

RIS-Aided Interference Cancellation for Joint Device-to-Device and Cellular Communications

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Abstract—Joint device-to-device (D2D) and cellular communication is a promising technology for enhancing the spectral efficiency of future wireless networks. However, the interference management problem is challenging since the operating devices and the cellular users share the same spectrum. The emerging reconfigurable intelligent surfaces (RIS) technology is a potentially ideal solution for this interference problem since RISs can shape the wireless channel in desired ways. This paper considers an RIS-aided joint D2D and cellular communication system where the RIS is exploited to cancel interference to the D2D links and maximize the minimum signal-to-interference plus noise (SINR) of the device pairs and cellular users. First, we adopt a popular alternating optimization (AO) approach to solve the minimum SINR maximization problem. Then, we propose an interference cancellation (IC)-based approach whose complexity is much lower than that of the AO algorithm. We derive a representation for the RIS phase shift vector which cancels the interference to the D2D links. Based on this representation, the RIS phase shift optimization problem is transformed into an effective D2D channel optimization. We show that the AO approach can converge faster and can even give better performance when it is initialized by the proposed IC solution. We also show that for the case of a single D2D pair, the proposed IC approach can be implemented with limited feedback from the single receive device.

I. INTRODUCTION

With the proliferation of mobile users and devices, joint device-to-device (D2D) and cellular communication has been envisioned as a promising technology for enhancing spectral efficiency in future wireless networks [1]. In this technology, devices and cellular users operate on the same spectrum, and therefore significantly improve the network spectral efficiency. However, the interference management problem is very challenging due to spectrum sharing between the operating devices and cellular users [2]–[4]. Fortunately, the D2D interference problem can be effectively addressed by reconfigurable intelligent surfaces (RISs)—a recent innovative technology capable of shaping the wireless channel in desired ways [5], [6]. For example, the works in [7]–[9] show that an RIS can be used to effectively null out or mitigate interference in D2D systems. While the work in [7] considers a conventional passive RIS structure which can only change the phase of the incoming signal, the authors in [8], [9] show that a hybrid RIS structure with the capability of simultaneously changing the phase and amplitude of the incoming signal can provide better interference cancellation performance. However, these prior works all

consider systems with only D2D links, i.e., there were no active co-channel cellular users present.

RIS-assisted joint D2D and cellular communication has been studied in several recent papers. For example, the works in [10] and [11] perform analyses for RIS-assisted D2D communications under Rician and Nakagami- m fading channels, respectively. The study in [10] investigates the effective capacity and performs mode selection to determine whether the D2D communication is established through an RIS or a base station (BS). The authors of [11] derived closed-form expressions for the outage probability of the D2D links and the resulting diversity order. Unlike [10], [11] which perform system analysis, some other recent papers focus on system design and optimization [12]–[17]. In particular, the sum-rate maximization problem was considered in [12]–[15] and deep reinforcement learning was used in [12], [14]. However, the works in [12], [14] assume that the BS is equipped with only one antenna and only one D2D pair is allowed to share the spectrum with a single cellular user. Multiple D2D pairs sharing the same spectrum with a cellular user were considered in [13], [15], but it was still assumed that the BS has only one antenna. The sum-rate maximization problem for systems with a multi-antenna BS was studied in [16], [17], but again they assume only one D2D pair sharing the spectrum with one cellular user.

Unlike the aforementioned works which consider the sum-rate maximization problem with relaxed system assumptions, we study a different problem that takes into account the fairness by maximizing the minimum signal-to-interference-plus-noise ratio (SINR) over the cellular users and devices. We also consider a more challenging RIS-assisted joint D2D and cellular communication system where multiple cellular users share the same spectrum with multiple D2D pairs and the BS is also equipped with multiple antennas. The contributions of our paper is summarized as follows:

- First, we adopt a popular alternating optimization (AO) approach and the semi-definite relaxation (SDR) technique to optimize the combining matrix at the BS and the RIS phase shift vector that maximize the minimum SINR over the cellular users and devices.
- Next, we propose an interference cancellation (IC)-based approach whose complexity is much lower than that of the AO algorithm. More specifically, we first derive a representation for the RIS phase shift vector that cancels the interference to the D2D links. Based on this representation,

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TABLE I: Channel description and notation.

Channel	Notation	Size
RIS $\rightarrow$ BS	$\mathbf{H}^{\text{RB}}$	$M \times N$
CU $\rightarrow$ RxD	$\mathbf{H}^{\text{UD}}$	$L \times K$
TxD $\rightarrow$ RxD	$\mathbf{H}^{\text{DD}}$	$L \times L$
CU $\rightarrow$ BS	$\mathbf{H}^{\text{UB}} \triangleq [\mathbf{h}_1^{\text{UB}}, \dots, \mathbf{h}_K^{\text{UB}}]$	$M \times K$
TxD $\rightarrow$ BS	$\mathbf{H}^{\text{DB}} \triangleq [\mathbf{h}_1^{\text{DB}}, \dots, \mathbf{h}_L^{\text{DB}}]$	$M \times L$
RIS $\rightarrow$ RxD	$\mathbf{H}^{\text{RD}} \triangleq [\mathbf{h}_1^{\text{RD}}, \dots, \mathbf{h}_L^{\text{RD}}]^H$	$L \times N$
CU $\rightarrow$ RIS	$\mathbf{H}^{\text{UR}} \triangleq [\mathbf{h}_1^{\text{UR}}, \dots, \mathbf{h}_K^{\text{UR}}]$	$N \times K$
TxD $\rightarrow$ RIS	$\mathbf{H}^{\text{DR}} \triangleq [\mathbf{h}_1^{\text{DR}}, \dots, \mathbf{h}_L^{\text{DR}}]$	$N \times L$
cascaded TxD $\rightarrow$ RxD	$(\mathbf{g}_{\ell,\ell'}^{\text{DD}})^H = (\mathbf{h}_{\ell'}^{\text{RD}})^H \text{diag}(\mathbf{h}_{\ell}^{\text{DR}})$	$1 \times N$
cascaded CU $\rightarrow$ RxD	$(\mathbf{g}_{\ell,k}^{\text{UD}})^H = (\mathbf{h}_{\ell}^{\text{RD}})^H \text{diag}(\mathbf{h}_k^{\text{UR}})$	$1 \times N$
cascaded CU $\rightarrow$ BS	$\mathbf{G}_k^{\text{UB}} = \mathbf{H}^{\text{RB}} \text{diag}(\mathbf{h}_k^{\text{UR}})$	$M \times N$
cascaded TxD $\rightarrow$ BS	$\mathbf{G}_{\ell}^{\text{DB}} = \mathbf{H}^{\text{RB}} \text{diag}(\mathbf{h}_{\ell}^{\text{DR}})$	$M \times N$

we transform the RIS phase shift optimization problem into an effective D2D channel optimization problem. We show that the AO approach can converge faster and can even give better performance when it uses the proposed IC solution as its initial point.

- We also show that for the case of a single D2D pair, the proposed IC approach can be implemented with limited feedback from the receive device. Finally, we numerically show the gains and benefits of the proposed approaches.

II. SYSTEM MODEL AND PROBLEM FORMULATION

A. System Model

We consider an uplink RIS-assisted MIMO system where an M -antenna base station serves K users with the help of an N -element RIS. There are also L device pairs sharing the same spectrum with the cellular system. We assume that the users and devices are all equipped with a single antenna and the transmit power of user- k and device- ℓ are denoted as p_k^{U} and p_{ℓ}^{D} , respectively. The BS employs a combining matrix $\mathbf{W} = [\mathbf{w}_1, \dots, \mathbf{w}_K]^H$ to recover the cellular users' data. The receive devices have only one antenna, so they directly detect data from their received signal. The RIS is defined by a vector $\phi = [\phi_1, \dots, \phi_N]^T$ where $|\phi_i| \leq 1$. Table I provides a description of all channels and their corresponding mathematical definition. We assume perfect channel state estimation information (CSI) at the BS and the receive devices. However, we do not assume knowledge of the individual channels to and from the RIS but their cascaded versions, the estimation of which has been intensively studied in the literature e.g., [18]–[20]. The receive devices feedback their CSI to the BS for optimizing $\mathbf{W}$ and ϕ . It is also assumed that the noise at the BS and at the receive devices is distributed as $\mathcal{CN}(\mathbf{0}_M, \sigma_{\text{B}}^2 \mathbf{I}_M)$ and $\mathcal{CN}(0, \sigma_{\text{D}}^2)$, respectively.

B. Problem Formulation

The problem of interest is to maximize the minimum SINR:

$$\begin{aligned} & \underset{\{\phi, \mathbf{w}_k\}}{\text{maximize}} && \min_{k,\ell} \{\text{SINR}_{\ell}^{\text{D}}, \text{SINR}_k^{\text{U}}\} \\ & \text{subject to} && |\phi_i| \leq 1, \forall i = 1, \dots, N. \end{aligned} \quad (1)$$

where $\text{SINR}_{\ell}^{\text{D}}$ and SINR_k^{U} given in (2) and (3) denote the SINR of the ℓ -th device pair and the SINR of user- k , respectively.

III. ALTERNATING OPTIMIZATION APPROACH

This section develops an AO approach to solve the joint D2D and cellular communication problem in (1). We alternately optimize the BS combiners $\{\mathbf{w}_k\}$ and the RIS phase shift ϕ .

A. Optimizing $\{\mathbf{w}_k\}$ given ϕ

Let $\mathbf{f}_k^{\text{UB}} \triangleq \mathbf{h}_k^{\text{UB}} + \mathbf{G}_k^{\text{UB}} \phi$ and $\mathbf{f}_{\ell}^{\text{DB}} \triangleq \mathbf{h}_{\ell}^{\text{DB}} + \mathbf{G}_{\ell}^{\text{DB}} \phi$ define the effective channel from user- k to the BS and from the transmit device- ℓ to the BS, respectively. The optimal linear minimum mean squared error (LMMSE) combiner at the BS for user- k is given as

$$\mathbf{w}_k = \left(\sum_{k'=1}^K p_{k'}^{\text{U}} \mathbf{f}_{k'}^{\text{UB}} (\mathbf{f}_{k'}^{\text{UB}})^H + \sum_{\ell=1}^L p_{\ell}^{\text{D}} \mathbf{f}_{\ell}^{\text{DB}} (\mathbf{f}_{\ell}^{\text{DB}})^H + \sigma_{\text{B}}^2 \mathbf{I}_M \right)^{-1} \mathbf{f}_k^{\text{UB}}. \quad (4)$$

B. Optimizing ϕ given $\{\mathbf{w}_k\}$

Let $(\psi_{k,k'}^{\text{UB}})^H \triangleq \mathbf{w}_k^H \mathbf{G}_{k'}^{\text{UB}}$ and $\alpha_{k,k'}^{\text{UB}} \triangleq \mathbf{w}_k^H \mathbf{h}_{k'}^{\text{UB}}$, then we can express the term $|\mathbf{w}_k^H (\mathbf{h}_{k'}^{\text{UB}} + \mathbf{G}_{k'}^{\text{UB}} \phi)|^2$ in (3) as follows:

$$|\mathbf{w}_k^H (\mathbf{h}_{k'}^{\text{UB}} + \mathbf{G}_{k'}^{\text{UB}} \phi)|^2 = \tilde{\phi}^H \Psi_{k,k'}^{\text{UB}} \tilde{\phi} = \text{tr}(\tilde{\Phi} \Psi_{k,k'}^{\text{UB}}) \quad (5)$$

where $\tilde{\phi} = [\phi^T, 1]^T$, $\tilde{\Phi} = \tilde{\phi} \tilde{\phi}^H$, and

$$\Psi_{k,k'}^{\text{UB}} = \begin{bmatrix} \psi_{k,k'}^{\text{UB}} (\psi_{k,k'}^{\text{UB}})^H & \alpha_{k,k'}^{\text{UB}} \psi_{k,k'}^{\text{UB}} \\ (\psi_{k,k'}^{\text{UB}})^H (\alpha_{k,k'}^{\text{UB}})^* & |\alpha_{k,k'}^{\text{UB}}|^2 \end{bmatrix}. \quad (6)$$

Similarly, by defining

$$(\psi_{k,\ell}^{\text{DB}})^H \triangleq \mathbf{w}_k^H \mathbf{G}_{\ell}^{\text{DB}} \text{ and } \alpha_{k,\ell}^{\text{DB}} \triangleq \mathbf{w}_k^H \mathbf{h}_{\ell}^{\text{DB}}, \quad (7)$$

we can write the term $|\mathbf{w}_k^H (\mathbf{h}_{\ell}^{\text{DB}} + \mathbf{G}_{\ell}^{\text{DB}} \phi)|^2$ in (3) as

$$|\mathbf{w}_k^H (\mathbf{h}_{\ell}^{\text{DB}} + \mathbf{G}_{\ell}^{\text{DB}} \phi)|^2 = \tilde{\phi}^H \Psi_{k,\ell}^{\text{DB}} \tilde{\phi} = \text{tr}(\tilde{\Phi} \Psi_{k,\ell}^{\text{DB}}) \quad (8)$$

where

$$\Psi_{k,\ell}^{\text{DB}} = \begin{bmatrix} \psi_{k,\ell}^{\text{DB}} (\psi_{k,\ell}^{\text{DB}})^H & \alpha_{k,\ell}^{\text{DB}} \psi_{k,\ell}^{\text{DB}} \\ (\psi_{k,\ell}^{\text{DB}})^H (\alpha_{k,\ell}^{\text{DB}})^* & |\alpha_{k,\ell}^{\text{DB}}|^2 \end{bmatrix}. \quad (9)$$

Using (5) and (8), the SINR of user- k in (3) is written as

$$\text{SINR}_k^{\text{U}} = \frac{p_k^{\text{U}} \text{tr}(\tilde{\Phi} \Psi_{k,k}^{\text{UB}})}{\sum_{k' \neq k} p_{k'}^{\text{U}} \text{tr}(\tilde{\Phi} \Psi_{k,k'}^{\text{UB}}) + \sum_{\ell} p_{\ell}^{\text{D}} \text{tr}(\tilde{\Phi} \Psi_{k,\ell}^{\text{DB}}) + \zeta_k} \quad (10)$$

where $\zeta_k = \|\mathbf{w}_k\|^2 \sigma_{\text{B}}^2$. We also have

$$\text{SINR}_{\ell}^{\text{D}} = \frac{p_{\ell}^{\text{D}} \text{tr}(\tilde{\Phi} \Psi_{\ell,\ell}^{\text{DD}})}{\sum_{\ell' \neq \ell} p_{\ell'}^{\text{D}} \text{tr}(\tilde{\Phi} \Psi_{\ell,\ell'}^{\text{DD}}) + \sum_k p_k^{\text{U}} \text{tr}(\tilde{\Phi} \Psi_{\ell,k}^{\text{UD}}) + \sigma_{\text{D}}^2} \quad (11)$$

where

$$\Psi_{\ell,\ell'}^{\text{DD}} = \begin{bmatrix} \mathbf{g}_{\ell,\ell'}^{\text{DD}} (\mathbf{g}_{\ell,\ell'}^{\text{DD}})^H & h_{\ell,\ell'}^{\text{DD}} \mathbf{g}_{\ell,\ell'}^{\text{DD}} \\ (\mathbf{g}_{\ell,\ell'}^{\text{DD}})^H (h_{\ell,\ell'}^{\text{DD}})^* & |h_{\ell,\ell'}^{\text{DD}}|^2 \end{bmatrix}, \quad (12)$$

$$\Psi_{\ell,k}^{\text{UD}} = \begin{bmatrix} \mathbf{g}_{\ell,k}^{\text{UD}} (\mathbf{g}_{\ell,k}^{\text{UD}})^H & h_{\ell,k}^{\text{UD}} \mathbf{g}_{\ell,k}^{\text{UD}} \\ (\mathbf{g}_{\ell,k}^{\text{UD}})^H (h_{\ell,k}^{\text{UD}})^* & |h_{\ell,k}^{\text{UD}}|^2 \end{bmatrix}. \quad (13)$$

$$\text{SINR}_\ell^D = \frac{p_\ell^D |h_{\ell,\ell}^{\text{DD}} + (\mathbf{g}_{\ell,\ell}^{\text{DD}})^H \phi|^2}{\sum_{\ell' \neq \ell} p_{\ell'}^D |h_{\ell,\ell'}^{\text{DD}} + (\mathbf{g}_{\ell,\ell'}^{\text{DD}})^H \phi|^2 + \sum_{k=1}^K p_k^U |h_{\ell,k}^{\text{UD}} + (\mathbf{g}_{\ell,k}^{\text{UD}})^H \phi|^2 + \sigma_D^2} \quad (2)$$

$$\text{SINR}_k^U = \frac{p_k^U |\mathbf{w}_k^H (\mathbf{h}_k^{\text{UB}} + \mathbf{G}_k^{\text{UB}} \phi)|^2}{\sum_{k' \neq k} p_{k'}^U |\mathbf{w}_k^H (\mathbf{h}_{k'}^{\text{UB}} + \mathbf{G}_{k'}^{\text{UB}} \phi)|^2 + \sum_{\ell=1}^L p_\ell^D |\mathbf{w}_k^H (\mathbf{h}_\ell^{\text{DB}} + \mathbf{G}_\ell^{\text{DB}} \phi)|^2 + \|\mathbf{w}_k\|^2 \sigma_B^2} \quad (3)$$

Therefore, problem (1) can be written as

$$\begin{aligned} & \underset{\{\xi, \tilde{\Phi} \geq \mathbf{0}\}}{\text{maximize}} \quad \xi \\ & \text{subject to} \quad (10) \geq \xi \quad \forall k \\ & \quad (11) \geq \xi \quad \forall \ell \\ & \quad |\tilde{\Phi}_{i,i}| \leq 1, \quad \forall i = 1, \dots, N \\ & \quad \tilde{\Phi}_{N+1,N+1} = 1. \end{aligned} \quad (14)$$

This is a fractional programming problem and thus can be solved by the Dinkelbach algorithm [21]. Given a solution $\tilde{\Phi}$ of (14), we need to convert $\tilde{\Phi}$ into a feasible solution $\hat{\Phi}$, which can be done by the Gaussian randomization approach [22]. Specifically, we first generate a set of Gaussian random vectors as $\tilde{\phi}_i \sim \mathcal{CN}(\mathbf{0}, \tilde{\Phi})$, $i = 1, \dots, I$. Since the elements of $\tilde{\phi}_i$ may not satisfy the constraints $|\tilde{\phi}_{i,n}| \leq 1$ for $n = 1, \dots, N$ and $\tilde{\phi}_{i,N+1} = 1$, we need to first normalize $\tilde{\phi}_i$ to obtain $\bar{\phi}_i = \tilde{\phi}_i / \tilde{\phi}_{i,N+1}$, then we can obtain a feasible candidate $\hat{\phi}_i = [\hat{\phi}_{i,1}, \dots, \hat{\phi}_{i,N}]^T$ where $\hat{\phi}_{i,n} = e^{j\angle(\bar{\phi}_{i,n})}$ if $|\bar{\phi}_{i,n}| > 1$, otherwise $\hat{\phi}_{i,n} = \bar{\phi}_{i,n}$. Finally, a solution $\hat{\Phi}$ of problem (14) can be obtained as

$$\hat{\Phi} = \arg \max_{\{\hat{\Phi}_1, \dots, \hat{\Phi}_I\}} \min \{\text{SINR}_\ell^D, \text{SINR}_k^U\}. \quad (15)$$

IV. INTERFERENCE CANCELLATION APPROACH

The AO approach presented above is efficient but its computational complexity is high because the BS combiners and the RIS phase shift vector are alternately optimized. In addition, each AO iteration requires use of the Dinkelbach algorithm which is an iterative algorithm itself, and each of its iterations also requires the solution of an SDR optimization problem. Here, we propose an IC approach whose computational complexity is significantly lower than that of the AO algorithm since the proposed IC approach only needs to solve one SDR problem. Details of the proposed IC approach are presented as follows.

Let $\mathbf{F}^{\text{DD}} \in \mathbb{C}^{L \times L}$ be the effective channel from the transmit devices to the receive devices, and define

$$\mathbf{f}^{\text{DD}} = \text{vec}((\mathbf{F}^{\text{DD}})^T) = \text{vec}((\mathbf{H}^{\text{DD}})^T) + \begin{bmatrix} \mathbf{G}_1^{\text{DD}} \\ \vdots \\ \mathbf{G}_L^{\text{DD}} \end{bmatrix} \phi \quad (16)$$

$$= \mathbf{h}^{\text{DD}} + \mathbf{G}^{\text{DD}} \phi, \quad (17)$$

where $\mathbf{G}_\ell^{\text{DD}} = [\mathbf{g}_{\ell,1}^{\text{DD}}, \dots, \mathbf{g}_{\ell,L}^{\text{DD}}]^H$. We use a permutation matrix $\mathbf{P}$ to separate the vector $\mathbf{f}^{\text{DD}}$ into two sub-vectors $\mathbf{f}_{\text{sig}}^{\text{DD}}$ and $\mathbf{f}_{\text{itf}}^{\text{DD}}$ which contain the diagonal and off-diagonal elements of

$\mathbf{F}^{\text{DD}}$, respectively. The diagonal elements of $\mathbf{F}^{\text{DD}}$ represent the useful channels for the D2D pairs, while the off-diagonal elements represent the interference channels from other D2D pairs. Hence we use the subscripts ‘sig’ and ‘itf’ to indicate the D2D signal and interference, respectively. This means we can write

$$\begin{bmatrix} \mathbf{f}_{\text{sig}}^{\text{DD}} \\ \mathbf{f}_{\text{itf}}^{\text{DD}} \end{bmatrix} = \begin{bmatrix} \mathbf{h}_{\text{sig}}^{\text{DD}} \\ \mathbf{h}_{\text{itf}}^{\text{DD}} \end{bmatrix} + \begin{bmatrix} \mathbf{G}_{\text{sig}}^{\text{DD}} \\ \mathbf{G}_{\text{itf}}^{\text{DD}} \end{bmatrix} \phi \quad (18)$$

where

$$\begin{bmatrix} \mathbf{f}_{\text{sig}}^{\text{DD}} \\ \mathbf{f}_{\text{itf}}^{\text{DD}} \end{bmatrix} = \mathbf{P} \mathbf{f}^{\text{DD}}, \quad \begin{bmatrix} \mathbf{h}_{\text{sig}}^{\text{DD}} \\ \mathbf{h}_{\text{itf}}^{\text{DD}} \end{bmatrix} = \mathbf{P} \mathbf{h}^{\text{DD}}, \quad \begin{bmatrix} \mathbf{G}_{\text{sig}}^{\text{DD}} \\ \mathbf{G}_{\text{itf}}^{\text{DD}} \end{bmatrix} = \mathbf{P} \mathbf{G}^{\text{DD}}. \quad (19)$$

Similarly, let $\mathbf{F}^{\text{UD}} \in \mathbb{C}^{L \times K}$ be the effective channel from the cellular users to the receive devices, so we can also write

$$\mathbf{f}^{\text{UD}} = \text{vec}((\mathbf{F}^{\text{UD}})^T) = \text{vec}((\mathbf{H}^{\text{UD}})^T) + \begin{bmatrix} \mathbf{G}_1^{\text{UD}} \\ \vdots \\ \mathbf{G}_L^{\text{UD}} \end{bmatrix} \phi \quad (20)$$

$$= \mathbf{h}^{\text{UD}} + \mathbf{G}^{\text{UD}} \phi, \quad (21)$$

where $\mathbf{G}_\ell^{\text{UD}} = [\mathbf{g}_{\ell,1}^{\text{UD}}, \dots, \mathbf{g}_{\ell,K}^{\text{UD}}]^H$.

Combining (18) and (21), we have

$$\begin{bmatrix} \mathbf{f}_{\text{sig}}^{\text{DD}} \\ \mathbf{f}_{\text{itf}}^{\text{DD}} \\ \mathbf{f}^{\text{UD}} \end{bmatrix} = \begin{bmatrix} \mathbf{h}_{\text{sig}}^{\text{DD}} \\ \mathbf{h}_{\text{itf}}^{\text{DD}} \\ \mathbf{h}^{\text{UD}} \end{bmatrix} + \underbrace{\begin{bmatrix} \mathbf{G}_{\text{sig}}^{\text{DD}} \\ \mathbf{G}_{\text{itf}}^{\text{DD}} \\ \mathbf{G}^{\text{UD}} \end{bmatrix}}_{\mathbf{A}} \phi, \quad (22)$$

where $\mathbf{A} \in \mathbb{C}^{L(K+L) \times N}$ is a matrix representing the RIS-aided channel. Assuming that $N \geq L(K+L)$, then using (22) we can write the phase shift vector ϕ in the following expression:

$$\phi = \mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1} \left(\begin{bmatrix} \mathbf{f}_{\text{sig}}^{\text{DD}} \\ \mathbf{f}_{\text{itf}}^{\text{DD}} \\ \mathbf{f}^{\text{UD}} \end{bmatrix} - \begin{bmatrix} \mathbf{h}_{\text{sig}}^{\text{DD}} \\ \mathbf{h}_{\text{itf}}^{\text{DD}} \\ \mathbf{h}^{\text{UD}} \end{bmatrix} \right). \quad (23)$$

Let $[\mathbf{B}, \mathbf{C}] \triangleq \mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1}$ where $\mathbf{B} \in \mathbb{C}^{N \times L}$ and $\mathbf{C} \in \mathbb{C}^{N \times L(K+L)-L}$, then decompose the right-hand side of (23) as follows:

$$\phi = \mathbf{B} \mathbf{f}_{\text{sig}}^{\text{DD}} - \mathbf{B} \mathbf{h}_{\text{sig}}^{\text{DD}} + \mathbf{C} \left(\begin{bmatrix} \mathbf{f}_{\text{itf}}^{\text{DD}} \\ \mathbf{f}^{\text{UD}} \end{bmatrix} - \begin{bmatrix} \mathbf{h}_{\text{itf}}^{\text{DD}} \\ \mathbf{h}^{\text{UD}} \end{bmatrix} \right). \quad (24)$$

The representation above shows a relationship between the RIS phase shift ϕ and the effective device-related channels including the useful D2D channels $\mathbf{f}_{\text{sig}}^{\text{DD}}$ and the other interference links $\mathbf{f}_{\text{itf}}^{\text{DD}}$ and $\mathbf{f}^{\text{UD}}$. If we let $\mathbf{f}_{\text{itf}}^{\text{DD}} = \mathbf{0}$ and $\mathbf{f}^{\text{UD}} = \mathbf{0}$, the RIS

solution (24) reduces to an IC ϕ solution expressed in terms of $\mathbf{f}_{\text{sig}}^{\text{DD}}$ as

$$\begin{aligned}\phi_{\text{IC}} &= \mathbf{B}\mathbf{f}_{\text{sig}}^{\text{DD}} - \mathbf{B}\mathbf{h}_{\text{sig}}^{\text{DD}} - \mathbf{C} \begin{bmatrix} \mathbf{h}_{\text{itf}}^{\text{DD}} \\ \mathbf{h}^{\text{UD}} \end{bmatrix} \\ &= \mathbf{B}\mathbf{f}_{\text{sig}}^{\text{DD}} + \mathbf{d}\end{aligned}\quad (25)$$

where $\mathbf{d} = -\mathbf{B}\mathbf{h}_{\text{sig}}^{\text{DD}} - \mathbf{C}[(\mathbf{h}_{\text{itf}}^{\text{DD}})^T, (\mathbf{h}^{\text{UD}})^T]^T$. This means that if we could design the RIS phase shifts with (25), the interference to the receive devices will be completely cancelled. In this case, the SINR at the receive device- ℓ would simplify to $\text{SINR}_\ell^{\text{D}} = p_\ell^{\text{D}} |f_{\text{sig},\ell}^{\text{DD}}|^2 / \sigma_{\text{D}}^2$.

With the ϕ_{IC} representation in (25), we can use the Cauchy-Schwarz inequality to find the following upper bound for the SINR of user- k :

$$\text{SINR}_k^{\text{U}} \leq p_k^{\text{U}} \|\mathbf{h}_k^{\text{UB}} + \mathbf{G}_k^{\text{UB}} \phi_{\text{IC}}\|^2 / \sigma_{\text{B}}^2 \quad (26)$$

$$= p_k^{\text{U}} \|\mathbf{h}_k^{\text{UB}} + \mathbf{G}_k^{\text{UB}} (\mathbf{B}\mathbf{f}_{\text{sig}}^{\text{DD}} + \mathbf{d})\|^2 / \sigma_{\text{B}}^2 \quad (27)$$

$$= p_k^{\text{U}} \|\mathbf{Z}_k \mathbf{f}_{\text{sig}}^{\text{DD}} + \mathbf{q}_k\|^2 / \sigma_{\text{B}}^2, \quad (28)$$

where $\mathbf{Z}_k = \mathbf{G}_k^{\text{UB}} \mathbf{B}$ and $\mathbf{q}_k = \mathbf{h}_k^{\text{UB}} + \mathbf{G}_k^{\text{UB}} \mathbf{d}$. Therefore, we propose the following IC-based optimization problem

$$\begin{aligned}&\text{maximize}_{\{\xi, \mathbf{f}_{\text{sig}}^{\text{DD}}\}} \quad \xi \\ &\text{subject to} \quad p_k^{\text{U}} \|\mathbf{Z}_k \mathbf{f}_{\text{sig}}^{\text{DD}} + \mathbf{q}_k\|^2 / \sigma_{\text{B}}^2 \geq \xi \quad \forall k \\ &\quad p_\ell^{\text{D}} |f_{\text{sig},\ell}^{\text{DD}}|^2 / \sigma_{\text{D}}^2 \geq \xi \quad \forall \ell \\ &\quad |\mathbf{b}_i^H \mathbf{f}_{\text{sig}}^{\text{DD}} + d_i|^2 \leq 1 \quad \forall i = 1, \dots, N,\end{aligned}\quad (29)$$

where the constraint $|\mathbf{b}_i^H \mathbf{f}_{\text{sig}}^{\text{DD}} + d_i|^2 \leq 1$ is equivalent to the constraint $|\phi_i|^2 \leq 1$. Hence, we have transformed the RIS phase shift ϕ optimization problem into an effective D2D channel optimization (29) by exploiting the IC representation (25).

The problem in (29) can also be easily solved using SDR. Specifically, let

$$\Omega_k = \begin{bmatrix} \mathbf{Z}_k^H \mathbf{Z}_k & \mathbf{Z}_k^H \mathbf{q}_k \\ \mathbf{q}_k^H \mathbf{Z}_k & \|\mathbf{q}_k\|^2 \end{bmatrix} \text{ and } \Upsilon_i = \begin{bmatrix} \mathbf{b}_i \mathbf{b}_i^H & \mathbf{b}_i d_i \\ \mathbf{b}_i^H d_i^* & |d_i|^2 \end{bmatrix}, \quad (30)$$

so that

$$\|\mathbf{Z}_k \mathbf{f}_{\text{sig}}^{\text{DD}} + \mathbf{q}_k\|^2 = \text{tr}(\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}} \Omega_k) \quad (31)$$

$$|\mathbf{b}_i^H \mathbf{f}_{\text{sig}}^{\text{DD}} + d_i|^2 = \text{tr}(\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}} \Upsilon_i), \quad (32)$$

where $\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}} = \tilde{\mathbf{f}}_{\text{sig}}^{\text{DD}} (\tilde{\mathbf{f}}_{\text{sig}}^{\text{DD}})^T$ with $\tilde{\mathbf{f}}_{\text{sig}}^{\text{DD}} = [(\mathbf{f}_{\text{sig}}^{\text{DD}})^T, 1]^T$. Problem (29) can be now relaxed to a convex optimization problem:

$$\begin{aligned}&\text{maximize}_{\{\xi, \mathbf{F}_{\text{sig}}^{\text{DD}} \succeq \mathbf{0}\}} \quad \xi \\ &\text{subject to} \quad p_k^{\text{U}} \text{tr}(\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}} \Omega_k) / \sigma_{\text{B}}^2 \geq \xi \quad \forall k \\ &\quad p_\ell^{\text{D}} \mathcal{R}\{\tilde{\mathbf{f}}_{\text{sig},\ell}^{\text{DD}}\} / \sigma_{\text{D}}^2 \geq \xi \quad \forall \ell \\ &\quad \text{tr}(\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}} \Upsilon_i) \leq 1 \quad \forall i = 1, \dots, N \\ &\quad \tilde{\mathbf{F}}_{\text{sig},L+1,L+1}^{\text{DD}} = 1,\end{aligned}\quad (33)$$

which again can be solved using SDR. Finally, we need to recover an IC solution $\hat{\phi}_{\text{IC}}$ from $\tilde{\mathbf{F}}_{\text{sig}}^{\text{DD}}$, which can also be done

using the Gaussian randomization method. Given a $\hat{\phi}_{\text{IC}}$, the corresponding LMMSE combiner at the BS can be computed.

It can be seen that unlike the AO approach which needs to solve a series of SDR problems, the IC approach involves only one SDR optimization and therefore significantly reduces the computational complexity. We will show later that if the AO approach is initialized with $\hat{\phi}_{\text{IC}}$, it converges more rapidly with better performance compared to using a random initialization.

Limited feedback for single D2D pair: To implement the IC method for the case of multiple device pairs, it is required that each receive device- ℓ forwards its estimated CSI including two cascaded channel matrices $\mathbf{G}_\ell^{\text{DD}} \in \mathbb{C}^{L \times N}$, $\mathbf{G}_\ell^{\text{UD}} \in \mathbb{C}^{K \times N}$ and two direct channel vectors $\mathbf{H}_{\ell,:}^{\text{DD}} \in \mathbb{C}^{1 \times L}$, $\mathbf{H}_{\ell,:}^{\text{UD}} \in \mathbb{C}^{1 \times K}$ via a control link to the BS, which results in a total number of $(L+K)(N+1)$ complex coefficients to be fed-back.

However, for the case of a single device pair, the representation in (23) can be obtained at the receive device as follows:

$$\phi = \mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1} \left(\begin{bmatrix} f^{\text{DD}} \\ \mathbf{f}^{\text{UD}} \end{bmatrix} - \begin{bmatrix} h^{\text{DD}} \\ \mathbf{h}^{\text{UD}} \end{bmatrix} \right) \quad (34)$$

where $\mathbf{A} = [(\mathbf{g}^{\text{DD}})^T, \mathbf{G}^{\text{UD}}]$ and we have dropped the device index ℓ since there is only D2D pair here. By setting $\mathbf{f}^{\text{UD}} = \mathbf{0}$, the ϕ_{IC} representation that cancels the interference at the device is

$$\phi_{\text{IC}} = \mathbf{b} f^{\text{DD}} + \mathbf{d}, \quad (35)$$

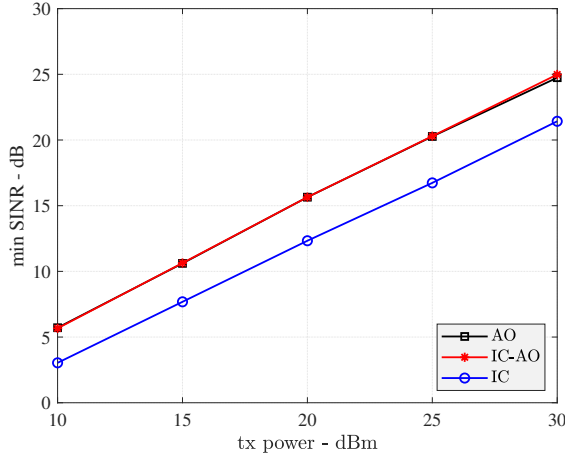
where $\mathbf{b}$ is the first column of $\mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1}$ and $\mathbf{d} = -\mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1} [h^{\text{DD}}, (\mathbf{h}^{\text{UD}})^T]^T$. This means the receive device can calculate the matrix $\mathbf{A}^H (\mathbf{A} \mathbf{A}^H)^{-1}$ using its local CSI, then obtain the two corresponding vectors $\mathbf{b}$ and $\mathbf{d}$, which will be forwarded to the BS to solve the RIS phase shift optimization problem:

$$\begin{aligned}&\text{maximize}_{\{\xi, f^{\text{DD}}\}} \quad \xi \\ &\text{subject to} \quad p_k^{\text{U}} \|\mathbf{z}_k f^{\text{DD}} + \mathbf{q}_k\|^2 / \sigma_{\text{B}}^2 \geq \xi \quad \forall k \\ &\quad p^{\text{D}} |f^{\text{DD}}|^2 / \sigma_{\text{D}}^2 \geq \xi \\ &\quad |b_i f^{\text{DD}} + d_i|^2 \leq 1 \quad \forall i = 1, \dots, N.\end{aligned}\quad (36)$$

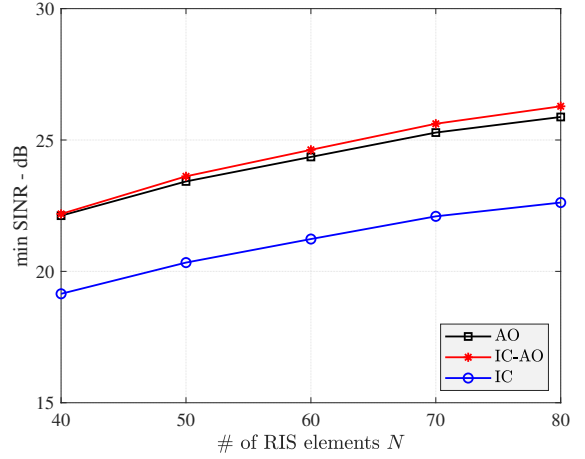
Thus, instead of forwarding the $(K+1)(N+1)$ complex coefficients from $\mathbf{g}^{\text{DD}} \in \mathbb{C}^{N \times 1}$, $\mathbf{G}^{\text{UD}} \in \mathbb{C}^{K \times N}$, h^{DD} , and $\mathbf{h}^{\text{UD}} \in \mathbb{C}^{K \times 1}$, the receive device finds $\mathbf{b}$ and $\mathbf{d}$ and forwards these two vectors to the BS. This only requires transmission of $2N$ complex coefficients, but still guarantees that the BS can solve the RIS phase shift optimization problem.

V. NUMERICAL RESULTS

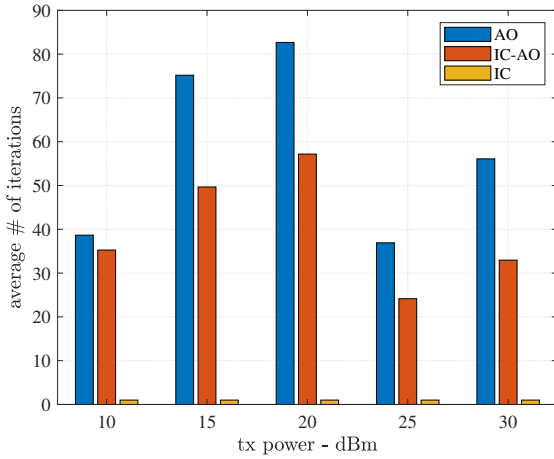
In this section, we present numerical results to show the superiority and benefits of the proposed IC and IC-AO approaches where IC-AO indicates the AO approach that uses the IC solution $\hat{\phi}_{\text{IC}}$ as an initialization. For the regular AO method, we use a random initial solution for ϕ . We consider $K = 2$ users, $L = 2$ device pairs, and $M = 8$ antennas at the BS. If not specifically stated, the number of RIS elements is set to 64. We position the BS and the RIS at the locations $(x, y) = (0, 0)$



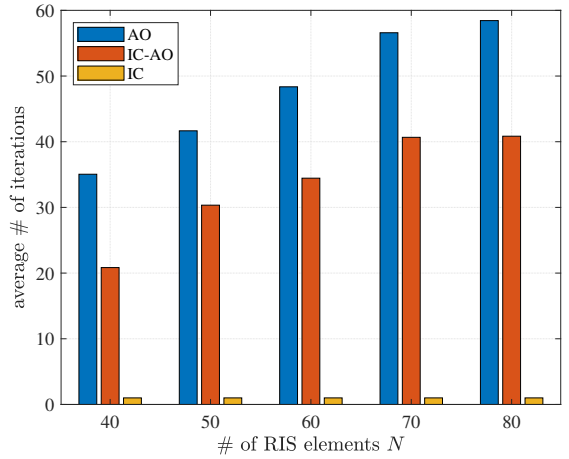
(a) Minimum SINR performance



(a) Minimum SINR performance



(b) Computational complexity comparison



(b) Computational complexity comparison

Fig. 1: Performance and computational complexity comparison versus transmit power with $N = 64$ RIS elements.

Fig. 2: Performance and computational complexity comparison versus number of RIS elements N at 30-dBm transmit power.

and $(x, y) = (100, 30)$, respectively. The cellular users and transmit devices are randomly located within a circular area whose center is $(x, y) = (200, 0)$ with a radius of 25 m, and we also locate the receive devices randomly also within a circular area centered at $(x, y) = (50, 0)$ with the same radius. The transmit power of the cellular users and the transmit devices are set to be the same. The noise power is set to -169 dBm/Hz and a bandwidth of 1 MHz is assumed. The large-scale fading is modeled as $\beta = \beta_0(d/d_0)^{-\eta}$, where η is the path loss exponent and d is the distance. We set $\beta_0 = -30$ dB as the path loss at the reference distance $d_0 = 1$ m. The path loss exponent of the user-RIS, TxD-RIS, RIS-RxD, and RIS-BS channel links is set to 2.2. However, the path loss exponent of the user-BS and TxD-BS channels is set to 4 and the path loss exponent of the user-RxD and TxD-RxD channels are set to 5, to model their weak propagation.

In Fig. 1, we show a comparison of the minimum SINR performance and computational complexity as the transmit

power changes. It can be seen from Fig. 1a that the AO and IC-AO approaches give the same minimum SINRs, which are about 2.5 to 3 dB higher than that of the IC approach. However, the computational complexity of the IC approach is much lower than that of AO and IC-AO since the IC approach requires only one iteration while AO and IC-AO require many more iterations as seen in Fig. 1b. It is also observed that although the AO and IC-AO approaches give the same SINR performance, IC-AO has a lower computational complexity since it requires a smaller number of iterations.

Next, in Fig. 2, we also show a comparison for the minimum SINR performance and computational complexity but with a fixed transmit power of 30 dBm and the number of RIS elements N is varied. The minimum SINRs for AO and IC-AO are still about 3-dB higher than that of the IC approach. However, it is interesting that as the number of RIS elements N increases, the IC-AO approach tends to perform better than AO even though IC-AO still requires a smaller number of iterations.

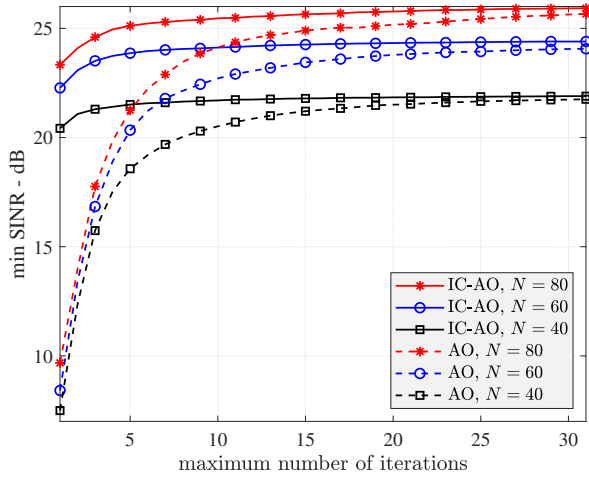


Fig. 3: Minimum SINR performance versus maximum number of iterations.

This indicates that IC-AO not only converges faster than AO but also converges to better local solutions.

Finally, we show an SINR performance comparison between the AO and IC-AO approaches in Fig. 3 as the maximum number of iterations changes. It is clear that IC-AO converges much faster than AO because IC-AO utilizes the IC solution as the initial point, which already gives a relatively good performance. If we set a small maximum number of iterations, the performance of IC-AO will be significantly higher than that of AO. For example, if we set the maximum number of iterations to 5, the IC-AO approach has already nearly converged and its minimum SINRs are about 4-dB, 3.5-dB, and 3-dB higher than that of AO for $N = 80, 60, 40$, respectively.

VI. CONCLUSION

This paper has considered a minimum SINR maximization problem in an RIS-aided joint D2D and cellular communication system where the RIS was exploited to simultaneously support the cellular users and the devices. We first presented an AO approach based on the SDR technique to solve the min-max SINR problem. We then derived a representation for the RIS phase shift vector that cancels the interference to the D2D links. Based on the IC representation, we proposed an IC algorithm whose complexity is much lower than that of the AO approach. We also showed that the IC solution can help the AO approach converge faster and achieve better performance. It was also pointed out that for the case of a single D2D pair, the proposed IC approach can be accomplished with limited feedback from the device.

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