by a $M_{\text{BH}} > 6 \times 10^8 M_{\odot}$ SMBH, assuming Eddington-limited accretion. Its high accretion rate suggests that it is in the phase of efficient growth required to explain the presence of extremely massive SMBHs in the centers of local galaxy clusters. Considering SPT2349–56 and DRC, a similar protocluster at $z = 4$, and under different assumptions on their volumes, we find that gas-rich protocluster cores at $z \approx 4$ enhance the triggering of luminous ($\log \frac{L_X}{\text{erg s}^{-1}} = 45 - 46$) AGN by 3–5 orders of magnitude with respect to the predictions from the AGN X-ray luminosity function at similar redshift in the field environment. This result is not merely driven by the overdensity of the galaxy population in the structures.

Conclusions. Our results indicate that gas-rich protoclusters at high redshift boost the growth of SMBHs, which will likely impact the subsequent evolution of the structures, and thus represent key science targets to obtain a complete understanding of the relation between environment and galaxy evolution. Dedicated investigations of similar protoclusters are required to definitively confirm this conclusion with higher statistical significance.

Key words. galaxies: active – galaxies: high-redshift – quasars: general – quasars: supermassive black holes – galaxies: starburst – X-rays: galaxies

1. Introduction

According to the hierarchical growth of cosmic structures, dense regions at high redshift collapse and merge into the most-massive gravitationally bound objects in the local universe, i.e., galaxy clusters, which are characterized by more evolved galaxy populations than the field environment (e.g. Alberts et al. 2014). Therefore, galaxy evolution must have been accelerated in their ancestors, i.e., protoclusters (e.g. Overzier 2016; Chiang et al. 2017). In these regions, star formation is efficiently fueled by large amounts of gas infalling from the forming cosmic web (e.g. Umehata et al. 2019), and is likely boosted by the high rates of

galaxy interactions and mergers in these dense and unvirialized systems (e.g. Liu et al. 2023).

Radiative and mechanical feedback produced by gas accretion onto supermassive black holes (SMBHs) observed as active galactic nuclei (AGN) plays a fundamental role in regulating, and eventually hindering, further galaxy and SMBH growth in cluster members (e.g. Fabian 2012; Gilli et al. 2019; Gaspari et al. 2020). However, the effect of a dense environment on the triggering of nuclear activity at high redshift is still not well understood. X-ray observations are the best tools to investigate the incidence and physical properties of the AGN population in protoclusters, as bright X-ray emission is a reliable and nearly complete tracer of nuclear activity, even in the pres-

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ence of heavy obscuration (e.g., Brandt & Alexander 2015; Ivison et al. 2019). Dedicated X-ray programs with *Chandra* generally find enhanced AGN activity in protoclusters with respect to the field environment at similar redshift and local galaxy clusters (e.g., Lehmer et al. 2009b, 2013; Digby-North et al. 2010; Tozzi et al. 2022b, but see also Yang et al. 2018a; Macuga et al. 2019). These results support a scenario in which the large reservoirs of gas and the high rate of galaxy interactions promote the growth of SMBHs in the protocluster galaxy members, in addition to boosting the star-formation activity. Theoretical models (e.g. Hopkins et al. 2006) predict that these conditions favor fast, efficient, and possibly heavily obscured nuclear accretion. Most protocluster AGN are indeed characterized as being heavily obscured (e.g. Vito et al. 2020; Monson et al. 2023). These properties are typical of the peak phases of SMBH mass building, after which AGN feedback hampers additional galaxy and SMBH growth, eventually impacting the entire cluster’s evolution. In addition, the AGN enhancement may also be an effect of galaxies in protoclusters being typically more massive than in the field environment (e.g., Monson et al. 2021), as luminous AGN are typically found in galaxy with large stellar masses (e.g. Yang et al. 2017, 2018b).

Protocluster candidates are identified via detections of overdensities of galaxies, selected in many different ways (see Overzier 2016 and references therein). The identification of protocluster candidates as overdensities of dusty star-forming galaxies (DSFGs), Ly α emitters (LAEs), or Lyman- break galaxies (LBGs) are among the most efficient techniques up to $z \approx 8$ (e.g. Laporte et al. 2022; Morishita et al. 2023). Recently, the high angular resolution and sensitivity of ALMA allowed the identification of two extremely massive and star-forming overdensities of DSFGs, the Distant Red Core (DRC) at $z = 4.0$ (e.g. Oteo et al. 2018; Ivison et al. 2020), and SPT 2349–56 at $z = 4.3$ (e.g. Miller et al. 2018; Hill et al. 2020, 2022), discovered originally by *Herschel* and the South Pole Telescope, respectively (Vieira et al. 2010; Ivison et al. 2016). The cores of these structures extend to a few hundred kpc in projection, and are unique in terms of overdensity, total gas mass, and SFR density. Based on cluster evolutionary models and simulations, Oteo et al. (2018) and Hill et al. (2020) argued that DRC and SPT 2349–56 are the likely progenitors of $\approx 10^{15} M_{\odot}$ Coma-like clusters in the local universe. DRC consists of at least 13 spectroscopically identified $z \approx 4.0$ DSFGs with individual SFRs in the range of $50 - 3000 M_{\odot} \text{ yr}^{-1}$, for a total SFR $\approx 6500 M_{\odot} \text{ yr}^{-1}$. A total molecular gas mass $M_{H_2} > 10^{12} M_{\odot}$ was estimated from the [C I](1–0) emission lines detected from the protocluster members.

SPT 2349–56 was identified with ALMA observations as an overdensity of 30 galaxies spectroscopically confirmed at $z \approx 4.3$ via the detection of [C II] and CO(4–3) emission lines (Miller et al. 2018; Hill et al. 2020; Rotermund et al. 2021). Among them, 21 objects are detected in sub-mm/mm continuum emission (850 μm , 1.1 mm, or 3.2 mm; Hill et al. 2020), and in this paper we refer to them as DSFGs. The protocluster members are located in a massive core with radius $R \lesssim 20$ arcsec ($\lesssim 100$ kpc), and two smaller components at ≈ 0.9 arcmin (≈ 0.75 Mpc) and ≈ 3.8 arcmin (≈ 1.5 Mpc) from the center of the main overdensity. Numerical simulations predict that the galaxies in the central core of SPT2349–56 will eventually merge into the brightest cluster galaxy of the descendant structure (Rennehan et al. 2020). Similar arguments as those used for DRC return total values of $SFR \approx 8000 M_{\odot} \text{ yr}^{-1}$ and $M_{vir} \approx 10^{13} M_{\odot}$. Notably, the derived SFR density is a factor of ten larger than the most extreme values found in simulations at the same redshift (Hill et

al. 2020). A total gas mass of $M_{gas} \gtrsim 3 \times 10^{11} M_{\odot}$ is estimated from the luminosity of the carbon monoxide emission lines (Hill et al. 2020).

Using deep optical/near-IR observations, Apostolovski et al. (2023) and Rotermund et al. (2021) identified additional members of the SPT2349–56 core as LAEs (9 spectroscopically confirmed galaxies, although 6 of them are marked as “tentative” in that work) and LBGs (4 galaxies),¹ respectively. One of the tentative LAE is the counterpart of a sub-mm continuum detected galaxy with neither [C II] nor CO(4–3) emission in Hill et al. (2020), increasing the number of spectroscopically identified DSFGs in the structure to 22. Among the four LBGs in the protocluster core, two are likely counterparts of the DSFGs, named C2 and C17 (Hill et al. 2022), one has been found by Rotermund et al. (2021) to be a weak [C II] emitter not included in the Hill et al. (2020) sample, and one is the counterpart of a LAE. Thus, accounting for the few galaxies selected with multiple methods, the total number of individual and spectroscopically confirmed protocluster members is 38.

Chapman et al. (2023) detected bright radio emission ($L_{1.4\text{GHz,rest}} = (2.2 \pm 0.2) \times 10^{26} \text{ W Hz}^{-1}$) with spectral index $\alpha = -1.45 \pm 0.16$, where $F_{\nu} \propto \nu^{\alpha}$, from the inner region of the SPT2349–56 core, likely of AGN origin. The spatial resolution of the radio observations prevented the secure identification of the optical/IR counterpart, as a few protocluster members are consistent with being the host of the radio source, and none of them shows clear AGN features at other wavelengths. Still, mainly based on its large mass, Chapman et al. (2023) proposed that one such galaxies, referred to as C6 in our work following the Hill et al. (2020) naming convention, is the AGN host.

Due to their extreme properties, these two protoclusters, at similar redshift and identified via similar selection techniques, are unique testbeds to study the link between the availability of huge reservoirs of gas in high-redshift overdense environments, and SMBH growth in the galaxy members. Vito et al. (2020) used *Chandra* observations (140 ks) to investigate the AGN content of DRC, and identified two obscured AGN among 13 DSFGs. These are the two brightest, gas-rich, most strongly star-forming members of the protocluster, and are possibly in a merger phase, as derived from a high angular-resolution ALMA observation of one of them. In particular, the X-ray brightest AGN ($L_{2-10\text{keV}} = 2.7^{+8.9}_{-1.8} \times 10^{45} \text{ erg s}^{-1}$), namely DRC-2, has remarkable properties. It is an X-ray luminous as optically selected QSOs at all redshifts, but, in contrast to those, obscured by Compton-thick gas column densities, similar to, but even more extreme than, other populations of luminous obscured QSOs such as hot dust-obscured galaxies (e.g., Vito et al. 2018a).

In this work, we present new *Chandra* observations (200 ks) of SPT2349–56. Our goals are to probe the population of AGN and their physical properties in the extremely gas-rich and dense environment of SPT 2349–56, and to study more generally the effect of an overdense environment on SMBH growth in the early universe by comparing the AGN content in $z \approx 4$ gas-rich protoclusters with lower redshift structures and blank fields. Errors are reported at 68% confidence levels, while limits are given at 90% confidence levels. We refer to the 0.5 – 2 keV, 2 – 7 keV, and 0.5 – 7 keV energy ranges as the soft band, hard band, and full band, respectively. We assume solar metallicities and abun-

¹ We note that Rotermund et al. (2021) selected tens of LBG candidates over a large area (i.e., up to a radius of ≈ 2 arcmin) centered on SPT2349–56. Following Rotermund et al. (2021), we considered only the four galaxies found in the core region as potential members of the protocluster.

dances (Anders & Grevesse 1989), and adopt a flat cosmology with $H_0 = 67.7 \text{ km s}^{-1}$ and $\Omega_m = 0.307$ (Planck Collaboration et al. 2016).

2. Data analysis

In this section, we describe the reduction of the *Chandra* observations (§ 2.1) and the source detection procedure (§ 2.2).

2.1. Data reduction

We observed the SPT2349–56 protocluster with *Chandra* for a total of 200 ks, split among 9 pointings (see Tab. 1). The protocluster core was placed at the aimpoint of the ACIS-S detector, where the *Chandra* sensitivity is maximum, and all of the confirmed or candidate protocluster members are covered by the back-illuminated S3 chip. We reprocessed the *Chandra* observations with the *chandra_repro* script in CIAO 4.15 (Fruscione et al. 2006),² using CALDB v4.10.4,³ and setting *check_vf_pha=yes*, since observations were taken in Very Faint mode.

In order to correct the astrometry of the *Chandra* observations, we performed source detection on each pointing with the *wavdetect* script with a significance threshold of 10^{-6} , and then used the *wcs_match* and *wcs_update* tools to compute and apply the astrometric offsets with respect to a reference catalog. First, we applied a relative astrometric correction to each pointing using OBSID 25267 (i.e., the pointing with the longest exposure, see Tab. 1) as reference. Only point-sources with PSF size ≤ 3 arcsec and with ≥ 5 detected counts are considered. Then, we mapped the individual observations onto OBSID 25267 and merged all of the observations with the *reproject_obs* tool. We repeated the source-detection procedure on the merged dataset, but this time we matched the detected point sources to the GAIA DR3 catalog (Gaia Collaboration et al. 2023)⁴, in order to derive and apply the absolute astrometric correction factors. Only two X-ray point sources could be matched with GAIA objects on the ACIS-S3 chip, and the average spatial offset is 0.15 arcsec. This value can be considered the systematic spatial uncertainty of the X-ray dataset.

We obtained images and exposure maps with the *reproject_obs* tool, while we extracted spectra, response matrices, and ancillary files of the detected sources (see § 2.2) from individual pointings using the *specextract* tool and added them using the *mathpha*, *addrmf*, and *addarf* HEASOFT tools⁵, respectively, weighting by the individual exposure times. Ancillary files, which are used to derive fluxes and luminosities, were aperture corrected by setting via the *correctpsf* parameter in *specextract*.

2.2. Source detection and X-ray photometry

We assessed the detection of the SPT2349–56 protoclusters member candidates (Hill et al. 2020, 2022; Rotermund et al. 2021) in the soft, hard, and full bands using the binomial no-source probability (Weisskopf et al. 2007; Broos et al. 2007)

$$P_B(X \geq S) = \sum_{X=S}^N \frac{N!}{X!(N-X)!} p^X (1-p)^{N-X}, \quad (1)$$

² <http://cxc.harvard.edu/ciao/>

³ <http://cxc.harvard.edu/caldb/>

⁴ <https://www.cosmos.esa.int/web/gaia/dr3>

⁵ <https://heasarc.gsfc.nasa.gov/docs/software/heasoft/>

Table 1. Summary of the *Chandra* observations of SPT2349–56.

OBSID	Start date	T_{exp} [ks]
25267	2023-06-13	36
25704	2023-09-21	30
25705	2023-08-25	30
25706	2023-02-13	14
25707	2023-08-07	32
25708	2023-04-20	14
27712	2023-04-14	16
27804	2023-04-23	14
27904	2023-06-18	13

where S is the total number of counts in the source region in the considered energy band, B is the total number of counts in the background region, $N = S + B$, and $p = 1/(1 + BACKSCAL)$, with *BACKSCAL* being the ratio of the background and source region areas. The source counts are extracted from circular regions with $R = 1''$, whereas the background counts are measured from nearby regions free of evident X-ray sources. We checked that reasonably different choices of extraction regions returned consistent results. We defined $(1 - P_B) > 0.99$ as the detection threshold, a value often used to assess the X-ray detections of objects with pre-determined positions (Vito et al. 2019, 2020). Due to the small projected distances between the protocluster members, especially in the core of the structure, the extraction regions may overlap. In such cases, we assign each detected photon to the nearest galaxy, to avoid double counting.

Two protocluster members are detected significantly in X-rays: sources C1 ($1 - P_B > 0.999$ in both the hard and full bands) and C6 ($1 - P_B = 0.999$ and 0.994 in the hard and full band, respectively), which are among the spectroscopically identified DSFGs in the core region of SPT2349–56 (Hill et al. 2020). Fig. 1 and 2 present X-ray cutouts of these two sources.

Net counts, which are reported in Tab. 2, were computed in the same $R = 1''$ region used for the detection for C6, whereas we used a larger region with $R = 1.5''$ for C1, given its relatively bright emission. We also derived the hardness ratios $HR = \frac{(H-S)}{(H+S)}$, where S and H are the net counts in the soft and hard band, respectively, and the corresponding effective power-law photon indices, following the procedure of Vito et al. (2019), which are also reported in Tab. 2.

We visually inspected all of the remaining secure protocluster members or member candidates presented by Hill et al. (2020, 2022); Rotermund et al. (2021); Apostolovski et al. (2023). Three X-ray photons clustered on three contiguous pixels on top of the galaxy named LBG2 in Rotermund et al. (2021) are detected in the full band, suggesting that this object might be a sub-threshold X-ray source.

3. Results

In this section, we report the results obtained from the X-ray observations of SPT2349–56. In § 3.1 and § 3.2 we present the results of a spectral analysis of the two detected X-ray sources, C1 and C6, respectively. In § 3.3, we used the X-ray emission of these two galaxies together with the available optical-to-mm photometry to estimate the physical parameters of the AGN host galaxies via a spectral energy distribution (SED) fitting procedure. In § 3.4 we investigate possible evidence of low-rate SMBh accretion in the individually undetected galaxies of the structure via an X-ray stacking analysis.

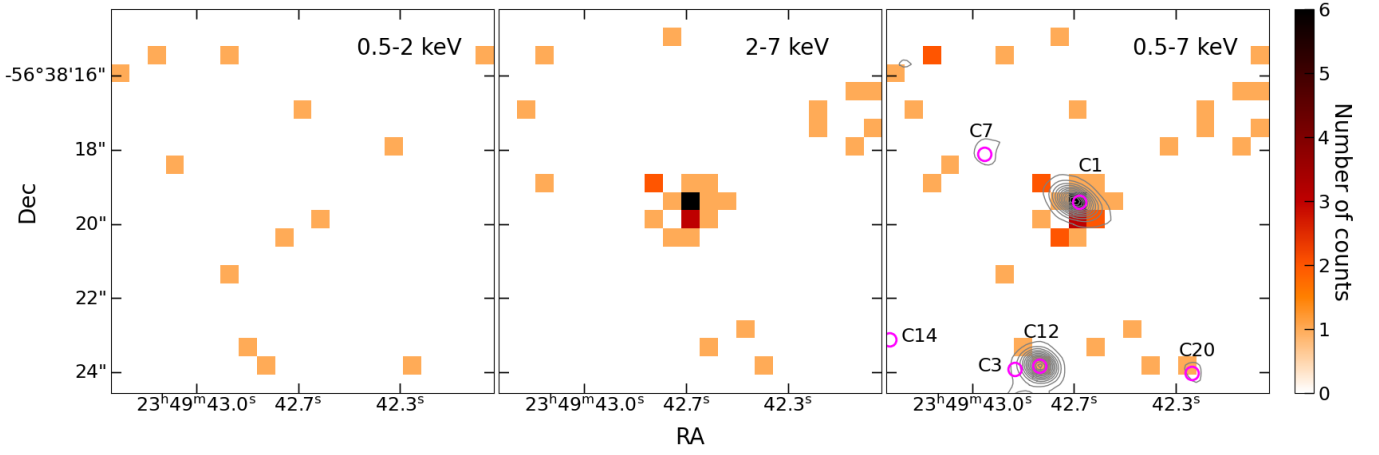


Fig. 1. From left to right, soft-band, hard-band, and full-band *Chandra* images ($10'' \times 10''$) of C1. In the right panel, we also plot the ALMA Band 7 continuum contours (in grey) and mark the positions (purple circles) of spectroscopically identified protocluster members. The contours have been derived from the reduced ALMA data of Hill et al. (2020) with beam size of $0.35'' \times 0.29''$, and start at 5σ with steps of 7σ .

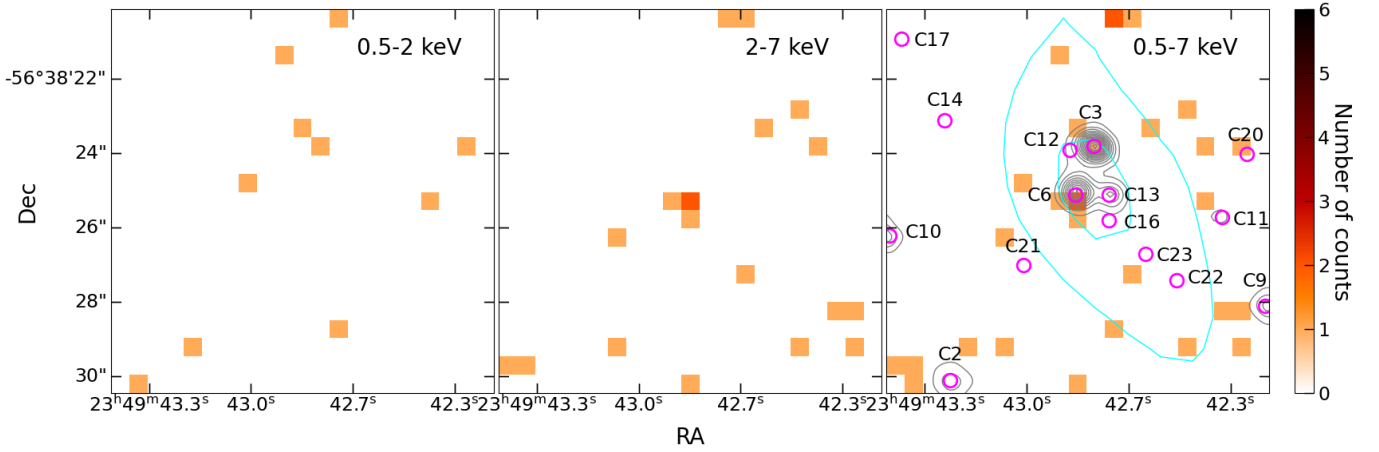


Fig. 2. Same as Fig 1, but for source C6. We added in cyan the ATCA 2.2 GHz contours (beam size of $7.7'' \times 4.2''$), starting at 3σ with steps of 3σ , obtained from the data reduced and presented by Chapman et al. (2023).

Table 2. Positions and X-ray photometric properties of the two members of the protocluster detected with *Chandra* (see § 2.2).

ID	RA J2000	DEC J2000	C_{sb}	C_{hb}	C_{fb}	HR	Γ_{eff}	N_H 10^{24} cm^{-2}	$F_{0.5-7 \text{ keV}}$ $10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$	$L_{2-10 \text{ keV}}$ $10^{45} \text{ erg s}^{-1}$
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
C1	23:49:42.65	-56:38:19.4	< 4.8	$19.1^{+4.8}_{-4.1}$	$20.5^{+5.0}_{-4.4}$	> 0.58	< 0.13	$2.4^{+2.3}_{-1.2}$	$2.4^{+4.9}_{-1.5}$	$2.2^{+4.5}_{-1.4}$
C6	23:49:42.84	-56:38:25.1	< 2.3	$3.6^{+2.4}_{-1.7}$	$3.3^{+2.4}_{-1.7}$	> 0.18	< 1.22	> 0.4	$0.3^{+0.2}_{-0.1}$	> 0.02

Notes. (1) ID, (2) RA, and (3) Dec from Hill et al. (2020) of the detected X-ray sources; (4) soft-band, (5) hard-band, and (6) full-band net counts; (7) hardness ratio and (8) corresponding effective photon index; (9) column density; (10) full-band flux; (11) intrinsic luminosity. The column density, flux, and luminosity of C1 are derived via a spectral analysis (Sec. 3.1), while these quantities are based on the hardness ratio for C6 (Sec. 3.2).

3.1. X-ray spectral analysis of C1

The relatively bright hard-band detection of C1 with no associated soft-band emission and the resulting flat effective photon index (Tab. 2) are strongly indicative of the presence of a large column density of gas (N_H) obscuring this high-redshift galaxy. We performed a basic spectral analysis with XSPEC v.12.13 (Ar-

naud 1996)⁶ to measure physical quantities, such as the N_H , the observed fluxes, and the intrinsic luminosity. Following the anal-

⁶ We used the *W*-statistic, which is suitable in case of background-subtracted spectra with low number of counts. See <https://heasarc.gsfc.nasa.gov/xanadu/xspec/manual/XSappendixStatistics.html> and Cash (1979).

ysis of DRC-2 (Vito et al. 2020), we used the MYTorus model (Murphy & Yaqoob 2009), accounting for the Galactic absorption (Kalberla et al. 2005), and fixing $\Gamma = 1.9$, the normalizations of the scattered and line components to that of the transmitted component, and the inclination angle $\Theta = 90$ degrees. Therefore, the only two parameters left free to vary were N_H and the intrinsic powerlaw normalization. Fig. 3 reports the observed and response-corrected spectrum and best-fitting model, highlighting the hardness of the source, as typically found for heavily obscured AGN.

Our best-fitting model returns $N_H = 2.4^{+2.3}_{-1.2} \times 10^{24} \text{ cm}^{-2}$, implying that C1 is a Compton-thick AGN. The observed flux $F_{0.5-7 \text{ keV}} = 2.4^{+4.9}_{-1.5} \times 10^{-15} \text{ erg cm}^{-2} \text{ s}^{-1}$ corresponds to an absorption-corrected, rest-frame luminosity $L_{2-10 \text{ keV}} = 2.2^{+4.5}_{-1.4} \times 10^{45} \text{ erg s}^{-1}$, that is, ≈ 1 dex larger than the break luminosity of the X-ray luminosity function at that redshift (e.g., Ueda et al. 2014; Aird et al. 2015; Vito et al. 2018b). In Fig. 4, we compare the column density and luminosity of C1 from the best-fitting model with other populations of AGN over wide redshift ranges. C1 has an X-ray luminosity typical of bright optically selected blue and red QSOs, which, however, are typically unobscured or, at most, obscured by Compton-thin column densities of gas (e.g. Just et al. 2007; Martocchia et al. 2017; Lansbury et al. 2020). C1 is even more obscured than hot dust-obscured galaxies (Hot DOGs; e.g., Stern et al. 2014; Vito et al. 2018a), which are often considered as representative of an extreme phase of galaxy and SMBH growth, while X-ray selected Compton-thick AGN and DSFGs have significantly lower luminosities. Intriguingly, C1 and DRC-2, both selected as luminous and obscured AGN in $z \approx 4$ gas-rich protoclusters, share the same position in Fig. 4. Only two other AGN with similar X-ray luminosities have been discovered in other protoclusters (Ivison et al. 2019; Tozzi et al. 2022b), but they are unobscured or, at most, mildly obscured, sources. In particular, Ivison et al. (2019) detected broad H α emission from the luminous AGN hosted in HATLAS J084933.4+021443, a DSFG in a $z = 2.41$ protocluster, which is surprising considering the expected high extinction in such a dust-rich galaxy.

The X-ray luminosity of C1 translates into a bolometric luminosity $L_{\text{bol}} \approx 8 \times 10^{46} \text{ erg s}^{-1}$ according to the bolometric correction of Duras et al. (2020). Assuming that the SMBH powering C1 is accreting at the Eddington limit, we can place a lower limit on its mass of $M_{\text{SMBH}} \approx 6.5 \times 10^8 M_{\odot}$ (but see the caveats raised by King 2024 about this approach). Therefore, either C1 is accreting at super-Eddington rate, or it has already accumulated a significant fraction of the SMBH mass characterizing AGN in the centers of local galaxy clusters. Similar conclusions were also drawn for DRC-2 by Vito et al. (2020).

We note that the spectrum of C1 can be fitted equally well with a pure reflection model by multiplying the intrinsic power-law continuum by a constant equal to zero. In this case, we obtain a similar value of N_H and a factor of ≈ 2 higher luminosity. We also tried leaving Γ free to vary, but the fit cannot constrain its value.

3.1.1. A note on the possible foreground nature of the X-ray emission

Rotermund et al. (2021) reported the spectroscopic identification of a foreground galaxy at $z = 2.54$ along the line of sight of C1. Based on considerations on the blue optical colors, magnitudes, and [O III] 5007Å emission-line width, they provide an upper limit on its stellar mass of $1.6 \times 10^9 M_{\odot}$. If

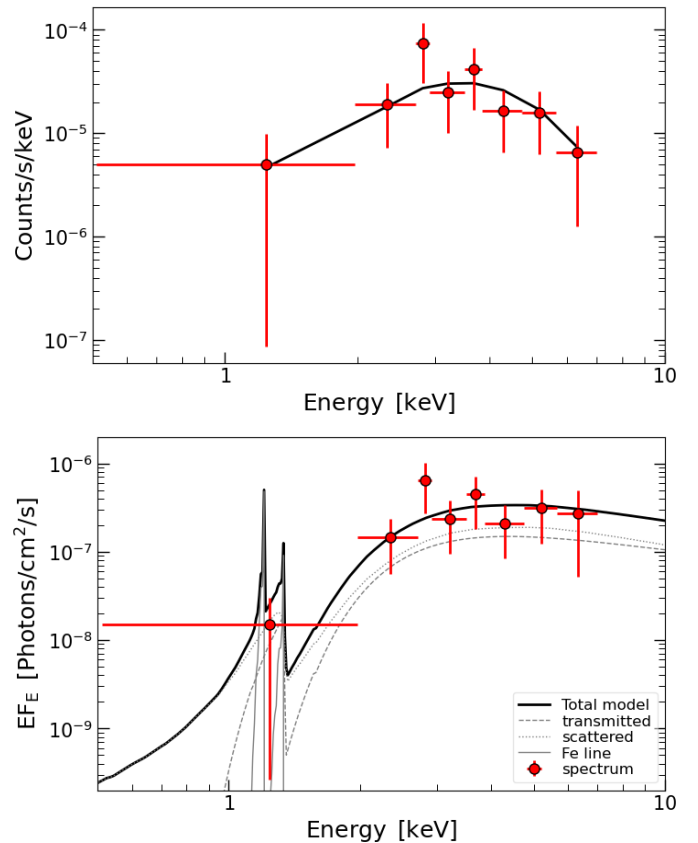


Fig. 3. Top panel: observed spectrum (red circles) and best-fitting MYTorus model (black line) of C1 (see § 3.1). Bottom panel: response-corrected spectrum and best-fitting model. We also show the individual additive components of the model with grey lines, as reported in the legend. In both panels, the spectrum is binned at 1σ for display purposes.

this were the host galaxy, the spectral analysis would return $N_H = 1.1^{+0.6}_{-0.5} \times 10^{24} \text{ cm}^{-2}$ and $L_{2-10 \text{ keV}} = 4.1^{+5.4}_{-2.2} \times 10^{44} \text{ erg s}^{-1}$. Given the well-known relation between AGN activity and stellar mass of the host galaxies (Xue et al. 2010; Lusso et al. 2011; Wang et al. 2017; Yang et al. 2017, 2018b, e.g.), it is highly unlikely that such a small object host a moderately luminous AGN. Moreover, its rest-frame UV spectrum present no indications of AGN activity (Rotermund et al. 2021). Therefore, in this paper we assume that the X-ray source is hosted by the DSFG at $z = 4.3$.

3.2. X-ray spectral properties of C6

Due to the low number of detected X-ray counts, we did not attempt to perform a spectral fit of C6. Instead, we assumed a simple $\Gamma = 1.9$ power-law as intrinsic spectrum, and estimated $N_H > 4.0 \times 10^{23} \text{ cm}^{-2}$ in order to reproduce the observed value of hardness ratio, accounting for the proper instrumental response and PSF correction by using the ancillary and response file extracted at the position of C6 (see Sec. 2.1). We used this model to estimate the observed flux and the intrinsic luminosity of C6 (Tab. 2). Based on these loose constraints, we conclude that C6 confidently is a heavily obscured AGN, although possibly not as extreme as C1.

The X-ray detection of C6 strongly supports that this galaxy is the host of the radio AGN discovered by Chapman et al. (2023) with . The ATCA 2.2 GHz contours presented by Chapman et al. (2023) are reported in Fig. 2 in cyan. The limit on the X-ray

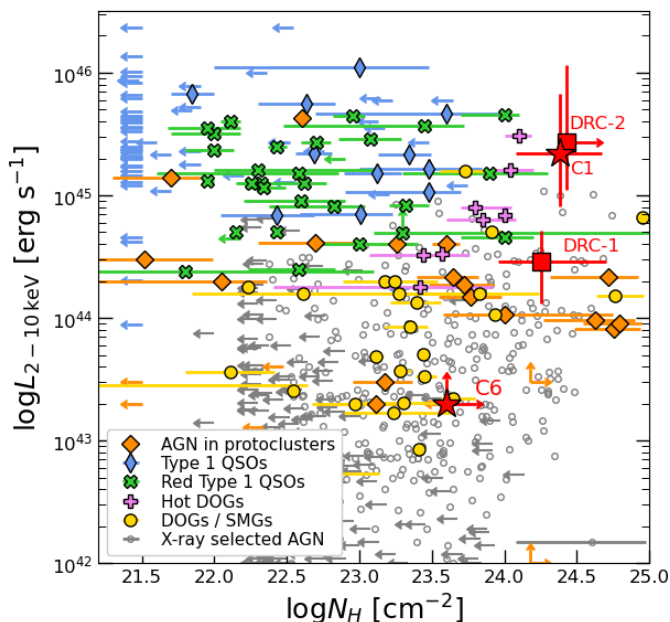


Fig. 4. X-ray luminosity versus column density for different populations of AGN: optically selected Type-1 QSOs at $z = 1.4 - 4.5$ (blue symbols; from Just et al. 2007; Martocchia et al. 2017), dust-reddened QSOs at $z = 0.4 - 3.2$ (green symbols; from Urrutia et al. 2005; Banerji et al. 2014; Mountrichas et al. 2017; Goulding et al. 2018; Lansbury et al. 2020), DSFGs at $z = 0.3 - 5.2$ (yellow symbols; from Wang et al. 2013; Corral et al. 2016; Zou et al. 2020), Hot DOGs at $z = 1.0 - 4.6$ (violet symbols; from Stern et al. 2014; Assef et al. 2016; Ricci et al. 2017; Vito et al. 2018a; Zappacosta et al. 2018), X-ray selected AGN in the Spiderweb and SSA protoclusters ($z = 2.2 - 3.2$, orange symbols, Ivison et al. 2019; Tozzi et al. 2022b; Monson et al. 2023), and X-ray selected AGN in the *Chandra* deep field-south at all redshifts (gray symbols, with median error bar showed in the bottom-right corner of the plot; from Li et al. 2019). The X-ray selected AGN in SPT2349–56 and DRC are plotted as red stars and squares, respectively. C1 and DRC-2 (Vito et al. 2020) have remarkably similar physical properties. Their X-ray luminosities are similar to those of luminous optically selected QSOs, but are obscured by gas column densities even thicker than Hot DOGs.

luminosity of C6 is consistent with the relation between radio and X-ray emission from radio-loud AGN (e.g., Fan & Bai 2016; D’Amato et al. 2020; Mazzolari et al. 2024).

3.3. SED fitting

We used CIGALE v2022.1 (e.g. Boquien et al. 2019; Yang et al. 2022) to fit the SEDs of the two X-ray selected AGN in SPT2349–56. Fig. 5 presents the best-fitting SED models, and the resulting physical parameters are reported in Tab. 3. CIGALE produces a SED model for every combination of the input parameters, convolves it with the filters corresponding to the utilized photometric points, and computes the likelihood $\exp(-\chi^2/2)$ of every model in a Bayesian framework. Then, it computes the marginalized probability distribution function of each physical parameter based on the likelihood of all models, and returns the mean and the standard deviation, which can be considered as the estimated value and associated uncertainty.

We used the optical-to-mm photometric points from Gemini-GMOS, FLAMINGOS-2, *HST*-WFC3, *Spitzer*-IRAC, and *ALMA* presented by Hill et al. (2020, 2022); Chapman et al. (2023). Upper limits at 3σ are adopted here for filters in which

the sources are not detected. We fitted the SEDs using simple stellar populations from Bruzual & Charlot (2003) and a delayed star-formation history with optional late burst and a Chabrier (2003) initial mass function. We also accounted for nebular emission, dust attenuation with a modified Calzetti et al. (2000) law, and dust thermal emission using the Draine et al. (2014) templates. In particular, CIGALE treats consistently dust attenuation and re-emission, thus conserving the total energy. A summary of the grid values used for SED fitting is reported in Appendix A.

Since we are fitting X-ray selected AGN SEDs, we also included the CIGALE AGN module based on Stalevski et al. (2016) and the X-ray module of Yang et al. (2020, 2022). The X-ray module is especially useful to constrain the AGN component in the SEDs. In fact, bright X-ray emission is largely dominated by the AGN flux, and CIGALE uses the well-known correlation between the AGN intrinsic luminosities at rest-frame UV and X-ray wavelengths (e.g., Just et al. 2007) as a prior to constrain the AGN intrinsic optical/UV luminosity. This procedure is particularly valuable in the presence of obscuration, as in this case the AGN optical/UV emission is strongly suppressed. The X-ray module includes the X-ray emission from binaries and hot gas that depends on the SFR and stellar mass, although it does not include shocks that a starburst can have. These contributions are expected to be negligible at the observed X-ray luminosities (e.g. Lehmer et al. 2016, 2019). The fitted X-ray fluxes used in the fitting procedure correspond to the X-ray models discussed in Sec. 3.1 and 3.2, and have been corrected for absorption, as required by CIGALE.

The optical photometry of C1 is contaminated by a spectroscopically identified foreground galaxy at $z = 2.54$ (Rotermund et al. 2021). Following Hill et al. (2022), we thus consider the optical fluxes as upper limits for source C1. The SED-fitting procedure for this object returns an AGN bolometric luminosity $L_{bol} = (1.9 \pm 0.7) \times 10^{47} \text{ erg s}^{-1}$, which is slightly higher than the value estimated in Sec. 3.1. The large uncertainties are probably due to the fact that only the X-ray point provides an anchor for the AGN component, as only upper limits are used for the optical photometry and the rest-frame mid-IR emission is not sampled by the available datasets. CIGALE returns a star-formation rate averaged over the last 100 Myr of $\text{SFR}_{100\text{Myr}} = 228 \pm 140 \text{ M}_{\odot} \text{ yr}^{-1}$. This value is significantly lower than the SFR reported by Hill et al. (2020), who estimated it from the FIR luminosity and thus on similar timescales, but did not account for the AGN component, which can contribute significantly to the total IR luminosity (e.g. Di Mascia et al. 2021; McKinney et al. 2021). The stellar mass $M_{*} = (3.5 \pm 2.8) \times 10^{10} \text{ M}_{\odot}$ is nominally lower than the estimate of Hill et al. (2022), but consistent within the large uncertainties.

Considering C6, we corrected the observed X-ray flux assuming the lower limit we could place on N_H in Sec. 3.2. Thus, the contribution of the AGN component to the best-fitting model for this source might have been underestimated, as higher intrinsic X-ray fluxes would correspond to the observed ones for higher values of N_H . We further assumed that the radio emission detected by Chapman et al. (2023) in the core region of SPT2349–56 is entirely associated with the X-ray AGN hosted in C6, and thus when fitting this source we considered also the radio fluxes and upper limits from ASKAP, MeerKAT, and ATCA observations presented in that work. This addition required us to employ the CIGALE radio module, that models non-thermal radio emission from star formation and AGN. The CIGALE fit requires a moderately luminous AGN ($L_{bol} = (3.3 \pm 0.2) \times 10^{45} \text{ erg s}^{-1}$), which is sub-dominant at all frequen-

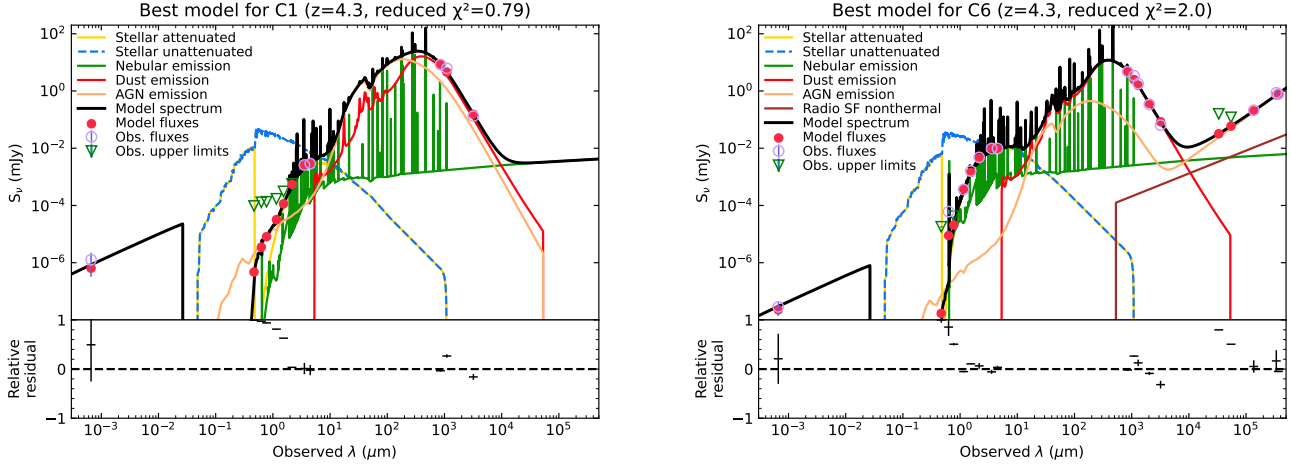


Fig. 5. Best-fitting models for C1 and C6 returned by the CIGALE fitting code. The optical-to-mm photometric points have been collected from Hill et al. (2020, 2022), while for C6 we added the radio measurements of Chapman et al. (2023). The absorption-corrected X-ray fluxes correspond to the X-ray models discussed in Sec. 3.1 and 3.2. The sub-mm/mm photometry of C1 is dominated by the AGN reprocessed emission. The AGN in C6 contributes more modestly at such wavelengths, but dominates the radio emission.

cies, except for the X-ray and radio bands. In particular, C6 is a radio-loud⁷ AGN, as also discussed by Chapman et al. (2023), with $R = 98 \pm 9$. We obtain $\text{SFR}_{100\text{Myr}} = 263 \pm 77 \text{ M}_{\odot} \text{ yr}^{-1}$ and $M_{*} = (3.6 \pm 1.3) \times 10^{10} \text{ M}_{\odot}$. Both of these values are significantly lower than those reported by Hill et al. (2020) and Hill et al. (2022). In particular, we note that the stellar-mass value that we find is more consistent with the dynamical mass of $\approx (2 - 5) \times 10^{10} \text{ M}_{\odot}$ estimated by Chapman et al. (2023).

The stellar masses of these two galaxies correspond roughly to the break mass of the galaxy stellar mass function at $z \approx 4$ (e.g. Song et al. 2016; Weaver et al. 2023). Comparing to the SED fitting results of Monson et al. (2023) on X-ray selected AGN in the SSA22 protocluster at $z = 3.09$, the AGN in SPT2349-56 on average are hosted in slightly less massive, but significantly more star-forming galaxies. In fact, Monson et al. (2023) found that most of the AGN in SSA22 are located below the main sequence, while few of them are consistent with it within the uncertainties on mass and SFR. Instead, according to our findings, both C1 and C6 are consistent with being main-sequence or even starbursting galaxies (e.g. Khusanova et al. 2021; Popesso et al. 2023). The AGN in SPT2349-56 might be in an earlier stage of galaxy evolution than those in SSA22, and are probably still in the peak phase of stellar and BH mass assembly. We also note that the SFRs of C1 and C6 averaged on a shorter timescale, i.e. 10 Myr, and the instantaneous SFRs returned by CIGALE are even higher than the values reported above (see Tab. 3). This is due to the SFHs of these galaxies favoring a recent and short burst of star formation.

3.4. X-ray stacking analysis

We performed an X-ray stacking analysis on the protocluster members to check for sub-threshold X-ray emission and constrain the average X-ray luminosity. We used the CIAO *wavdetect* and *dmfilth* tools to identify detected X-ray sources, and replace them with Poisson noise sampled from nearby regions. We

Table 3. Best-fitting physical parameters of C1 and C6 obtain via SED fitting.

	C1	C6
$\text{SFR}_{100\text{Myr}} [\text{M}_{\odot} \text{ yr}^{-1}]$	228 ± 141	263 ± 77
$\text{SFR}_{10\text{Myr}} [\text{M}_{\odot} \text{ yr}^{-1}]$	1447 ± 677	1105 ± 198
$\text{SFR}_{0\text{Myr}} [\text{M}_{\odot} \text{ yr}^{-1}]$	2127 ± 1292	1232 ± 242
$M_{*} [10^{10} \text{ M}_{\odot}]$	3.5 ± 2.8	3.5 ± 1.4
$L_{\text{bol,AGN}} [\text{erg s}^{-1}]$	$(1.9 \pm 0.7) \times 10^{47}$	$(3.3 \pm 0.2) \times 10^{45}$
Radio Loudness	—	98 ± 9

Notes. The rows report the best-fitting SFRs averaged over 100 Myr and 10 Myr, the instantaneous SFRs, the stellar masses, and the AGN bolometric luminosities.

then used the *dmcopy* tool to cut thumbnails of the X-ray images and exposure maps centered at the positions of the protocluster galaxies, excluding C1 and C6 that are detected individually. We summed them separately in the soft, hard, and full bands. We note that all of the protocluster members are within ≈ 3 arcmin from the average aim point of the observations, such that we do not expect a strong variation of the PSF at their positions. The sum of the counts in a $R = 2$ pixel (i.e., ≈ 1 arcsec) region around the centers of the stacked images divided by the average values of the stacked exposure maps in the same regions returns the stacked count rates in the three bands. We estimated the background level from nearby regions in the stacked images. We assessed detection significance and net-count numbers following the procedure in § 2.2.

We did not detect significant stacked X-ray emission from the protocluster members in any energy band. We repeated the procedure considering first all of the possible members (i.e., 97 objects), then only those identified spectroscopically (i.e., 36 objects), and finally only the DSFGs (i.e., 20 objects). Assuming obscured powerlaw emission with $\Gamma = 1.9$ and $N_H = 10^{24} \text{ cm}^{-2}$, the lack of significant stacked signal for the sample of DSFGs corresponds to an average intrinsic X-ray luminosity $< 2 \times 10^{43} \text{ erg s}^{-1}$. We estimate similar values for the other samples of stacked galaxies. We stress that the stacked exposure

⁷ The radio-loudness parameter is defined in CIGALE as $R = f_{\nu,5\text{GHz}}/f_{\nu,2500\text{\AA}}$, i.e. the ratio of the flux densities at rest-frame 5 GHz and 2500 Å (Kellermann et al. 1989; Yang et al. 2022).

times are in the range 5×10^6 s to 1.9×10^7 s, depending on the stacked sample. Based on these results, we did not find evidence for widespread low-rate SMBH accretion in the structure, although we cannot exclude that some of the protocluster members host faint AGN.

4. Discussion

In this section we discuss some implications of the results presented in § 3. In particular, in § 4.1 we estimate the contribution of the diffuse gas in the AGN host galaxies, i.e., the interstellar medium, to the nuclear obscuration. In § 4.2 we estimate the incidence of AGN among the protocluster member galaxies, and we compare it with other protoclusters and expectations in the field environment. In § 4.3 we quantify the enhancement of luminous AGN discovered in $z \approx 4$ gas-rich protocluster cores.

4.1. ISM obscuration

In the past decades, several works based on X-ray surveys established observationally that the fraction of obscured AGN increases significantly from the local universe up to at least $z \approx 4 - 5$ (e.g. La Franca et al. 2005; Treister & Urry 2006; Buchner et al. 2015; Lanzuisi et al. 2018; Vito et al. 2018b; Iwasawa et al. 2020; Peca et al. 2023). A possible explanation for that behaviour is that the contribution of the diffuse gas in the host galaxies (i.e., the interstellar medium; ISM) to the nuclear obscuration of AGN increases strongly from the local to the high-redshift universe, due to the larger gas content and smaller sizes characterizing galaxies at early cosmic epochs that almost automatically produce larger gas column densities. This scenario has been tested both observationally and via numerical simulations (e.g. Gilli et al. 2014; Circosta et al. 2019; Trebitsch et al. 2019; D’Amato et al. 2020; Ni et al. 2020; Lupi et al. 2022; Vito et al. 2022). In particular, Gilli et al. (2022) developed an analytical model for the ISM obscuration that accounts for the ISM clumpiness with a distribution of cloud sizes, masses, and densities, and showed that it predicts well the measured evolution of the obscured AGN fraction up to $z \approx 4$.

We tested whether the ISM in the two AGN discovered in SPT2349–56 can contribute significantly to their heavy nuclear obscuration, under simple geometrical assumptions. Following Sec. 4.1 of Gilli et al. (2022), we assumed a smooth distribution of the ISM and that the [C II] surface brightness traces the ISM density, which is distributed in a disk with an exponential profile. This is consistent with the ALMA high-resolution imaging of C1 presented by Hill et al. (2022), in which the galaxy appears as a nearly edge-on disk, and the [C II] light profile is best fitted with a Sersic model with index $n = 1.07 \pm 0.02$, that is, close to an exponential profile. Gilli et al. (2022) showed that, in that case, the gas column density for a line-of-sight inclined by an angle θ is

$$N_H(\theta) = \frac{r_0 \rho_0}{\sin \theta} (1 - e^{-\frac{h}{r_0} \tan \theta}) \quad (2)$$

where r_0 is the scale radius, which for a pure exponential disk can be expressed in terms of the half-light radius $r_{hl} = 1.678 r_0$, $\rho_0 = \frac{2.8 M_{gas}}{4\pi r_{hl}^2}$ is the central gas density, and $2h$ is the disk thickness. It is further assumed a typical thickness $h = 0.15 r_{hl}$ (Gilli et al. 2022, and references therein) and no vertical gradient for the gas density.

For C1, Hill et al. (2020) estimated a molecular gas mass of $M_{H_2} = 7.5 \times 10^{10} M_\odot$ from the CO(4–3) emission line, and Hill

et al. (2022) measured a [C II] half-light radius⁸ $r_{hl} = 2.91$ kpc. Following D’Amato et al. (2020), we consider $M_{gas} = \frac{6}{5} M_{H_2}$ to account for the mass of atomic gas in the galaxy. Therefore, assuming an edge-on configuration for C1, we obtain $N_H^{\theta=90^\circ} \approx 1.2 \times 10^{24} \text{ cm}^{-2}$, while assuming the average viewing angle for random inclinations we get $N_H^{\theta=57.3^\circ} \approx 4 \times 10^{23} \text{ cm}^{-2}$. Smaller inclinations would not be consistent with the nearly edge-on [C II] image of this galaxy, under the assumption of a disk geometry, which is consistent with recent ALMA observations of $4 < z < 5$ DSFGs (e.g. Rizzo et al. 2021). These order-of-magnitude values are close to the column density measured for C1 from our X-ray spectral analysis (Tab. 2), confirming that the gas distributed in the host galaxy can contribute significantly to the nuclear obscuration. We note that the use of the [C II] profile as a proxy of the molecular gas extension is conservative, as that transition traces also atomic gas, which is typically more extended than the dense molecular phase.

The molecular gas mass and [C II] half-light radius of C6 are $M_{H_2} = 3.7 \times 10^{10} M_\odot$ and $r_{hl} = 1.30$ kpc (Hill et al. 2020, 2022). Although the [C II] morphology is best fitted with a Sersic profile $n = 0.78$ (Hill et al. 2022), we considered an exponential profile for simplicity. C6 appears close to face-on in the [C II] imaging (Hill et al. 2022), and thus we use $\theta = 57.3$ and $\theta = 0$ as boundary values of its inclination, finding $N_H^{\theta=57.3^\circ} \approx 1.1 \times 10^{24} \text{ cm}^{-2}$ and $N_H^{\theta=0^\circ} \approx 7 \times 10^{23} \text{ cm}^{-2}$. Therefore, also for C6 the nuclear obscuration observed in the X-ray band can be due partly or totally to the gas in the host galaxy. In particular, we note that the ISM in C6 can reach higher column densities than C1 at a given inclination angle because of its compactness, that only high-resolution ALMA imaging could probe.

We stress that in this section we do not aim to measure the ISM contribution to the nuclear obscuration estimated via the X-ray observations, but rather to check whether such contribution can in principle be significant. One key assumption of the computations above is that the ISM is distributed smoothly in the galaxies, while it is known to be clumpy. Thus, depending on the geometry and physical properties (e.g., size and mass distribution) of the individual clouds, the ISM column density can be significantly different from, and possibly much lower than, the values estimated in this section. However, due to the large total gas masses estimated for C1 and C6 and depending on the assumed sizes and masses of molecular gas clouds (e.g., Miville-Deschênes et al. 2017; Dessauges-Zavadsky et al. 2019), the cloud filling factors in these galaxies can be as large as 100%. Therefore, the assumption of a smooth ISM is reasonable for the order-of-magnitude computations of this section.

4.2. Incidence of AGN activity in SPT2349–56

We detected two X-ray AGN out of 38 known members, implying an overall AGN fraction of $0.05^{+0.05}_{-0.03}$, where uncertainties are based on the Jeffrey Bayesian credible interval for binomial proportions (e.g. Brown et al. 2001). However, different populations of galaxies are intrinsically characterized by different AGN incidences, such that any comparison with other protoclusters or blank fields should take the specific galaxy selection into account (e.g. Vito et al. 2023). Therefore, in the following we consider separately galaxies selected as DSFGs, LAEs, and LBGs.

Two out of the 22 galaxies selected as DSFGs in SPT2349–56 are X-ray selected AGN, corresponding to an X-ray AGN

⁸ Since the [C II] emission traces the total gas, including the diffuse component, and is thus an upper limit on the extension of the molecular gas. In this sense, our estimate of N_H is conservative.

Table 4. Fractions of X-ray selected AGN among different galaxy populations in protoclusters, as described in Appendix B.

Protocluster	z	$f_{\text{AGN}}^{\text{DSFG}}$ spec.	$f_{\text{AGN}}^{\text{SED}}$		$f_{\text{AGN}}^{\text{LAE}}$		$f_{\text{AGN}}^{\text{HAE}}$	
			spec.	all	spec.	all	spec.	all
CL 0218.3–0510	1.62	—	—	$0.17^{+0.06}_{-0.05}$	—	—	—	$0.03^{+0.05}_{-0.02}$
Spiderweb	2.156	$0.14^{+0.17}_{-0.08}$	$0.50^{+0.13}_{-0.13}$	$0.14^{+0.03}_{-0.04}$	$0.19^{+0.09}_{-0.06}$	$0.09^{+0.05}_{-0.03}$	$0.17^{+0.05}_{-0.04}$	$0.13^{+0.04}_{-0.03}$
PHz G237.01+42.50	2.16	$0.50^{+0.22}_{-0.22}$	$0.10^{+0.07}_{-0.04}$	—	—	—	$0.17^{+0.20}_{-0.10}$	—
2QZ Cluster	2.23	—	—	—	—	—	—	$0.32^{+0.10}_{-0.09}$
HS 1700+643	2.30	< 0.36	$0.05^{+0.05}_{-0.02}$	—	$0.07^{+0.06}_{-0.03}$	—	$0.08^{+0.11}_{-0.05}$	—
USS 1558–003	2.53	< 0.19	—	—	—	—	$0.04^{+0.03}_{-0.02}$	$0.02^{+0.02}_{-0.01}$
SSA22	3.09	$0.50^{+0.14}_{-0.14}$	—	$0.22^{+0.09}_{-0.07}$	—	$0.03^{+0.02}_{-0.01}$	—	—
DRC	4.002	$0.15^{+0.12}_{-0.07}$	—	—	—	—	—	—
SPT2349–56	4.3	$0.09^{+0.04}_{-0.08}$	< 0.36	—	< 0.21	—	—	—

Notes. Uncertainties (upper limits) are at the 68% (90%) confidence level, and have been computed as the Jeffrey Bayesian Intervals for binomial proportions (e.g. Brown et al. 2001).

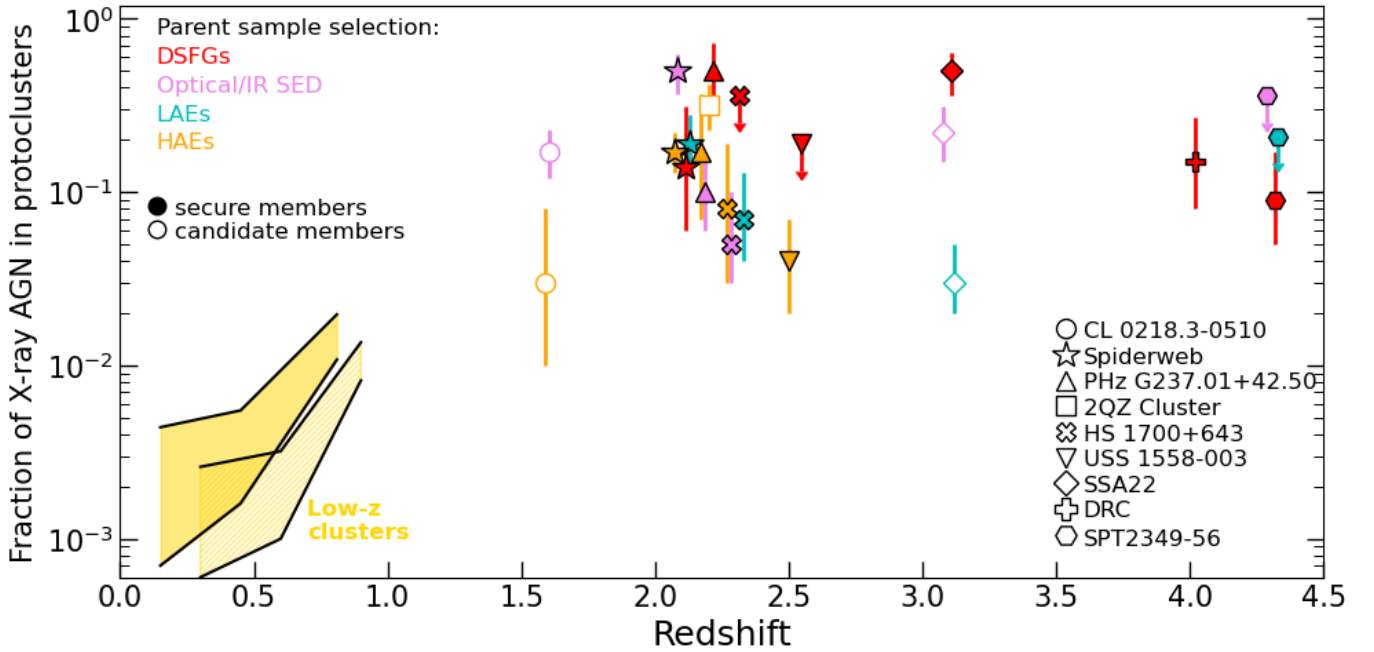


Fig. 6. Fraction of X-ray selected AGN in a sample of protoclusters as a function of redshift. The different symbol shapes and colors correspond to different structures and selection methods of the parent galaxy population, as marked in the figure. Different symbols for the same structure are slightly shifted in redshift for clarity. We consider the parent samples of spectroscopically confirmed protocluster members when available (filled symbols), otherwise we consider all member candidates (empty symbols). We refer to Sec. 4.2 and Appendix B for the computation of these values and the relevant citations. For comparison with low-redshift, virialized systems, the filled and hashed yellow stripes represent the X-ray AGN fractions in galaxy clusters presented by Martini et al. (2009) and Bufanda et al. (2017), respectively.

fraction in such a galaxy population of $0.09^{+0.08}_{-0.04}$. This value is remarkably close to the AGN fraction in DRC (Vito et al. 2020) down to similar FIR luminosity limits, adding the AGN content to other physical properties in common between the two protoclusters, thus suggesting that they have been caught during a similar phase of their galaxy and SMBH evolution. Since SPT2349–56 and DRC share a similar selection and are located at similar redshifts, we use both of them jointly to improve the number statistics and estimate the fraction of AGN among DSFGs in $z \approx 4$ gas-rich protoclusters by considering all of their DSFG members together (35, four of which are X-ray AGN), finding an X-ray AGN fraction of $0.11^{+0.06}_{-0.04}$.

These results are consistent with the typical ranges found for DSFGs (e.g. Alexander et al. 2005; Georgantopoulos et al. 2011; Wang et al. 2013; Shanks et al. 2021). However, such samples have typically lower redshift (i.e., $z = 2 - 3$, where the cosmic

AGN activity peaks; e.g., Aird et al. 2015) than SPT2349–56, such that a direct comparison may be misleading. This is due to the quite strong evolution of the cosmic AGN and DSFG populations, which is also dependent on the considered luminosity regimes (e.g. Ueda et al. 2014; Aird et al. 2015; Traina et al. 2024). For example, if the space density of the X-ray selected AGN decreases from $z = 2$ to $z = 4$ more strongly than the density of DSFGs, as it appears from observational works, it will cause generally a decreasing AGN fraction at increasing redshift. In this case, observing similar AGN fractions at $z = 4$ as at $z = 2$ would suggest stronger positive environmental effects at high redshift, but this is currently quite speculative.

In order to factor out the cosmic evolution of the AGN population, the comparison should be made with a sample of DSFGs at similar redshift as SPT2349–56. We collected a total of 54 sub-mm-selected galaxies in the E-CDFS, COSMOS, and UDS

fields from da Cunha et al. (2015), Scoville et al. (2016), and Dudzevičiūtė et al. (2020), respectively, with photometric redshift $3.5 < z < 4.5$ and overlapping with the available X-ray coverage in those fields (Civano et al. 2016; Xue et al. 2016; Kocovski et al. 2018), with sensitivities similar to, or deeper than, the *Chandra* observations covering SPT2349–56 and DRC. We found no match with the X-ray catalogs, corresponding to an observed AGN fraction among field DSFGs < 0.04 . To test quantitatively if the AGN fraction in $z \approx 4$ gas-rich protoclusters is consistent with the field value, we ran the Boschloo’s exact test for a 2x2 contingency table. The null hypothesis is that the intrinsic AGN fractions in protoclusters and in the field are equal, with the observed difference due only to statistical fluctuations. Considering SPT2349–56 only, the test returns a probability of $\approx 5\%$ to obtain only by chance a case at least as extreme as the observed ones (i.e., no AGN out of 54 DSFGs in the field, and ≥ 2 AGN out of 22 DSFGs in SPT2349–56). Considering SPT2349–56 and DRC together (i.e., ≥ 4 AGN out of a total of 35 DSFGs), such probability decreases to $\approx 1\%$. This comparison points toward a higher AGN incidence among DSFGs in $z \approx 4$ protoclusters than in the field at similar redshift, although the AGN content of additional and similar structures should be investigated to obtain a definitive proof. Moreover, we caution that the reference samples have been selected differently from observations performed at different sub-mm/mm frequencies and with different depths, and thus might have different flux, luminosity, and mass distributions from the DSFGs population in protoclusters.

Considering the entire sample of 30 protocluster members spectroscopically identified with ALMA via detection of the [C II] and CO(4–3) emission lines, thus including both DSFGs and sources undetected in sub-mm/mm continuum, the AGN fraction decreases slightly to $0.07^{+0.06}_{-0.03}$. None of the 8 spectroscopically confirmed Ly α emitter galaxies (LAEs) discovered by Apostolovski et al. (2023) in the SPT2349–56 structure is significantly detected in the X-rays, resulting in an upper limit on AGN fraction among that galaxy population of < 0.21 , consistent with results from blank fields (e.g. Lehmer et al. 2009b; Digby-North et al. 2010; Zheng et al. 2010). We obtain no X-ray detection also of the 4 LBGs in the SPT2349–56 core (Rotermund et al. 2021), implying an AGN fraction of < 0.36 .

In Fig. 6, we compare the X-ray AGN fractions of SPT2349–56 with those of a collection of other protoclusters covered with sensitive X-ray observations, as computed in Appendix B and reported in Tab. 4. The AGN incidence among DSFGs in SPT2349–56 is consistent with the results for other $z > 2$ protoclusters, although a couple of structures have significantly higher AGN fractions. Instead, the AGN fraction drops dramatically in virialized clusters at lower redshift. This behavior might be connected to the virialization of the structures or strong AGN feedback hindering the infall of large amounts of cold gas into galaxies, and thus the triggering of luminous nuclear activity. We note that the points in Fig. 6 are observed fractions, and we refer to Appendix B for a discussion of the caveats. A more in-depth investigation of the possible cosmic evolution of the AGN incidence in protoclusters would require taking several effects into account, among which are the different sensitivities of the multi-wavelength observations, the dependence of SMBH accretion on the host-galaxy stellar mass, and the intrinsic cosmic evolution of the AGN population (e.g., Aird et al. 2015, 2018; Yang et al. 2017, 2018b; Zou et al. 2024), which can be controlled for by comparing with the field AGN incidence. Such analysis require, among other things, a proper assessment of the multi-band observation sensitivities across multiple extragalactic fields and of the different specific selections applied on such fields, as well as

a consistent SED fitting analysis of the resulting large samples of SMGs. These tasks are beyond the scope of this paper, and we reserve it for a dedicated future work.

4.3. Enhancement of fast SMBH growth in $z \approx 4$ overdensities of DSFGs

The obscuration level and luminosity of C1 are remarkably similar to those of DRC-2 (Fig. 4). To our knowledge, AGN with similar X-ray luminosities in protocluster environments have been detected only in two structures at $z = 2.16 - 2.41$ by (Iverson et al. 2019; Tozzi et al. 2022a, see Fig. 4), and those are unobscured or at most mildly obscured objects. The detection of a luminous, Compton-thick AGN in the core regions of the only two $z \approx 4$ protoclusters selected as overdensities of dusty star-forming galaxies and covered by sensitive X-ray observations suggests that gas-rich and dense regions of the Universe at those epochs may promote the triggering of extremely fast SMBH growth in heavily obscured conditions.

To estimate the level of enhancement of luminous AGN in SPT2349–56 and DRC, we compare their space density with that of AGN in the field environment with similar luminosity and redshift. We assume that the two protoclusters are enclosed in spherical volumes with radii equal to the projected distances between the observed centers of the structures and the farthest spectroscopically confirmed members, which are ≈ 8.8 comoving Mpc (cMpc) and ≈ 3.8 cMpc, respectively (Iverson et al. 2020; Hill et al. 2022). Accounting for the uncertainties on their estimated luminosities, we consider the two luminous AGN in SPT2349–56 and DRC as representative of the AGN population in the range $\log \frac{L_X}{\text{erg s}^{-1}} = 45 - 46$ in $z \approx 4$ gas-rich protoclusters. The space density of such a population is then two divided by the sum of the volumes computed above; i.e., $\Phi_{\text{AGN}}^{\text{prot}} = 6.4^{+8.5}_{-4.2} \times 10^{-4} \text{ cMpc}^{-3} \text{ dex}^{-1}$, where the uncertainties account for the statistical errors on the number of objects (Gehrels 1986). The space density of $\log \frac{L_X}{\text{erg s}^{-1}} = 45 - 46$ at $z = 4.15$ in the field environment is $\Phi_{\text{AGN}}^{\text{field}} \approx 5 \times 10^{-8} \text{ cMpc}^{-3} \text{ dex}^{-1}$ (Fig. 7; e.g., Gilli et al. 2007; Ueda et al. 2014; Aird et al. 2015; Vito et al. 2018b), corresponding to an expected number of 1.5×10^{-4} luminous AGN in the considered volume. The Poisson probability of instead finding two AGN with such luminosity by chance only is negligible. This simple computation suggests that the triggering of luminous AGN in gas-rich protocluster environments at $z \approx 4$ is enhanced by about four orders of magnitude with respect to the field environment at similar redshift with high significance.

The most uncertain quantities that enter in the estimate are the volumes of the two protoclusters. As a second and more conservative estimate, we assumed that these structures extend up to $R = 28$ cMpc. According to Muldrew et al. (2015), this is the average radius that encloses 90% of the stellar mass of protoclusters at $z = 4$ that form massive galaxy clusters at $z = 0$. In this case, we estimate $\Phi_{\text{AGN}}^{\text{prot}} = 1.0^{+1.4}_{-0.6} \times 10^{-5} \text{ cMpc}^{-3} \text{ dex}^{-1}$, which is still > 2 dex higher than the field value. The Poisson probability of finding two luminous AGN while expecting the number predicted by the field environment is negligible also in this case.

As a comparison, Tozzi et al. (2022b) found for the Spiderweb protocluster at $z \approx 2$ an AGN enhancement of a factor of tens, depending on the AGN luminosity. This lower value might be due to the fact that $z \approx 2$ protoclusters have often already consumed most of their gas, as suggested by the large fraction of passively evolving galaxies in the Spiderweb structure (Shimakawa et al. 2024), and to the overall cosmic evolution of the AGN space density, that peaks close to that epoch.

The much higher space density of luminous AGN in SPT2349-56 and DRC than in the field at similar redshift can in principle be driven by the space density of the underlying galaxy population, which in protoclusters is enhanced with respect to the field by definition. For instance, Miller et al. (2018) estimated a SMG overdensity in SPT2349-56 of a factor > 1000 . However, they considered only the central $R = 130$ kpc region, where their selection is complete at $S_{1.1\text{ mm}} > 0.5 \mu\text{Jy}$. In that same region we detected C1, i.e., $1.0^{+2.3}_{-0.8}$ X-ray luminous AGN, which is at least several million times larger than the expected number of 4×10^{-8} similar objects in the field, assuming a spherical volume with that radius. This enhancement largely exceeds and thus is hardly driven by the overdensity level of the underlying galaxy population in the considered protoclusters. We stress that C1 is not an extreme galaxy in terms of stellar mass (see § 3.3), and thus the comparison with the overdensity estimated by Miller et al. (2018) for the entire population of DSFGs in the structure is fair. This result is only in apparent contrast with the lower significance found for the enhanced AGN fraction in protoclusters with respect to the field environment discussed in § 4.2, since in this section we focused on the high-luminosity regime only, and compared space densities rather than AGN fractions. Given the shape of the X-ray luminosity function (Fig. 7), such luminous AGN are extremely rare in the field, and finding two of them in small volumes corresponds to a large enhancement factor. In fact, the small enhancement of the overall AGN fraction coupled with the large enhancement of the space density of high-luminosity AGN suggests that the AGN X-ray luminosity function in these protoclusters is flatter than in the field, as also found by Tozzi et al. (2022b) for the Spiderweb protocluster. These computations suggest that gas-rich overdensities of DSFGs at $z \approx 4$ promote extremely luminous and obscured AGN activity. A larger sample of similar protoclusters is needed to confirm it with better statistics.

We note that Yang et al. (2018a) investigated the possible dependence of the average SMBH accretion rate density in samples of galaxies in the COSMOS field as a function of their environments up to 10 Mpc, finding no significant difference in the SMBH accretion power between overdense and field regions at a fixed stellar mass. However, their analysis is limited to $z < 3$ and the environments that they probed are not as dense as SPT2349-56.

The luminous AGN in the $z \approx 4$ protocluster cores represent the phase of fast SMBH growth required to explain the masses of SMBHs in the centers of low-redshift galaxy clusters. Such AGN are likely caught just before the "blow-out" phase, when AGN feedback clears the line of sight of most of the obscuring material (e.g. Ivison et al. 2019), and eventually hinders star formation and further SMBH growth. X-ray observations of a larger sample of similar environments are required to investigate the AGN population in such structures and prove this scenario securely. The specific selection that led to the identification of SPT2349-56 and DRC appears to be key to identifying high-redshift structures hosting such luminous AGN. In fact, other protoclusters selected as overdensities of Lyman-break galaxies via optical observations do not present strong evidence for the presence of such an AGN population, although they host an unusual large number of rest-frame UV bright galaxies (Toshikawa et al. 2024).

5. Summary and conclusions

We presented new *Chandra* observations of the $z = 4.3$ SPT2349-56 protocluster, which was identified as an extreme

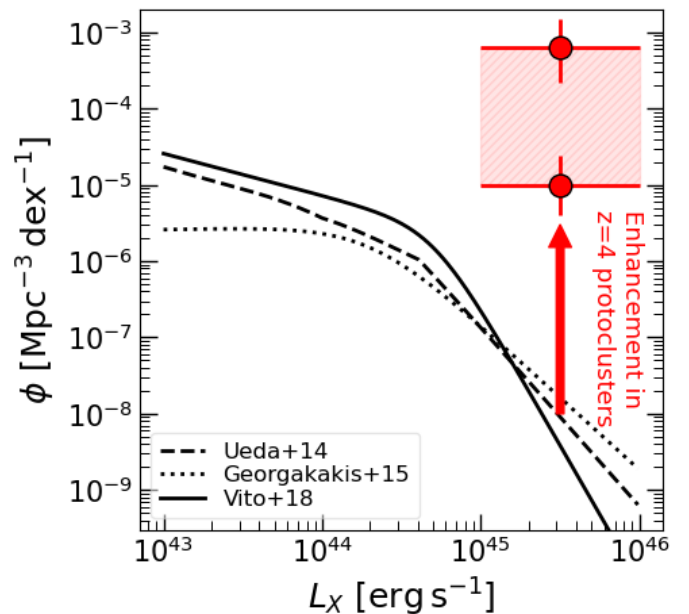


Fig. 7. Space density of luminous ($\log \frac{L_X}{\text{erg s}^{-1}} = 45 - 46$) and obscured AGN in gas-rich protocluster cores at $z = 4.0 - 4.3$ (red circles) computed under two assumptions for the volumes of the structures (see Sec. 4.3), compared with the predictions of AGN X-ray luminosity functions at $z = 4.15$ in blank fields (Ueda et al. 2014; Georgakakis et al. 2015; Vito et al. 2018b). Gas-rich overdense environments at high redshift enhance the triggering of luminous AGN by 3–5 orders of magnitude. This is likely a physical effect, as it appears not to be simply driven by the large number of galaxies in the structures (see § 4.3).

overdensity of DSFGs (Miller et al. 2018; Hill et al. 2020; Rotermund et al. 2021; Hill et al. 2022; Chapman et al. 2023). We summarize here our main results.

- We identified two X-ray detected AGN among the SPT2349-56 member galaxies, namely C1 and C6, which are among the most gas-rich galaxies in the system (Hill et al. 2020). We did not detect significant emission by stacking the X-ray data of the individually undetected galaxies, implying an average X-ray luminosity $< 2 \times 10^{43} \text{ erg s}^{-1}$. See § 2 and § 3.4.
- C1 is an extremely luminous ($L_{2-10\text{ keV}} = 2 \times 10^{45} \text{ erg s}^{-1}$), Compton-thick ($N_H = 2 \times 10^{24} \text{ cm}^{-2}$) AGN. The X-ray luminosity translates into a bolometric power $\approx 10^{47} \text{ erg s}^{-1}$, which is also confirmed via SED fitting. Assuming that the SMBH accretion is capped at the Eddington limit, we place a lower limit on its mass of $\approx 7 \times 10^8 M_\odot$. Both its luminosity and obscuration level are similar to those of another AGN previously detected in the central region of DRC, a similar protocluster at $z = 4$ (Vito et al. 2020). Both of these AGN might have already accreted a significant fraction of the typical mass of SMBHs in the centers of local clusters at much later (> 10 Gyr) cosmic times. See § 3.1.
- Due to the low number of detected X-ray photons, we can only place lower limits on the luminosity ($L_{2-10\text{ keV}} > 2 \times 10^{43} \text{ erg s}^{-1}$) and column density ($N_H = 4 \times 10^{23} \text{ cm}^{-2}$) of C6, which is also a radio-loud AGN. See § 3.2.
- Both C1 and C6 are hosted in galaxies with stellar masses $\approx 3 \times 10^{10} M_\odot$, which is close the break value of the galaxy stellar mass function at $z = 4.3$, and have star formation rates consistent with, or in excess of, the expectation of the main sequence of star-forming galaxies at that redshift. See § 3.3.

- Under simple, but reasonable, assumptions on the geometries of the host galaxies, we conclude that the ISM can in principle contribute significantly to the observed nuclear obscuration of both AGN, in agreement with previous works on high-redshift AGN, although that contribution can be lower in the case of highly clumpy medium. See § 4.1.
- The X-ray AGN fraction among DSFGs in SPT2349–56 is about 10%, consistent with other $z > 2$ protoclusters, and in particular with DRC. The fraction is higher than the X-ray AGN incidence in DSFGs in the field environment at $z \approx 4$. We could place only loose upper limits on the AGN incidence in LBGs and LAEs in SPT2349–56, due to their small number. See § 4.2.
- Both SPT2349–56 and DRC, which share similar selection and physical properties, host highly luminous Compton-thick AGN, indicating the existence of a tight link between vigorous phases of star formation, fed by the availability of huge gas reservoirs, and high SMBH accretion rates in the densest environments at high redshift. Such luminous AGN probably represent the period of fast SMBH growth required to explain the presence of $10^9 - 10^{10} M_\odot$ SMBHs in the central galaxies of local clusters. Under different assumptions about the volumes of these structures and comparing with the predictions of the X-ray luminosity function $z = 4$, we suggest that gas-rich and dense protoclusters at $z \approx 4$ enhance the triggering of extremely fast SMBH accretion by a factor of 3–5 dex with respect to the field environment. This factor exceeds the galaxy overdensity level of the protoclusters, and thus is probably not merely driven by the large number of galaxies in the structures. Further X-ray observations of similar structures are needed to confirm this result. See § 4.3.

Our results demonstrate that sensitive X-ray observations with high angular resolution are crucial to identify AGN in high-redshift protoclusters, which are characterized by large amounts of dust and gas, and thus heavy nuclear obscuration. In the next years, *Chandra* will play a leading role in this respect, by increasing the samples of high-redshift gas-rich protoclusters with the deep X-ray coverage required to investigate their AGN content. Future X-ray missions will then be crucial to obtain a complete view of the relation between overdense environments and SMBH growth at high redshift (e.g., Vito et al. 2023).

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Appendix A: Grid of parameters value used for the SED fitting

Tab. A.1 lists the parameters and values used for the SED fitting procedure with CIGALE, as described in Sec. 3.3.

Appendix B: AGN fraction in protoclusters

We report here the computations used to estimate the X-ray selected AGN fractions f_{AGN} among members of a few protoclusters for which dedicated X-ray observations have been obtained and published (Fig. 6). We consider different galaxy populations, based on their selections: sub-mm selected dusty star-forming galaxies (DSFGs), objects selected on the basis of their optical/IR SED (e.g., Lyman-break or BX/MD galaxies), Ly α emitters (LAEs), and H α emitters (HAEs). We also consider separately the secure members of a protocluster (i.e., those identified spectroscopically) and all possible members, including candidate members, except for the DSFG population, for which only spectroscopically identified galaxies are considered. The resulting AGN fractions are summarized in Tab. 4.

The intention of this collection is to provide an easy-to-access list of values of AGN fractions in the literature, for first-order comparisons. Several caveats should be considered when using these values, some of them are discussed here. First, we consider these structures as *bona fide* protoclusters, based on the definitions provided by the referenced papers. Second, the selection methods (e.g., definitions of colors, thresholds, sampled rest-frame wavelengths, etc.) and sensitivities of the multi-wavelength observations, including the X-ray coverage used to identify AGN, are not homogeneous among these objects. Third, the fractions have been computed simply considering the number of X-ray detected AGN divided by the number of known galaxies belonging to a given class. A more reliable and complete procedure would take into account, for instance, the varying sensitivities of the X-ray and multi-wavelength observations on a field, and control for the stellar mass distribution of the parent populations of galaxies. A few of the works mentioned below did take these precautions into account for individual protoclusters, but extending such procedures homogeneously to the entire protocluster sample considered here is beyond the scope of this paper. Finally, we rely on the published X-ray-to-multiwavelength counterpart matching, unless otherwise noted. The matching procedures generally vary among different works. As a consequence, the following list is far from being complete and homogeneous.

CL 0218.3-0510 ($z = 1.62$): Krishnan et al. (2017) considered 46 massive (i.e., $M_* > 10^{10} M_\odot$) galaxies identified as robust protocluster member candidates via optical/IR SED fitting by Hatch et al. (2016), and found that 8 of them are detected in the X-ray band, corresponding to an AGN fraction of $f_{\text{AGN}}^{\text{SED}} = 0.17^{+0.06}_{-0.05}$. SMGs have been identified as potential protocluster members (e.g., Smail et al. 2014; Chen et al. 2016), but spectroscopic confirmation is not available to our knowledge, so we do not consider this population. Tran et al. (2015) reported that 1 out of 33 H α emitters associated with the protocluster is X-ray detected, corresponding to $f_{\text{AGN}}^{\text{HAE}} = 0.03^{+0.05}_{-0.02}$.

Spiderweb protocluster ($z = 2.156$). Tozzi et al. (2022b) studied the X-ray selected AGN in this structure using deep (700 ks) *Chandra* observations. They reported the detection of 14 protocluster members (13 of which identified spectroscopically), corresponding to an AGN fraction of $f_{\text{AGN}} = 0.25 \pm 0.04$ (including systematic uncertainties) among spectroscopically identified, massive ($\log \frac{M_*}{M_\odot} > 10.5$) protocluster members. Here, we

instead report the X-ray AGN fractions corresponding to the different galaxy selection methods, considering no threshold in stellar mass. The galaxy parent populations are collected from the same catalogs used by (Tozzi et al. 2022b, see their Tab. 2), to which we added the spectroscopic sample recently presented by Pérez-Martínez et al. (2023a). We obtained AGN fractions of $f_{\text{AGN}}^{\text{DSFG}} = 0.14^{+0.17}_{-0.08}$, $f_{\text{AGN}}^{\text{LAE}} = 0.09^{+0.05}_{-0.03}$, $f_{\text{AGN}}^{\text{HAE}} = 0.13^{+0.04}_{-0.03}$, and $f_{\text{AGN}}^{\text{SED}} = 0.14^{+0.05}_{-0.04}$. All DSFGs are spectroscopically identified, while considering only spectroscopically confirmed objects for the other populations we obtained $f_{\text{AGN}}^{\text{LAE}} = 0.19^{+0.09}_{-0.06}$, $f_{\text{AGN}}^{\text{HAE}} = 0.17^{+0.05}_{-0.04}$, and $f_{\text{AGN}}^{\text{SED}} = 0.50^{+0.13}_{-0.13}$. We note that Jin+21 selected 46 protocluster members as CO-emitters. Among this population we found $f_{\text{AGN}}^{\text{CO}} = 0.09^{+0.05}_{-0.03}$.

PHz G237.01+42.50 ($z = 2.16$). Polletta et al. (2021) reported the identification of this protocluster with 31 spectroscopic members detected in optical/IR observations. Among them, three are known X-ray AGN, corresponding to $f_{\text{AGN}}^{\text{SED}} = 0.10^{+0.07}_{-0.04}$. We note that Polletta et al. (2021) included also an X-ray undetected broad emission-line AGN in their computation of the AGN fraction in the structure, while here we limited to X-ray selected AGN. Among the 31 members of the protocluster, 6 were also selected as HAEs, one of which is an X-ray AGN, i.e., $f_{\text{AGN}}^{\text{HAE}} = 0.17^{+0.20}_{-0.10}$. Finally, 2 out of the 4 DSFGs selected with Herschel/SPIRE among the members are X-ray AGN, corresponding to $f_{\text{AGN}}^{\text{DSFG}} = 0.50^{+0.22}_{-0.22}$.

2QZ Cluster ($z = 2.23$). Lehmer et al. (2013) presented the *Chandra* observations of this structure. Seven out of 22 HAEs are X-ray detected (i.e., $f_{\text{AGN}}^{\text{HAE}} = 0.32^{+0.10}_{-0.09}$), including the four optically selected AGN that were used as signposts of the protocluster.

QSO HS 1700+643 ($z = 2.30$). Among the spectroscopically confirmed members of the protocluster which do not reside in regions affected by high X-ray background due to the presence of foreground clusters, Digby-North et al. (2010) reported the X-ray detection of 2 out of 29 LAEs ($f_{\text{AGN}}^{\text{LAE}} = 0.07^{+0.06}_{-0.03}$), 1 out of 12 HAEs ($f_{\text{AGN}}^{\text{HAE}} = 0.08^{+0.11}_{-0.05}$), and 2 out of 39 BX/MD selected galaxies ($f_{\text{AGN}}^{\text{SED}} = 0.05^{+0.05}_{-0.02}$). We note that these fraction are different from those reported by Digby-North et al. (2010), because they considered also objects not confirmed spectroscopically and applied corrections for the X-ray sensitivity over the field. Lacaille et al. (2019) identified spectroscopically four DSFGs as members of the protocluster, and none of them are detected in the X-rays, corresponding to $f_{\text{AGN}}^{\text{DSFG}} < 0.36$.

USS 1558-003 ($z = 2.53$). Combining the catalogs of Shimakawa et al. (2018), Aoyama et al. (2022), and Pérez-Martínez et al. (2023b), 57 HAEs are secure members of this structure, either because of spectroscopic identification or matching detection in narrow-band imaging targeting the Ly α emission line (but we note that the catalog of LAEs has not been published to our knowledge). Two of them are detected in the X-rays (Macuga et al. 2019); i.e., $f_{\text{AGN}}^{\text{HAE}} = 0.04^{+0.03}_{-0.02}$. Considering also member candidates, the fraction is $f_{\text{AGN}}^{\text{HAE}} = 0.02^{+0.02}_{-0.01}$. Nine DSFGs have been spectroscopically identified in the structure Aoyama et al. (2022), and all of them are also selected as HAEs. Matching their positions with the catalog of Macuga et al. (2019), we found no X-ray detection; i.e., $f_{\text{AGN}}^{\text{DSFG}} < 0.19$.

SSA22 ($z = 3.09$). We base the computation of the X-ray AGN fraction in this protocluster on the work of (Lehmer et al. 2009b, see also Monson et al. 2023), who reported X-ray detection of six out of 27 member candidates selected as LBGs, i.e., $f_{\text{AGN}}^{\text{SED}} = 0.22^{+0.09}_{-0.07}$, and five out of 144 LAEs candidates, i.e., $f_{\text{AGN}}^{\text{LAE}} = 0.03^{+0.02}_{-0.01}$. These fractions are slightly different than

Table A.1. Parameters and values for the modules used with CIGALE. Parameters not listed here are fixed to their default values.

Parameter	Model/values
Star formation history: delayed model and recent burst	
Age of the main population	250, 500 Myr
e-folding time	100, 250, 500 Myr
Age of the burst	5, 10, 25, 50 Myr
e-folding time of the burst ^a	10000 Myr
Burst stellar mass fraction	0, 0.1, 0.3, 0.5, 0.7, 0.9, 1.0
Simple Stellar population: Bruzual & Charlot (2003)	
Initial Mass Function	Chabrier (2003)
Metallicity	0.008, 0.02 (Solar)
Nebular emission	
Gas metallicity	0.008, 0.014
f_{dust}	0, 0.25, 0.5, 0.75, 1.0
Galactic dust extinction	
Dust attenuation	modified Calzetti et al. (2000)
$E(B-V)_{\text{lines}}$	0.1, 0.3, 0.5, 1, 1.5, 2.0
Scale factor to $E(B-V)_{\text{stars}}$	1
Power-law slope	-1, -0.75, -0.5, -0.25, 0
Extinction law	SMC
Galactic dust emission: Draine et al. (2014)	
u_{min}	2.0, 5, 10, 30, 50
gamma	0.02, 0.1, 0.25, 0.5, 0.75
AGN module: SKIRTOR	
Angle between the equatorial plan and edge of the torus	60°
Viewing angle	90°
AGN fraction	0.0, 0.1, 0.25, 0.5, 0.75, 0.9, 0.99
$E(B-V)$ of polar dust	0.1
X-ray module	
AGN photon index Γ	1.9
α_{ox}	-2.0, -1.9, -1.8, -1.7, -1.6, -1.5
Radio module: ^b	
R_{AGN}	10, 25, 50, 75, 100, 125
α_{AGN}	1.45

Notes. ^a Using an e-folding time of the star-formation burst much higher than its age effectively reproduces a constant burst of star formation over a period equal to the burst age. ^b The Radio module is used only for C6 (see Sec. 3.3).

those reported in Lehmer et al. (2009b), due to the different way in which they are computed. Umehata et al. (2019) presented deep ALMA observations of the SSA22 fields. Among the 12 DSFGs spectroscopically confirmed as members of the protocluster, 6 are detected in the X-ray catalog of Lehmer et al. (2009a); i.e., $f_{\text{AGN}}^{\text{DSFG}} = 0.50^{+0.14}_{-0.14}$. We also note that since the publication of those works a few new relevant datasets have been presented (e.g. Yamada et al. 2012; Kubo et al. 2015, 2016; Topping et al. 2016; Radzom et al. 2022), but are not considered here.

DRC ($z=4.002$). Among the 13 spectroscopically identified SMGs in this structure (Oteo et al. 2018; Ivison et al. 2020), two are X-ray selected AGN, corresponding to $f_{\text{AGN}}^{\text{DSFG}} = 0.15^{+0.12}_{-0.07}$ (Vito et al. 2020).

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