



# Expanding the Ultracompacts: Gravitational-wave-driven Mass Transfer in the Shortest-period Binaries with Accretion Disks

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## Abstract

We report the discovery of three ultracompact binary white dwarf systems hosting accretion disks, with orbital periods of 7.95, 8.68, and 13.15 minutes. This significantly augments the population of mass-transferring binaries at the shortest periods, and provides the first evidence that accretors in ultracompacts can be dense enough to host accretion disks even below 10 minutes (where previously only direct-impact accretors were known). In the two shortest-period systems, we measured changes in the orbital periods driven by the combined effect of gravitational-wave emission and mass transfer. We find  $\dot{P}$  is negative in one case, and positive in the other. This is only the second system measured with a positive  $\dot{P}$ , and it is the most compact binary known that has survived a period minimum. Using these systems as examples, we show how the measurement of  $\dot{P}$  is a powerful tool in constraining the physical properties of binaries, e.g., the mass and mass–radius relation of the donor stars. We find that the chirp masses of ultracompact binaries at these periods seem to cluster around  $\mathcal{M}_c \sim 0.3M_\odot$ , perhaps suggesting a common origin for these systems or a selection bias in electromagnetic discoveries. Our new systems are among the highest-amplitude known gravitational-wave sources in the millihertz regime, providing an exquisite opportunity for multimessenger study with future space-based observatories such as LISA and TianQin. We discuss how such systems provide fascinating laboratories to study the unique regime where the accretion process is mediated by gravitational waves.

*Unified Astronomy Thesaurus concepts:* Compact binary stars (283); Gravitational wave sources (677); Stellar accretion disks (1579); White dwarf stars (1799)

## 1. Introduction

Binary systems containing accreting white dwarfs (WDs) with orbital periods  $\lesssim 65$  minutes—the minimum period at which a hydrogen-rich star can attain the density to fit within its Roche lobe—are known as AM Canum Venaticorum (AM CVn) systems (for reviews, see G. Nelemans 2005;

J. E. Solheim 2010; G. Ramsay et al. 2018), which are part of the class of ultracompact binaries. The dense donor stars in AM CVns lack hydrogen, and the systems show spectra comprising stellar material dominated by helium, carbon, and nitrogen (B. Warner 1995; G. Nelemans et al. 2010).

Several dozen AM CVns are known, discovered via an eclectic range of signatures including optical outbursts (D. Levitan et al. 2015), X-ray pulsations (G. L. Israel et al. 1999), spectral/color properties (G. H. A. Roelofs et al. 2007, 2009; A. Rau et al. 2010; A. C. Rodríguez et al. 2023, 2024), and short-period photometric variability in the

accretion disks (J. Smak 1967; M. J. Green et al. 2018a; K. B. Burdge et al. 2020a; J. van Roestel et al. 2022). The current population has orbital periods spanning from 65 down to 5 minutes (G. Ramsay et al. 2018; M. Green 2024; T. Kupfer et al. 2024). Below 10 minutes, all known systems are so compact that the accretion stream directly collides with the accretor surface (direct-impact accretion; T. R. Marsh & D. Steeghs 2002; T. R. Marsh et al. 2004).

The extremely short periods of these objects mean emission of gravitational waves (GWs) is the primary factor driving their orbital evolution (B. Paczyński 1967). They will be the dominant source of millihertz gravitational waves detected by future space-based observatories, such as the Laser Space Antenna Interferometer (LISA; P. Amaro-Seoane et al. 2017, 2023), TianQin (J. Luo et al. 2016), and Taiji (W.-H. Ruan et al. 2020) missions. As the instantaneous GW strain amplitude, expressed in terms of the chirp mass ( $\mathcal{M}_c$ ), orbital period ( $P$ ), and distance ( $d$ ), is roughly (G. Nelemans et al. 2004)

$$h = 0.5 \times 10^{-21} \left( \frac{\mathcal{M}_c}{M_\odot} \right)^{5/3} \left( \frac{P}{1 \text{ hr}} \right)^{-2/3} \left( \frac{d}{1 \text{ kpc}} \right)^{-1}, \quad (1)$$

the shortest-period systems will typically have the highest intrinsic strains and most rapid evolution. Having inspiral set primarily by GWs makes AM CVns unique among accreting binary systems; the certainty of our understanding of gravitational radiation provides a convenient foothold in understanding their complex accretion properties, in contrast to binaries with poorly understood angular momentum loss mechanisms (e.g., magnetic braking).

Apart from their nature as GW sources, ultracompact binaries provide interesting laboratories for astrophysics. They are potential progenitors of Type Ia supernovae, making them central to understanding one of the foundational standard candles for local Universe cosmology both observationally (D. Maoz et al. 2014; S. W. Jha et al. 2019) and theoretically (W. Hillebrandt et al. 2013; K. J. Shen & K. Moore 2014; Z.-W. Liu et al. 2023). Yet, we lack a complete understanding of AM CVn formation and evolution, which has significant implications for their effect on SN Ia rates and, more generally, the long-term fate of binary stars in the Galaxy. There are up to three channels contributing significantly to the population, most easily distinguished via their imprints on the donor C/O, N/O, and N/C ratios (G. Nelemans et al. 2010; M. J. Green et al. 2018b):

1. *Double white dwarf channel.* Two detached white dwarfs evolve closer due to gravitational-wave emission following a common envelope phase, eventually starting mass transfer at  $P \lesssim 10$  minutes (G. Nelemans et al. 2001). Depending whether tidal synchronization efficiently returns angular momentum to the donor, their orbits may stabilize, reaching a period minimum at 4–9 minutes before outspiral to produce a long-lived AM CVn (T. R. Marsh et al. 2004; D. L. Kaplan et al. 2012). The donors are He-dominated, with a possible low-mass residual hydrogen envelope. They have metal abundances according to the equilibrium of the CNO cycle depending on the main-sequence progenitor mass. In the relevant mass ranges for AM CVn donors, they transfer mass with equilibrium N/C  $\approx 100$ .
2. *Helium star channel.* If the donor is instead a helium core-burning star (e.g., an sdB/O star; U. Heber 2016), a

minimum period of  $P \approx 11$  minutes is reached before the onset of mass transfer (G. J. Savonije et al. 1986). The orbital evolution is set by the degeneracy level in the mass-transferring outer envelope. N/O and N/C  $\ll 100$  are expected, because fusion and CNO processing were interrupted to produce these donors (L. R. Yungelson 2008).

3. *Hydrogen CV channel.* For a partially evolved main-sequence donor, mass transfer may begin while the system is still hydrogen-rich. The stripped donor gradually becomes degenerate enough to reach a compact orbit. These systems will have undergone H fusion the longest, so N/C will be  $> 100$  (B. Kalomeni et al. 2016), and will also show traces of H. It is uncertain how significantly this channel contributes to the shortest-period population, and our understanding of their period minima is still evolving (G. Ramsay et al. 2018; K. B. Burdge et al. 2022).

Discovery and spectral characterization of further AM CVns is the most promising route to determining the importance of each channel, which then constitutes a key input into binary population synthesis models (K. Breivik et al. 2020), the all-sky millihertz GW signal (T. B. Littenberg et al. 2020), and Type Ia SNa rates (A. J. Ruiter et al. 2009).

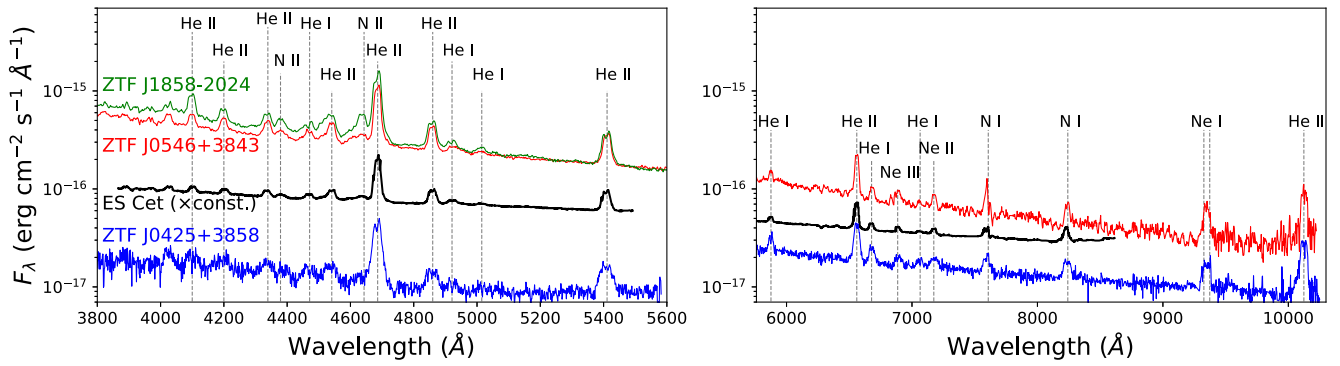
Here we report the discovery of three new ultracompact binaries with accretion disks: ZTF J0546+3843, ZTF J1858–2024, and ZTF J0425+3858. Two of these systems have orbital periods under 10 minutes, where previously only direct-impact accretors were known. Our systems are thus the most compact known binaries with accretion disks, showing that the accretors in AM CVns can become dense enough to host disks even at  $P < 10$  minutes. Our study significantly augments the population for systematic study of binary evolution closest to the period minimum, and provides exquisite laboratories to test the accretion process mediated by strong gravitational radiation.

In Section 2 we describe the observations and data analysis procedures used in this work. In Section 3 we give an overview of the results, including time-resolved photometry and spectroscopy and phase-coherent timing. In Section 4 we discuss implications of the spectroscopic and timing measurements of these systems on AM CVn evolution. We further describe how direct measurement of a period derivative is a powerful tool for significantly constraining binary systems driven by GWs, and that their high GW strain will aid in fully characterizing them with the future space-based GW detectors. We make remarks on the thus-far observed population of binaries below  $\sim 15$  minutes. In Section 5 we make concluding remarks and suggest directions for future work.

## 2. Methods and Observations

### 2.1. High-speed Photometry and Phase-coherent Timing

The sources presented in this work were discovered by a bulk periodicity search (K. B. Burdge et al. 2020a) of data from the Zwicky Transient Facility (ZTF; E. C. Bellm et al. 2019; M. J. Graham et al. 2019; F. J. Masci et al. 2019; R. Dekany et al. 2020). We obtained high-speed photometric follow-up observations of our three targets to confirm their orbital periods and determine their timing solutions. We used four high-speed photometers: HiPERCAM, ULTRACAM, CHIMERA, and Lightspeed. HiPERCAM (V. S. Dhillon et al. 2021) is a frame-transfer, quintuple-beam imager on the 10.4 m Gran Telescopio



**Figure 1.** LRIS optical spectra (blue and red arms separated) of new ultracompact binaries, plus archival spectra of ES Cet (K. Bąkowska et al. 2021) scaled by an arbitrary normalization constant for ease of comparison. All systems are dominated by double-peaked emission lines of ionized helium, nitrogen, and neon from the accretion disk. The offsets in normalization across the red and blue arms are due to flux-calibration systematic error.

Canarias (GTC) at Roque de los Muchachos Observatory, which can simultaneously image in the  $u_s/g_s/r_s/i_s/z_s$  bands at rates  $>1$  kHz. ULTRACAM (V. S. Dhillon et al. 2007) is a three-channel high-speed photometer mounted on the 3.5 m New Technology Telescope at La Silla Observatory. CHIMERA (L. K. Harding et al. 2016) is a two-channel photometer on the 200 inch Hale telescope at Palomar Observatory. Lightspeed is a high-speed imager under construction for the Magellan telescopes (K. Burdge 2025, in preparation). We obtained 0.6 hr of observations using the Lightspeed camera while it was being tested on the 200 inch Hale telescope at Palomar observatory. The camera is Hamamatsu’s qCMOS sensor, which offers deeply subelectron readout noise, making it possible to obtain higher time resolution observations of J0546 without paying a prohibitive readout noise penalty. We calibrated the absolute timing solution of Lightspeed using a pulse per second signal from a GPS, and have ensured that it is stable to microsecond precision (and we verified this using observations of the Crab Pulsar). The camera’s first exposure is time tagged by a GPS reference card, and we use timestamps from the internal clock to compute the timestamps of each exposure.

All instruments were operated in frame-transfer mode to minimize the readout time between exposures. ZTF J0546+3843 and ZTF J1858–2024 also fell within ZTF Deep-Drill fields, i.e., they each have  $\sim 100$  photometric measurements within a span of three nights; this higher-than-usual cadence allowed us to use these data as an independent timing epoch without significant decoherence. All HiPERCAM and ULTRACAM data were reduced using the HiPERCAM reduction pipeline,<sup>20</sup> while the CHIMERA and Lightspeed data were reduced with a custom aperture photometry pipeline. Appendix A contains a full observations log listing the dates of observation, instruments used, filters, exposure times, and total exposure lengths. The unique instrument capabilities of rapid exposures ( $<10$  s) and no dead-time between exposures were pivotal in determining eclipse mid-times with sufficient precision to test for long-term period changes.

Timing solutions were obtained by first fitting the single epoch with highest signal-to-noise ratio with a five-term Fourier model, which was the minimum needed to fit the overall light-curve profile without overfitting the accretion-induced variability. We used Fourier frequencies corresponding to the first five harmonics of the orbital frequency. We then applied this model to each epoch to determine the eclipse times,

then fit a timing model using the nested sampling package UltraNest (J. Buchner 2021). Except in ZTF J0425+3858 (where the data are significantly sparser than the two shorter-period systems), clear deviations from a constant period were apparent, so we expanded quadratically around the initial best-fit period to account for a period derivative term:

$$\phi(t) = f_0(t - t_0) + \frac{1}{2}\dot{f}_0(t - t_0)^2 + \dots, \quad (2)$$

where  $\phi(t)$  is the orbital phase at a given time;  $t_0$  is some reference epoch;  $f_0 = P_0^{-1}$  is the orbital frequency at  $t_0$ ; and  $\dot{f}_0 = -\dot{P}_0 P_0^{-2}$  is the frequency derivative, assumed to be constant in time. We defer the measurement of higher-order terms, e.g.,  $\ddot{f}$ , to future work with a longer timing baseline.

## 2.2. Spectroscopic Follow-up

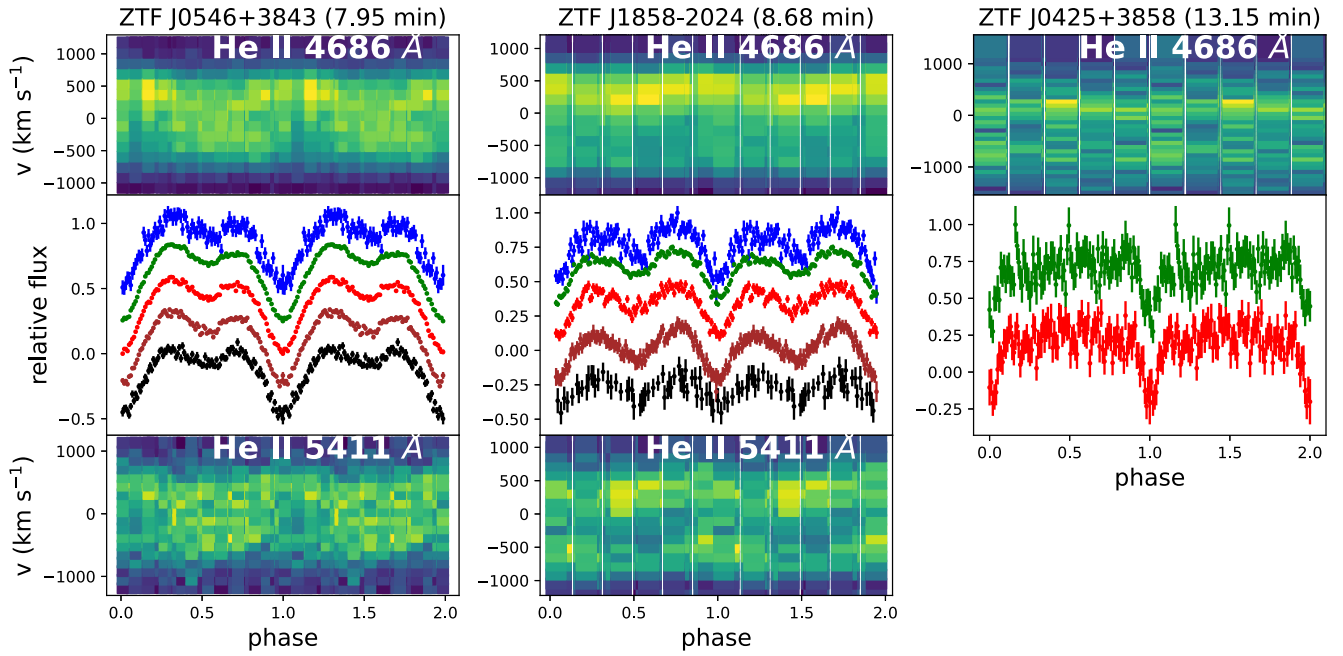
We obtained spectroscopic follow-up (Figure 1) with the Low Resolution Imaging Spectrometer (LRIS; J. B. Oke et al. 1995) on the 10 m W.M. Keck I Telescope at Maunakea Observatory, which we reduced using the `lpipe` pipeline version 2020.09 (D. A. Perley 2019). Observations were made with the  $1 \times 175''$  long slitmask, the clear filter, 60 s exposures, and  $2 \times 2$  CCD binning. For the red arm, we used the 300/5000 grism, and for the blue arm, we used 600/4000. We obtained spectra of ZTF J0546+3843 on 2020 December 10; ZTF J1858–2024 on 2023 April 20; and ZTF J0425+3858 on 2022 August 26. We computed orbital phases by correcting for the period derivatives, then plotted trailed spectra from the LRIS data by phase-folding the barycenter-corrected, time-resolved spectra (Figure 2).

In addition to optical spectroscopy, we obtained a far-ultraviolet (FUV) spectrum of the shortest-period system in the sample of AM CVns, ZTF J0546+3843, using the Space Telescope Imaging Spectrograph (STIS) aboard the Hubble Space Telescope (HST). We used the G140L grating mode  $52 \times 2$  aperture. The observations were taken on 2022 October 7 (PI: Burdge, proposal ID 16689). We compare our FUV spectrum to that of ES Cet, taken from the International Ultraviolet Explorer (IUE) archive<sup>21</sup> (Figure 3). To our knowledge, this is the first published UV spectrum of ES Cet. We fit both UV spectra with a power-law continuum model, plus Lorentzian line profiles to obtain fluxes (or upper

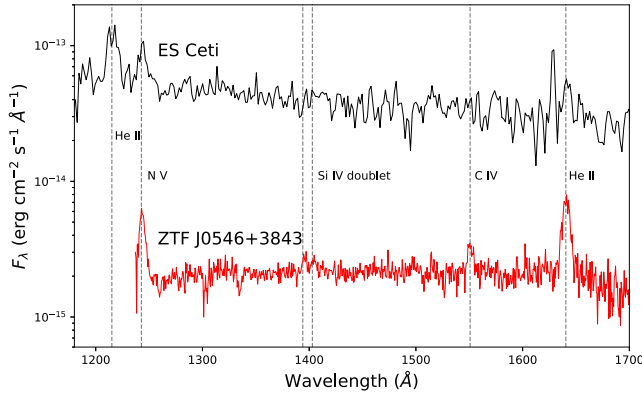
<sup>20</sup> <https://cygnus.astro.warwick.ac.uk/phsaap/hipercam/docs/html/>

<sup>21</sup> <https://archive.stsci.edu/iue/>





**Figure 2.** Top and bottom panels: trailed spectra (continuum-subtracted) of the He II 4686 and 5411 Å emission lines that might show S-wave variability at the orbital period. The orbital cycle is plotted twice. All spectra were taken with the LRIS instrument on Keck. Middle panels: phase-folded light curves in different filters. The pictured light curves of ZTF J0546+3843 and ZTF J1858–2024 were taken with HiPERCAM ( $u_s/g_s/r_s/i_s/z_s$  filters from top to bottom), while ZTF J0425+3858 was observed with CHIMERA ( $g/r$ ). Different bands are offset for visual clarity.



**Figure 3.** A comparison of the UV spectra of ZTF J0546+3843 (HST STIS) and ES Cet (IUE). Both objects exhibit detectable nitrogen and helium features (though the strength of the nitrogen emission lines relative to helium is much larger in ES Cet). The carbon emission line visible in the spectrum of ZTF J0546+3843 is notably absent in the spectrum of ES Cet.

limits) for the lines of ionized helium, carbon, silicon, and nitrogen commonly observed in accreting white dwarfs.

### 2.3. X-Ray Upper Limits with Swift/XRT

We obtained upper limits on the X-ray flux using the Neil Gehrels Swift Observatory (N. Gehrels et al. 2004) X-ray Telescope (XRT) instrument. Upper limits were computed from the Swift Living X-ray Point Source Catalog<sup>22</sup> (P. A. Evans et al. 2023), then converted from counts  $s^{-1}$  to energy units by assuming a 1 keV blackbody spectrum (motivated by the X-ray spectrum of the 10.3 minutes orbital period AM CVn ES Cet; T. E. Strohmayer 2004a). The upper limits are reported in Table 1, and are of the order of  $10^{-13}$  erg  $cm^{-2}$   $s^{-1}$ .

This is a surprisingly deep nondetection of X-rays. Assuming that matter falls from the inner Lagrange point (L1) to the boundary layer of the accretor, and that half of its gravitational potential energy is dissipated in the accretion disk, the emitted X-ray luminosity ( $L_X$ ) is:

$$L_X \approx \frac{GM_1\dot{M}}{2R_1} \left(1 - \frac{R_1}{R_{L1}}\right) \quad (3)$$

where  $M_1$  is the accretor mass,  $R_1$  is the donor radius,  $R_{L1}$  is the donor Roche lobe radius, and  $\dot{M}$  is the mass accretion rate. Rearranging to yield  $\dot{M}$  for an observed X-ray flux gives:

$$\dot{M} \approx 3 \times 10^{-11} M_\odot \text{ yr}^{-1} \times \left(\frac{F_X}{10^{-13} \text{ cgs}}\right) \times \left(\frac{d}{3 \text{ kpc}}\right)^2 \times \left(\frac{R_1}{0.01 R_\odot}\right) \times \left(\frac{M_1}{0.8 M_\odot}\right)^{-1} \times \left(1 - \frac{R_1}{R_{L1}}\right)^{-1}. \quad (4)$$

This is 3–4 orders of magnitudes smaller than the  $\dot{M}$  typical of ultracompact binaries at such short orbital periods. We are left to conclude that either (1) the X-ray flux in our systems is significantly obscured, perhaps by the inner disk or foreground ISM absorption, which is particularly severe for small blackbody temperatures  $\lesssim 100$  eV; or (2) only a very small fraction of the total accretion luminosity is even released in X-rays, for reasons not understood. A similar magnitude discrepancy was also found in ES Cet (T. E. Strohmayer 2004a) and most AM CVn systems below 30 minutes (T. Begari & T. J. Maccarone 2023), meaning this tension is a common feature of the shortest-period disk accretors.

## 3. Results

### 3.1. Optical Photometry and Spectroscopy

In Figure 1 we show optical spectra of the three new ultracompact binaries ZTF J0546+3843, ZTF J1858–2024, and

<sup>22</sup> <https://www.swift.ac.uk/LSXPS/>

**Table 1**  
System Parameters for the Three Sources

Name	$P_0$ (min)	R.A. (J2000.0) (deg)	Decl. (J2000.0) (deg)	Distance (est.) (pc)	Optical Mag. ( $L_{\text{opt}}$ ) [ $L_{\text{AB}}$ (erg s $^{-1}$ )]	$F_X$ ( $L_X$ ) [erg s $^{-1}$ cm $^{-2}$ (erg s $^{-1}$ )]
ZTF J0546+3843	7.94691(1)	86.6142	38.7204	$3707^{+1631}_{-1258}$	$19.31 \pm 0.0068$ ( $2.55^{+2.7}_{-1.4} \times 10^{33}$ )	$< 2.1 \times 10^{-13}$ ( $< 2.11^{+3.7}_{-1.9} \times 10^{32}$ )
ZTF J1858–2024	8.67990(1)	284.5248	–20.4135	$2895^{+2733}_{-1449}$	$19.37 \pm 0.012$ ( $2.03^{+5.6}_{-1.5} \times 10^{33}$ )	$< 1.1 \times 10^{-13}$ ( $< 1.10^{+3.1}_{-0.83} \times 10^{32}$ )
ZTF J0425+3858	13.154(1)	66.4592	38.9827	...	$21.62 \pm 0.19$	$< 1.3 \times 10^{-13}$

**Note.** Geometric distances derived from Gaia Data Release 3 are quoted from C. A. L. Bailer-Jones et al. (2021). The g-band optical magnitudes are quoted from Gaia DR3 for ZTF J0546+3843 and ZTF J1858–2024, and ZTF for ZTF J0425+3858. Optical luminosities are calculated by integrating a power-law fit to the flux-calibrated LRIS spectra from 3000–10,000 Å. X-ray flux upper limits were obtained via Swift Target-of-Opportunity observations.

ZTF J0425+3858. All three systems are dominated by strong Keplerian profiles of doubly ionized He, N, and Ne, as well as weak He I emission, indicating a hot, optically thin accretion disk. These lines are all labeled in Figure 1.

From our photometric follow-up, we find orbital periods of 7.95, 8.68, and 13.15 minutes, which we report alongside the optical X-ray fluxes/upper limits in Table 1. In Figure 2 we show the photometric data phase-folded on the orbital periods in different bands. All systems show significant variability in flux, by 40%–60% through each orbit. While these sources are too faint to have robust parallax measurements with Gaia (Gaia Collaboration et al. 2016), we quote the geometric distance estimates (where available) from C. A. L. Bailer-Jones et al. (2021). ZTF J0425+3858 was too faint for even a Gaia detection, so we have no distance estimate.

Figure 2 also shows the optical spectra in a phase-resolved sequence (trailed spectra), for the strongest emission lines (He II 4686 Å and He II 5411 Å). One feature in the trailed spectra is the presence of sinusoidal trails of brightness peaks and troughs offset from the line centroid at zero velocity, known as *S*-wave signatures (though the feature is less clear in the lower-quality spectrum of ZTF J0425+3858). *S*-waves are induced by the corotation of the disk-impact/bright-spot region near the outer disk edge with the binary orbit (J. Smak 1985), and they constitute the most robust evidence that the photometric period is indeed the orbital period of these systems.

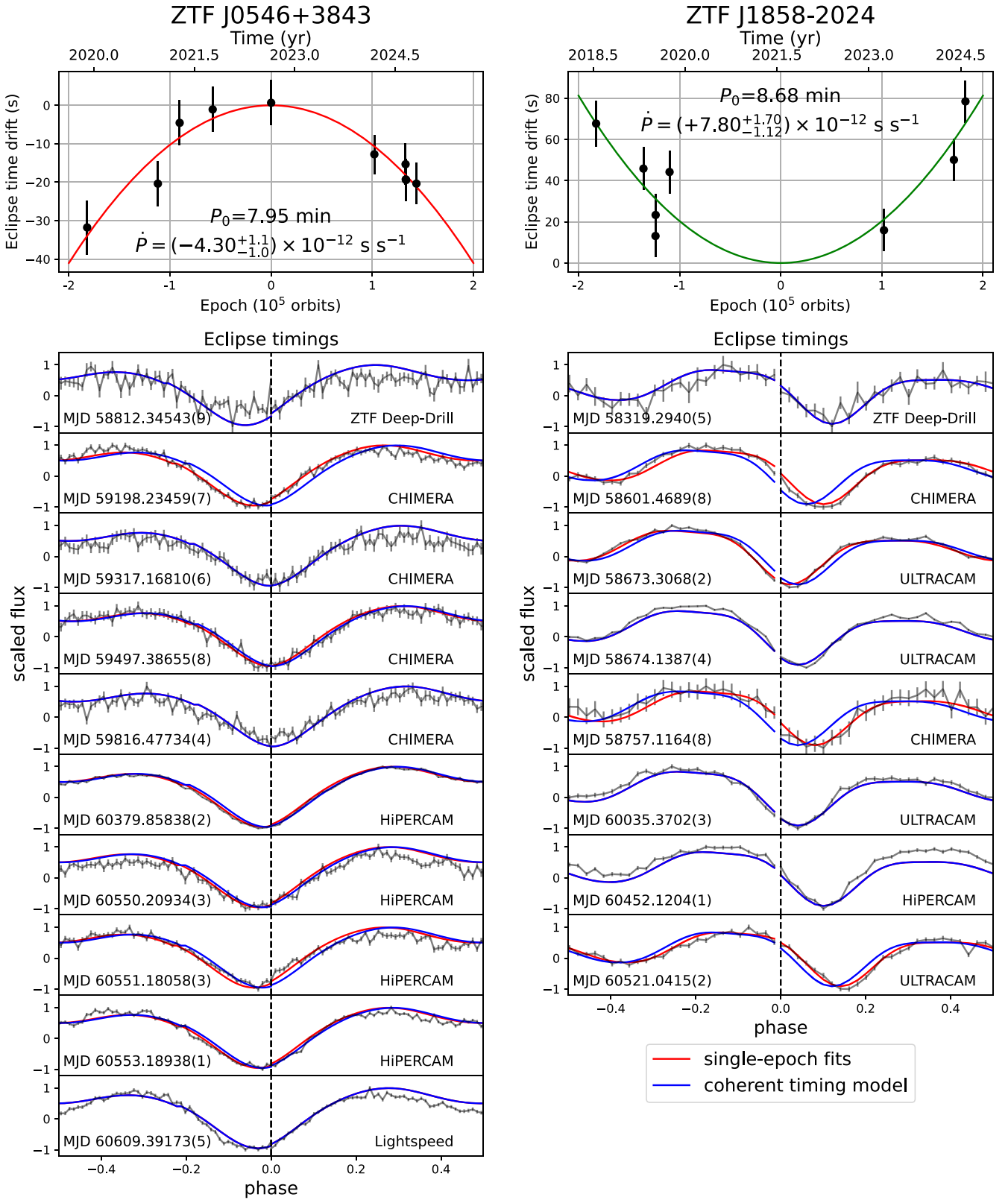
While it is tempting to proceed by measuring emission-line radial velocities (RVs), the presence of a disk significantly complicates our ability to infer physical properties of the systems from RVs. They would be contaminated by the uncertain dynamics of the accretion disk and bright spot, and it is unclear which emission components contribute most strongly to the observed Doppler shifts. Then, too, it is uncertain which radii within the disk dominate the contribution to the Keplerian line profile; directly translating measured RVs to system parameters of interest is thus unfeasibly complicated (though some limits could be obtained using Doppler tomography, which would require significantly higher-quality spectra than present). Not all hope is lost, as we can still significantly constrain the physical properties of systems by arguments related to their ultracompact orbits (Section 4.2), and even further in the two systems with direct measurements of  $\dot{P}$  (Section 4.3).

### 3.2. Ultraviolet Spectroscopy

For ZTF J0546+3843, we also obtained an HST STIS UV spectrum, which is shown in Figure 3 in comparison to the spectrum of ES Cet. The UV spectra of both objects show emission lines of He II and N V. In ZTF J0546+3843, we also detect Si IV and C IV, the latter of which is particularly interesting as a direct measure of the degree of CNO processing the donor has undergone (Section 4.1). We note that our spectrum loses signal around 1250 Å, so we are insensitive to the detection of Ly $\alpha$ , which was detected in the inspiraling system HM Cnc (J. Munday et al. 2023). From the UV lines of N and C, we infer an N V/C IV line ratio of 2.3 in ZTF J0546+3843, compared to a lower limit of N V/C IV  $> 5.6$  in ES Cet (we can only quote a lower limit, as C IV was not detected in ES Cet). It is surprising that the optical spectrum of ZTF J0546+3843 appears identical to that of ES Cet (K. Bąkowska et al. 2021), yet lines uniquely accessible in the UV reveal differing chemical abundances. This emphasizes the importance of far-UV spectroscopy in distinguishing AM CVn evolutionary stages and channels, and the need for future UV spectroscopy missions such as UVEX (S. R. Kulkarni et al. 2021) and CASTOR (P. Cote et al. 2019).

### 3.3. Long-term Timing Results

In Figure 4 we show the *O*–*C* diagrams corresponding to our best-fit timing solutions for the 7.9 and 8.7 minute systems. We infer  $t_0 = 59816.4773(1)$  MJD,  $P_0 = 7.94691(5)$  minutes, and  $\dot{P} = (-4.30^{+1.1}_{-1.0}) \times 10^{-12}$  s s $^{-1}$  for ZTF J0546+3843; and  $t_0 = 59420.0012(1)$  MJD,  $P_0 = 8.67990(3)$  minutes, and  $\dot{P} = (+7.80^{+1.70}_{-1.12}) \times 10^{-12}$  s s $^{-1}$  for ZTF J1858–2024. It is noteworthy that the period derivatives have opposite signs, despite similar optical spectra and orbital periods. The inspiral seen in ZTF J0546+3843 is driven by the familiar effects of GR: gravitational waves remove angular momentum from the system, shrinking the binary orbit. The physical driver of the expanding orbit of ZTF J1858–2024 is less obvious. This is an effect seen directly in only one other ultracompact binary so far (E. de Miguel et al. 2018), though it is expected to happen eventually in every AM CVn as a consequence of angular momentum conservation during mass transfer from a low-mass donor to a high-mass accretor (see Section 4.3 for details). Thus, in the standard evolutionary picture, initially the outermost high-entropy layers are stripped, tending to produce contraction and negative  $\dot{P}$ . This is gradually



**Figure 4.** Top panels: *O-C* diagrams for ZTF J0546+3843 (left) and ZTF J1858-2024 (right). Bottom panels: phase folds with a fixed  $P_0$ , with eclipse times and instruments noted for each epoch. The eclipse time drifts by  $\sim 0.1\text{--}0.15P$  over the baseline. We overplot the predicted waveforms from our coherent timing models (blue), as well as the single-epoch fits used to construct the *O-C* diagrams. The 5–10 s discrepancies are likely dominated by timing jitter due to accretion (see Section 3.3).

dominated by the expansion of the underlying layers, causing the donor to expand and the system to outspiral (C. J. Deloye et al. 2007).

In Figure 4, we see that the coherent timing models (blue) are not always a perfect match to the epoch-by-epoch phase files (black data points and red models). This is likely due to

**Table 2**

Integrated Far-UV Emission Line Fluxes for ZTF J0546+3843 (HST STIS) and ES Cet (IUE) Derived from the Spectra Displayed in Figure 3

Far-ultraviolet Emission Line Fluxes		
Line	ZTF J0546 (7.9 minutes) $10^{-15} \text{ erg s}^{-1} \text{ cm}^{-2}$	ES Cet (10.3 minutes) $10^{-14} \text{ erg s}^{-1} \text{ cm}^{-2}$
N V 1242.8 Å	$25.7 \pm 0.6$	$27.6 \pm 1.8$
Si IV 1393.8 Å	$4.18 \pm 0.9$	$<1.8$
Si IV 1402.8 Å	$6.04 \pm 1.3$	$<4.3$
C IV 1550.8 Å	$11.4 \pm 0.7$	$<5.0$
He II 1640.5 Å	$47.5 \pm 0.7$	$22.3 \pm 2.7$

the optical emission being dominated by the accretion disk: as a result, short-term changes in the accretion flow (flicker noise) can result in the center of light shifting by  $\sim 5\%$ – $10\%$  of the orbital period (E. de Miguel et al. 2018; J. Munday et al. 2023). However, the magnitude of this flickering effect is extremely unlikely to explain the long-term trend of 40–80 s drift in the eclipse timings caused by period evolution (Figure 4).

#### 4. Discussion

##### 4.1. Spectroscopic Properties and Evolutionary Channels

As reviewed in Section 1, the chemical abundances of AM CVns carry imprints of their formation channels, in particular the differences in C/O, N/O, and N/C ratios due to donors that have undergone varying levels of He and CNO fusion (G. Nelemans et al. 2010). To this end, far-ultraviolet (FUV) spectroscopy is particularly rewarding, as the highest density of diagnostic metal-line transitions resides in the FUV. Following the approach of T. R. Marsh et al. (1995) and B. T. Gänsicke et al. (2003), we use the ratio of N V/C IV as a diagnostic of CNO processing rather than directly fitting for the N/C or N/He ratios, which would require full LTE modeling, which is beyond the scope of this work.

We measured a line ratio  $\text{N V/C IV} = 2.3$  in ZTF J0546+3843 and  $\text{N V/C IV} > 5.6$  in ES Cet (Figure 3, Table 2). For comparison, typical long-period CVs show  $\text{N V/C IV} \approx 0.3$ . FUV spectroscopy of ultracompact binaries is sparse, but as an example, the 46 minute system GP Com shows a significantly higher  $\text{N V/C IV} = 10$  (T. R. Marsh et al. 1995). The donor in ZTF J0546+3843 has thus undergone significantly more CNO processing than typical CVs with  $P \gtrsim 80$  minutes, but slightly less than the longer-period GP Com and ES Cet.

Modest variations in the equilibrium CNO abundances from fusion are expected for different main-sequence progenitors of the WD donors in these systems. Moreover, gravitational settling will tend to stratify the CNO-burning products within the WD core itself, meaning donors that have been transferring mass for longer (and are therefore more stripped) can show changes in N/C ratio over their lifetimes. The lower N/C measurement in ZTF J0546+3843 therefore does not necessarily mean it descended from the He star channel. Most problematically, such systems are expected to reach period minima around 9–11 minutes (L. R. Yungelson 2008), slightly longer than the 7.95 minute orbital period observed in the system. We speculate the ZTF J0546+3843 descends from an He WD donor whose main-sequence progenitor was less massive than that of ES Cet or GP Com, and also less stripped, as it is earlier in its mass-transferring lifetime (inspiral rather than outspiral phase).

Our ability to make similar inferences for ZTF J1858–2024 and ZTF J0425+3858 is limited by our lack of UV spectra of those sources. Our results tentatively support the idea that AM CVns showing positive  $\dot{P}$  preferentially exhibit greater N/C abundances than those with negative  $\dot{P}$ , in part due to gradual stripping of the donor via mass transfer. This speculation can be confirmed by obtaining high-resolution UV spectroscopy of ZTF J1858–2024, which is known to be outspiral, thus must be more evolved than ZTF J0546+3843.

The extreme similarity between the optical spectra of the inspiraling system ZTF J0546+3843, and the outspiral systems ZTF J1858–2024 and ES Cet, is surprising, especially given the nondetection of H in ZTF J0546+3843. Evolutionary models of double white dwarfs typically assume the initial inspiral phase after mass-transfer contact consists primarily of stripping the thin, thermally inflated H/He envelope remaining on the He WD surface from the progenitor main-sequence star (F. D’Antona et al. 2006; C. J. Deloye et al. 2007; D. L. Kaplan et al. 2012; T. L. S. Wong & L. Bildsten 2021; H.-L. Chen et al. 2022). This layer is nondegenerate, and it contracts upon mass loss, which allows the donor radius to shrink rapidly as the system undergoes orbital decay. Eventually, the H/He shell is depleted, leaving only the degenerate core, which expands upon mass loss resulting in a net positive  $\dot{P}$ .

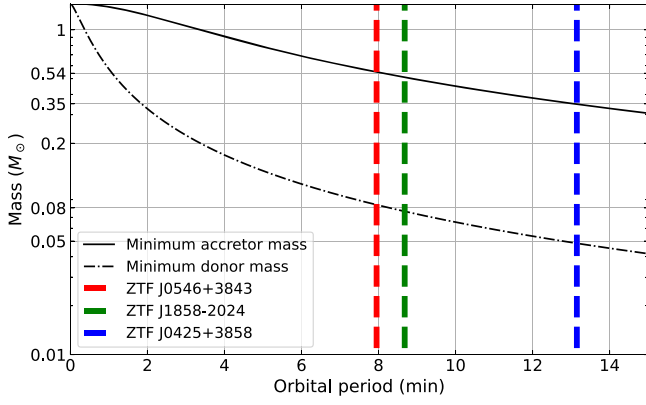
ZTF J0546+3843 complicates this picture, showing both a negative  $\dot{P}$  and no H. One clue toward an explanation comes from considering the double WD evolutionary models of D. L. Kaplan et al. (2012): their Equation (10) finds that  $\dot{P}_{\text{in}}$  for inspiraling systems prior to period minimum and turnaround should be approximately  $-1.7 \times 10^{-11} \text{ s s}^{-1}$  (for  $P = 7.95$  minutes, and assuming typical donor/accretor masses of  $0.15/0.8 M_{\odot}$ ). This is  $>35\sigma$  larger in magnitude than our measured  $\dot{P} = -4.30^{+1.1}_{-1.0} \times 10^{-12} \text{ s s}^{-1}$ , leading us to speculate that ZTF J0546+3843 is well past its loss of an H envelope and nearly turning around to a positive  $\dot{P}$ . In this scenario, most of the H shell must have already been stripped, resulting in an extremely low surface H abundance resulting in the nondetection.

##### 4.2. Mass Constraints Based on Period

As discussed in Section 4.1, it is difficult to make informed conclusions about the donor or accretor masses because the optical emission is entirely dominated by the accretion disks in all of these systems. However, we can still make some inferences to place strict lower limits, and make some estimates, on the possible accretor and donor masses.

Accretor mass bound: Observing the presence of an accretion disk in a system (via double-peaked line profiles) means that a system is not undergoing direct-impact accretion. In other words, the radius of the accretor must be small enough that the ballistic trajectory of the accretion stream through the first Lagrange point (L1) does not intersect the accretor outer radius. This upper bound on the radius translates to a lower bound on the mass, which is given by assuming a zero-temperature electron-degenerate equation of state (an arbitrarily more massive white dwarf could attain the same radius by having a nonzero temperature.) We use Equation (6) of G. Nelemans et al. (2001) to estimate this maximum accretor





**Figure 5.** Minimum mass bounds for disk-accreting systems as a function of orbital period, computed by the argument outlined in Section 4.2. For the relevant orbital periods of 7.95, 8.68, and 13.15 minutes, we obtain minimum donor/accretor masses of 0.084/0.54, 0.076/0.51, and 0.048/0.35  $M_\odot$ , respectively.

radius in units of the orbital separation:

$$\frac{R_1}{a} \lesssim 0.04948 - 0.03815 \log(q) + 0.04752 \log^2(q) - 0.006973 \log^3(q), \quad (5)$$

where  $q = M_2/M_1$  is the mass ratio for donor and accretor masses of  $M_2$  and  $M_1$ , respectively. We then cite the zero-temperature white dwarf mass–radius relation quoted by F. Verbunt & S. Rappaport (1988):

$$\frac{R}{R_\odot} = 0.0114 \left[ \left( \frac{M}{M_{\text{Ch}}} \right)^{-2/3} - \left( \frac{M}{M_{\text{Ch}}} \right)^{2/3} \right]^{1/2} \times \left[ 1 + 3.5 \left( \frac{M}{M_p} \right)^{-2/3} + \left( \frac{M}{M_p} \right)^{-1} \right]^{-2/3}, \quad (6)$$

where  $M$  is the accretor mass,  $M_{\text{Ch}}$  denotes the Chandrasekhar limit for the mass of a white dwarf, which is  $1.44 M_\odot$ , and  $M_p$  is a constant with a value of  $0.00057 M_\odot$ , to convert this to an accretor mass constraint (see F. Verbunt & S. Rappaport 1988). We emphasize that although white dwarfs realized in nature deviate significantly from the zero-temperature relation (e.g., Figure 11 of M. J. Green et al. 2018b; Figure 12 of J. van Roestel et al. 2022), our purpose in quoting it here is for an absolute physically allowed lower bound. Attempting to fit a lower-mass object into this orbit is guaranteed to result in direct-impact, rather than disk, accretion.

**Donor mass bound:** For the donor mass, we can use the relation of P. P. Eggleton (1983), in a simplified form valid for the relevant mass-ratio range of CVs ( $0.01 \lesssim q \lesssim 1$ ):

$$P_{\text{RLO}} \approx 6.192 \text{ minutes} \times \left( \frac{\rho}{10^4 \text{ g cm}^{-3}} \right)^{-1/2}, \quad (7)$$

where  $P_{\text{RLO}}$  is the orbital period at which an object of mean density  $\rho$  overflows its Roche lobe. Again assuming the zero-temperature equation of state quoted above gives the minimum possible mass to attain this density.

We applied these constraints to the orbital periods of our systems. The results are illustrated in Figure 5. These yield, for the orbital periods of 7.95, 8.68, and 13.15 minutes, firm lower

limits on the minimum donor/accretor masses of 0.084/0.54, 0.076/0.51, and 0.048/0.35  $M_\odot$ , respectively.

#### 4.3. Further Constraints Based on $\dot{P}$

The direct measurement of the orbital period first derivative,  $\dot{P}$  (Figure 4), is a valuable tool. As an instructive example of how it can significantly constrain the properties of an accreting binary system where angular momentum loss is driven by the well-understood properties of gravitational radiation, we outline the following arguments for ZTF J0546+3843 and ZTF J1858–2024.

Expressing the orbital period of the system in terms of its angular momentum ( $J$ ) and component masses,

$$P = J^3 (M_1 + M_2) (M_1 M_2)^{-3} \left( \frac{2\pi}{G^2} \right), \quad (8)$$

taking the logarithmic derivative, and assuming approximately steady-state conservative mass transfer ( $\dot{M}_1 = -\dot{M}_2 \equiv \dot{M}$ , where  $\dot{M}$  is strictly positive) yields:

$$\frac{\dot{P}}{P} = 3 \left[ \frac{\dot{J}}{J} + \frac{\dot{M}}{M_2} (1 - q) \right]. \quad (9)$$

The rate of change in orbital angular momentum is driven by three effects: gravitational radiation, angular momentum loss in the mass-transfer stream, and tidal coupling of the accretor/disk/donor, which scales with the difference between accretor spin angular momentum and binary orbital angular momentum (T. R. Marsh et al. 2004). In the presence of a radially extended accretion disk (as opposed to a direct-impact stream), it is generally assumed that tidal coupling is efficient, so that the accretor spin is kept close to the orbital frequency, and the angular momentum lost in the accretion stream is quickly returned to the orbit (F. Verbunt & S. Rappaport 1988; J. Frank et al. 2002). In this case, the angular momentum evolution of the system is set entirely by gravitational-wave emission ( $\dot{J} = \dot{J}_{\text{GR}}$ ). We quote the standard expression for  $\dot{J}_{\text{GR}}$  in an inspiraling binary system (P. C. Peters 1964):

$$\left( \frac{\dot{J}}{J} \right)_{\text{GR}} = -\frac{32}{5} \frac{G^{5/3} M_1 M_2}{c^5 (M_1 + M_2)^{1/3}} \left( \frac{2\pi}{P} \right)^{8/3} \quad (10)$$

$$= -\frac{32}{5} \left( \frac{G M_c}{c^3} \right)^{5/3} \left( \frac{2\pi}{P} \right)^{8/3}. \quad (11)$$

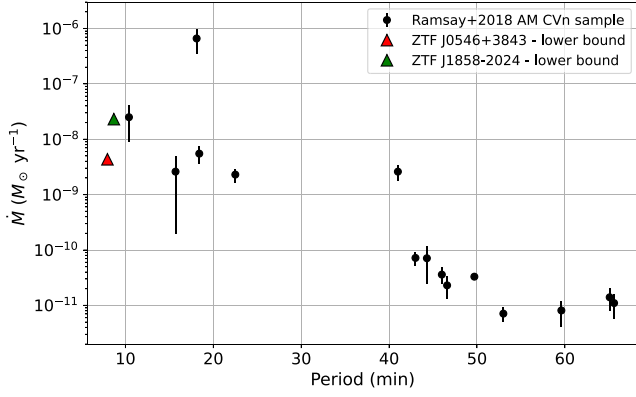
Thus, the inferred mass transfer rate for a disk-accreting system is:

$$|\dot{M}| = \frac{M_2}{1 - q} \left[ \frac{\dot{P}}{3P} - \left( \frac{\dot{J}}{J} \right)_{\text{GR}} \right]. \quad (12)$$

This is already a useful result: using the strict lower bounds on  $M_1$ ,  $M_2$  (Figure 5) and the measured values of  $P/\dot{P}$  (Figure 4) yields approximate lower bounds of  $\dot{M} \gtrsim 4.3 \times 10^{-9} M_\odot \text{ yr}^{-1}$  to  $2.5 \times 10^{-8} M_\odot \text{ yr}^{-1}$  for ZTF J0546+3843/ZTF J1858–2024, respectively. These are reasonable values compared to extrapolation from systems at similar orbital periods, which we illustrate in Figure 6.

We can further eliminate the  $\dot{M}$ -dependence of Equation (9) by considering the response of the donor star to mass loss. We begin by assuming steady-state contact of the donor with its





**Figure 6.** Orbital period vs.  $\dot{M}$  for AM CVns. G. Ramsay et al. (2018) obtained their values by fitting UV-optical-IR spectral energy distributions. The lower bounds for ZTF J1858–2024 and ZTF J0546+3843 were obtained by using the lowest allowable masses (via the argument in Section 4.2) and Equation (12).

Roche lobe, meaning  $R_2 = R_L$  at all times (where  $R_L$  denotes the Roche lobe radius). For simplicity, we use the B. Paczyński (1971) result for  $R_L$ ,

$$\frac{R_L}{a} = 0.46 \left( \frac{M_2}{M_1 + M_2} \right)^{1/3}, \quad (13)$$

where  $a$  is the binary semimajor axis. We take the logarithmic derivative of Equation (13), replace  $R_L = R_2$ , express  $a$  in terms of  $P$ , and assume conservative mass transfer ( $\dot{M}_1 + \dot{M}_2 = 0$ ) to obtain:

$$\frac{2\dot{P}}{3P} - \frac{|\dot{M}|}{3M_2} = \left( \frac{\dot{R}_2}{R_2} \right) = \left( \frac{\dot{R}_2}{R_2} \right)_{\text{ad}} + \left( \frac{\dot{R}_2}{R_2} \right)_{\text{evol}}. \quad (14)$$

On the right hand, we split  $(\dot{R}_2/R_2)$  into a portion describing the adiabatic (short-term) response of the donor to mass loss, and a portion describing the long-term radius evolution of the donor star driven by thermal contraction and/or nuclear burning. We define the adiabatic response in terms of the index  $\xi_{\text{ad}}$ :

$$\xi_{\text{ad}} \equiv \left. \frac{d(\ln R_2)}{d(\ln M_2)} \right|_{\text{ad}} = \left. \frac{M_2}{R_2} \frac{dR_2}{dM_2} \right|_{\text{ad}} = - \left( \frac{\dot{M}}{M_2} \right)^{-1} \left( \frac{\dot{R}_2}{R_2} \right)_{\text{ad}}, \quad (15)$$

which, for low-mass white dwarfs, is very near  $-1/3$ . We also cast the longer-term evolution in terms of a dimensionless parameter:

$$\chi_{\text{evol}} \equiv \frac{\tau_{\text{GR}}}{\tau_{\text{evol}}} = \frac{(\dot{R}_2/R_2)_{\text{evol}}}{(\dot{J}/J)_{\text{GR}}}, \quad (16)$$

which compares the donor thermal/nuclear contraction rate to the gravitational-wave-driven orbital evolution rate.  $\chi_{\text{evol}} \ll 1$  corresponds to systems in which the GR decay is much faster than the donor evolution due to thermal contraction/nuclear burning (e.g., LIGO mergers), and  $\chi_{\text{evol}} \gg 1$  corresponds to systems where the donor contraction quickly brings the system out of Roche lobe contact.

Plugging Equations (15) and (16) into Equation (14), subtracting from Equation (9) to eliminate the

$\dot{M}/M_2$ -dependence, and writing the final result in terms of  $\xi_{\text{ad}}$  and  $\chi_{\text{evol}}$  gives:

$$\left( \frac{\dot{P}}{P} \right)_{\text{eq}} = 3 \left( \frac{\dot{J}}{J} \right)_{\text{GW}} \left[ \frac{\xi_{\text{ad}} + \chi_{\text{evol}}(1 - q) - 1/3}{\xi_{\text{ad}} + 5/3 - 2q} \right]. \quad (17)$$

This result expresses the observable quantity  $\dot{P}/P$  purely in terms of the system parameters  $\xi_{\text{ad}}$ ,  $\chi_{\text{evol}}$ ,  $M_1$ , and  $M_2$ . For mass ratios  $0 < q \lesssim 2/3$  relevant for most AM CVns, the term in brackets typically spans the range of  $-1$  to  $1$ , with a heavy skew toward positive values (orbital decay).

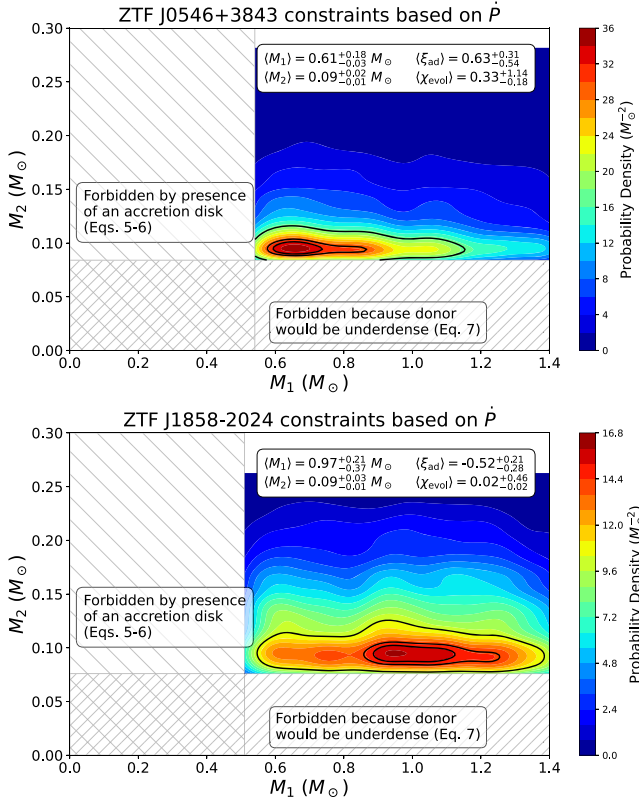
Further progressing beyond this point would involve assuming values for  $\xi_{\text{ad}}$  and/or  $\chi_{\text{evol}}$ . This is a difficult problem to solve exactly, given our uncertainty on the nature of the donors in these systems (white dwarf versus He star), as well as general uncertainty in the thermal structure and adiabatic response of degenerate/semidegenerate matter to rapid mass loss. However, we can loosely constrain the systems by exploring a large range of feasible parameters via a Monte Carlo search. We drew from a random grid of  $10^7$  combinations from:

$$M_1 \sim \mathcal{U}(M_{1,\text{min}}, M_{\text{Ch}}); \quad M_2 \sim \mathcal{U}(M_{2,\text{min}}, M_1); \\ \xi_{\text{ad}} \sim \mathcal{U}(-1, 3); \quad \chi_{\text{evol}} \sim \mathcal{U}(0, 2);$$

where  $M_{1,\text{min}}$ ,  $M_{2,\text{min}}$  are taken from Figure 5, and  $\mathcal{U}$  is the uniform distribution. We retained acceptable parameter combinations if they produced a  $\dot{P}$  within  $1\sigma$  of the measured values. We also required solutions to fill their Roche lobe, i.e.,  $R_2 = R_L$ . Here, rather than using the zero-temperature mass-radius relation (Equation (6)), we allowed thermal bloating of the donor star by up to 50% (following the finite-entropy evolutionary models of T. L. S. Wong & L. Bildsten 2021, which found that He WD donors in AM CVn can have this degree of bloating compared to the cold WD equation-of-state close to period minimum). After retaining the acceptable solutions, we used a Gaussian kernel density estimator to determine the most probable parameter combinations reproducing the observed system properties; the resulting contours for  $M_1$  and  $M_2$  are shown in Figure 7.

We obtain mass estimates of  $M_1 = 0.61^{+0.18}_{-0.03} M_\odot$  and  $M_2 = 0.09^{+0.02}_{-0.01} M_\odot$  for ZTF J0546+3843, and  $M_1 = 0.97^{+0.21}_{-0.37} M_\odot$ ,  $M_2 = 0.09^{+0.03}_{-0.01} M_\odot$ , for ZTF J1858–2042 (see Figure 5 for more detailed system parameters). As expected qualitatively, the donor in ZTF J0546+3843 must be semidegenerate ( $\xi_{\text{ad}} > 0$ ), likely a white dwarf with a small inflated envelope, for the orbit to decay (T. L. S. Wong & L. Bildsten 2021). On the other hand, the donor in ZTF J1858–2024 is consistent with the equilibrium  $\xi_{\text{ad}} = -1/3$  for a cold WD.

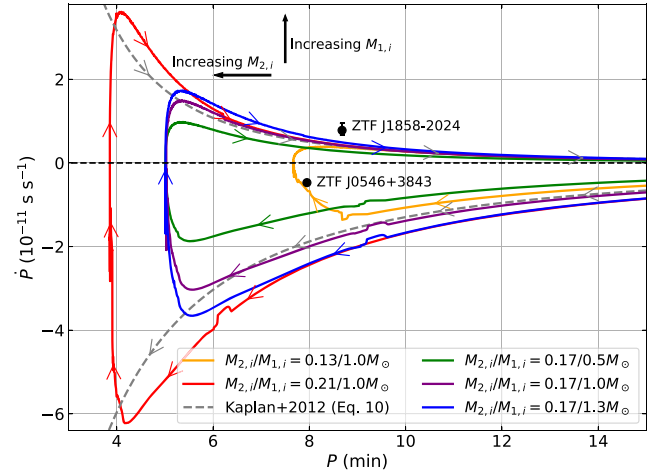
To further verify our estimates, we ran a small grid of five binary stellar evolution models using MESA (version 12115; B. Paxton et al. 2011, 2013, 2015, 2018, 2019), and also compared to literature results (D. L. Kaplan et al. 2012; H.-L. Chen et al. 2022). In our calculations, the accretor is considered as a point mass. The initial He WD models and assumptions about the mass retention efficiency are adopted from H.-L. Chen et al. (2022). For our models, we assumed initial binary parameters of  $M_{1,i} = 1.3/1.0/1.0/1.0/0.50 M_\odot$ ,  $M_{2,i} = 0.17/0.21/0.17/0.13/0.17 M_\odot$ ,  $P_{\text{orb},i} = 0.05$  days, and an initial H envelope mass of  $7 \times 10^{-3} M_\odot$  (where the subscript  $i$  indicates the initial value of a parameter; see Figure 8 for



**Figure 7.** Likelihood contours of  $M_1$  and  $M_2$  for our Monte Carlo runs based on the argument outlined in Section 4.3. Solid black lines correspond to  $1\sigma/2\sigma/3\sigma$  contours. These imply chirp masses close to  $0.3 M_\odot$  in both systems. As expected from the inward vs. outward  $\dot{P}$ , the donor of ZTF J0546+3843 is significantly less degenerate ( $\xi_{\text{ad}}$  larger) than that of ZTF J1858–2024.

details). The relatively large initial envelope mass was motivated by the recent direct detection of H in HM Cnc (J. Munday et al. 2023), suggesting that a significant residual envelope may survive all the way down to  $<10$  minutes periods. We have not explicitly verified that the entire envelope is lost by the periods measured for our systems, as we did not place upper bounds on the H fraction from our optical spectra. The purpose of our model grid is to illustrate the magnitude and direction of changing these parameters: increasing the initial donor mass results in a shorter minimum period, while increasing the initial accretor mass results in a larger overall  $|\dot{P}|$  (Figure 8). We note that the discontinuities around 6 and 9 minutes in these tracks are due to the onset of mass transfer and stripping of the H/He envelopes. The angular momentum sink of direct-impact accretion is not included in these models, as they are intended to serve as a qualitative illustration of the effects of varying  $M_1/M_2$  on the overall trajectories.

The small  $\dot{P}$  in ZTF J0546+3843 is constraining: we infer the system is likely close to its period minimum, as it should otherwise have  $\dot{P} \lesssim -1.7 \times 10^{-11} \text{ s s}^{-1}$  (our Figure 8; D. L. Kaplan et al. 2012, their Figure 6). Double WD systems that reach period minima at  $P \approx 7.9$  minutes require the lowest initial donor masses of around  $0.12\text{--}0.13 M_\odot$  ( $M_i$  cannot be much lower than this, as it is set by the He core mass at the end of the common envelope phase). Our binary evolution models find that the donor mass remains relatively constant for the entire ingoing track, and only begins to change significantly around period minimum (due to the sharp  $\dot{M}$  increase); so



**Figure 8.** Evolutionary tracks (from MESA binary modeling) of double WDs with different binary parameters. The observed  $P$  and  $\dot{P}$  in ZTF J0546+3843 are compatible with a donor of  $M_2 \lesssim 0.13 M_\odot$  close to period minimum. The large observed  $\dot{P}$  in ZTF J1858+2024 is more difficult to reconcile. In all cases, the donors initially have a hydrogen envelope mass of  $7 \times 10^{-3} M_\odot$ .

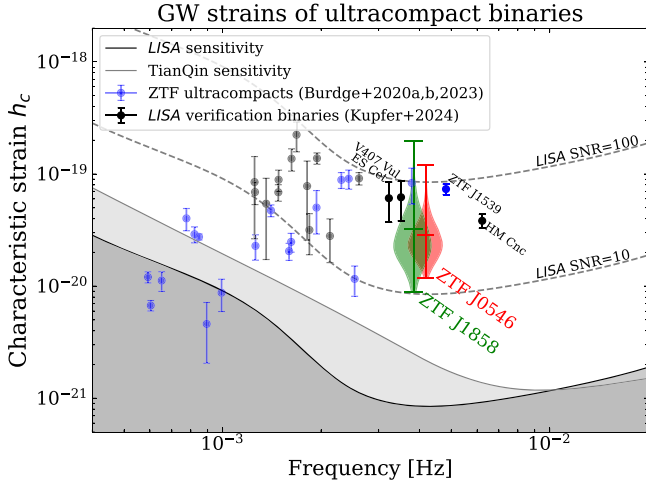
indeed, our inferred  $M_2 = 0.09^{+0.02}_{-0.01} M_\odot$  seems compatible with such a low initial mass followed by mass loss.

On the other hand, our results, and those of D. L. Kaplan et al. (2012), have difficulty reproducing the large observed  $\dot{P}$  in ZTF J1858–2024 (except for the smallest values of  $M_2$  and the largest values of  $M_1$ ). Our Equation (17) accommodates this by pushing toward unphysically small values of  $\xi_{\text{ad}} < -1/3$ , but in reality, we are uncertain exactly how the system is evolving so rapidly. It is possible that finite-entropy donors can accelerate the orbital evolution (e.g., T. L. S. Wong & L. Bildsten 2021), though whether this is a sufficiently large effect to account for the observed discrepancy is unclear. Reproducing such a large  $\dot{P}$  via binary evolutionary models is an interesting direction for future study, though observations of  $\dot{P}$  may only be expected to agree with models over longer timescales due to the finite time required for the Roche lobe and donor star radius to reach equilibrium.

#### 4.4. Accreting Ultracompact Binaries as Multimessenger GW Sources

With estimates in hand for  $M_1$ ,  $M_2$  (Section 4.3), and distance (Table 1), we can readily assess the strength of the GW emission from these systems and ask: will these sources be detectable by space-based gravitational-wave interferometers such as LISA, TianQin, and Taiji, opening up the possibility of multimessenger study? We show in Figure 9 that the answer to this question is a resounding yes. Using our  $M_1$ ,  $M_2$  distributions from Figure 7, and drawing from a uniform distance distribution enclosing the  $1\sigma$  posteriors (Table 1), we computed characteristic GW strains assuming 4 yr missions. ZTF J0546+3843 and ZTF J1858–2024 are comfortably detected, with signal-to-noise ratios  $>10$  even in pessimistic scenarios.

This prompts a discussion of what additional insights are to be gained by supplementing electromagnetic (EM) observations of ultracompact binaries, such as those presented in this paper, with a GW signal. Significant previous work has been done examining the population-level inferences made possible from a multimessenger signal (e.g., G. Nelemans et al. 2004; S. Shah et al. 2012; T. Kupfer et al. 2018); here, we instead



**Figure 9.** Violin plots of characteristic strains (over 4 yr) of ZTF J0546+3843 and ZTF J1858-2024 using the constraints from Section 4.3. We also plot the strains of several ZTF-discovered ultracompact binaries (K. B. Burdge et al. 2020a, 2020b, 2023) and LISA verification binaries (T. Kupfer et al. 2024) for comparison.

focus on how joint EM/GW observations can aid in the detailed characterization of individual systems. We first review the basic observables of a GW signal, then outline how they can allow for deeper constraints on these systems via the three key observables of (i) orbital phase, (ii) inclination, and (iii) chirp mass.

For our simplified case of a non-eccentric, slowly evolving binary, the polarization amplitude of a GW signal is characterized by six parameters: distance ( $d$ ), chirp mass ( $\mathcal{M}_c$ ), two angles related to the sky position (R.A.  $\alpha$ , decl.  $\delta$ ), and two angles related to the orbital plane orientation (inclination  $\iota$ , polarization angle  $\psi$ ). The instantaneous GW strain in the source frame is a combination of three of the above parameters, and can be decomposed into two different polarizations:

$$h_+(t) = \mathcal{A} \frac{1 + \cos^2 \iota}{2} \cos\left(\frac{4\pi t}{P} - \frac{\pi \dot{P} t^2}{P^2} + \phi_0\right) \quad (18)$$

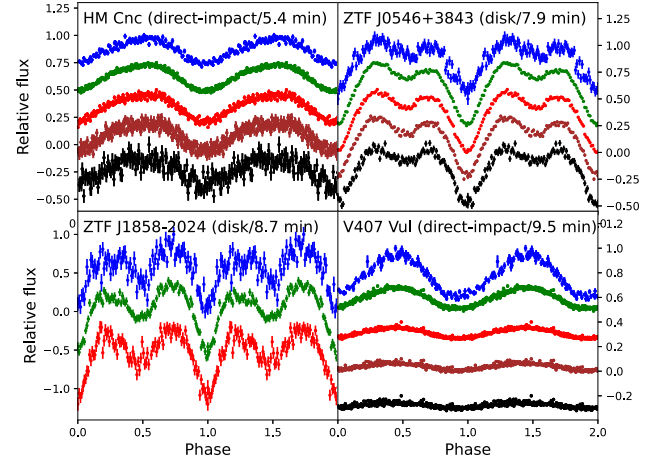
$$h_\times(t) = \mathcal{A} \cos \iota \sin\left(\frac{4\pi t}{P} - \frac{\pi \dot{P} t^2}{P^2} + \phi_0\right) \quad (19)$$

where  $d$  and  $\mathcal{M}_c$  are combined into the amplitude  $\mathcal{A}$ :

$$\mathcal{A} = \frac{4(G\mathcal{M}_c)^{5/3}}{c^4 d} \left(\frac{2\pi}{P}\right)^{2/3} \quad (20)$$

(S. Shah et al. 2012). The amplitude of the measured GW signal thus encodes a combination of the chirp mass, distance, and inclination. The remaining parameters enter when converting from the source frame to the radiation frame ( $\psi$ ) and calculating the response of the detector for a given sky position ( $\alpha$ ,  $\delta$ ), but they are not intrinsically related to the system.

**Orbital phase:** As the typical  $\dot{P}$  in these systems is of  $\mathcal{O}(10^{-11})$ , their periods will change by only milliseconds over the course of the LISA mission. For this reason, they are often referred to as monochromatic GW sources, characterized by sinusoids of near-constant frequency. The relative simplicity of this signal is actually a blessing when taken alongside the far more complicated and uncertain EM signal. To illustrate this, in



**Figure 10.** Multiband phase-folded light curves of four illustrative ultracompact binaries ( $u_s/g_s/r_s/i_s/z_s$  filters from top to bottom). Light curves of HM Cnc/V407 Vul are drawn from J. Munday et al. (2023)/J. Munday (2024, in preparation), respectively.

Figure 10 we showcase the remarkable diversity of UV/optical/infrared light curves of four ultracompact binaries. Some systems show multiple eclipses interspersed with flicker noise from the accretion disk, while others show a quasisinusoidal waveform. Some show clear color-dependence in their variation, indicating components of differing temperature, while others show almost an almost unchanged modulation across different wavelengths. Some are dominated by accretion luminosity, while others show a complicated blend of the donor/accretor stars alongside the signal from the accreting material. It is often impossible to assign a unique physical interpretation to each of these features with only EM data due to the many degrees of freedom, and the emergent huge variety of light curves, associated with accreting systems. As discussed in Section 3.1, this limits our ability to directly infer donor/accretor masses from RV measurements, which can otherwise be done readily for detached systems.

However, a GW signal will uniquely determine the binary orbital phase via the rightmost terms in Equations (18) and (19). This is the single most constraining tool in interpreting the EM data: with complete phase information, one can uniquely determine which eclipses are of the donor, accretor, or accretion stream. This unlocks the potential of RV measurements to constrain masses, and in-eclipse color variations to constrain temperatures. With additional knowledge of the inclination, one could also use the eclipses to measure donor/accretor radii; however, inclinations are difficult to constrain from EM data alone. Conveniently, a GW signal can also constrain this parameter.

**Inclination:** a GW detector does not independently measure the polarizations  $h_+$  and  $h_\times$  directly. Rather, the detector response is set by a weighted sum of the two, with coefficients of the antenna beam patterns  $F^+$ ,  $F^\times$  (N. J. Cornish & S. L. Larson 2003):

$$h^2(t) \propto [h_+ F^+(t, \alpha, \delta, \psi)]^2 + [h_\times F^\times(t, \alpha, \delta, \psi)]^2. \quad (21)$$

$F^+$  and  $F^\times$  are time-dependent functions with a period of 1 yr (for detectors co-orbiting with the Earth). The variation in  $h(t)$  over a year of continuous observations can thus distinguish between systems of differing inclination.



**Table 3**  
Orbital Period ( $P$ ), Period Derivative ( $\dot{P}$ ), and Chirp Mass ( $\mathcal{M}_c$ ) for the Shortest-period Binaries Systems Known

Name	$P$ (min)	$\dot{P}$ (s s <sup>-1</sup> )	$\mathcal{M}_c$ ( $M_\odot$ )	System Type	References
HM Cnc	5.35	$(-3.66 \pm 0.001) \times 10^{-11}$	...	Direct-impact accretor	(1, 2, 3)
eRASSU J060839.5-704014	6.23	...	...	Likely direct-impact accretor	(4)
ZTF J1539+5027	6.91	$(-2.37 \pm 0.005) \times 10^{-11}$	$0.30 \pm 0.01$	Detached binary	(5)
ZTF J0546+3843	7.95	$(-4.30^{+1.1}_{-1.0}) \times 10^{-12}$	...	Disk accretor	This work
ZTF J1858-2024	8.68	$(+7.80^{+1.70}_{-1.12}) \times 10^{-12}$	...	Disk accretor	This work
ZTF J2243+5242	8.80	$(-1.6 \pm 0.18) \times 10^{-11}$	$0.31 \pm 0.06$	Detached binary	(6)
V407 Vul	9.48	$(-2.27 \pm 0.25) \times 10^{-12}$	...	Direct-impact accretor	(7, 8, 9)
ES Cet	10.33	$(+3.2 \pm 0.1) \times 10^{-12}$	...	Disk accretor	(10, 11)
SDSS J0651+2844	12.75	$(-9.8 \pm 2.8) \times 10^{-12}$	$0.30 \pm 0.01$	Detached binary	(12)
ZTF J0425+3858	13.15	...	...	Disk accretor	This work
ZTF J0127+5258	13.71	$(-6.53 \pm 0.19) \times 10^{-12}$	$0.31 \pm 0.03$	Disk accretor	(13)

**Note.** Chirp masses are only shown for systems where M1 and M2 are directly measured

**References:** (1) G. H. A. Roelofs et al. (2010), (2) T. E. Strohmayer (2021), (3) J. Munday et al. (2023), (4) C. Maitra et al. (2024), (5) K. B. Burdge et al. (2019), (6) K. B. Burdge et al. (2020b), (7) C. Motch et al. (1996), (8) T. R. Marsh & D. Steeghs (2002), (9) T. E. Strohmayer (2004b), (10) M. Kondo et al. (1984), (11) E. de Miguel et al. (2018), (12) J. J. Hermes et al. (2012), (13) K. B. Burdge et al. (2023).

For edge-on systems, a GW signal can constrain inclinations to within  $\lesssim 10^\circ$ , which can then be combined with the photometric variation to measure donor/accretor radii via the eclipse depth. For all systems, inclinations together with complete phase information will unlock the power of RV measurements to constrain the component masses. The caveat is that not all systems will have visible donors/accretors, such as the ones in this work. But even for these systems, measurement of a chirp mass combined with our arguments in Section 4.3 can yield finer  $M_1/M_2$  constraints, as we now discuss.

Chirp mass: a GW signal does not yield separate component masses, but their combination via the chirp mass, then too degenerate with the distance (Equation (20)). For sources with well-constrained EM distances, the latter degeneracy is lifted. Then, combining with our mass transfer arguments outlined in Section 4.3 significantly constrains  $M_1$  and  $M_2$ : only a small range of solutions lying within the density contours of Figure 7 will agree with a measured  $\mathcal{M}_c$ . Coupled with radius constraints as discussed above, joint EM/GW measurements will directly constrain the amount of entropy in the donor WDs via their mass-radius relations, which is a key uncertainty in current binary evolution models (T. L. S. Wong & L. Bildsten 2021).

With the precise mass constraints unlocked by multi-messenger study of accreting binaries, one can compare an observed Type Ia SNe rate to the incidence of ultracompact binaries with sufficient mass to induce a double-degenerate supernova (K. J. Shen 2015). Adding the radius constraints further probes the white dwarf/He star mass-radius relation (Section 4.3), which is set by the amount of residual thermal energy remaining from the common envelope phase. Finally, population studies of accreting systems across a range of inclinations will be a direct probe into the vertical structure of accretion disks, whose scale heights, as a function of accretion rate and radial extent, are highly uncertain.

#### 4.5. Orbital Evolution of the Ultracompact Binary Population

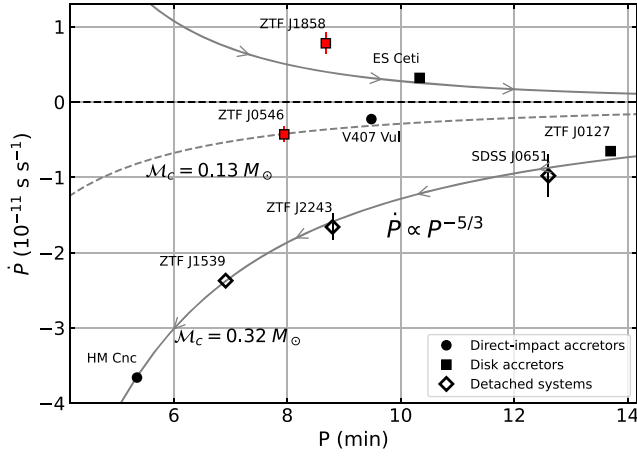
Having significantly expanded the sample of accreting ultracompacts with measured  $\dot{P}$  (Table 3), we now discuss

population-level implications for the trends observed so far in the orbital evolution of the shortest-period accreting binaries.

It is of great relevance whether initially detached systems, shortly after they come into mass-transfer contact, can stabilize via efficient angular momentum transfer back to the orbit. The generally assumed mechanism for this angular momentum transfer is synchronization of the accretor spin with the binary orbit via tidal torques (T. R. Marsh et al. 2004; V. Gokhale et al. 2007). The fraction of systems that stabilize versus merge is an extremely sensitive function of the timescale over which this angular momentum redistribution occurs (the tidal synchronization timescale; K. Kremer et al. 2015; S. Biscoveanu et al. 2023; A. Toubiana et al. 2024). Numerical simulations in T. R. Marsh et al. (2004) note that this timescale needs to be extremely rapid,  $\mathcal{O}(1000)$  yr, for a significant fraction of systems to stabilize.

T. E. Strohmayer (2021) and J. Munday et al. (2023) reported that HM Cnc, despite having a negative  $\dot{P}$  as expected from GR-dominated decay, has a positive second derivative ( $\ddot{P}$ ); the inferred period minimum will occur within  $\sim 1200$ – $2000$  yr, after which HM Cnc will begin to outspiral. The fact that HM Cnc was caught a mere  $\lesssim 2000$  yr prior to period minimum suggests that there is a selection bias at play, namely that  $\dot{M}$  and  $L$  peaks enormously during the short-lived passage through period minimum, making the systems much easier to discover. This is broadly in agreement with evolutionary models and simulations, which find  $\dot{M}$  spikes of 2–3 orders of magnitude near turnaround (T. R. Marsh et al. 2004; P. M. Motl et al. 2007). The lower observed rate of direct-impact accretors compared to detached and disk-accreting systems (Table 3) is further evidence toward this speculation, which will be tested by discovery of further systems at the shortest periods. Sufficiently long-baseline timing observations of ZTF J0546+3843 will also allow for direct detection of a  $\ddot{P}$  (which for the derived mass constraints in Section 4.3 are likely negative). Comparison of a measured  $\ddot{P}$  with that of HM Cnc would constitute an observational test of the efficiency of tidal torques with and without an accretion disk, with implications for the total number of direct- versus disk-accreting systems in the Galaxy at a given time.





**Figure 11.** The orbital period and its derivative ( $\dot{P}$ ) for all ultracompact binaries in which both are measured (Table 3). Our new systems are highlighted in red. Pure gravitational-wave decay, in the absence of mass transfer and tides, corresponds to  $\dot{P} \propto P^{-5/3}$ , which we illustrate for two different chirp masses. All detached systems lie nearly on the same curve of constant chirp mass ( $M_c = 0.32 M_\odot$ ), while some accreting systems diverge significantly due to the effects of mass transfer.

The remarkable accuracy with which several inspiraling systems follow a single  $P^{-5/3}$  curve (Figure 11), across both accreting and detached systems, suggests comparable chirp masses ( $M_c$ ) in all systems, suggesting a common binary evolution process is responsible for the majority of stable systems at these orbital separations. Indeed, in the systems with direct mass measurements (mostly detached binaries), all have  $M_c \approx 0.3 M_\odot$  (Table 3). The notable exceptions from this curve are V407 Vul and ZTF J0546+3843, with  $|\dot{P}|$  several times smaller than naively anticipated from the empirical trend in Figure 11. The two possibilities are that (1) the chirp mass in these systems is smaller, either via the effect of sustained mass transfer or an alternate formation channel; or (2) these systems are on course for a period minimum ( $\dot{P} = 0$ ) within the next few thousand years. Case (2) would be additional evidence for efficient tidal synchronization in ZTF J0546+3843, as this implies a large  $\dot{P}$  (hence a large spread in  $\dot{P}$ ). Measurements of  $\dot{P}$  in more accreting systems, or directly constraining  $\dot{P}$  in V407 Vul/ZTF J0546+3843, would test this hypothesis.

We also consider the relative likelihood of detecting systems near  $P_{\min}$  in their inspiral versus outspiral phase. The CO + ELM WD evolutionary models of D. L. Kaplan et al. (2012) found that, as the time spent at a particular period scales as  $\propto |1/\dot{P}|$ , the model population of ingoing versus outgoing systems should be:

$$\mathcal{N}_{\text{out/in}} \equiv \left| \frac{\dot{P}_{\text{in}}}{\dot{P}_{\text{out}}} \right| \approx 4 \left( \frac{P}{10 \text{ minutes}} \right) \left( \frac{M_{2,i}}{0.15 M_\odot} \right).$$

Considering only the systems with donor/accretor masses near  $0.8/0.15 M_\odot$  (so that the evolutionary models of D. L. Kaplan et al. 2012) are relevant, the observed ratio of ingoing versus outgoing systems  $\mathcal{N}_{\text{out/in}} = 2/4$  (Table 3) appears in tension with the results of these evolutionary models, albeit still with small number statistics. There are a handful of possible unmodeled effects contributing to this disagreement. For one, most systems may never stabilize to produce a long-lived outspiral AM CVn due to inefficient tidal synchronization or nova eruptions resulting in rapid orbital destabilization and

merger (K. J. Shen 2015). Another alternative is that our understanding of the outspiral phase is incomplete, and  $\dot{P}_{\text{out}}$  is significantly larger than expected for unknown reasons. The larger-than-expected  $\dot{P}$  of ZTF J1858–2024 provides compelling evidence toward this possibility.

As a large enough sample of  $\dot{P}$  measurements for population studies is just beginning to emerge, we cannot favor either scenario with confidence, but time will tell whether our theoretical picture of double WDs near period minimum requires significant rethinking. This work represents an important step toward building up the statistics to rigorously test these evolution models.

## 5. Conclusions

In this work, we present the discovery of three new ultracompact accreting binaries, with orbital periods of 7.95, 8.68, and 13.15 minutes. We draw the following conclusions:

1. We infer that all three systems accrete via a disk from the presence of double-peaked emission lines in their spectra (Figures 1 and 2). Previously, only direct-impact accreting systems were known below 10 minutes (Table 3), but our new systems show that the accretors in ultracompact binaries can get compact enough to host accretion disks even at these periods.
2. All three systems show remarkably similar optical spectra dominated by ionized helium and nitrogen (Figure 1). The similarity of the outspiral systems ZTF J1858–2024 and ES Cet with the inspiraling binary ZTF J0546+3843—especially the lack of hydrogen in the latter—is particularly surprising from an evolutionary standpoint. We obtained an FUV spectrum indicating lower N/C in ZTF J0546+3843 compared to ES Cet (Figure 3), which is qualitatively consistent with a less-stripped donor and/or a less-massive main-sequence progenitor.
3. We measured ZTF J0546+3843 to have  $\dot{P} = -4.30^{+1.1}_{-1.0} \times 10^{-12} \text{ s s}^{-1}$ , and ZTF J1858–2024 to have  $\dot{P} = +7.80^{+1.70}_{-1.12} \times 10^{-12} \text{ s s}^{-1}$  (Figure 4). We have shown how the measured  $\dot{P}/P$  can be combined with mass-transfer arguments, as well as some loose assumptions about the adiabatic and thermal/nuclear evolution properties of the donor, to place tighter bounds on the system parameters (Figure 7). With these constraints, we infer the donor in ZTF J1858–2024 to have an adiabatic index comparable to that expected for a zero-temperature degenerate star, while the donor in ZTF J0546+3843 must have  $\xi_{\text{ad}}$  significantly larger. The small magnitude of  $\dot{P}$  in ZTF J0546+3843 heavily implies a system close to period minimum, whereas the large  $\dot{P}$  in ZTF J1858–2024 is difficult to explain with current binary evolution models (Figure 8).
4. Based on the range of allowed donor/accretor masses and distance posteriors, we infer that ZTF J0546+3843 and ZTF J1858–2024 are loud GW sources detectable by future space-based millihertz GW detectors, e.g., TianQin, Taiji, and LISA (Figure 9). A GW signal, when combined with our EM analysis and mass-transfer arguments, can significantly constrain the component masses/radii, system inclinations, and donor structure (Section 4.4), demonstrating a compelling multimessenger science case.

5. At a population level, the observed scarcity of direct-impact accretors, compared to disk accretors and detached systems at short orbital periods (Table 3) seems to suggest there is an observational bias against detecting them, e.g., if their high- $\dot{M}$  phase is very short-lived. Such an effect could be achieved if the tidal synchronization efficiency scales sharply with  $\dot{M}$ , so that period turnaround occurs rapidly after  $\dot{M}$  spikes. A future measurement of  $\dot{P}$  in the inspiraling system ZTF J0546+3843, compared to the recent positive  $\dot{P}$  measured for HM Cnc (T. E. Strohmayer 2021; J. Munday et al. 2023), will allow for direct comparison of the efficiency of tidal synchronization with and without an accretion disk. It is also curious that only two outspiralng systems are known, while the population of inspiraling systems seemingly continues to grow. It is possible there is an observational selection effect at play, or that most interacting double WDs are unstable to mergers, lowering the rate of long-lived AM CVn (K. J. Shen 2015). The implications of these effects will extend to Type Ia SNa rates (A. J. Ruiter et al. 2009), galaxy-scale binary population synthesis models (K. Breivik et al. 2020), and the all-sky megahertz GW signal (T. B. Littenberg et al. 2020).

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Based on observations made with the Gran Telescopio Canarias (GTC) installed in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias, on the island of La Palma. Based on observations made at the European Southern Observatory New Technology Telescope (NTT), La Silla.

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### Appendix Supplementary Figures and Tables

In Table A1, we include an observation log of all high-speed photometry epochs used for our timing solutions.

**Table A1**  
Observation Log of All High-speed Photometry Epochs

Object	Instrument	Date	Filters	Total Exposure (hr)	Exposure Time (s)	$T_0$ (BJD)
ZTF J0546+3843	CHIMERA	2020-12-15	$g/r$	8.25	6	59198.23459(7)
	CHIMERA	2021-04-13	$g/r$	1.84	11	59317.16810(6)
	CHIMERA	2021-10-10	$g/r$	2.01	5	59497.38655(8)
	CHIMERA	2022-08-25	$g/r$	1.15	5	59816.47734(4)
	HiPERCAM	2024-03-10	$u_s/g_s/r_s/i_s/z_s$	2.85	1.7	60379.85838(2)
	HiPERCAM	2024-08-28	$u_s/g_s/r_s/i_s/z_s$	0.47	1.7	60550.20934(3)
	HiPERCAM	2024-08-29	$u_s/g_s/r_s/i_s/z_s$	0.95	1.7	60551.18058(3)
	HiPERCAM	2024-08-31	$u_s/g_s/r_s/i_s/z_s$	0.47	1.7	60553.18938(1)
	Lightspeed	2024-10-26	$L$	0.60	1.0	60609.39173(5)
ZTF J1858–2024	CHIMERA	2019-04-28	$g/r$	1.67	3.0	58601.4689(8)
	ULTRACAM	2019-07-09	$g_s/r_s/i_s$	1.02	6.5	58673.3068(2)
	ULTRACAM	2019-07-10	$g_s/r_s/i_s$	2.01	6.5	58674.1387(4)
	CHIMERA	2019-10-01	$g/r$	1.22	5.5	58757.1164(8)
	ULTRACAM	2023-04-01	$g_s/r_s/i_s$	1.22	5.7	60035.3702(3)
	HiPERCAM	2024-05-22	$u_s/g_s/r_s/i_s/z_s$	2.68	3.8	60452.1204(1)
	ULTRACAM	2024-07-30	$g_s/r_s/i_s$	1.18	10	60521.0415(2)
ZTF J0425+3858	CHIMERA	2022-08-24	$g/r$	0.84	5.63	59815.4026(4)

**Note.** These observations were fit with a quadratic timing model to determine the  $\dot{P}$  as shown in Figure 4.

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