

# 1 Optimizing and Exploring Untapped Micro-Hydro Hybrid Systems: a 2 Multi-Objective Approach for Crystal Lake as a Large-Scale Energy Storage Solution

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## 6 Abstract

7 This paper proposes a method of exploring existing geographic locations with untapped pump hydro storage potentials  
8 for accommodating intermittent renewable energy generation profiles. Measured data in 2022 were gathered for sizing  
9 system's components and thorough, realistic analysis. Employing a multi-objective grey wolf optimization algorithm,  
10 we formulate optimal sizing and energy management strategies for different scenarios. The 1<sup>st</sup> scenario aims to  
11 maximize the reliability objective function (ROF) index of reliability (IR) whilst minimizing the cost objective function  
12 (COF) leveled cost of energy (LCOE). The 2<sup>nd</sup> scenario focuses on maximizing ecological objective function (EOF)  
13 CO<sub>2</sub> reduction amount (CO<sub>2</sub>RA) whilst minimizing COF, and the 3<sup>rd</sup> scenario is for maximizing both ROF and EOF  
14 while minimizing COF. Considering economic, environmental, and reliability factors as the three objective functions  
15 (OFs), has proven to yield promising results in the third scenario when including triple OFs with multiple solutions. A  
16 case study is done for the region of Crystal Lake, Michigan. Findings reveal that, although Crystal's Lake would only  
17 function as a micro-hydro power facility, it is a promising and huge storage unit with a substantial storage capacity of  
18 around 14.9734GWh. These outcomes include a notably low LCOE at 0.046147\$/kWh, a robust IR of 99.705%, and a  
19 significant reduction in CO<sub>2</sub> emissions amounting to 7.9142×10<sup>3</sup> ton/year, when considering the triple OFs. Validation  
20 of the findings was conducted using multi-objective particle swarm optimization algorithms, affirming the robustness  
21 of the proposed solutions. The paper's methodology provides valuable insights for regions aiming to utilize renewable  
22 energy from untapped storage sources.

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24 **Keywords:** Fuzzy logic, Levelized cost of energy, Optimal configuration, Pumped hydro storage, Solar photovoltaic array, Triple  
25 objective functions.

## 26 **Nomenclature**

### 27 **Abbreviations Meaning**

|          |                                   |
|----------|-----------------------------------|
| 28 DDM   | Double Diode Model                |
| 29 DHI   | Direct Horizontal Irradiance      |
| 30 DNI   | Direct Normal Irradiance          |
| 31 EOF   | Ecological Objective Function     |
| 32 ESS   | Energy Storage System             |
| 33 GHG   | Greenhouse Gas Emissions          |
| 34 MHPP  | Micro-Hydropower Plant            |
| 35 MGA   | Messy Genetic Algorithm           |
| 36 NSRDB | National Solar Radiation Database |

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|    |                         |   |
|----|-------------------------|---|
| 37 | PHESS                   | Pumped Hydro Energy Storage System                                    |
| 38 | PV                      | Solar Photovoltaic  |
| 39 | RES                     | Renewable Energy Systems  |
| 40 | RERs                    | Renewable Energy Resources  |
| 41 | ROF                     | Reliability Objective Function  |
| 42 | UCL                     | Upper Crystal Lake  |
| 43 | <b>Symbol Name Unit</b> |   |
| 44 | ACS                     | Annualized Cost of the System   |
| 45 | CC                      | Capital Cost  |
| 46 | CEA                     | Carbon-Dioxide Emission Amount  |
| 47 | COE                     | Cost of Energy  |
| 48 | COF                     | Cost Objective Function   |
| 49 | CRF                     | Capital Recovery Factor   |
| 50 | IR                      | Index of Reliability  |
| 51 | LCOE                    | Levelized Cost of Energy  |
| 52 | LOLP                    | Loss of Load Probability  |
| 53 | LPSP                    | Loss of Power Supply Probability                                      |
| 54 | GTI                     | Global Tilted Irradiance  |
| 55 | NPC                     | Net Present Cost  |
| 56 | P&L                     | Transmission and Distribution Line Losses Percentage                  |
| 57 | OMC                     | Operation and Maintenance Cost  |
| 58 | QOW                     | Quantity of Water in m <sup>3</sup>                                   |
| 59 | RC                      | Replacement Cost  |
| 60 | RSF                     | Renewable Storage Factor  |
| 61 | SC                      | Salvage Cost  |
| 62 | TCC                     | Total Current Cost  |
| 63 | $T_{mpv}$               | Solar PV Module Temperature in °C                                     |
| 64 | $T_{amb}$               | Ambient Temperature in °C   |
| 65 | NOCT                    | Nominal Operating Cell Temperature in °C                              |
| 66 | $T_{MDS,STC}$           | Manufacturer Data Sheet Temperature at Standard Test Conditions in °C |
| 67 | $v$                     | Hourly Measured Wind Speed in m/s                                     |
| 68 | $V_{adj}$               | Adjusted Wind Speed at Hub Height in m/s                              |
| 69 | $H_{hub}$               | Hub Height in m   |
| 70 | $H_{measured}$          | Height at Wind Speed Measured in m                                    |
| 71 | $I_{ph}$                | Photon Current in Ampere  |
| 72 | $P_{WT}$                | Power Extracted from Wind Turbine in MW                               |
| 73 | $N_{WT}$                | Number of Wind Turbines   |
| 74 | $P_r$                   | Rated Power in MW   |
| 75 | $V_{ci}$                | Cut-in Speed in m/s   |
| 76 | $V_{co}$                | Cut-out Speed in m/s  |
| 77 | $q_p$                   | Pump Flow Rate in m <sup>3</sup> /s                                   |
| 78 | $q_t$                   | Water Volumetric Flow Rate in m <sup>3</sup> /s                       |

|    |                      |  |
|----|----------------------|--|
| 79 | $E_C$                | Gravitational Potential Energy                               |
| 80 | $n_{day}$            | The Duration of Autonomy days                                |
| 81 | $P_{gen}$            | Power Generated from Hybrid System in MW                     |
| 82 | $P_{PV\,inv}$        | Power Generated Inverted from PV System                      |
| 83 | $P_L$                | Load Demand in MW  |
| 84 | $P_{MHPP\,dis}$      | Generated Power from MHPP Turbines in MW                     |
| 85 | $P_{gp}$             | Power Grid Purchased in MW                                   |
| 86 | $P_{extra}$          | Extra Generated Power from Hybrid System in MW               |
| 87 | $P_{MHPP\,ch}$       | Power Stored in MHPP in MW                                   |
| 88 | $P_{gsold}$          | Power Sold to the Grid in MW                                 |
| 89 | <b>Greek Symbols</b> |  |
| 90 | $a_w$                | Wind Power Law Exponent                                      |
| 91 | $\alpha_s$           | Solar Altitude Angle in degree                               |
| 92 | $\beta_s$            | Solar Tilted Angle in degree                                 |
| 93 | $\varphi$            | Latitude Angle in degree                                     |
| 94 | $\delta$             | Declination Angle in degree                                  |
| 95 | $\theta_z$           | Zenith Angle in degree                                       |
| 96 | $\rho$               | water density ( $1000\,kg/m^3$ )                             |
| 97 | $\rho_o$             | Air density at sea level, and it is equal to $1.225\,kg/m^3$ |
| 98 | $\eta_T$             | Efficiency of the hydro turbine (in %)                       |

## 1. Introduction

Climate change, fossil fuel usage, and energy prices have constantly been top global topics. Based on the current global climate change, energy utilization, and climate policies, it is estimated that the fossil fuel share in global energy will drop from 80% to around 73% by the end of the year 2029 [1]. Hence, the adoption of new sustainable energy technologies will ease the challenges related to energy shortages and balance the energy transition domestically and internationally. As energy is crucial for our lives, in recent decades, hybrid renewable energy systems (RESSs) have appeared as a practical solution for supplying electricity to several areas, including remote rural areas where expanding the grid is impractical and extremely expensive [2]. A RES may include several sustainable resources, such as solar photovoltaic, wind energy, micro-hydro, and biomass energy, which can work along with conventional backup generators. In addition to generating clean electricity, large-scale solar, and wind power plants contribute to issues such as environmental waste accumulation and electricity generation intermittence. Therefore, there is a constant and urgent need for clean and dispatchable sources of energy production and storage. Among several RES technologies, hydro power stands out as a promising economic and reliable choice. Indeed, building large-scale hydropower facilities encounters challenges such as ecological impacts and high capital costs, which make them less attractive. Moreover, large-scale, centralized hydropower resources have already been extensively (if not fully) exploited in many countries and regions. Nevertheless, there still exist many untapped pico- and micro-hydro power resources from relatively small rivers and lakes and hydro storages, which show notable potential for long-term electricity generation and storage. For instance, Michigan, a state with thousands of lakes [3], presents a substantial opportunity for micro-hydro projects, in addition to its abundant rivers and high rainfall that serve those storage lakes.

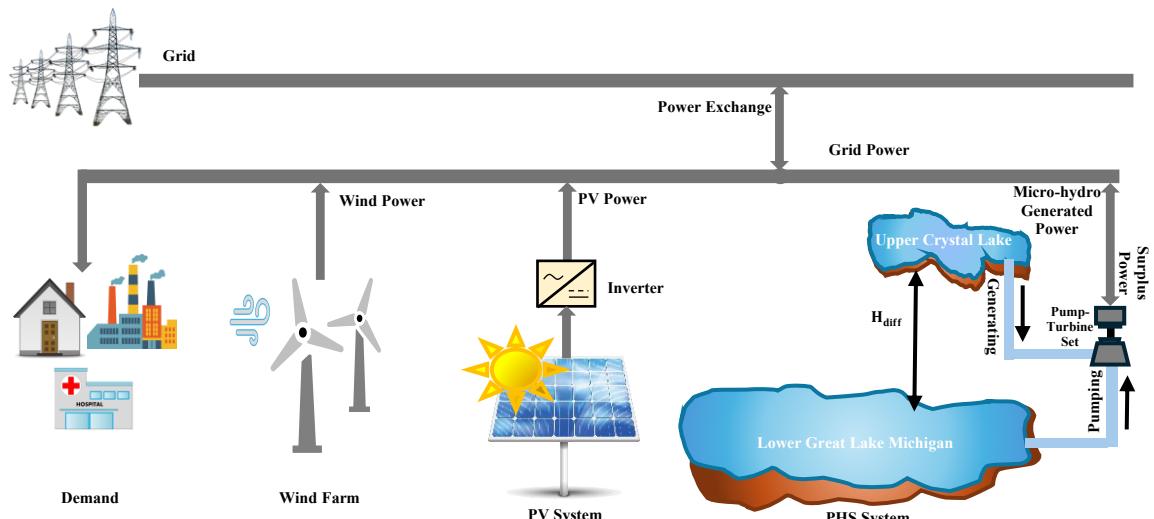
The authors in [4] propose an effective methodology for optimal production benefits for hydropower

systems, particularly for installing micro hydropower within water distribution networks. Their methodologies were to investigate technical and economic studies to evaluate practicability and economic feasibility, in terms of optimal sizing using an optimization algorithm. They applied the proposed algorithm to a case study in Morocco's water supply network, including the design and installation of a micro-hydro power plant (MHPP) and considering environmental aspects. Results indicate a substantial cost drop by utilizing existing infrastructures, and an annual average emission reduction of 282 tons, which proves the potential of integrating micro hydropower into water supply systems. They also found the proposed installation is ecologically sustainable and will generate clean energy with an obtained power output of 69 kW. In [5], the researchers discussed an on-grid solar PV combined with MHPP in Unand, Indonesia. This study aimed to find the optimal sizing of micro-hydro hybrid systems to enhance renewable power generation. They implement their system using HOMER software to optimize the head height and flow rate of the MHPP by minimizing the cost of energy (COE). The results showed that the head height was 30m with a flow rate of 800L/s at the lowest value of COE of 0.065 \$/kWh. Moreover, the optimal capacity enhances renewable energy generation by a renewable fraction improvement from 26.4% to 36.5%. Reference [6], discussed the availability of renewable energy resources (RERs) in Pakistan as a developing country and how to effectively harness these resources for electricity generation. This is done by introducing an MHPP situated at a specific canal in KPK, Pakistan. The modeling and optimization of the project were implemented using RETScreen software and were thoroughly discussed. The authors compute the net present value (NPV) and the COE using the RETScreen optimization assessment and validate the feasibility of the MHPP. RETScreen simulated a micro-hydro system as a case study with a capacity of 107 kW over a 20-year lifespan. The suggested micro hydropower project is technically applicable and economically viable, with a NPV of \$139,280 and a COE of 0.049 \$/kWh. The findings revealed that the proposed project will recover all the spending by the 4th year of its planned duration. Notably, when compared to the country's baseline energy mix, the proposed project is identified as clean energy with greenhouse gas (GHG) emission free. To solve the issue of intermittency in RERs due to the natural variations in power generation, which also follow daily and seasonal patterns, it becomes mandatory to combine a complementary energy storage system in those hybrid RERs. A viable alternative for energy storage in hybrid systems is a pumped hydro energy storage system (PHESS). The authors in [7], introduced a technique to represent a PHESS by creating an equivalent battery in HOMER since HOMER didn't have a PHESS component at that time, which was demonstrated through a detailed example. They designed another example consisting of a wind-hydro hybrid power system to validate their methods. The results confirm that the method outlined in their paper effectively represents PHESS for electric energy storage. In order to address energy scarcity challenges such as limited resources which can lead to lower efficiency, especially in sub-generation systems, the researchers in [8] present a design methodology utilizing a customized messy evolutionary approach called the Messy Genetic Algorithm to determine the optimal layout for MHPP. Their methodology considers multiple constraints associated with supply requirements, maximum flow use, and the substantial feasibility of the plant based on the actual geographical profile. This profile allows a continuous, variable-length Messy Genetic Algorithm (MGA) to optimize the layout, by applying two scenarios: cost minimization as a single-objective in one case and minimization of both cost and power supply as a multi-objective in the other case. The algorithm is implemented for a real remote community system in Honduras. Results show that a significant cost reduction of around 56.96% occurred compared to previous designs. On the other hand, considering other boundaries, the MGA was employed to optimize the problem without handling the penstock diameter as a variable. They found that shorter penstocks were created when considering fixed penstock diameter, reaching a 24.22% reduction in length compared to the solution with the optimized diameter, but with significantly higher costs of 285% increase. The PHESS boasts a global installed power capacity of 153GW [9]. This inspires the authors in [10], to introduce a novel Mixed Integer Linear Programming model intended to optimize the operation of such

storage plants by maximizing the system's profits. Their model can accommodate a larger number of breakpoints, allowing for more practical solutions with the lowest computational effort. To validate the effectiveness of their model, it was applied to two real plants in the Argentine Republic: the Rio Grande and Los Reyunos power plants, with a combined installed power capacity of 975 MW. The results demonstrate that the suggested model provided feasible solutions with an adequate level of accuracy, within CPU times of less than one second. In [11], the researchers integrated two types of energy storage specifically, MHPP and battery storage, into a small-scale RES. Their study implemented optimal design for off-grid renewable-micro PHESS and battery storage systems in a remote area of Sweden. Their objective was to estimate efficiency, cost, and storage duration. In addition to find the most suitable solution by considering techno-economic performance indicators such as investment cost, life cycle cost, leveled COE (LCOE), and loss of power supply probability (LPSP). The system was optimized using the modified non-dominated sorting Genetic Algorithm. Results reveal that the hybrid PV-wind-battery storage system is the best option in terms of economic benefits and reliability, as the demand is fully satisfied. They found that 18.61% lower life cycle cost and a 6.12% lower oversupply compared to the hybrid PV-wind-micro PHS system. Although this study compared two types of storage, they did not consider the impact of their design on a large-scale hybrid RES. In [12], the authors provided a practical analysis and sizing of a solar PV system linked with an existing dam as an upper reservoir of the PHESS in Jordan. They explored two scenarios. In the first scenario, they included both RER losses: the losses due to solar PV diffusion and recombination phenomena in the two-diode power model, and the effective head loss in the PHS plant. In the second scenario, they did not consider these types of losses. The system was optimized using particle swarm optimization to determine the optimal value of the index of reliability. They found that to fully cover the load demand, the necessary number of PV panels and the volume of the lower reservoir were to be 44,063 panels and 69.348 Million  $m^3$ , in case no losses are considered, respectively. These values decrease by 14.33% and 5.39% for the second case. Therefore, considering renewable component losses will result in a higher but accurate sizing and prevent undersized design in the case of real system implementation. The authors in [13], proposed a new approach for water and energy management within a wide water supply system, aiming to reduce the costs of energy through the installation of PV plants. They integrate a PHESS to address the intermittency of PV systems. This integrated strategy is applied as a case study to two distinct pumping stations: the "Basso Flumendosa" and the "Monteleone-Roccadoria" pumping stations by maximizing energy self-consumption. Various sizes of PV arrays and hydro turbines are examined to evaluate the obtained self-sufficiency rate and cost performance. The impact of the pumping station's availability for storage purposes was also assessed. The findings indicate that more than 65% of the self-sufficiency rates are attainable only with the integration of the PHESS. A reduction in profitability is observed if full self-sufficiency is achievable for both pumping stations. The researchers in [14], discussed the design of different scenarios for microgrid hybrid RES. They optimized the system by considering multiple objectives, including economic and environmental aspects, namely net percentage cost (NPC) and the reduction of CO<sub>2</sub> emissions. To achieve this, a non-dominated sorting genetic algorithm was implemented to design and optimize the proposed system. The results, when directed toward economic objectives, show the achievement of the lowest energy cost across all scenarios with and without storage units. In contrast, when the optimization technique was centred on environmental objectives, the outcomes indicated a higher overall system cost compared to economic optimization across all scenarios. In [15], the authors discussed a novel tool for creating a penstock layout of MHPP. This proposed procedure depended on a detailed topographic survey of the terrain and used a Genetic Algorithm to optimize the layout of installations. Their mechanism allows for clear integration of several constraints, such as power supply, installation costs, available water flow, and layout feasibility by the actual terrain profile. The algorithm operates in both single-objective mode, aiming to minimize costs, and multi-objective mode, which considers both minimizing cost and maximizing power supply. The application of this algorithm to a real-

215 life case in a distant community in Honduras, Central America, has yielded promising results in terms of  
 216 generation capacity and cost minimization.

217 After reviewing existing research and identifying gaps, this paper introduces a new approach: a hybrid  
 218 renewable energy system (RES) coupled with a utility-scale micro PHESS, as depicted in Fig. 1, to  
 219 demonstrate and model the proposed methodology. This system integrates solar PV arrays and wind plant  
 220 installations integrated with the Upper Crystal Lake (UCL) as PHESS. The motivation for this research  
 221 stems from the limited exploration of MHPP design on a large scale in previous studies, particularly in  
 222 hydro facilities categorized as MHPPs. Moreover, it aims to address the engineering challenge of  
 223 integrating hydro facilities with low head heights. Thus, the renewable energy strategy outlined in this paper  
 224 offers a long-term solution to effectively meet energy demands in Michigan and similar regions globally.  
 225 Additionally, a double-diode (DD) PV model was employed to ensure precise sizing of the proposed solar  
 226 system. The proposed mathematical modeling, methodology, optimization algorithm application, and  
 227 energy management flowchart presented in this paper apply globally to similar cases. In this paper, Crystal  
 228 Lake's geographical location is utilized as a case study to validate these aspects, employing the realistic  
 229 measured data for the chosen location in the year 2022, as detailed in Section 2. Multiple multi-objective  
 230 scenarios were investigated for two and three objectives simultaneously. These scenarios include  
 231 maximizing power system reliability and reducing  $CO_2$  emissions while minimizing overall system costs.  
 232 Additionally, the triple Pareto front was simulated to provide a comprehensive view of the combined  
 233 objective functions for the system's methodology. It is important to note that each scenario yields several  
 234 solutions, including the best-compromised solution using a fuzzy logic approach. The performance of  
 235 various renewable energy scenarios is evaluated using a multi-objective approach that considers economic  
 236 feasibility, reliability, and environmental impacts. This assessment employs a recent multi-objective  
 237 metaheuristic optimization algorithm, namely the Multi-objective Grew-Wolf optimization algorithm  
 238 (MOGWOA), to determine optimal system sizing and performance indicators for each scenario, aiming for  
 239 cleaner energy production. Finally, a comparative analysis is utilized using a multi-objective feasibility-  
 240 enhanced particle swarm optimization algorithm (MOFEPSOA) to test the effectiveness of MOGWOA. In  
 241 other words, by comparing the findings obtained using MOFEPSOA, the performance of MOGWOA can  
 242 be estimated.



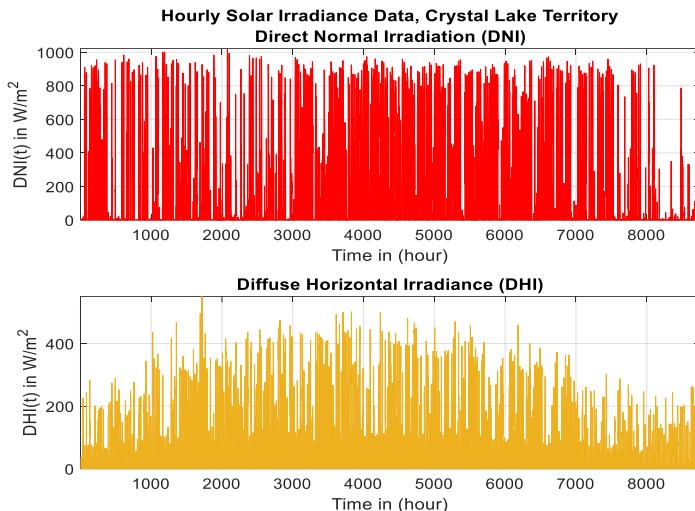
243  
 244 Fig. 1. Schematic diagram of the proposed solar PV and wind power plants combined with the MHPP.

245        **2. System's Realistic Raw and the Corresponding Input Data**

246        The realistic measured data is substantial to accurately design and simulate a real power system and  
 247        eventually obtain realistic results. This section shows the hourly realistic data for systems' components,  
 248        including the solar PV system, wind farm, MHPP, and utility-scale load demand for Crystal's Lake territory.  
 249        It also illustrates the acquired raw and adjusted data that are ready for implementation in the mathematical  
 250        formulation of the proposed system. Note that, those measured data, i.e., 8760 hours for the year 2022, are  
 251        obtained from formal US institutions and websites for the proposed geographical location, as explained  
 252        later in this section.

253        *2.1 Solar PV System Data*

254        The solar PV system data was collected from the National Solar Radiation Database (NSRDB) for the  
 255        Crystal Lake location [16]. Those data include the hourly measured direct normal irradiance (DNI), diffused  
 256        horizontal irradiance (DHI), and ambient temperature ( $T_a$ ). Fig. 2 depicts the hourly DNI and DHI in the  
 257        Crystal Lake terrain throughout 2022, covering a total of 8,760 hours. It can be noticed that the maximum  
 258        values of DNI and DHI are  $1022\text{W/m}^2$  and  $550\text{W/m}^2$ , respectively, whereas the average values are  
 259         $171.76\text{W/m}^2$  and  $61.99\text{W/m}^2$ .



260  
 261        Fig. 2. Hourly measured DNI and DHI values in Crystal Lake terrain in a year.

262        The data must be converted in the appropriate form in order to be implemented in the double-diode  
 263        solar PV module presented in section 3.1. Note that,  $GHI(t)$  is the total amount of horizontal solar radiation  
 264        falling on a surface. It is also used to calculate the solar radiation on a tilted surface. GHI resulted in Fig.  
 265        3, is mathematically computed based on the hourly raw data of DNI, DHI, and the acquired zenith angle  
 266        ( $\theta_z(t)$ ) using (1) [17].

$$267 \quad GHI(t) = DHI(t) + DNI(t) \times \cos(\theta_z(t)) \quad (1)$$

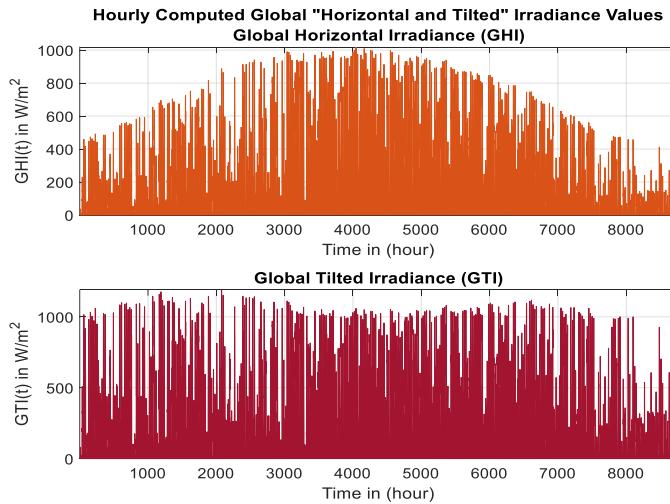
268        Now, the global tilted solar irradiance ( $GTI(t)$ ) is ready to be computed and entered in the modeling of a  
 269        solar PV module, as will be explained later in section 3.1. Note that, GTI, shown in Fig. 3, is calculated at  
 270        each time step using (2) [18].

$$271 \quad GTI(t) = GHI(t) \times \frac{\sin(\alpha_s(t) + \beta_s)}{\sin(\alpha_s(t))} \quad (2)$$

272 Where  $\alpha_s$  is computed as in (4), and it depends on the latitude angle ( $\varphi$ ) and the declination angle ( $\delta$ ) as  
 273 in (3).  $\beta_s$  is  $37^\circ$  for Crystal Lake territory [19].  $\varphi$  is  $44.668677^\circ$  based on the selected site coordinates, and  
 274  $n$  is the number of days within a year, ranging from 1 to 365. This iteration allows ( $\delta$ ) to vary as a function  
 275 of the specific day of the year[20].

$$\delta(t) = 23.45^\circ \sin \left[ \frac{360}{365} (n + 284) \right] \quad (3)$$

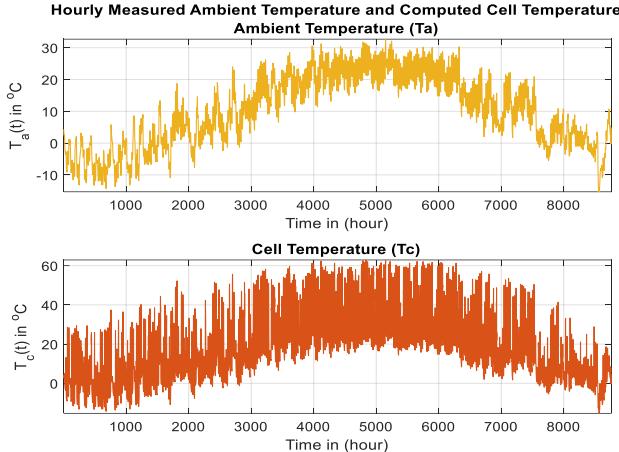
$$\alpha_s(t) = 90 - \varphi + \delta(t) \quad (4)$$



278  
 279 Fig. 3. Hourly measured GHI and computed GTI solar values for Crystal Lake terrain in a year.

280 The module temperature ( $T_{m_{PV}}(t)$ ) are calculated as in (5) and (6).  $T_{amb}(t)$  in (5) is the hourly air  
 281 ambient temperature obtained from NSRDB [16], and it is converted to  $T_{m_{PV}}(t)$  as illustrated in Fig. 4.  
 282 The selected solar PV is “CanadianSolar All-Black CS6K-290MS” with rated power of 290 Watt. The  
 283 complete required data and the value of NOCT,  $T_{MDS,STC}$  and  $GTI_{NOCT}$  are given in Appendix A.

$$T_{m_{PV}}(t) = T_{amb}(t) + \frac{(NOCT - T_{MDS,STC}) \times GTI(t)}{GTI_{NOCT}} \quad (5)$$



285  
 286 Fig. 4. Hourly measured ambient and computed module temperature values for Crystal Lake terrain.

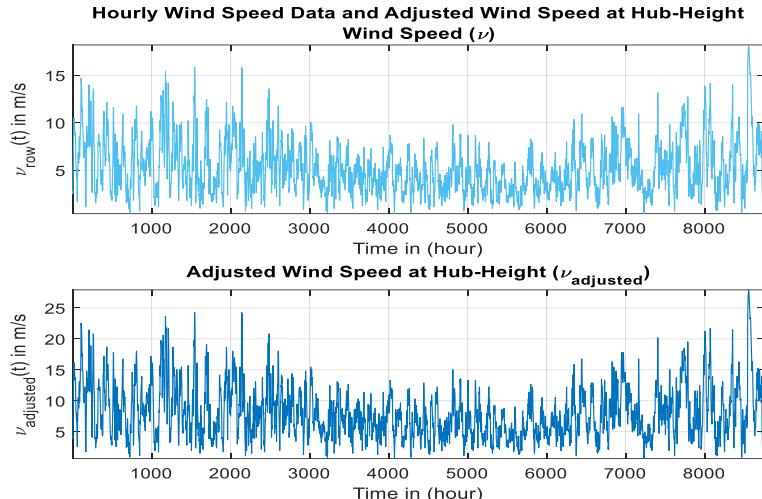
287 

## 2.2 Wind Turbine Data

288 The hourly measured wind speeds  $v(t)$ , shown in Fig. 5, are obtained from the Weather API [21].  $v(t)$  are  
 289 fluctuating between 0.42m/s and 18.2 m/s. Before these data can be utilized in the mathematical formulation  
 290 of wind turbine output power discussed in section 3.2, it is required to calibrated this data according to the  
 291 hub height ( $H_{hub}$ ) as in (6) [22].

292 
$$V_{adj}(t) = v(t) \times \left( \frac{H_{hub}}{H_{measured}} \right)^{a_w} \quad (6)$$

293 The wind power law exponent, denoted by ( $a_w$ ), relates the wind speed measured at the  $H_{hub}$  of a wind  
 294 turbine ( $V_{adj}$ ) to the wind speed measured by an anemometer at  $H_{measured}$ , as expressed in Equation (6).  
 295 In addition, empirical studies suggest that  $a_w$  is equivalent to 1/7, typically provides the best fit for most  
 296 sites, see Appendix A. The average wind speed has increased from around 5.28 m/s to 8.11 m/s, as in Fig.  
 297 5, after considering the hub height for the proposed wind turbine.



298  
 299 Fig. 5. Hourly measured and computed wind speed values for Crystal Lake terrain.

300 

## 2.3 Hydropower Plant and Crystal Lake Data

301 Crystal's Lake history is greatly constrained to several geological shifts in the past as it was initially  
 302 formed as part of glacial Lake Algonquin around 11,000 years ago [23]. It was found perched 11.5824 m  
 303 overhead of present-day Lake Michigan at an elevation of around 187.452 m after the glacier's retreat,  
 304 presenting exposed terraces and flooded shoals along its shoreline [24]. In 1873, the lake witnessed a  
 305 considerable drop in its levels due to a critical storm that faded and swept away a temporary dam during an  
 306 attempt to build a canal to Lake Michigan. This event created new beach areas and set the stage for the  
 307 development of the surrounding region, including a network of roads and trails and the establishment of a  
 308 resort community. Over the years, the water levels fluctuated due to several issues, which resulted in a  
 309 subsequent drop of water and a net volume loss of approximately 1.93 million m<sup>3</sup> with an about 6 m drop  
 310 in head height. However, in the late 18<sup>th</sup> century, it rebounded again and reached a height of around 183 m,  
 311 the same as its current level. Hence, the lake's area changed, creating beach zones and impacting its overall  
 312 features. Crystal Lake became one of the first in Michigan to set a "natural level" at 600.48 feet (183 m).  
 313 An automatic gauge installed in 2014 helps record lake levels, contributing to the moderation of seasonal  
 314 changes [25]. It is important to mention that the lake's level plays a pivotal role in defining the water body.  
 315 The lake is primarily replenished by precipitation and groundwater; therefore, its water level remains  
 316 relatively independent of Lake Michigan.

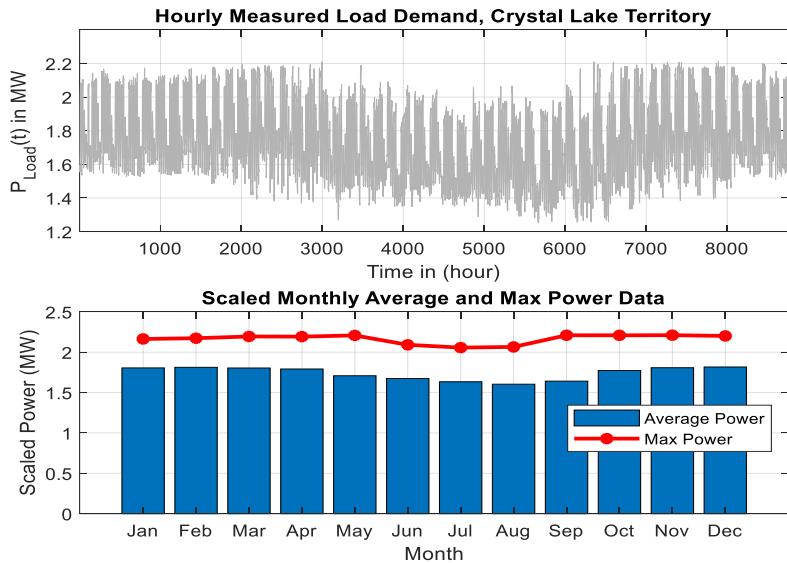
317 In this paper, UCL, depicted in Fig. 6, is designated as the upper reservoir for the MHPP, as illustrated  
 318 previously in the proposed system in Fig. 1. With a substantial water capacity of around 1.93 million cubic  
 319 meters, UCL inspires this study to investigate the potential of how lakes of this size function as efficient  
 320 energy storage systems (ESS). In addition to focusing on the capability of generating electricity within such  
 321 MHPPs, this research delves into the capacity of lakes like UCL to store energy effectively. Further details  
 322 regarding UCL can be found in Appendix A [26].



323  
 324 Fig. 6. Geographical representation of the UCL reservoir and the surrounding territory [26].

#### 325 2.4 Load Demand Data

326 The load demand data, sourced from UtilityAPI, represents measurements in megawatts (MW) supplying  
 327 a residential consumers in Benzie County, Michigan [27]. The observed load demand fluctuates within a  
 328 range spanning from 1.2552 MW to 2.2104 MW, as depicted in Fig. 7.



329  
 330 Fig. 7. The hourly measured demand for a 22 kV sub-feeder.

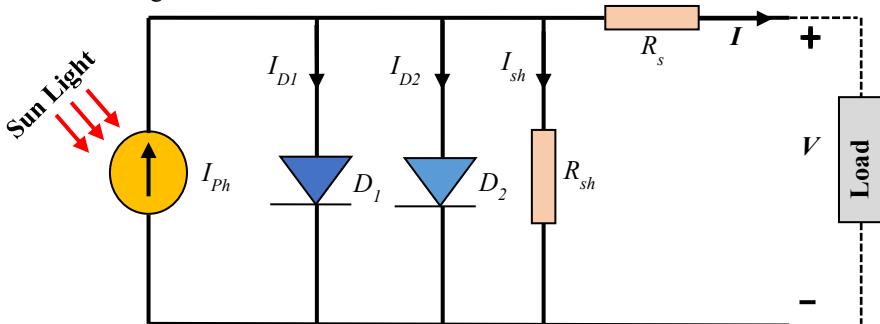
331 Notably, in Michigan, residential energy usage tends to spike during the winter months compared to the  
 332 summer. This trend is driven by the cold temperatures experienced during winters, prompting residents to  
 333 heavily utilize heating systems such as furnaces and boilers to maintain indoor warmth. The increased  
 334 demand for heating results in peak electricity usage in households during this season. On the other hand,  
 335 during the summer, although air conditioning usage may rise to beat the heat and humidity, overall  
 336 electricity demand from homes usually does not hit the same heights as in the winter. It can be noticed that  
 337 the monthly average demand is within a narrow range of around 1.7389MW during the year, as depicted in  
 338 Fig. 7.

### 339 3. Mathematical and Design Formulation

340 Mathematical modeling serves as the cornerstone and initial phase for precisely simulating and  
 341 optimizing the proposed system. Accurate modeling is crucial for determining the appropriate  
 342 configurations of the systems involved. For the renewable components, a quality factor-based model is  
 343 utilized for the solar PV array, while a cubic function is chosen to model the wind farm, accounting for  
 344 parameters such as the wind power coefficient and tip speed ratio. These models rely on input data presented  
 345 in Section 2. The energy management strategy, depicted in Fig. 8, guides the precise sizing and optimization  
 346 of the system using MOGWOA.

#### 347 3.1 Modeling of Solar PV Output Power

348 In this paper, the double-diode model (DDM) will be utilized to simulate the solar PV module. DDM  
 349 is commonly used for representing the behaviour of solar PV modules. However, DDM has rarely been  
 350 implemented in utility applications because of its large computation time and its complexity. This is because  
 351 it considers all types of losses in the modeling of solar PV module. Nonetheless, DDM gives a more  
 352 accurate and realistic description of the electrical characteristics of a solar cell compared to other types of  
 353 solar models, i.e., the single-diode model or the ideal single diode model. Hence, implementing this DDM  
 354 leads to a true sizing of the PV array and hence, the size and cost of the entire system [28]. The first diode  
 355 ( $D_1$ ) represents the diffusion process whilst the second diode ( $D_2$ ) simulates the recombination phenomena  
 356 [29]. In other words,  $D_1$  reflects how minority carriers diffuse into the depletion layer, while  $D_2$  mimics the  
 357 recombination within the junction's space charge region [30]. Therefore, the DDM takes into account solar  
 358 losses comprehensively, including diffusion, recombination, leakage to ground losses ( $R_{sh}$ ), and series  
 359 losses ( $R_s$ ) as shown in Fig. 8.



360  
 361 Fig. 8. Equivalent circuit of a two-diode PV module

362 The DDM gives a more precise and realistic output current from the cell compared with the simpler single-  
 363 diode model. This is due to considering the recombination process, i.e.,  $D_2$  current ( $I_{D2}$ ) as depicted in  
 364 equation (7) [31].  $I_{D1}$ ,  $I_{D2}$  and  $I_{sh}$  are computed as in (8), (9) and (10), respectively [32, 33].

365 
$$I = I_{ph} - I_{D1} - I_{D2} - I_{sh} \quad (7)$$

$$366 \quad I_{D1} = I_{o_1} \left( e^{\left( \frac{V+IR_s}{\alpha_1 V_T} \right)} - 1 \right) \quad (8)$$

$$367 \quad I_{D2} = I_{o_2} \left( e^{\left( \frac{V+IR_s}{\alpha_2 V_T} \right)} - 1 \right) \quad (9)$$

$$368 \quad I_{Sh} = \frac{V+IR_s}{R_{sh}} \quad (10)$$

369 After substituting (8), (9), and (10) in (7), equation (11) is resulted. The photon current ( $I_{Ph}$ ) as shown  
 370 in Fig. 8 and Equ. (11) affects by varying solar irradiance and temperature according to equation (12) [34].  
 371 The diode saturation currents  $I_{o_1}$  and  $I_{o_2}$  depend on temperature and can be expressed as given in (13).  
 372 Where  $E_g$  in (13) represents the band gap energy of the semiconductor and  $I_{o,STC}$  is the nominal saturation  
 373 current at (STC) and can be expressed by (14).

$$374 \quad I = I_{Ph} - I_{o_1} \left( e^{\left( \frac{V+IR_s}{\alpha_1 V_T} \right)} - 1 \right) - I_{o_2} \left( e^{\left( \frac{V+IR_s}{\alpha_2 V_T} \right)} - 1 \right) - \frac{V+IR_s}{R_{sh}} \quad (11)$$

$$375 \quad I_{Ph} = [I_{pv,STC} + K_I (T - T_{STC})] \frac{GTI}{G_{STC}} = I_{pv,STC} (1 + \alpha_{lsc} \Delta T) \frac{GTI}{G_{STC}} \quad (12)$$

$$376 \quad I_o = I_{o,STC} \left( \frac{T_{STC}}{T} \right)^3 \exp \left( \frac{qE_g}{\alpha K} \left( \frac{1}{T_n} - \frac{1}{T} \right) \right) \quad (13)$$

$$377 \quad I_{o,STC} = \frac{I_{sc,STC}}{\exp \left( \frac{V_{oc,STC}}{\alpha V_{T,STC}} \right) - 1} \quad (14)$$

378 From the previous two equations (13) and (14),  $I_o$  can be expressed as given in (15). As the diode  
 379 saturation current is very small, to simplify the model, the reverse saturation currents,  $I_{o_1}$  and  $I_{o_2}$  are set to  
 380 be equal as in (16) [31]. As  $\alpha_1$  and  $\alpha_2$  in equation (16) are the diode ideality factors that represent the  
 381 diffusion and recombination effects. Referring to Shockley's diffusion theory,  $\alpha_1$  must be unity while the  
 382 value of  $\alpha_2$  is varying. If the value of  $\alpha_2$  is in the range of  $1.2 \leq \alpha_2 \leq 2$ , the best match between the proposed  
 383 model and the practical I-V curve is obtained according to the simulation results. Hence,  $\frac{\alpha_1 + \alpha_2}{P} = 1$  and  
 384  $\alpha_1 = 1$ . It follows that the variable  $P$  can be chosen to be within  $2.2 \leq P \leq 3$ . Hence, considering these  
 385 constraints, (16) becomes as in (17) [35].

$$386 \quad I_o = \frac{I_{sc,STC} + K_I \Delta T}{[\exp \left( \frac{V_{oc,STC} + K_V \Delta T}{V_T * \alpha} \right) - 1]} \quad (15)$$

$$387 \quad I_{o_1} = I_{o_2} = \frac{I_{sc,STC} + K_I \Delta T}{[\exp \left( \frac{V_{oc,STC} + K_V \Delta T}{V_T (\alpha_1 + \alpha_2)/P} \right) - 1]} \quad (16)$$

$$388 \quad I_{o_1} = I_{o_2} = \frac{I_{sc,STC} + K_I \Delta T}{[\exp \left( \frac{V_{oc,STC} + K_V \Delta T}{V_T} \right) - 1]} = I_o \quad (17)$$

### 3.2 Mathematical modeling of Wind Farm

390 The power extracted from wind turbines ( $P_{WT}$ ) can be expressed as in (18). Note that, it depends on local  
 391 wind speed ( $V(t)$ ), the number of wind turbines ( $N_{WT}$ ), and the parameters of the manufactured wind  
 392 turbine, such as the rated power in kW ( $P_r$ ), cut-in speed ( $V_{ci}$ ) in m/s, and cut-out speed ( $V_{co}$ ) in m/s [36].

$$393 \quad P_{WT} = \begin{cases} 0 & , V(t) < V_{ci} \\ \frac{N_{WT} P_r (V(t)^3 - V_{ci}^3)}{(V_r^3 - V_{ci}^3)} & , V_{ci} < V(t) < V_r \\ N_{WT} P_r & , V_r < V(t) < V_{co} \\ 0 & , V(t) > V_{co} \end{cases} \quad (18)$$

### 3.3 Mathematical Modeling of Micro-Hydro and PHESS

395 MHPP can be in different types such as dam, run-off-river, and PHESS, or a combination of them. In this  
 396 study, the MHPP will be in the form of PHESS. The PHESS system operates as a giant battery to store  
 397 energy. They can store energy as a form of potential energy by pumping the water from the lower reservoir  
 398 (i.e., Lake Michigan) to the upper Crystals Lake (UCL) reservoir, shown in Fig. 6. This process is called  
 399 pumping mode. When the hybrid system comprised of solar PV and wind turbines cannot sufficiently meet  
 400 the load demand, the water is released from the UCL to the lower reservoir, in the process of generating  
 401 mode.

### 402 3.3.1. Pumping (or Charging) Mode

403 The pump flow rate ( $q_p(t)$ ) from the lower reservoir to UCL is expressed as in Equation (19). It is the  
 404 relation of surplus or extra power from the hybrid system ( $P_{MHPP\_ch}(t)$ ) in kW, pump efficiency ( $\eta_p$ ), head  
 405 height ( $h$ ) in m, water density ( $\rho$ ) (1000 kg/m<sup>3</sup>), and gravity acceleration ( $g$ ) (9.8 m/s<sup>2</sup>) [37].

$$406 q_p(t) = \frac{\eta_p P_{MHPP\_ch}(t)}{\rho g h} \quad (19)$$

### 407 3.3.2. Generating (or Discharging) Mode

408 The released power from the UCL is used to spin the turbine/generator set when the solar PV and wind  
 409 turbine renewable facilities cannot meet the load demand, and this power can be computed as in (20) [37].  
 410 Note that,  $\eta_t$  is the efficiency the turbine/generator set and  $q_t(t)$  is the water volumetric flow rate in m<sup>3</sup>/s.

$$411 P_{MHPP\_dis}(t) = \eta_t \times \rho \times g \times h \times q_t(t) \quad (20)$$

### 412 3.3.3. Upper Crystal Lake (UCL) Reservoir

413 The quantity of water ( $QOW$ ) stored in the UCL at any time ( $t$ ) is expressed as in (21) [37]. The  $QOW$  in  
 414 the UCL is governed by the constraints as explained in (22), as the upper and lower safety limit.  $\alpha$  is the  
 415 loss factor from evaporation and leakage to ground. In this paper,  $\alpha$  will be considered zero due to the  
 416 massive volume of UCL.

$$417 QOW_{UCL}(t) = QOW_{UCL}(t-1)(1-\alpha) + q_p(t) - q_t(t) \quad (21)$$

$$418 QOW_{UR\min} \leq QOW_{UR} \leq QOW_{UR\max} \quad (22)$$

### 419 3.3.4. Storage Capacity

420 The UCL must have sufficient water stored to meet the power requirements of the demand during extended  
 421 power outages [38]. The water level ( $QOW$ ) in the UCL essentially acts as the state of charge explained  
 422 before for the storage tank. The gravitational potential energy ( $E_C$ ) in kWh stored in the UCL can be  
 423 measured as in (23) [39], where  $V$  stands for the volume or storage capacity of the water reservoir in cubic  
 424 meters (m<sup>3</sup>).

$$425 E_C = \frac{\mu_t \times \rho \times V \times g \times h}{3.6 \times 10^6} \quad (23)$$

426 Based on the planned capacity of the UCL, and the daily energy consumption by the load ( $E_{Load}$ ) in (kWh),  
 427 the duration of autonomy days ( $n_{day}$ ) can be determined by assessing the potential energy stored in the  
 428 UCL. This calculation can be performed using the following formula (24) [34].

$$429 n_{day} = \frac{E_C}{E_{Load}} \quad (24)$$

## 430 4. System's Operational Flow Chart

431 Fig. 9 illustrates the operational flow chart and energy management system. This flow chart explains the  
 432 priority and the flow of energy within the system to meet the load demand. It begins with the power  
 433 generated by the solar PV and wind plants, followed by the MHPP, and is then sourced from the grid. It  
 434 also provides a general overview of the algorithm's functionality to optimally design the system.

If the power generated from the hybrid system ( $P_{gen}(t)$ ), as defined in (25), originating from both the PV system ( $P_{PV\,inv}(t)$ ) as in (26) and wind farm ( $P_{WT}(t)$ ) as specified in (18), is insufficient to satisfy the load demand ( $P_L(t)$ ) presented in section 2.4, the needed load will be covered by generating power during discharging mode from the MHPP facility ( $P_{MHPP\,dis}(t)$ ). Hence, if  $P_{gen}(t)$  and  $P_{MHPP\,dis}(t)$  are still inadequate to meet the load demand, the grid feeds the load demand ( $P_{gp}(t)$ ) as outlined in (27). On the other hand, in the event of extra power generated from the hybrid system ( $P_{extra}(t)$ ) as in (28), then this power is stored in MHPP by pumping the water from the lower reservoir to the UCL ( $P_{MHPP\,ch}(t)$ ) if and only if the QOW in the UCL is less than the  $QOW_{max}$ , if not, the QOW is at the maximum limit, and the extra power is sold to the grid ( $P_{g sold}(t)$ ) [11, 12].

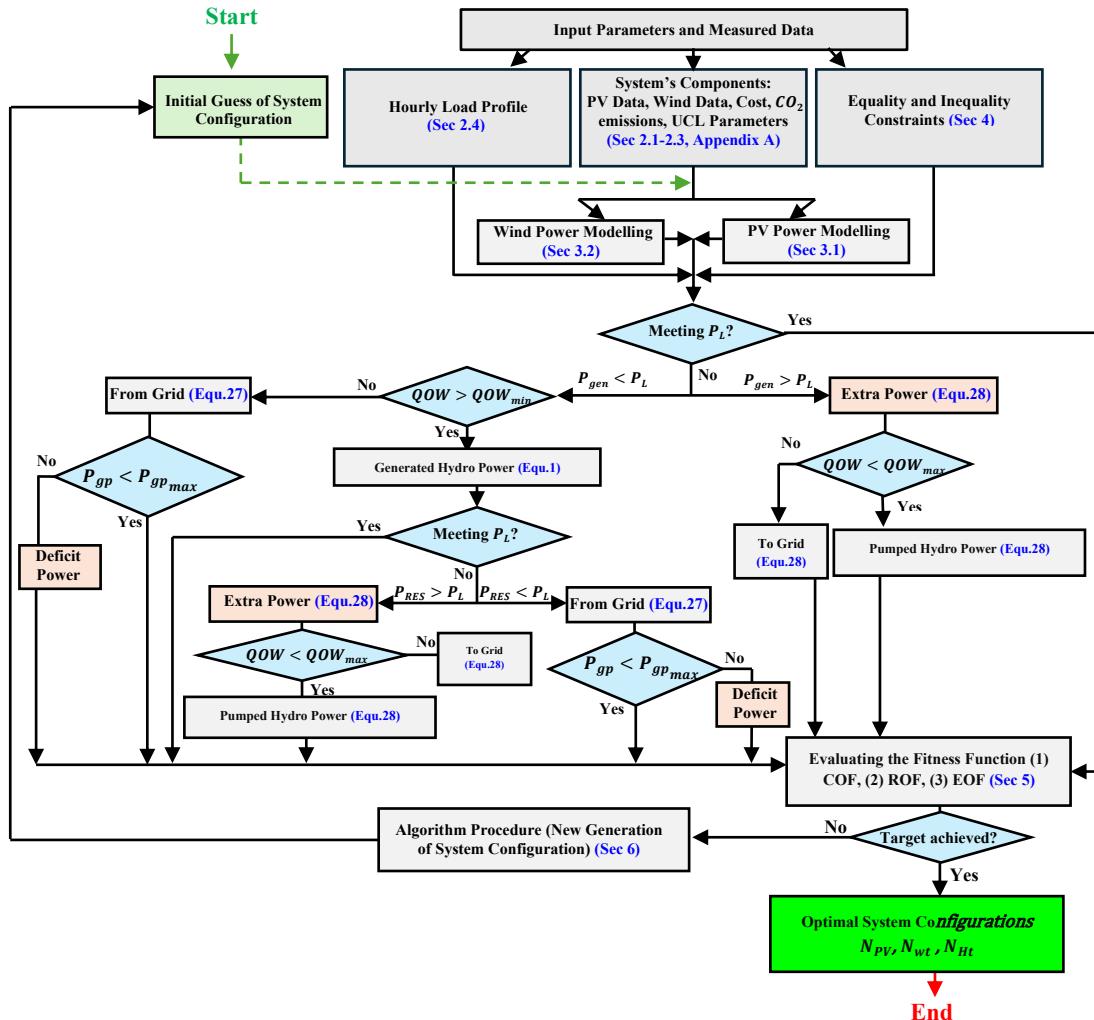


Fig. 9. Energy management strategy and Operational flowchart.

446 The multi-objective function is assessed at each time step, as shown in Fig. 9. In the case that the  
 447 maximum power obtained from all renewables covers the load demand and increases, but the grid capacity  
 448 limit is reached, then the extra power will be directed to a dummy load. In scenarios where the power

449 produced from all renewables and the grid purchased are insufficient to satisfy the load demand, then there  
 450 is a deficit power ( $P_{deficit}(t)$ ) as depicted in the balance power equation in (28) [11, 12].

$$451 \quad P_{gen}(t) = P_{PV\,inv}(t) + P_{WT}(t) \quad (25)$$

$$452 \quad P_{PV\,inv}(t) = \eta_{inv} \times P_{PV}(t) \times f_{PV} \quad (26)$$

$$453 \quad P_{gp}(t) = P_L(t) - (P_{gen}(t) + P_{MHPP\,dis}(t)) , if \quad P_{gp}(t) \leq P_{gp}(t)_{max} \quad (27)$$

$$454 \quad P_{extra}(t) = P_{gen}(t) - P_L(t) = \begin{cases} P_{MHPP\,ch}(t) & , QOW < QOW_{max} \\ P_{gsold}(t) & , QOW \geq QOW_{max} \end{cases} \quad (28)$$

$$455 \quad P_{gen}(t) + P_{MHPP\,dis}(t) + P_{gp}(t) = P_L(t) + P_{MHPP\,ch}(t) + P_{gsold}(t) + P_{deficit}(t) \quad (29)$$

## 456 5. System's Multi-Objective Functions and Performance Evaluators

457 This section discusses the multi-objective functions that govern the performance of the system and other  
 458 performance indicators to be computed for each case scenario. In this paper, there are three multi-objective  
 459 scenarios, including economic aspects versus reliability in one case, ecological and cost impacts in the  
 460 second case scenario, and all objective functions in the 3<sup>rd</sup> scenario. The 1<sup>st</sup> multi-objective function  
 461 scenario will consider minimizing the levelized cost of energy (LCOE) and maximizing the index of  
 462 reliability (IR) using the Multi-Objective Grey Wolf Optimizer (MOGWO) algorithm to find the best  
 463 optimal solution. However, minimizing the LCOE and maximizing the carbon-dioxide reduction amounts  
 464 ( $CO_2RA$ ) will be taken into account for the 2<sup>nd</sup> case scenario. In the 3<sup>rd</sup> scenario, IR and  $CO_2RA$  will be  
 465 maximized, and LCOE will be minimized as a triple objective function.

466 The set of solutions in the optimized multi-objective function, namely Pareto front solutions, will  
 467 provide all types of solutions, including affordable, reliable, and ecological solution sets. For instance, if  
 468 the designer focuses on the system to be more economic, the set of solutions closer to the minimal cost  
 469 would be better regardless of the reliability and so on. Note that the optimal configuration of the system  
 470 depends on the multi-objective function or the best decision variables, including the number of PV panels  
 471 ( $N_{PV}$ ), the number of wind turbines ( $N_{wt}$ ), and the number of hydro-turbine units ( $N_{Ht}$ ).

### 472 5.1. Cost Objective Function (COF)

473 The LCOE is a mathematical estimation process used in the energy business to calculate the average  
 474 cost of generating one unit of electricity during the system's lifetime. It considers several parameters,  
 475 including initial capital costs, operations and maintenance expenses, fuel costs, and the system's projected  
 476 lifespan energy production.

477 The COF of LCOE will be minimized, and it is considered as the 1<sup>st</sup> objective function. It is noted that  
 478 the computation of the LCOE involves dividing the Annualized Cost of the System (ACS) by the energy  
 479 supplied to meet the load demand (EL), as illustrated in equation (30). The ACS is derived by multiplying  
 480 the Total Current Cost (TCC) with the Capital Recovery Factor (CRF). TCC is computed by summing the  
 481 discounted values of various costs in the system, including Capital Cost (CC), Operation and Maintenance  
 482 Cost (OMC), Replacement Cost (RC), and Salvage Cost (SC). The CRF is determined by (31), while the  
 483 real interest rate ( $i$ ) is found using (32) depending on  $i'$  representing the nominal interest rate and the  
 484 inflation rate ( $f_{inf}$ ). Appendix B provides the cost values for each component, including their respective  
 485 lifetimes, along with the financial parameters required for constructing both nominal and discounted  
 486 cashflows [40].

$$487 \quad LCOE = \frac{ACS}{E_s} \quad (30)$$

$$488 \quad CRF = \frac{i(1+i)^N}{(1+i)^N - 1} \quad (31)$$

$$489 \quad i = \frac{i' - f_{inf}}{1 + f_{inf}} \quad (32)$$

### 490 5.2. Reliability Objective Function (ROF)

491 The Index of reliability (IR) refers to the system's ability to satisfy the load demand, mentioned in  
 492 section 2.4, without any interruptions or deficit in energy. The 2<sup>nd</sup> ROF is to be maximized and can be  
 493 computed as in (33) [41].

$$494 \quad IR = 1 - \frac{\sum_{t=1}^{8760} [P_L(t) - (P_{PV\,inv}(t) + P_{WT}(t) + P_{MHPP\,dis} + P_{gp}(t))]}{\sum_{t=1}^{8760} P_L(t)} \quad (33)$$

### 495 5.3. Ecological Objective Function (EOF)

496 Carbon-Dioxide Reduction Amount ( $CO_2RA$ ) stands for the reduction in harmful emissions achieved by  
 497 the utilization of renewable energy resources ( $E_{R\,gen}$ ) rather than the conventional fossil fuels, as indicated  
 498 in equation (34) [42].  $F_{CO_2}$  represents the carbon dioxide emission factor, and it is estimated to be 0.553  
 499 tCO<sub>2</sub>/MWh in the context of Michigan [43]. The 3<sup>rd</sup> EOF of  $CO_2RA$  is maximized using MOGWO  
 500 algorithm as explained in sections 6 and 7.

$$501 \quad CO_2RA = E_{R\,gen} \times F_{CO_2} \quad (34)$$

### 502 5.4. Complete constrained objective function formulation

503 The system optimization and sizing are determined by decision variables and a set of equality and  
 504 inequality constraints, as outlined in Equ. (35) [44]. These decision variables include the number of PV  
 505 panels ( $N_{PV}$ ), the number of wind turbines ( $N_{WT}$ ) and the number of hydro-turbine units ( $N_{Ht}$ ).

$$506 \quad \left\{ \begin{array}{l} COF: \text{Min} \left( LCOE = \frac{ACS}{E_s} \right) \\ ROF: \text{Max} \left( IR = 1 - \frac{\sum_{t=1}^{8760} [P_L(t) - (P_{PV\,inv}(t) + P_{WT}(t) + P_{MHPP\,dis} + P_{gp}(t))]}{\sum_{t=1}^{8760} P_L(t)} \right) \\ EOF: \text{Max} \left( CO_2RA = E_{R\,gen} \times F_{CO_2} \right) \\ (COF \& ROF) \parallel (COF \text{ and } EOF) \parallel (COF \& ROF \& EOF) \\ N_{PV}, N_{WT}, N_{Ht} \\ \text{Subject to} \\ \left\{ \begin{array}{l} P_{gp}(t) \leq P_{gp\,max} \\ QOW_{min} \leq QOW(t) \leq QOW_{max} \\ P_{extra}(t) = P_{gen}(t) - P_L(t) = \begin{cases} P_{MHPP\,ch}(t), & QOW < QOW_{max} \\ P_{gsold}(t), & QOW \geq QOW_{max} \end{cases} \\ P_{gp}(t) = P_L(t) - (P_{gen}(t) + P_{MHPP\,dis}(t)) \\ P_{gen}(t) + P_{MHPP\,dis}(t) + P_{gp}(t) = P_L(t) + P_{MHPP\,ch}(t) + P_{gsold}(t) + P_{deficit}(t) \end{array} \right. \end{array} \right. \quad (35)$$

### 507 5.5. Other Performance Evaluators

508 This section shows other appropriate performance indicators to assess the behavior of the system at an

optimal solution of each scenario. This includes estimating the Loss of Load Probability (LOLP), Carbon-Dioxide Emissions Amount (CEA), and Renewable Storage Factor (RSF).

LOLP serves as a metric to assess the number of hours in a given year during which the system falls short of meeting the load requirements, as indicated in equation (36). A lower LOLP value indicates a higher level of reliability in the system. Essentially, LOLP delves into the hours when the system experiences inadequacy in meeting the load demand or encounters a power deficit [45].

$$LOLP = \frac{\sum_{t=1}^{8760} h_{[P_L(t) > (PPV_{inv}(t) + PWT(t) + PMHPP_{dis} + Pgp(t))]}}{8760} \quad (36)$$

CEA is a measure of the greenhouse gas emissions (GHGEs), primarily  $CO_2$ , released when relying on the utility grid, as specified in equation (37) [42]. This quantity is related to the  $CO_2$  emission factor ( $F_{CO_2}$ ), mentioned before. Additionally, it factors in the losses percentage in transmission and distribution lines (PL), with Michigan registering approximately 5% in this regard [46]. Notably, a lower CEA value signifies a more efficient utilization of renewable energies, highlighting the environmental benefits associated with reduced carbon emissions.

$$CEA = \frac{E_{gp} \times F_{CO_2}}{1-PL} \quad (37)$$

RSF gauges the extent to which the energy supplied by the UCL of the MHPP facility fulfills the overall demand, as expressed in equation (38) [47]. Here,  $E_{Storage}$  represents the energy conveyed to the load by PHS, while  $E_{System}$  encompasses the energy output of the entire system, inclusive of MHPP.

$$RSF = \sum_0^t \frac{E_{Storage}}{E_{System}} \quad (38)$$

## 6. System's Multi-Objective Optimization Algorithms

This research employs two multi-objective algorithms to simulate the proposed system. Initially, the MOGWOA is adapted to model the system, incorporating various multi-objective scenarios. This involves modifying the algorithm to minimize system costs while maximizing reliability and ecological considerations. Subsequently, the MOFEPSOA is utilized to validate the results obtained from the MOGWOA. It is important to note that each scenario yields multiple solutions, including reliable, ecological, economic, and optimal compromise solutions, based on the preferences of the designers. The optimal solution, balancing all objectives, is determined using a fuzzy logic approach, as detailed in section 7.

### 6.1. Multi-objective Grew-Wolf optimization algorithm (MOGWOA)

Mirjalili and Lewis introduced the Grey Wolf Optimizer (GWO) algorithm, which was originally inspired by the social leadership and hunting strategies of grey wolves. The MOGWOA incorporates a fixed-size external archive into the GWO, which enables the storage and retrieval of Pareto optimal solutions. This archive plays a crucial role in establishing a social hierarchy and emulating the hunting behavior of grey wolves in multi-objective search environments. It is worth mentioning that the MOGWOA algorithm was used to solve multi-objective optimization problems, as it is preferred in research for its simplicity and ability to adaptively tune parameters. Many studies, as in [48-52], recommend MOGWOA for tackling complex optimization challenges. Consequently, we employed MOGWOA in this article. For instance, in [53], the primary aim of the proposed MOGWO was to optimize the switching matrix structure to minimize row current differences and maximize output power. This method effectively addressed the challenge of adjusting objective function weights to ensure system reliability and efficiency. The comparison demonstrated MOGWO's superiority in handling multi-peak issues in P-V characteristics, achieving the highest power levels.

551 When formulating the social hierarchy within the GWO, the most appropriate solution is designated as  
 552 the alpha ( $\alpha$ ) wolf. Subsequently, the second and third best solutions are identified as the beta ( $\beta$ ) and delta  
 553 ( $\delta$ ) wolves respectively as shown in Fig. 10. All other candidate solutions are classified as omega ( $\omega$ )  
 554 wolves. Within the GWO algorithm, the optimization process is directed by  $\alpha$ ,  $\beta$ , and  $\delta$  wolves, while  $\omega$   
 555 wolves follow their lead in the pursuit of the global optimum. Appendix C imitates the encircling behavior  
 556 equations observed in grey wolves during hunts [54]. It is observed that  $t$  denotes the present iteration, while  
 557  $\vec{A}$  and  $\vec{C}$  represent coefficient vectors.  $\vec{X}_p$  refers to the position vector of the prey and  $\vec{X}$  signifies the  
 558 position vector of a grey wolf. The elements of the coefficient vector  $\vec{a}$  linearly decrease from 2 to 0  
 559 throughout the iterations. Additionally,  $\vec{r}_1$  and  $\vec{r}_2$  denote random vectors within the range of [0,1] [55].

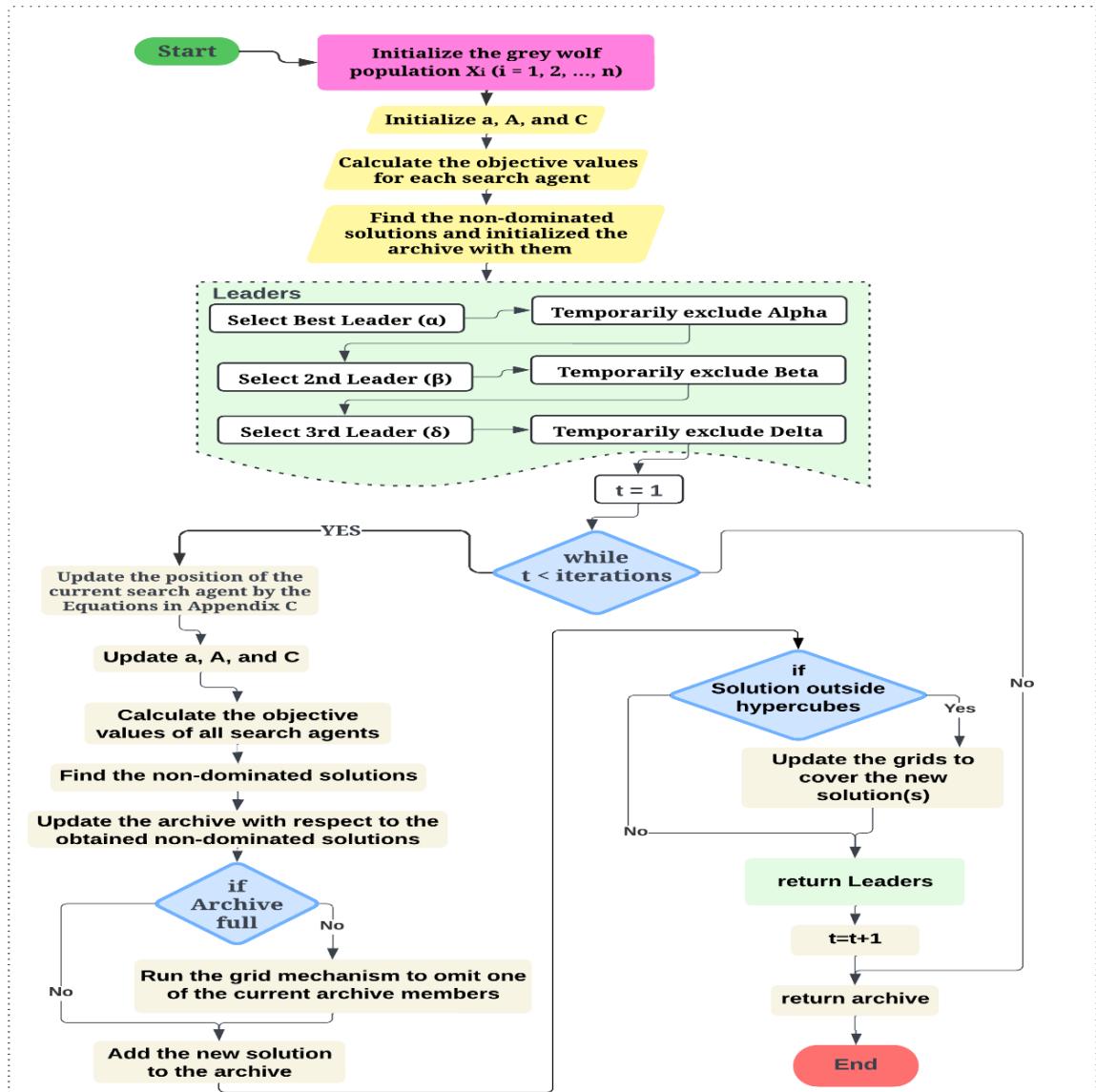


Fig. 10. General operational flowchart of the proposed MOGWOA.

562 The MOGWO algorithm uses simulated social leadership and encircling mechanisms to obtain the  
 563 optimal solution for optimization problems. This algorithm retains the initial three best solutions acquired  
 564 and directs other search agents, including omegas, to refresh their positions accordingly. The parameters a,  
 565 A, and C are important in guiding the exploration process of the algorithm, as shown in Appendix C and  
 566 Fig. 10. Both variables A and C are coefficient vectors, with a starting from 2 and linearly decreasing to 0  
 567 over the iterations. This decrease causes the algorithm to gradually shift its focus from exploration, which  
 568 involves a broad search of the solution space, to exploitation, which involves a more focused search in the  
 569 local area around the best solutions found so far. Finally, to simulate the hunting process and identify  
 570 promising areas within the search space, formulas in Appendix C are executed continually for each search  
 571 agent during optimization, as illustrated in Fig. 10 [54].

### 572 6.2. Multi-objective Feasibility Enhanced Particle Swarm Optimization Algorithm (MOFEPSOA)

573 MOFEPSOA, developed by Hasanoglu and Dolen, is a method designed for addressing multi-objective  
 574 problems with constraints. It deals exclusively with inequality constraints, requiring any equality  
 575 constraints to be converted into inequality constraints. The algorithm begins by initializing parameters and  
 576 assessing particle positions for feasibility. If a position is feasible, it updates velocities and flight behaviours  
 577 accordingly; otherwise, it adjusts them for infeasible positions. Subsequently, the algorithm rechecks the  
 578 particle's new position for feasibility [56]. In this paper, MOFEPSOA will compute the objective vectors  
 579 (LOCE, IR, and CO<sub>2</sub>RA) and include the current solution in the best set. It will update the best solution in  
 580 the objective vector if others do not dominate it. If the new particle position is not the best, it checks if it is  
 581 not the final particle. If there are remaining iterations, MOFEPSOA repeats the previous steps from  
 582 initialization. Finally, upon reaching the stopping criteria for the number of particles and iterations,  
 583 MOFEPSOA presents all feasible non-dominant trade-off solutions as the Pareto front. More detailed  
 584 explanations of the algorithm are presented in [57].

### 585 6.3. Employing Fuzzy Logic method for compromised Solution Identification

586 Many common approaches can find the best non-dominant solution, such as the fuzzy logic method. The  
 587 fuzzy logic method uses the fuzzy membership function  $\mu_i(F_i)$  to find the best non-dominant solution out  
 588 of all non-dominant solutions stored in the archive of the MOGWOA [58]. The fuzzy membership function  
 589 in (39) is used to convert each objective function ( $F_i$ ) to a membership value in range between (0, 1) [59].  
 590 Where  $F_i^{\min}$  and  $F_i^{\max}$  represent the minimum and maximum objective function values, respectively.

$$591 \mu_i(F_i) = \begin{cases} 1, & F_i(x) \leq F_i^{\min} \\ 0, & F_i(x) \geq F_i^{\max} \\ \frac{F_i^{\max} - F_i(x)}{F_i^{\max} - F_i^{\min}}, & F_i^{\min} \leq F_i(x) \leq F_i^{\max} \end{cases} \quad (39)$$

592 As introduced before, this study will investigate three main scenarios. Therefore, a multi-objective  
 593 optimization is performed to find three corresponding best solutions which are the reliable and affordable.  
 594 Equation (40) is used to minimize  $LCOE(x)$  and maximize  $IR(x)$ , whereas (41) is used to maximize  
 595  $CO_2RA(x)$  while minimizing  $LCOE(x)$ . Finally, (42) is used to minimize  $LCOE(x)$  and maximize  
 596  $CO_2RA(x)$  and  $IR(x)$  simultaneously.

$$597 \text{Minimize } F_1(x) = \left[ LCOE(x), \frac{1}{IR(x)} \right] \quad (40)$$

$$598 \text{Minimize } F_2(x) = \left[ \frac{1}{CO_2RA(x)}, LCOE(x) \right] \quad (41)$$

$$599 \text{Minimize } F_3(x) = \left[ LCOE(x), \frac{1}{IR(x)}, \frac{1}{CO_2RA(x)} \right] \quad (42)$$

600

## 7. Results and Discussion

601

MATLAB R2022a is utilized to simulate the energy management system for the Crystal Lake territory case study. The MOGWO algorithm is employed to execute the system based on the data collected for the year 2022. The analysis includes three scenarios: the 1<sup>st</sup> scenario aims to maximize ROF (IR) whilst minimizing COF (LCOE), the 2<sup>nd</sup> scenario focuses on maximizing EOF ( $CO_2RA$ ) whilst minimizing COF, and the 3<sup>rd</sup> scenario is for maximizing both ROF and EOF while minimizing COF. Accordingly, the MOFEPSOA is utilized to validate the findings obtained from MOGWOA.

607

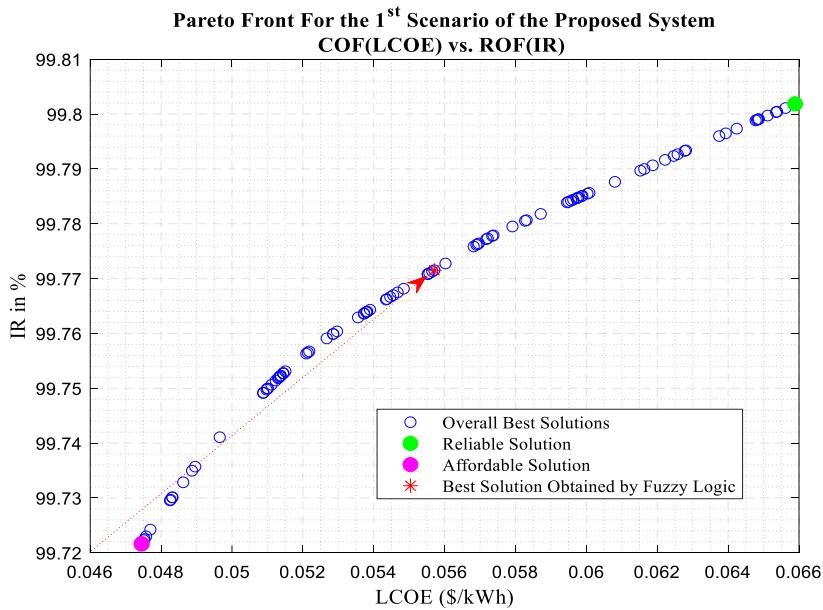
### 7.1. Optimization using MOGWO algorithm

608

This study employs the MOGWOA technique to tackle the optimization problem, utilizing the mentioned decision variables of renewable components. For each scenario, a set of solutions is generated, typically amounting to around 100 solutions for each Pareto front. From this set, four essential solutions are selected and discussed, depending on the specific scenario. For instance, in the 1<sup>st</sup> scenario, the first solution, termed the reliable solution, represents the highest IR value and the highest LCOE value. The second solution known as the economic solution, exhibits the lowest IR value and the lowest LCOE value, named. The third solution, referred to as the compromised solution, lies somewhere between reliable and affordable solutions. The compromised solution is chosen based on its proximity to the origin, indicating reliability and cost-effectiveness in one aspect, and affordability and ecological sustainability in another. The Pareto frontier optimization for the 1<sup>st</sup> scenario is shown in Fig. 11.

617

Table 1 presents the optimization outcomes for the 1<sup>st</sup> scenario with three selected solutions, as observed in Fig. 11, detailing the objective functions of LCOE, and IR, and the decision variables  $N_{PV}$ ,  $N_{WT}$ , and  $N_{Ht}$ . Notably, the optimal solution highlights the system's reliability, achieving an IR of 99.772%. However, this reliability comes at a cost, with an LCOE of 0.055708\$/kWh. Economic insights reveal that the LCOE stands at 0.04745\$/kWh, with an associated IR of 99.722% for the economic solution. Subsequently, the best solution is to install 4710 solar panels, 19 wind turbines, and 8 hydro-turbines. The chosen point aims to minimize the system's LCOE, whilst maximizing systems reliability.



625

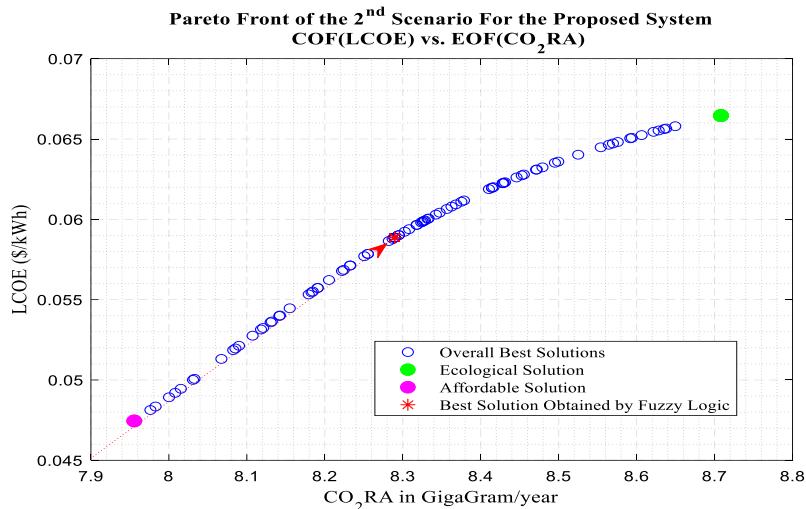
626

Fig. 11. Pareto Front For the 1<sup>st</sup> Scenario of the proposed system by MOGWOA.

627 Table 1. Optimization using MOGWOA for the 1<sup>st</sup> Scenario; COF (LCOE) vs. ROF (IR)

| Quantity             | COF (LCOE) vs. ROF (IR)  |             |               |
|----------------------|--------------------------|-------------|---------------|
|                      | Economic                 | Reliable    | Best Solution |
| Objective Functions  | LCOE in \$/kWh           | 0.04745     | 0.06589       |
|                      | IR in %                  | 99.722      | 99.802        |
| Decision Variables   | $N_{PV}$                 | 2500        | 7878          |
|                      | $N_{WT}$                 | 17          | 20            |
|                      | $N_{Ht}$                 | 7           | 9             |
| Energies in GWh/year | $E_{PV\,inv}$            | 1.224321    | 3.85808       |
|                      | $E_{WT}$                 | 4.711992    | 5.54352       |
|                      | $E_{hydro\,turbine}$     | 7.2039247   | 6.126815      |
|                      | $E_{gsold}$              | 0.00318518  | 0.52458969    |
|                      | $E_L$                    |             | 15.2327969    |
|                      | $E_{purchased}$          | 2.43467     | 1.0199436     |
|                      | $E_{MHPP\,ch}$           | 0.096581824 | 0.8211559     |
| Other Indicators     | $LOLP$ in %              | 3.6         | 1.701         |
|                      | $ACS$ in Million \$/year | 1.04597354  | 1.0903        |
|                      | $CEA$ in $10^3$ ton/year | 1.27260922  | 0.61141779    |
|                      | $RSF$ in %               | 47.292      | 40.221        |
|                      |                          |             | 0.3989326     |
|                      |                          |             | 44.012        |

628 Fig. 12 illustrates the Pareto frontier optimization for the 2<sup>nd</sup> scenario implemented using MOGWOA.  
629 It aims to minimize COF (LCOE) and maximize EOF (CO<sub>2</sub>RA). This way, it could help decision makers  
630 and design engineers who care more about environmental impacts to effectively recognize how integrating  
631 renewables could mitigate GHG emissions while minimizing the system's cost, as shown in Fig. 12.

632 Fig. 12. Pareto Front For the 2<sup>nd</sup> Scenario of the proposed system by MOGWOA.  
633

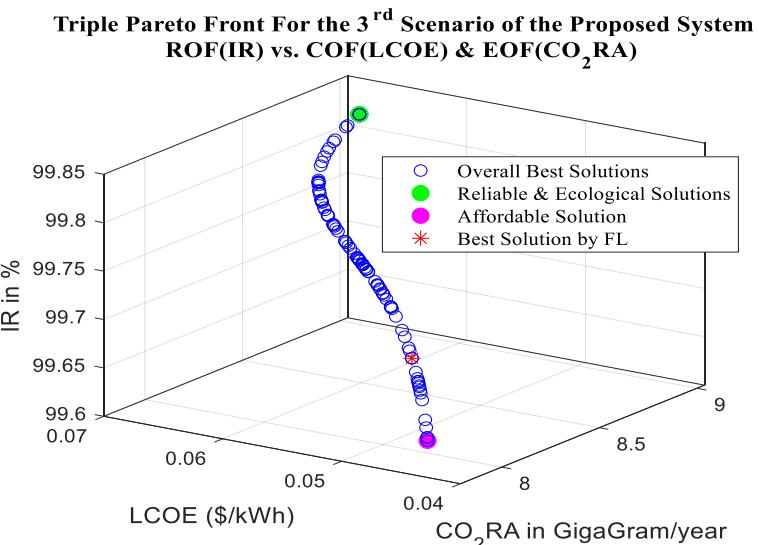
634 Table 2 shows the objective functions, decision variables, energies, and other performance indicators  
635 for the 2<sup>nd</sup> scenario. Compared with the economic and ecological cases, it can be noticed that the optimal  
636 solution achieved a compromised set of solutions, with 5639 solar panels, 19 wind turbines, and 8 hydro-  
637 turbines. Additionally, the findings are close to those obtained using the 1<sup>st</sup> scenario, which proves the

638 effectiveness of the optimization algorithm and the proposed methodology.

639 Table 2. Optimization using MOGWOA for the 2<sup>nd</sup> Scenario; COF (LCOE) vs. EOF (CO<sub>2</sub>RA)

| Quantity            |  | COF (LCOE) vs. EOF (CO <sub>2</sub> RA)           |  |  |
|---------------------|--|---|--|--|
|                     |  | Economical  | Ecological                                     | Best Solution                                      |
| Objective Functions | LCOE in \$/kWh<br>CO <sub>2</sub> RA in 10 <sup>3</sup> ton/year   | 0.04911<br>8.0056                                 | 0.066457<br>8.7082                             | 0.059181<br>8.3008                                 |
| Decision Variables  | $N_{PV}$<br>$N_{WT}$<br>$N_{Ht}$   | 2964<br>18<br>7                                   | 8150<br>20<br>9                                | 5639<br>19<br>8                                    |
| Energies in GWh     | $E_{PV\,inv}$<br>$E_{WT}$<br>$E_{hydro\,turbine}$<br>$E_{gsold}$<br>$E_L$<br>$E_{purchased}$<br>$E_{MHPP\,ch}$ | 1.4515561<br>4.9891683<br>6.9300397<br>0.01125435 | 3.991289<br>5.5435203<br>6.085227<br>0.5805854 | 2.7615806<br>5.2663443<br>1.35779573<br>0.17126333 |
| Other Indicators    | $LOLP$ in %<br>$ACS$ in Million \$/year<br>$CEA$ in 10 <sup>3</sup> ton/year<br>$RSF$ in %                     | 3.3904<br>1.0482<br>1.202346<br>45.494            | 1.7009<br>1.1054<br>0.6072172<br>39.948        | 2.2945<br>1.051<br>0.81394744<br>42.352            |

640 In this paper, modified triple objective functions are employed to enhance the simulation and accuracy  
641 of the proposed system. This approach is uncommon in similar studies as it incorporates three objective  
642 functions (reliability, ecological, and economic) into a triple Pareto frontier analysis, as illustrated in Table  
643 3 and Fig. 13. Existing research typically focuses on two objective functions, making this method distinct  
644 in its comprehensive consideration of all three aspects simultaneously.



645 Fig. 13. Triple Pareto Front For the 3<sup>rd</sup> Scenario of the proposed system using MOGWOA.  
646

647 Table 3. Optimization using MOGWOA for the 3<sup>rd</sup> Scenario: Triple Objective Functions  
 648 “ROF (IR) vs. COF (LCOE) & EOF (CO<sub>2</sub>RA)”

|                         |  | ROF (IR) vs. COF (LCOE) & EOF (CO <sub>2</sub> RA) |              |            |               |
|-------------------------|--|--|--------------|------------|---------------|
| Quantity                |  | Economic   | Reliable     | Ecological | Best Solution |
| Objective Functions     | IR in %  | 99.638   | 99.812       | 99.812     | 99.705        |
|                         | LCOE in \$/kWh                                 | 0.042771   | 0.069025     | 0.069025   | 0.046147      |
|                         | CO <sub>2</sub> RA in 10 <sup>3</sup> ton/year | 7.7887   | 9.0393       | 9.0393     | 7.9142        |
| Decision Variables      | $N_{PV}$                                       | 2052   | 9823         | 9823       | 5124          |
|                         | $N_{WT}$                                       | 17   | 20           | 20         | 19            |
|                         | $N_{Ht}$                                       | 7  | 9            | 9          | 8             |
| Storage Capacity in GWh |  |  | 14.9734      |            |               |
| $n_{day}$ in days       |  |  | 8807         |            |               |
| Energies in GWh         | $E_{PV\,inv}$                                  | 1.00492347   | 4.81060586   | 4.81060586 | 2.50937       |
|                         | $E_{WT}$                                       | 4.71199224   | 5.54352      | 5.54352    | 5.2663443     |
|                         | $E_{hydro\,turbine}$                           | 7.31769778   | 5.86857699   | 5.86857699 | 6.5881848     |
|                         | $E_{purchased}$                                | 2.20215013   | 0.9769594    | 0.9769594  | 1.3859264     |
|                         | $E_{gsold}$                                    | 0.00141861   | 0.99834236   | 0.99834236 | 0.12942049    |
|                         | $E_L$  |  | 15.232796912 |            |               |
| Other Indicators        | $E_{MHPP\,ch}$                                 | 0.076158288  | 0.99708479   | 0.99708479 | 0.42996824    |
|                         | LOLP in %                                      | 3.6872   | 1.6324       | 1.6324     | 2.3516        |
|                         | ACS in Million \$/year                         | 1.0303   | 1.1877       | 1.1877     | 1.0167        |
|                         | CEA in 10 <sup>3</sup> ton/year                | 1.32010613   | 0.58565      | 0.58565    | 0.830810725   |
| RSF in %                |  | 48.039   | 38.526       | 38.526     | 43.25         |

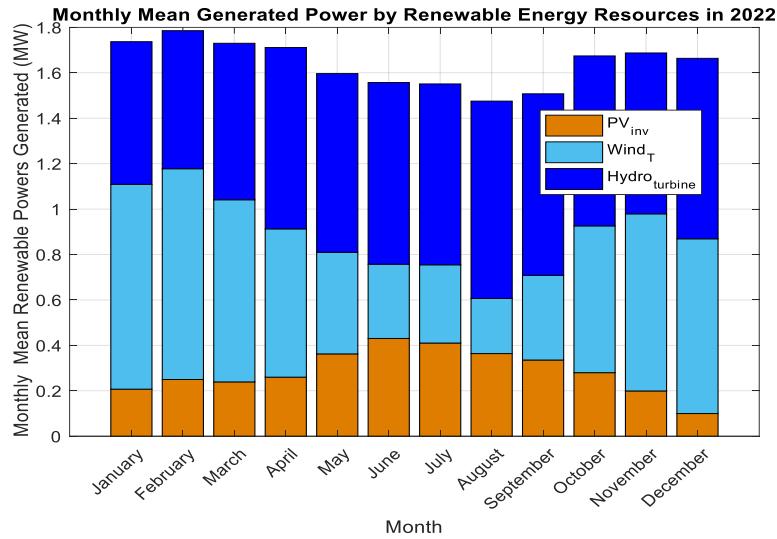
649 The blue circles represent the candidate solutions, while the green circle highlights a solution that is both  
 650 reliable and ecological, with the values of 99.812% and  $0.069025 \times 10^3$  ton/year, respectively, as outlined  
 651 in Table 3. This is because the algorithms aim to maximize both IR and CO<sub>2</sub>RA. However, the cost is taken  
 652 into account with a minimum economic LCOE of 0.042771\$/kWh. Upon closer examination of Table 3, it  
 653 becomes evident that the fuzzy logic approach yields the optimal solution among the economic, reliable,  
 654 and ecological objective functions. This optimal solution achieves an IR of 99.705%, a LCOE of 0.046147  
 655 \$/kWh, and a CO<sub>2</sub>RA of  $7.9142 \times 10^3$  ton/year. The associated decision variables are  $N_{PV} = 5124$ ,  $N_{WT} = 19$ ,  
 656 and  $N_{Ht} = 8$ .

## 657 7.2. Power computation analysis

658 Once the objective functions, decision variables, energy values, and other system indicators are  
 659 determined for each scenario outlined in section 7.1, an evaluation of the system's performance in the 3<sup>rd</sup>  
 660 scenario will be provided in this section. Fig. 14 illustrates how much renewable power could be generated  
 661 monthly throughout 2022. It reveals the contributions from solar PV, wind, and hydro energy resources,  
 662 showing their combined generated power. Each month is visible along the horizontal axis, with the amount  
 663 of power generated in MW, shown on the vertical axis. This visualization helps us understand patterns in  
 664 renewable energy production over the year, revealing any seasonal fluctuations and emphasizing the  
 665 importance of each renewable energy source in sufficiently meeting the load demand.

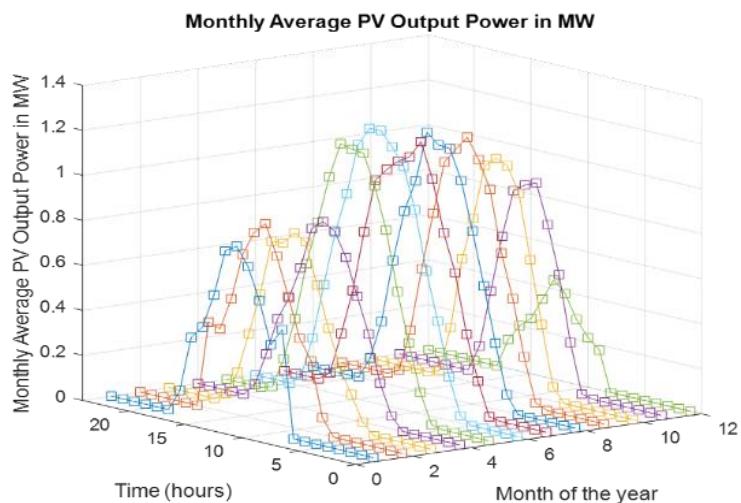
666 Solar PV is chosen from renewable resources to show the average monthly output power for the year  
 667 2022, shown in Fig. 15. From the graph, it is evident that the highest PV output occurs between April and  
 668 August, coinciding with periods of increased solar irradiance during these months. Conversely, the lowest  
 669 average PV output power is observed in winter, corresponding to times when solar irradiance is

670 comparatively lower in Michigan. This highlights the influence of seasonal variations in solar irradiance  
 671 on PV power generation throughout the year.

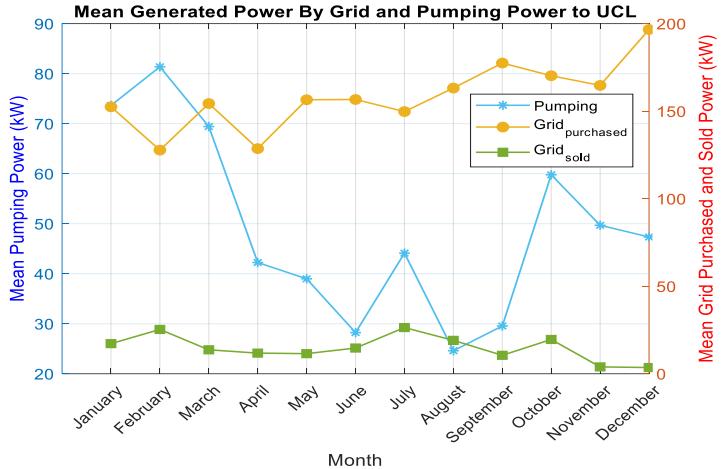


672 Fig. 14. The monthly mean generated power by renewable energy resources of the 3<sup>rd</sup> scenario in MW.  
 673

674 The average purchased and sold power from and to the grid and the pumping power to UCL for each  
 675 month are depicted in Fig. 16. It presents the performance in the best case of the third scenario. The plot  
 676 effectively visualizes the monthly trends in power generation, with distinct lines representing grid-  
 677 purchased power, grid-sold power, and pumping power. It is noticeable that grid-purchased power exhibits  
 678 fluctuations throughout the year, with higher values observed after September till the end of the year,  
 679 possibly indicative of increased energy demand during winter. On the other hand, the grid-sold power  
 680 shows relatively consistent levels across the months because of the priority of the extra power being pumped  
 681 to the UCL. Overall, the visualization offers valuable insights into the dynamics of power generation and  
 682 consumption for the year, providing useful information for energy management and decision-making.  
 683

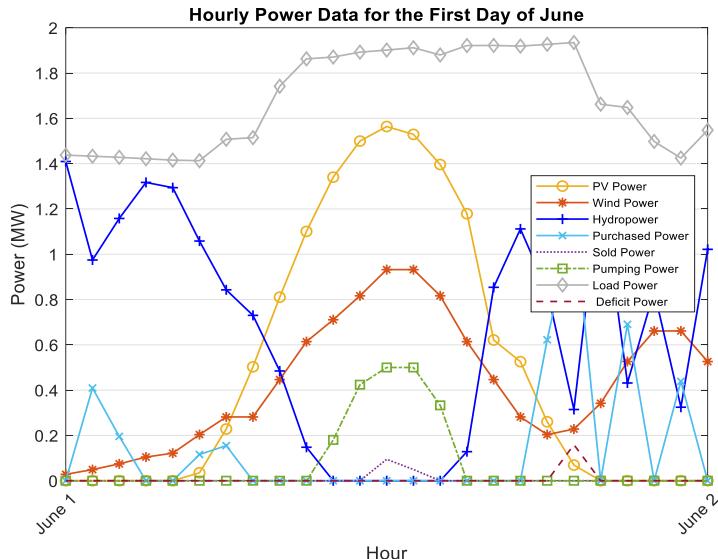


684 Fig. 15. The monthly average solar PV output power for the best solution of the 3<sup>rd</sup> scenario in MW.  
 685



686  
687 Fig. 16. Average generated power by grid and pumping power to UCL in each month  
688 for the best case of the 3<sup>rd</sup> scenario.

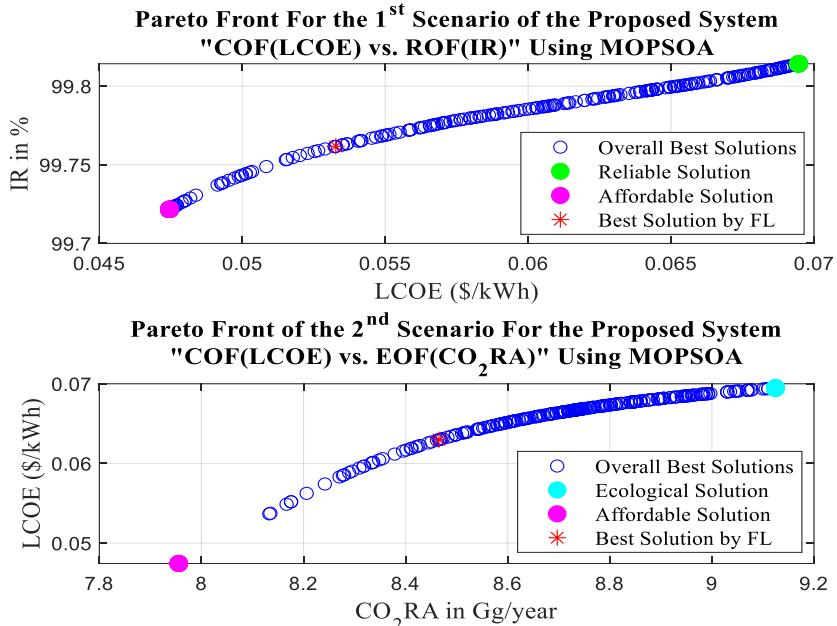
689 Fig. 17 states the findings of the operational strategy simulation for the optimized 3<sup>rd</sup> scenario, focusing  
690 on a summer day, specifically July 1<sup>st</sup>, 2022. One notable observation is the absence of hydro pumping  
691 during nighttime hours, attributed to the lack of solar PV power availability. During the daytime, typically  
692 between 10:00 A.M. and 4:00 P.M., the solar and wind-generated power meets the load demand, with  
693 excess energy utilized for pumping water from the lower reservoir to the UCL. Additionally, it is  
694 highlighted that the energy balance equation is maintained in each scenario, as described previously in  
695 equation (29). Subsequently, around 2:00 P.M., the total load demand, sold, and pumping power comprises  
696 the energy supplied by both the PV system and the wind plant, with zero purchased power since the grid  
697 serves as a backup source in instances of renewable energy deficit.



698  
699 Fig. 17. Hourly power data for June, 1<sup>st</sup> 2022 for the optimal case of the 3<sup>rd</sup> scenario.

700 *7.3. Comparative analysis of findings using MOFEPSOA*

701 In this section, a comparative analysis of the findings in Section 7.1 is carried out using MOFEPSOA to  
 702 test the effectiveness of MOGWOA. By comparing the results obtained previously, the performance of  
 703 MOGWOA can be assessed. The Pareto fronts of the 1<sup>st</sup> and 2<sup>nd</sup> scenarios are shown in Fig. 18.



704 Fig. 18. Pareto fronts for the 1<sup>st</sup> and 2<sup>nd</sup> scenarios of the proposed system by MOFEPSOA.

705  
 706 Table 4 displays the objective function values and decision variables for the 3<sup>rd</sup> scenario obtained using  
 707 MOFEPSOA. The percentage difference between MOGWOA and MOFEPSOA is consistently below 7%  
 708 for all values, particularly compared with the findings in the optimal solution of Table 3. Moreover, the  
 709 triple Pareto front optimization curve produced by MOFEPSOA closely aligns with MOGWOA's results in  
 710 Fig. 19, affirming the accuracy and effectiveness of the proposed methodology in simulating the system.

711 Table 4. Comparative analysis for the 3<sup>rd</sup> Scenario using MOFEPSOA based on MOGWOA findings.

| Quantity            | ROF (IR) vs. COF (LCOE) & EOF (CO <sub>2</sub> RA) |                       |          |               | Percentage difference for Best Solution from MOGWOA in % |  |
|---------------------|--|-----------------------|----------|---------------|--|--|
|                     | Using MOFEPSOA                                     |                       |          | Best Solution |  |  |
|                     | Economic   | Reliable & Ecological |          |               |  |  |
| Objective Functions | IR in %  | 99.722                | 99.814   | 99.739        | 0.09   |  |
|                     | LCOE in \$/kWh                                     | 0.04745               | 0.069464 | 0.049348      | 6.704  |  |
|                     | CO <sub>2</sub> RA in 10 <sup>3</sup> ton/year     | 7.9556                | 9.1243   | 8.0124        | 1.23   |  |
| Decision Variables  | $N_{PV}$   | 2117                  | 10251    | 5029          | 1.8714   |  |
|                     | $N_{WT}$   | 17                    | 19       | 20            | 5.128  |  |
|                     | $N_{Ht}$   | 8                     | 9        | 8             | 0  |  |

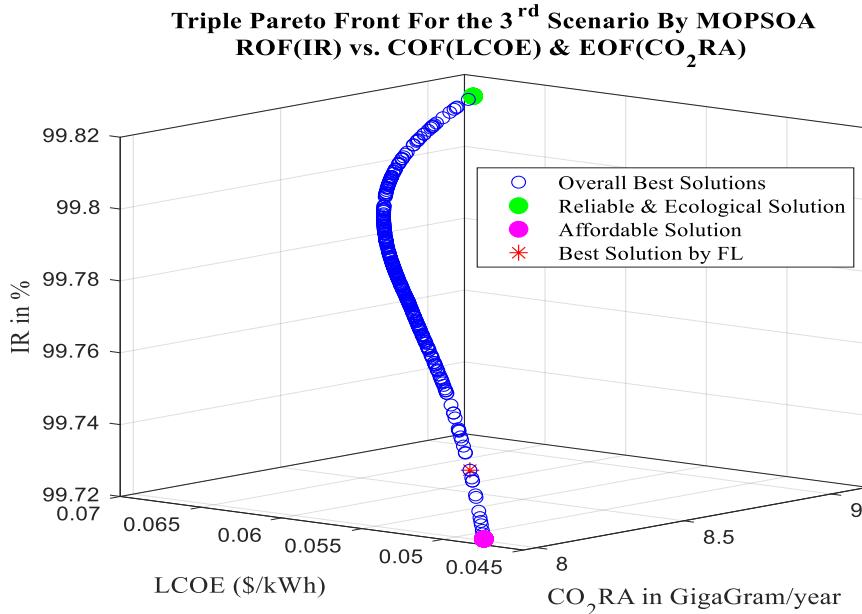


Fig. 19. Triple Pareto Front For the 3<sup>rd</sup> Scenario of the proposed system using MOFEPSOA.

712

## 8. Conclusions

713 Recently, with growing electricity demand and increasing ecological concerns, the significance of  
 714 RERs, including hydro storage systems, has become increasingly apparent. This has made a global shift  
 715 towards cleaner and more sustainable energy alternatives to replace conventional fossil fuel infrastructure  
 716 with clean, affordable, and reliable options. This has inspired this paper to investigate renewable energy  
 717 resource concerns, painting the maximum reliability, maximum emission reduction, and minimum systems'  
 718 lifetime cost. This paper examines the utilization of on-grid solar PV, wind farms, and PHESS to meet the  
 719 energy needs of Crystal's Lake territory in Michigan as a case study. A realistic analysis was conducted  
 720 using measured data for the system's design from the year 2022, including solar data, ambient temperature,  
 721 wind velocity, hydrological information, and community-scale energy demand specific to the chosen  
 722 location. The primary objective is to assess the potential of untapped sites for renewable energy generation,  
 723 with Crystal's Lake identified as particularly promising due to its substantial storage capacity of about  
 724 14.9734 GWh, despite being classified as a MHPP. Through the application of a MOGWOA, optimal  
 725 sizing, and energy management strategies were formulated for various scenarios. Economic, environmental,  
 726 and reliability criteria were utilized as the three objective functions, yielding promising outcomes,  
 727 particularly in the third scenario where triple objective functions were considered. For each scenario,  
 728 multiple solutions were identified, including economic, ecological, reliable, and a best-compromised  
 729 solution achieved through a fuzzy logic approach. Notably, the third scenario yielded the lowest LCOE at  
 730 0.046147 \$/kWh, a strong index of reliability of 99.705%, and a significant reduction in CO<sub>2</sub> emissions by  
 731 7.9142 10<sup>3</sup> tons per year. This scenario also revealed the optimum number of solar panels was 5124, 19  
 732 wind turbines, and 8 hydro-turbine generator sets. Furthermore, the renewable storage factor was  
 733 determined to be 43.25%, indicating optimal utilization of available PHESS. Energy management analysis  
 734 further validated the efficacy of the system. Subsequently, the findings were validated using a MOFEPSOA,  
 735 ensuring accuracy with a percentage difference lower than 7% across all results. The approach described in  
 736 this research offers valuable perspectives for comparable locations aiming to utilize renewable energy,  
 737

738 specifically from unused storage reservoirs. By optimizing the integration of RES, this research offers a  
 739 roadmap for maximizing the utilization of clean energy sources and promoting a more sustainable future.

740 **Appendix A**

741 TABLE 5. Specifications of Renewable Components

| Component                                     | Parameters  | Value                |
|---|---|----------------------|
| Solar PV Module<br>(CanadianSolar CS6K-290MS) | <i>Maximum power (<math>P_{max}</math>) in Watt</i>                       | 290                  |
|   | <i>Module Efficiency STC in %</i>   | 17.72 %              |
|   | <i>Short circuit current (<math>I_{sc}</math>) in A</i>                   | 9.67                 |
|   | <i>Open circuit voltage (<math>V_{oc}</math>) in V</i>                    | 39.3                 |
|   | <i>Maximum power current (<math>I_{MPP}</math>) in A</i>                  | 9.05                 |
|   | <i>Maximum power voltage (<math>V_{MPP}</math>) in V</i>                  | 32.1                 |
|   | <i>Temperature coefficient of <math>V_{oc}</math> in %/°C</i>             | -0.3                 |
|   | <i>Temperature coefficient of <math>I_{sc}</math> in %/°C</i>             | 0.053                |
|   | <i>NOCT (°C)</i>  | 45                   |
|   | <i><math>T_{MDS,STC}</math> in °C</i>                                     | 20                   |
|   | <i>GTI<sub>NOCT</sub> in Watt/m<sup>2</sup></i>                           | 800                  |
|   | <i>Dimensions for Area (<math>L_m \times W_m</math>) in m<sup>2</sup></i> | 1.65×0.992           |
| Wind Turbine<br>(Vestas V200-100 kW)          | <i>Nominal Power</i>  | 100 kW               |
|   | <i>Frequency</i>  | 50 Hz                |
|   | <i>Diameter</i>   | 20 m                 |
|   | <i>Swept Area</i>   | 314.0 m <sup>2</sup> |
|   | <i>Hub height</i>   | 40 m                 |
|   | <i>Cut-in Wind Speed (<math>v_{ci}</math>)</i>                            | 3.3 m/s              |
|   | <i>Rated Wind Speed (<math>v_r</math>)</i>                                | 13 m/s               |
|   | <i>Cut-out Wind Speed (<math>v_{co}</math>)</i>                           | 25 m/s               |
| Upper Crystal Lake<br>Dimensions [26]         | <i>Average Lake width (<math>\bar{W}_{UCL}</math>)</i>                    | 3.12 km              |
|   | <i>Elevation</i>  | 183 m                |
|   | <i>Difference from Lake Michigan (<math>H_{diff}</math>)</i>              | 0.8 km               |
|   | <i>Average Lake length (<math>\bar{L}_{UCL}</math>)</i>                   | 12.87 km             |
|   | <i>Average depth (<math>\bar{D}_{UCL}</math>)</i>                         | 21.55 m              |

742 **Appendix B**

743 TABLE 6. Financial data for LCOE computation

| Cost type              | PV array [60] | Wind farm [60] | PHS facility [61] | Converter [61] |
|------------------------|---------------|----------------|-------------------|----------------|
| CC (\$/kW)             | 896           | 998            | 930               | 687            |
| OMC (\$/kW.year)       | 15            | 20             | 15.52             | 687            |
| RC (\$/kW)             | 896           | 998            | 930               | 0              |
| Lifetime (years)       | 25            | 20             | 25                | 15             |
| Grid costs             |               |                |                   |                |
| $E_{gp}$ Cost (\$/kWh) |               |                | 0.37              |                |

|                                |       |
|--------------------------------|-------|
| $E_{gsold}$ Cost (\$/kWh) [62] | 0.176 |
| Financial Parameters           |       |
| $i'$ (%)                       | 8     |
| $f_{inflation}$ (%)            | 2     |
| Project lifetime ( $N$ )       |       |
|                                | 25    |

## 744 Appendix C

$$745 \quad \vec{D} = |\vec{C} \cdot \vec{X}_p(t) - \vec{X}(t)| \quad (43)$$

$$746 \quad \vec{X}(t+1) = \vec{X}_p(t) - \vec{A} \cdot \vec{D} \quad (44)$$

$$747 \quad \vec{A} = 2\vec{a} \cdot \vec{r}_1 - \vec{a} \quad (45)$$

$$748 \quad \vec{C} = 2 \cdot \vec{r}_2 \quad (46)$$

$$749 \quad \vec{D}_\alpha = |\vec{C}_1 \cdot \vec{X}_\alpha - \vec{X}| \quad (47)$$

$$750 \quad \vec{D}_\beta = |\vec{C}_2 \cdot \vec{X}_\beta - \vec{X}| \quad (48)$$

$$751 \quad \vec{D}_\delta = |\vec{C}_3 \cdot \vec{X}_\delta - \vec{X}| \quad (49)$$

$$752 \quad \vec{X}_1 = \vec{X}_\alpha - \vec{A}_1 \cdot (\vec{D}_\alpha) \quad (50)$$

$$753 \quad \vec{X}_2 = \vec{X}_\beta - \vec{A}_2 \cdot (\vec{D}_\beta) \quad (51)$$

$$754 \quad \vec{X}_3 = \vec{X}_\delta - \vec{A}_3 \cdot (\vec{D}_\delta) \quad (52)$$

$$755 \quad \vec{X}(t+1) = \frac{\vec{X}_1 + \vec{X}_2 + \vec{X}_3}{3} \quad (53)$$

## 756 Acknowledgment

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 761 of the authors and do not necessarily reflect the views of the Department of Energy.

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