

Letter

Observation of $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K}$ and measurement of the effective couplings of $\Omega(2012)^-$ to $\Xi(1530)\bar{K}$ and $\Xi\bar{K}$



The Belle Collaboration

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ABSTRACT

Using $Y(1S)$, $Y(2S)$, and $Y(3S)$ data collected by the Belle detector, we discover a new three-body decay, $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$, with a significance of 5.2σ . The mass of the $\Omega(2012)^-$ is $(2012.5 \pm 0.7 \pm 0.5)$ MeV and its effective couplings to $\Xi(1530)\bar{K}$ and $\Xi\bar{K}$ are $(39^{+31}_{-39} \pm 9) \times 10^{-2}$ and $(1.7 \pm 0.3 \pm 0.3) \times 10^{-2}$, where the first uncertainties are statistical and the second are systematic. The ratio of the branching fraction for the three-body decay to that for the two-body decay to $\Xi\bar{K}$ is $0.99 \pm 0.26 \pm 0.06$, assuming isospin symmetry.

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1. Introduction

In the last twenty years, physicists have discovered new hadrons that are difficult to explain with the conventional quark model [1–3]. Some of these, like the $X(3872)$, $Z_c(3900)$, and $T_{cc}(3875)$ mesons and the $P_c(4312)$ baryon, are close to the mass thresholds of pairs of conventional hadrons. Many authors propose that they are hadronic molecules [3,4]. All these hadrons have two heavy quarks, but the study of such hadrons containing only light quarks is rather limited. The $\Lambda(1405)^0$, close to the pK^- threshold, is widely regarded as an $N\bar{K}$ molecule [5–8]. New measurements of the properties of similar hadrons will let us refine the model of hadronic molecules and improve our understanding of the strong interaction between quarks and gluons [9,10].

One such hadron is the Ω^- , which with three strange quarks is the strangest baryon. Its excited states have been difficult to find. The *Review of Particle Physics* [11] lists only four excited Ω^- baryons: $\Omega(2012)^-$, $\Omega(2250)^-$, $\Omega(2380)^-$, and $\Omega(2470)^-$. The last three were established four decades ago [12–14]. The $\Omega(2012)^-$ was first observed in 2018 by the Belle experiment in decays to $\Xi^0 K^-$ and $\Xi^- \bar{K}^0$ in e^+e^- -collision data near the $Y(1S)$, $Y(2S)$, and $Y(3S)$ resonances, who reported it to have a mass of (2012.4 ± 0.9) MeV [15] and a width of $(6.4^{+3.0}_{-2.7})$ MeV [16].

Theorists are strongly interested in understanding the $\Omega(2012)^-$ [17–36]. There are mainly two interpretations: a standard baryon [17–26] and a $\Xi(1530)\bar{K}$ molecule [27–36]. A large rate for $\Omega(2012)^-$ to $\Xi(1530)\bar{K}$ was predicted in the molecule scenario [27–31]—18% to 86% of that for decay to $\Xi\bar{K}$ [28,29]. Therefore, measuring the branching fraction for $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$ may inform us about the $\Omega(2012)^-$'s internal structure.

We report a search for $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K}$ using $Y(1S)$, $Y(2S)$, and $Y(3S)$ data collected by the Belle experiment [37,38] at the KEKB energy-asymmetric e^+e^- collider [39,40]. We measure its branching fraction with respect to that for $\Omega(2012)^- \rightarrow \Xi\bar{K}$. Charge-conjugate modes are included throughout.

2. Comparison with previous analysis

Belle previously searched for $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K}$, but observed no signal and set an upper limit at 90% confidence on the branching-fraction ratio [41],

$$\mathcal{R}_{\Xi\bar{K}}^{\Xi\pi\bar{K}} \equiv \frac{B(\Omega(2012)^- \rightarrow \Xi(1530)\bar{K})}{B(\Omega(2012)^- \rightarrow \Xi\bar{K})} < 11.9\%. \quad (1)$$

That analysis was based on an inaccurate model of the decay, which led to selection criteria that accepted more background events than expected, a misestimation of the detection efficiency, and an uncertain signal yield. Our new analysis is based on a more accurate model of the decay and uses different selection criteria, accounting for the fact that the $\Xi(1530)$ is produced below threshold. We use this model, including a more detailed resonance shape and a previously neglected three-body phase-space factor, to fit for the signal yield. The distribution of $M(\Xi^- \pi^+)$ in the previous model peaks more narrowly and at higher masses than the distribution in the updated model (Fig. 1). This leads us to determine different selection criteria than the previous analysis. We further improve upon the previous analysis by vetoing events in which the K^- may come from a ϕ instead of an Ω^- .

These improvements increase the signal yield and greatly change the results for $\mathcal{R}_{\Xi\bar{K}}^{\Xi\pi\bar{K}}$, which supersede those of [41]. In the new decay model, the mass of the $\Omega(2012)^-$ and its couplings to $\Xi\pi\bar{K}$ and $\Xi\bar{K}$ are free parameters. We measure these parameters, superseding the results reported in [16].

3. Data sample and Belle detector

The data used in this analysis were taken at the $Y(1S)$, $Y(2S)$, and $Y(3S)$ resonances with integrated luminosities of 5.7, 24.9, and 2.9 fb $^{-1}$, corresponding to 102 million $Y(1S)$, 158 million $Y(2S)$, and 12 million

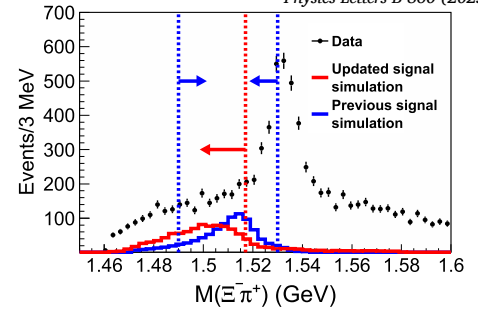


Fig. 1. The $\Xi^- \pi^+$ mass distributions in $\Xi^- \pi^+ K^-$ events in data (points) and in simulations using the models of the previous analysis [41] (solid blue line) and this work (solid red line), with each simulation normalized to have an exaggerated $\mathcal{R}_{\Xi\bar{K}}^{\Xi\pi\bar{K}}$ value of 4. The red arrow shows the mass requirement of this analysis; the blue arrows show the mass requirement of the previous analysis [41].

$Y(3S)$ events. Since the $Y(1S)$, $Y(2S)$, and $Y(3S)$ states decay via three gluons or two gluons and a photon, they produce more baryons than continuum $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) [42–45], so the signal-to-background ratio in on-resonance $Y(1S)$, $Y(2S)$, and $Y(3S)$ data is larger than those in continuum and heavier Y data.

The Belle detector is a large solid-angle magnetic spectrometer consisting of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provided a 1.5 T magnetic field and an iron flux return placed outside the coil instrumented to detect K_L^0 and identify muons.

We use simulated events to determine detection efficiencies, signal shapes, and selection criteria. We use EVTGEN [46] to generate simulated events. We use a Flatté-like function [47] to simulate $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$. We determine preliminary selection criteria assuming the $\Omega(2012)^-$ mass is 2012.4 MeV [16] and its couplings to $\Xi\bar{K}$ and $\Xi\pi\bar{K}$ are 0.01 and 0.1. We then update the model to the values we find in data and re-optimize our selection criteria. We repeat this several times until the values stabilize. Simulated samples of inclusive $Y(1S)$, $Y(2S)$, and $Y(3S)$ decays and $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) with four times the luminosity as the real data are produced to check for possible peaking backgrounds [48]. GEANT3 [49] is used to simulate detector response.

4. Selection criteria

We search for the $\Omega(2012)^-$ in the $\Xi^0 K^-$, $\Xi^- \bar{K}^0$, $\Xi^- \pi^+ K^-$, $\Xi^- \pi^0 \bar{K}^0$, $\Xi^0 \pi^- \bar{K}^0$, and $\Xi^0 \pi^0 K^-$ final states, where the three-body final states are used to look for the $\Xi(1530)$ resonance via its decay to $\Xi\pi$. We use the same selection methods and criteria for π^+ , K^- , p , π^0 , $\bar{K}^0$, Λ^0 , Ξ^- , and Ξ^0 as in Refs. [16,41]. We require the mass of $\Xi\bar{K}$ and $\Xi\pi\bar{K}$ be less than 2200 MeV.

We veto K^- that may come from decay of a ϕ instead of an $\Omega(2012)^-$ by rejecting events fulfilling $|M(K^- K^+) - m_\phi| < 10$ MeV for any K^+ in the rest of the event, where the K^+ must be identified as a kaon with the same requirements as for the K^- . This window covers five units of the mass resolution and rejects 96% of ϕ -induced backgrounds.

5. $\Xi\pi$ distributions

Fig. 1 shows the $\Xi^- \pi^+$ mass distributions in $\Xi^- \pi^+ K^-$ events in data and in simulation using the model of the previous analysis [41] and our updated model. Each simulated distribution is normalized to have an exaggerated $\mathcal{R}_{\Xi\bar{K}}^{\Xi\pi\bar{K}}$ value of 4 so that it is visible in comparison to the data. In this updated work, we require $M(\Xi^- \pi^+) < 1517$ MeV, shown by the red arrow, which maximizes $S/\sqrt{S+B}$, where S and B are the numbers of signal and background events according to simulation,

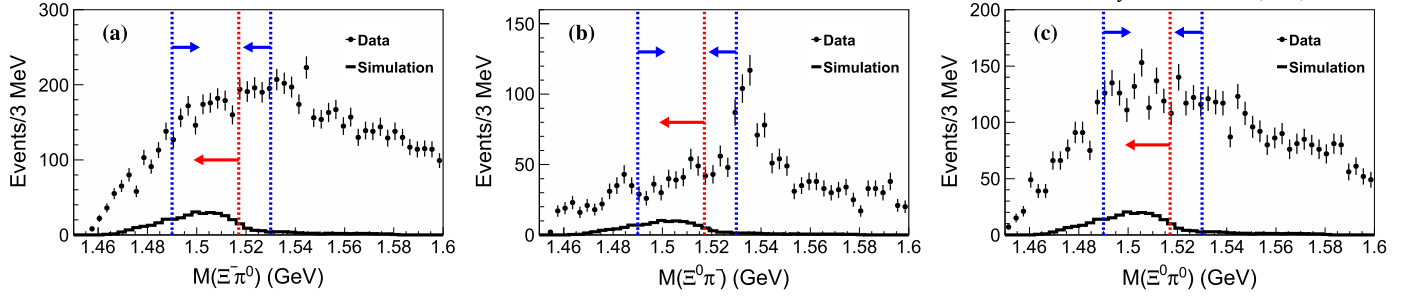


Fig. 2. The (a) $\Xi^- \pi^0$, (b) $\Xi^0 \pi^-$, and (c) $\Xi^0 \pi^0$ mass distributions in $\Xi \pi \bar{K}$ events in the data and simulated $\Omega(2012)^- \rightarrow \Xi(1530)^- K_S^0 \rightarrow \Xi^- \pi^0 K_S^0$, $\Omega(2012)^- \rightarrow \Xi(1530)^- K_S^0 \rightarrow \Xi^0 \pi^- K_S^0$, and $\Omega(2012)^- \rightarrow \Xi(1530)^0 K^- \rightarrow \Xi^0 \pi^0 K^-$ data. The numbers of simulated signal events are scaled arbitrarily. The red arrows show the mass requirements of this analysis; the blue arrows show the mass requirements of the previous analysis [41].

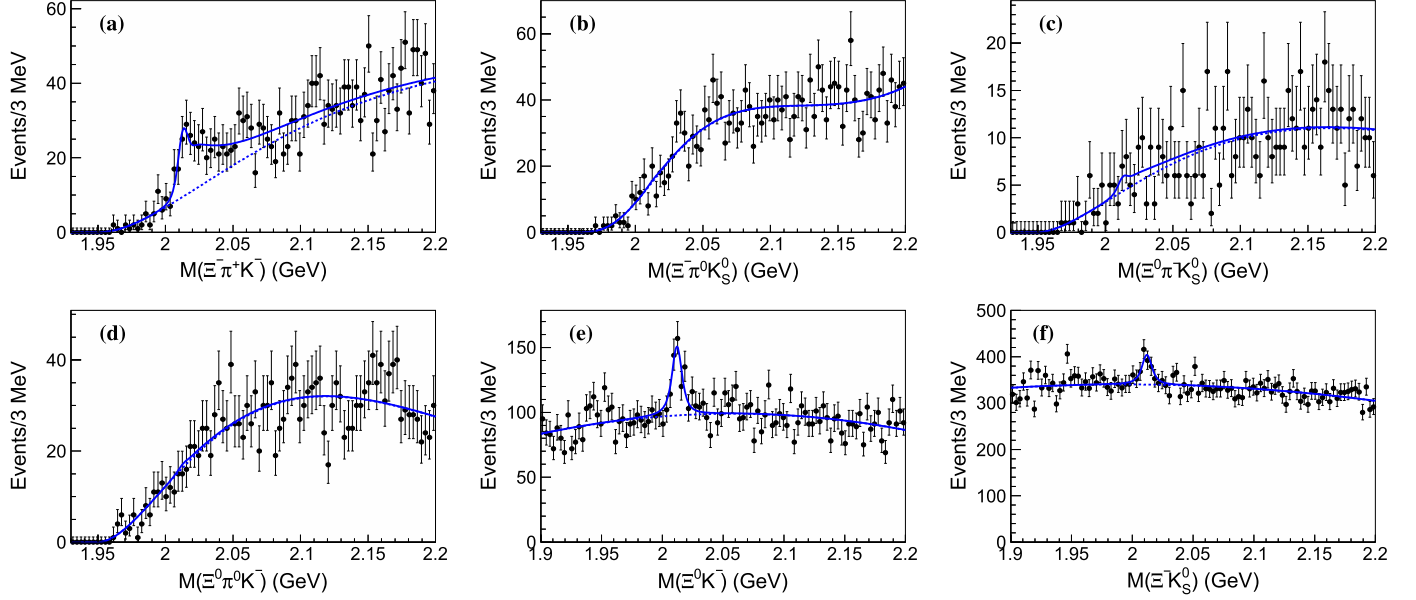


Fig. 3. The (a) $\Xi^- \pi^+ K^-$, (b) $\Xi^- \pi^0 K_S^0$, (c) $\Xi^0 \pi^- K_S^0$, (d) $\Xi^0 \pi^0 K^-$, (e) $\Xi^0 K^-$, and (f) $\Xi^- K_S^0$ mass distributions in data. The solid curves are the best fits and the dashed curves are backgrounds.

assuming $\mathcal{R}_{\Xi \pi \bar{K}}^{\Xi \pi \bar{K}} = 1$ and isospin symmetry relates the branching fractions for the different $\Xi \pi \bar{K}$ final states to each other. This retains 79% of signal candidates and removes large backgrounds from $\Xi(1530)$ not produced from $\Omega(2012)^-$ and from $\Xi^- \pi^+$ not produced from $\Xi(1530)$. These backgrounds cause a large peak at the $\Xi(1530)^0$ mass in the $\Xi^- \pi^+$ mass distribution. Signal events peak below the $\Xi(1530)$ mass because the $\Xi(1530)$ is produced below threshold in $\Omega(2012)^- \rightarrow \Xi(1530) \bar{K}$. We apply the same $M(\Xi \pi)$ requirement for all three-body channels, optimizing it from the $\Xi^- \pi^+ K^-$ channel since it has the largest signal yield, according to isospin symmetry, and largest signal-to-background ratio, owing to it having the simplest final state to detect.

The previous analysis required $M(\Xi \pi) \in [1490, 1530]$ MeV [41], shown by the blue arrows in Fig. 1. This removed the 23% of signal candidates that are below 1.49 GeV and accepted a large number of background events close to the $\Xi(1530)$ mass. The updated $\Xi^- \pi^+$ mass requirement improves $S/\sqrt{S+B}$ by a factor of 1.4. Fig. 2 shows the invariant mass distributions for $\Xi \pi$ for the final states $\Xi^- \pi^0 \bar{K}^0$, $\Xi^0 \pi^- \bar{K}^0$, and $\Xi^0 \pi^0 K^-$ and the previous and new mass requirements.

6. $\Xi \pi \bar{K}$ and $\Xi \bar{K}$ distributions

Fig. 3 shows the $\Xi \pi \bar{K}$ and $\Xi \bar{K}$ mass distributions in data after the all criteria. No peaking backgrounds are found in simulated events. To determine the $\Omega(2012)^-$ branching fractions and resonance parameters, we

fit simultaneously to the binned $\Xi^- \pi^+ K^-$, $\Xi^- \pi^0 K_S^0$, $\Xi^0 \pi^- K_S^0$, $\Xi^0 \pi^0 K^-$, $\Xi^0 K^-$, and $\Xi^- K_S^0$ mass distributions.

Under isospin symmetry, the branching fractions for $\Omega(2012)^-$ decay to $\Xi^- \pi^+ K^-$ and $\Xi^0 \pi^- \bar{K}^0$ are equal, the branching fractions for $\Omega(2012)^-$ decay to $\Xi^- \pi^0 \bar{K}^0$ and $\Xi^0 \pi^0 K^-$ are equal, and the latter two are half the former two. Accounting for detection efficiencies and the branching fractions for how we observe the decays of the final-state particles, the proportions of events we should see in each final state are 86.4% $\Xi^- \pi^+ K^-$, 7.4% $\Xi^0 \pi^- \bar{K}^0$, 3.9% $\Xi^0 \pi^0 K^-$, and 2.3% $\Xi^- \pi^0 \bar{K}^0$. In the fit, we assume the yields for the final states have these proportions. The yields for $\Omega(2012)^-$ two-body decay are floated in the fit.

All signal shapes are described using Flatté-like functions [47], convolved with Gaussian functions to model detector resolutions—1.5, 2.5, 2.3, 2.8, 1.7, and 2.1 MeV for $\Omega(2012)^- \rightarrow \Xi^- \pi^+ K^-$, $\Xi^- \pi^0 K_S^0$, $\Xi^0 \pi^- K_S^0$, $\Xi^0 \pi^0 K^-$, $\Xi^- K_S^0$, and $\Xi^0 K^-$, determined from inspection of simulated data, and multiplied by efficiency functions linearly dependent on mass. The Flatté-like function is

$$T_n(M) \equiv \frac{g_n k_n(M)}{|M - m_{\Omega(2012)^-} + \frac{1}{2} \sum_{j=2,3} g_j [\kappa_j(M) + i k_j(M)]|^2}, \quad (2)$$

where g_n is the effective coupling of $\Omega(2012)^-$ to the n -body final state, κ_n and k_n parameterize the real and imaginary parts of the $\Omega(2012)^-$ self-mass, and M is $M(\Xi \bar{K})$ or $M(\Xi \pi \bar{K})$. The forms of κ_n and k_n are found in Eqs. (47) and (48) in Ref. [47] with mass-dependent widths.

Table 1

The efficiencies (ϵ), signal yields (Y), and branching-fraction products (b) for all channels.

Mode	ϵ (%)	Y	b (%)
$\Omega(2012)^- \rightarrow \Xi(1530)^0 K^- \rightarrow \Xi^- \pi^+ K^-$	6.97 ± 0.07	267 ± 60	64
$\Omega(2012)^- \rightarrow \Xi(1530)^- \bar{K}^0 \rightarrow \Xi^- \pi^0 \bar{K}^0$	1.06 ± 0.01	7 ± 2	22
$\Omega(2012)^- \rightarrow \Xi(1530)^- \bar{K}^0 \rightarrow \Xi^0 \pi^- \bar{K}^0$	1.74 ± 0.02	23 ± 5	22
$\Omega(2012)^- \rightarrow \Xi(1530)^0 K^- \rightarrow \Xi^0 \pi^+ K^-$	0.63 ± 0.01	12 ± 3	62
$\Omega(2012)^- \rightarrow \Xi^0 K^-$	4.00 ± 0.04	242 ± 40	63
$\Omega(2012)^- \rightarrow \Xi^- \bar{K}^0$	15.5 ± 0.16	293 ± 65	22

Such modeling of the $\Omega(2012)^-$ shape, not included in the previous analysis [41], improves the signal-background separation and hence increases the signal yield. For $\Omega(2012)^- \rightarrow \Xi\pi\bar{K}$, we assume the decay proceeds only through the $\Xi(1530)$ resonance. When we include a non-resonant component in the fit, its yield is consistent with zero.

Background events in the $\Xi\pi\bar{K}$ mass distributions are modeled by the same threshold function from Ref. [41], but with a threshold of 1.95 GeV. Background events in the $\Xi\bar{K}$ mass distributions are modeled by second-order polynomials.

The fit results are shown as blue lines in Fig. 3 and the yields are listed in Table 1. The statistical significance for $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$ is 5.4σ , calculated from the logarithm of a ratio of likelihoods [50], $-2\ln(\mathcal{L}_0/\mathcal{L})$, which is 33, accounting for the difference in the number of degrees of freedom (2), where $\mathcal{L}_0$ and $\mathcal{L}$ are the maximized likelihoods without and with the signal components [50]. Including systematic uncertainties, the significance is 5.2σ . The significance of the two-body decays is 8.8σ . The correlations of the yields are 0.136 for $\Omega(2012)^- \rightarrow \Xi^- \bar{K}^0$ and $\Omega(2012)^- \rightarrow \Xi^0 K^-$, 0.142 for $\Omega(2012)^- \rightarrow \Xi^- \bar{K}^0$ and $\Omega(2012)^- \rightarrow \Xi\pi\bar{K}$, and 0.167 for $\Omega(2012)^- \rightarrow \Xi^0 K^-$ and $\Omega(2012)^- \rightarrow \Xi\pi\bar{K}$. The signal yields for $\Omega(2012)^- \rightarrow \Xi^0 K^-$ and $\Omega(2012)^- \rightarrow \Xi^- K_S^0$ are consistent with those from Ref. [16]. The mass of $\Omega(2012)^-$ is

$$m_{\Omega(2012)^-} = (2012.5 \pm 0.7 \pm 0.5) \text{ MeV}. \quad (3)$$

The values of g_3 and g_2 are

$$g_3 = (38.9^{+31.1}_{-38.9} \pm 9.0) \times 10^{-2}, \quad (4)$$

$$g_2 = (1.7^{+0.3}_{-0.3} \pm 0.3) \times 10^{-2}.$$

The value of g_3/g_2 is

$$g_3/g_2 = (22.9^{+17.9}_{-22.4} \pm 2.2). \quad (5)$$

Where two uncertainties are given, the first is statistical and the second systematic. The effective couplings essentially determine the width of the $\Omega(2012)^-$. The shape of the signal does not change greatly with g_3 . Even if g_3 is very close to zero, the Flatté-like function can still describe the $M(\Xi\pi\bar{K})$ distribution in the data. We do not have enough data to precisely determine g_3 in the limited range where it has an effect, so its relative statistical uncertainty is much larger than those of $m_{\Omega(2012)^-}$ and g_2 .

The previous analysis found only 22 ± 13 signal events with a χ^2 per degree of freedom of 37.3/12 [41]. The signal yield increases greatly with the new model. This supports that we now more accurately model $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$ and that the selection criteria and fit functions based on this model are reasonable.

For comparison, we also fit the $M(\Xi^- \pi^+ K^-)$ distribution using a Breit-Wigner function convolved with a Gaussian resolution function for the $\Omega(2012)^-$ signal shape, the same used in previous analysis [41]. This fit function does not describe the data very well especially, in the $\Omega(2012)^-$ signal region. The χ^2 per degree of freedom of the result of the fit is 16.2/12. In the fit using our new model, it is much smaller, 4.8/11.

We also fit our new model to data selected with the previous mass requirement, $M(\Xi\pi) \in [1490, 1530]$ MeV, shown in Fig. 4, to demon-

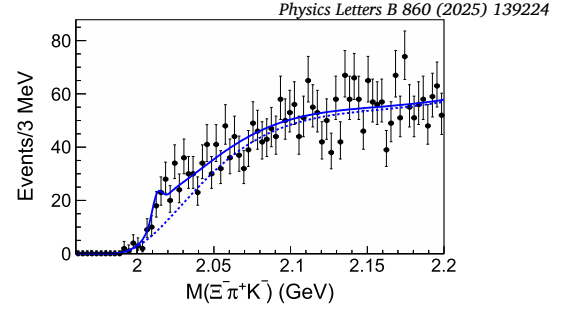


Fig. 4. The $\Xi^- \pi^+ K^-$ mass distribution for events with $M(\Xi\pi) \in [1490, 1530]$ MeV in data. The solid curve is the best fit and the dashed curve is the background.

strate the improvement of the new mass requirement. We fix $m_{\Omega(2012)^-}$, g_2 , and g_3 to the central values in equations (3) and (4). The yield for $\Omega(2012)^- \rightarrow \Xi(1530)^0 K^- \rightarrow \Xi^- \pi^+ K^-$ is 212 ± 53 with a χ^2 per degree of freedom of 23.0/14. The yield reduction is consistent with the 23% loss expected from inspection of simulated data.

7. Branching-fraction ratio

The numerator in $\mathcal{R}_{\Xi\pi\bar{K}}^{\Xi\pi\bar{K}}$ is the sum of the branching fractions for the four decays $\Omega(2012)^- \rightarrow \Xi(1530)\bar{K}$ with subsequent $\Xi(1530)$ decay resulting in the final states $\Xi^- \pi^+ K^-$, $\Xi^- \pi^0 \bar{K}^0$, $\Xi^0 \pi^- \bar{K}^0$, and $\Xi^0 \pi^0 K^-$. Assuming isospin symmetry,

$$\mathcal{R}_{\Xi\pi\bar{K}}^{\Xi\pi\bar{K}} = \frac{3 \times B(\Omega(2012)^- \rightarrow \Xi(1530)^0 K^- \rightarrow \Xi^- \pi^+ K^-)}{B(\Omega(2012)^- \rightarrow \Xi^- \bar{K}^0) + B(\Omega(2012)^- \rightarrow \Xi^0 K^-)}, \quad (6)$$

where

$$B(X) = \frac{Y(X)}{\epsilon(X) b(X) N_{\Omega(2012)^-}}, \quad (7)$$

with $Y(X)$ the yield of channel X , $\epsilon(X)$ the efficiency to detect it, $b(X)$ the product of branching fractions for the final-state-particle detection modes needed to detect channel X (a subset of $\Xi^+ \rightarrow \Lambda^0 \pi^+$, $\Xi^0 \rightarrow \Lambda^0 \pi^0$, $\Lambda^0 \rightarrow p \pi^-$, $\bar{K}^0 \rightarrow \pi^+ \pi^-$, and $\pi^0 \rightarrow \gamma\gamma$), and $N_{\Omega(2012)^-}$ the number of $\Omega(2012)^-$ produced at Belle, which cancels in the ratio. The yields, efficiencies, and branching-fraction products (calculated with values from [11]) are listed in Table 1. We obtain

$$\mathcal{R}_{\Xi\pi\bar{K}}^{\Xi\pi\bar{K}} = 0.99 \pm 0.26 \pm 0.06. \quad (8)$$

Since the $\Omega(2012)^-$ and the intermediate state, $\Xi(1530)\bar{K}$, have similar masses, the branching-fraction ratio depends more strongly on $m_{\Omega(2012)^-}$ and g_2 than on g_3 . We can therefore measure it more precisely than g_3/g_2 .

8. Systematic uncertainties

Systematic uncertainties on the branching-fraction ratio are summarized in Table 2. Systematic uncertainty on the detection efficiency comes from tracking (0.35% per track), particle identification (1.3% per kaon and 1.1% per pion), K_S^0 selection (2.2%) [51], and π^0 reconstruction (4%) [52]. Uncertainties from Λ^0 detection cancel. The particle-identification uncertainties are added linearly. By including these uncertainties in the fit, we obtain the total systematic uncertainty from detection efficiency, 3.1%.

The masses and widths of Λ^0 , Ξ^- , Ξ^0 , and $\Xi(1530)^0$ and the mass resolution of $\Omega(2012)^-$ are fixed in our fit. We change the masses and widths each by one unit of their uncertainty, refit, and take the differences in yields as systematic uncertainties. Simulation usually underestimates the resolutions of mass peaks within 10% [16]. We enlarge the resolution by 10% and take the resulting change as a conservative

Table 2

Systematic uncertainties on the branching-fraction ratio, $\Omega(212)^-$ mass, and effective couplings.

Source	$\mathcal{R}_{\Xi\pi K}^{\Xi\pi K}$	$m_{\Omega(212)^-}$ [MeV]	g_3	g_2
Detection efficiency	3.1	—	—	—
Resonance parameters	5.3	0.1	0.034	0.001
Fit model	—	0.5	0.083	0.002
Isospin symmetry	—	0.1	0.002	0.001
Total	6.1	0.5	0.090	0.003

systematic uncertainty. These uncertainties are added in quadrature to obtain a systematic uncertainty due to resonance parameters, 5.3%.

Fit-model uncertainties are estimated using simulated pseudoexperiments, with events distributed according to the mass spectra observed in data. We repeat this numerous times and find that the mean of the results of these fits is consistent with the fit to data. This cross checks the fit's stability.

When we allow the proportions of the three-body decays to break isospin symmetry by up to 10%, the fitted yields change by less than 1%. So uncertainty on the branching-fraction ratio from isospin-symmetry is negligible. The statistical uncertainties on the efficiencies determined from simulation and the uncertainties from the branching fractions for $\Xi \rightarrow \Lambda^0 \pi$, $K_S^0 \rightarrow \pi^+ \pi^-$, and $\pi^0 \rightarrow \gamma \gamma$ are also negligible [11].

Systematic uncertainties on the $\Omega(212)^-$ mass and effective couplings are summarized in Table 2. The uncertainties from the input resonance parameters are 0.1 MeV for the $m_{\Omega(212)^-}$, 0.034 for g_3 , and 0.001 for g_2 . We change the fit ranges and change the background shapes to higher-order polynomials and take the differences of 0.5 MeV on the $m_{\Omega(212)^-}$, 0.083 on g_3 , and 0.002 on g_2 as systematic uncertainties. We allow the proportions of the three-body decays to break isospin symmetry by up to 10% and take the differences of 0.1 MeV on the $m_{\Omega(212)^-}$, 0.002 on g_3 , and 0.001 on g_2 as systematic uncertainties. The statistical uncertainties on the efficiencies determined from simulation and the uncertainties from the branching fractions are negligible in determinations of the $\Omega(212)^-$ mass and effective couplings. The total systematic uncertainties on the $m_{\Omega(212)^-}$, g_3 , and g_2 are 0.5 MeV, 0.090, and 0.003, respectively.

9. Summary

We report the first observation of $\Omega(212)^- \rightarrow \Xi(1530)\bar{K} \rightarrow \Xi\pi\bar{K}$, using $Y(1S)$, $Y(2S)$, and $Y(3S)$ data from Belle. The mass of the $\Omega(212)^-$ is $(2012.5 \pm 0.7 \pm 0.5)$ MeV; its effective coupling to $\Xi(1530)\bar{K}$ is $(39^{+31}_{-39} \pm 9) \times 10^{-2}$; and its effective coupling to $\Xi\bar{K}$ is $(1.7 \pm 0.3 \pm 0.3) \times 10^{-2}$. Assuming isospin symmetry, the $\mathcal{R}_{\Xi\pi\bar{K}}^{\Xi\pi\bar{K}}$ is $0.99 \pm 0.26 \pm 0.06$.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Data availability

Data will be made available on request.

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