



Composite Motion Learning with Task Control

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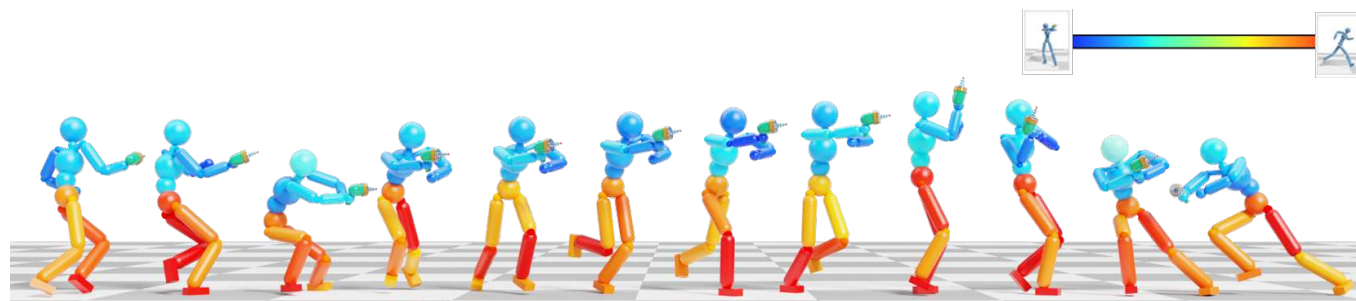


Fig. 1. Example of a physically simulated character performing composite motion with locomotion and aiming a weapon. The colors show the automatic mixing of the combined inputs that change dynamically over time based on the state. As indicated in the inset, red denotes body parts that are vital for locomotion while blue for aiming respectively. Our multi-objective approach learns this mixture along with imitation from two disparate reference motions and two goal-directed task rewards for each action.

We present a deep learning method for composite and task-driven motion control for physically simulated characters. In contrast to existing data-driven approaches using reinforcement learning that imitate full-body motions, we learn decoupled motions for specific body parts from multiple reference motions simultaneously and directly by leveraging the use of multiple discriminators in a GAN-like setup. In this process, there is no need of any manual work to produce composite reference motions for learning. Instead, the control policy explores by itself how the composite motions can be combined automatically. We further account for multiple task-specific rewards and train a single, multi-objective control policy. To this end, we propose a novel framework for multi-objective learning that adaptively balances the learning of disparate motions from multiple sources and multiple goal-directed control objectives. In addition, as composite motions are typically augmentations of simpler behaviors, we introduce a sample-efficient method for training composite control policies in an incremental manner, where we reuse a pre-trained policy as the meta policy and train a cooperative policy that adapts the meta one for new composite tasks. We show the applicability of our approach on a variety of challenging multi-objective tasks involving both composite motion imitation and multiple goal-directed control. Code is available at <https://motion-lab.github.io/CompositeMotion>.

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1 INTRODUCTION

Despite significant advancements in physics-based character control, the majority of existing techniques rely on reference data consisting of motion capture recordings of an expert performing the behavior of interest [Bergamin et al. 2019; Chentanez et al. 2018; Lee et al. 2019; Park et al. 2019; Peng et al. 2018, 2022, 2021; Won et al. 2020; Xu and Karamouzas 2021]. While such reference data is paramount to train motor control policies that lead to natural and robust control, in this paper, we are interested in synthesizing composite behaviors for physically simulated humanoids by combining *multiple* motion capture reference clips into the training of a single policy. Further, we augment these imitation controllers with task-specific rewards to train the policy to accomplish specific functional tasks at the same time. To this end, we propose a novel multi-objective learning framework that builds *composite* motion behaviors through multiple discriminators, each with its own distinct reference motion as well as task-level control. Our framework is based on deep reinforcement learning, and allows us to adaptively balance the learning of disparate motions from multiple sources and also multiple goal-directed control objectives.

The motivation for this technique is twofold. First, humans are capable of sophisticated behaviors, including performing multiple

tasks simultaneously, such as walking and gesturing or using a mobile phone. To accomplish this with virtual characters, existing control approaches need to be extended to accommodate the ability to train with multiple objectives as a goal. Second, with limited exception, most current control frameworks rely on imitation with the style of a behavior being derived from reference motion examples. Our aim is to be able to combine examples automatically through what we call “composite motion control” to avoid the need to continuously seek new example motions for every new permutation of combined behaviors. We also explore the ability to add multiple task objectives to support our aim of multi-objective control.

The core difference of our approach from existing imitation learning approaches is decoupling full-body control during training, turning imitation and goal-directed full-body training into a multi-objective learning framework. To this end, we propose a modification to generative adversarial networks (GANs) to accommodate multiple discriminators (for each subtask in the desired end behavior) and to incorporate the mixing of the behaviors as a part of the training. In this way, we sidestep the need to dictate weights for combining the subtasks as well as the need to shape careful reward functions manually for each new composite behavior. In addition, as we expect composite motions to often be augmentations from simpler behaviors, we introduce a method for learning composite motion control policies from existing policies through *incremental learning*. To this end, we train a meta policy, for example for walking, and then train a new policy to *cooperate* with the meta policy, producing a composite motion control policy significantly faster than learning from scratch. Thus, we can quickly add on to walking new activities from reference data such as punching or waiving, even if we do not have examples of these activities being combined previously with the meta policy.

One naive approach to produce the composite motions we target is to blend motion capture clips to produce a single new motion, and perform traditional imitation learning from there. This suggested technique may be plausible for simple composite behaviors, like waiving an arm while walking as the two behaviors do not use the same joints, nor do they influence each other greatly, and therefore the blending can be done by simple splicing in a way that is fixed over time. Even so, there is no guarantee of physical plausibility without subsequent training – and the approach does not scale for more complex behaviors which may have more complicated tradeoffs between body parts used, especially over time. In contrast, our approach offloads the need to create this weighting as it is produced automatically by the policy as a part of the dictated action. Likewise, the output of our system is automatically guaranteed to be physically valid. Finally, our approach also has the capability to add task-directed goals, such as walk to a specified location, which is not possible without significant manual effort being added to the naive approach described.

Overall, this paper makes the following contributions:

- We introduce a novel approach for physics-based character control that decouples full-body control in order to learn imitation and task goals from disparate sources and across distinct body parts.
- To this end, we extend GAN-style reinforcement learning and introduce a multi-objective learning framework to support

multiple discriminators and automatic weighting of imitation and goal-driven subtask rewards.

- We propose an incremental learning scheme that uses a meta-policy from an existing behavior to augment the behavior with new subtasks, producing a composite motion control policy that can be learned significantly faster than learning from scratch. Our scheme automatically learns weights across the body that are state dependent in order to effectively mix the original behavior with a new subtask in a temporally dynamic fashion.

2 BACKGROUND AND RELATED WORK

2.1 Physics-Based Character Control

Developing controllers for physically simulated humanoids has wide applications in computer graphics, robotics, and biomechanics. Over the years, a number of trajectory optimization approaches for physics-based control have been proposed that leverage heuristics or feedback rules [Coros et al. 2010; De Lasa and Hertzmann 2009; Wampler et al. 2014; Ye and Liu 2010a; Zordan et al. 2014], including open-loop control schemes [Liu et al. 2015, 2010; Mordatch et al. 2012], close-loop feedback control [da Silva et al. 2017; Mordatch and Todorov 2014] and model predictive control approached [Hämäläinen et al. 2015; Kwon and Hodgins 2010; Tassa et al. 2012, 2014]. Given the difficulty in controller design, which often involves multiple optimization objectives, data-driven methods using demonstrations from real humans has also drawn a lot of attention [Da Silva et al. 2008; Kwon and Hodgins 2017; Lee et al. 2010; Liu et al. 2016, 2012; Muico et al. 2009; Sok et al. 2007; Yin et al. 2007; Zordan and Hodgins 2002].

In recent years, with the advancement of machine learning techniques, deep reinforcement learning frameworks have gained a lot of popularity for training physics-based character controllers. While some works [Karpathy and Van De Panne 2012; Won et al. 2018; Xie et al. 2020; Yu et al. 2018] purely rely on reward functions designed heuristically or using curriculum learning to perform control and encourage the character to act in an expected, human-preferred style, most recent works leverage motion capture data to perform imitation learning in order to generate high-fidelity, life-like motions. DeepLoco [Peng et al. 2017] employs a hierarchical controller to perform walking-style imitation in navigation tasks for a physically simulated character. DeepMimic [Peng et al. 2018] combines imitation learning with goal-conditioned learning, and enables a physics-based character to learn a motor skill from a reference motion collected by motion capture or handcrafted by artists. Chentanez et al. [2018] explore the training of recovery policies that would prevent the character from deviating significantly from the reference motion. While the aforementioned works rely on a phase variable to synchronize with the reference motion, DReCon [Bergamin et al. 2019] utilizes a motion matching technique to find the target pose from a collection of reference motions dynamically in response to user control input.

Besides relying on direct tracking of reference motions, researchers have offered a number of ways to extend the use of reference data in various ways. For example, Park et al. [2019] leverage the kinematic characteristics of unorganized motions to generate target poses for

the control policy to imitate. UniCon [Wang et al. 2020] adopts a similar strategy, where a high-level motion scheduler is employed to provide the target pose for the low-level character controller. MotionVAE [Ling et al. 2020] employs data-driven generative models using variational autoencoders to generate target motion poses for a reinforcement learning based controller. A similar model is employed by Won et al. [2022] and tested with various goal-directed downstream tasks. To ensure synthesis of desired motions, these approaches rely on carefully designed reward functions to assess the controlled character motion. Drawn from GAIL [Ho and Ermon 2016; Merel et al. 2017], AMP [Peng et al. 2021] and ICCGAN [Xu and Karamouzas 2021] avoid manually designing reward functions by exploiting the idea of generative adversarial network (GAN) and relying on a discriminator to obtain the imitation reward for training.

Beyond the simple use of full-body motions, many works explore motion generation by combining together multiple basic motions with respect to different body parts [Alvarado et al. 2022; Jang et al. 2022, 2008; Liu and Hodgins 2018; Soga et al. 2016; Starke et al. 2021; Yazaki et al. 2015]. However, these works focus on the editing and synthesis of motion animation or using inverse kinematic solvers, and do not work well with current frameworks for controlling physically simulated characters using reinforcement learning. To date, existing works for physics-based character control solely focus on the learning of full-body motions. As complementary to such works, in this paper, we target composite motion learning from multiple references without needing to generate any target full-body motion for tasks involving both goal-directed control and imitation control.

2.2 Training Efficiency

Characters employed during physics-based control typically are highly articulated with many degrees of freedom defined in continuous action spaces. Given the vast feasible choices of action, controlling so many degrees of freedom is essentially ambiguous, resulting in control problems that are under specified and highly dimensional. A qualified control policy usually needs millions of samples for training. The time consumption depends on the exploited algorithms and the motion complexity, varying from tens of hours to several days. While some works such as [Yang and Yin 2021] explore approaches to speed up the training by improving the reinforcement learning algorithm itself, a lot of attention has been recently drawn on sample-efficient training by reusing pre-trained policies or action models for fast new motion learning. For example, many recent approaches employ mixture of experts (MoE) models [Peng et al. 2019; Won et al. 2020, 2021], where a batch of pre-trained expert policies are exploited to provide primitive actions that are combined by a newly trained policy to generate the final actions. Other approaches explore using pre-trained latent space models such as variational autoencoders [Ling et al. 2020; Won et al. 2022] and GAN-based models [Peng et al. 2022] to facilitate the training of a control policy. In such approaches, the latent space model encapsulates a variety of reference motions and is used by the control policy to generate motions for a specific task. The works in [Merel et al. 2019, 2020] combine MoE with a latent space model and rely on an encoder-decoder architecture to perform distillation

for motion learning. Ranganath et al. [2019] utilize principal component analysis to extract coactivations from reference motions and use them as the atomic actions for motor skill learning.

Despite achieving impressive results, exploring the latent space or learning how to combine expert policies is not always easier compared to performing exploration directly in the original action space. We note that all of these works focus only on reusing models that provide full-body motions. In contrast, we propose an incremental learning approach that allows a newly trained policy to take only partial actions from a pre-trained policy, and add on that to generate composite motions. Our approach can largely reduce the training time for composite and multi-objective tasks involving multiple imitation and goal-directed objectives as compared to training from scratch.

2.3 Multi-Objective Control

In multi-objective character control, the reward function of the underlying optimization problem is expressed as the weighted sum of multiple, possibly competing, goals. Depending on the task in hand, we seek for objective terms that encourage the character to accomplish behavior goals, follow reference motion and/or style, adopt certain behavior characteristics such as low energy movement, attaining specified goals, etc., resulting in an extensive list of objective terms (see [Abe et al. 2007; Macchietto et al. 2009; Muico et al. 2009; Peng et al. 2018; Wu and Zordan 2010; Ye and Liu 2010a,b] for some examples). But how we handle all these competing objectives to create coherent, natural, and coordinated control remains an open question. A common solution is to employ a manual weighting scheme based on intuition, experience, and trial and error. However, such approaches often require excessive, often tricky manual effort to obtain desired results. While prioritized-based schemes have been employed that optimize each term in the reward function based on a given priority [De Lasa and Hertzmann 2009; De Lasa et al. 2010], such schemes cannot automatically address the problem of multiple competing objectives.

This problem becomes worse within a reinforcement learning setting, as small changes in the reward function can have a significant impact on the resulting behavior. It may need laborious work to finetune the weight of each objective to ensure that the control policy can effectively balance the learning of multiple objectives in a desired way. For tasks with hierarchical objectives, hierarchical reinforcement learning with multiple controllers can be employed, where a different controller is selected at different task levels [Clegg et al. 2018; Nachum et al. 2019; Peng et al. 2017; Xie et al. 2020]. However, such approaches cannot work for nonhierarchical tasks, where different objective terms need to simultaneously be optimized such as when the character has to perform composite motion imitation and goal-directed control as in our problem domain. In our approach, we propose the use of a multi-critic optimization scheme, where each objective is regarded as an independent task and is assigned a separate critic. By evaluating each objective independently, the contribution (gradient) of each objective can be normalized into the same scale, and, thus, the control policy will be updated toward each objective at the same pace. As such, we avoid scalarizing and

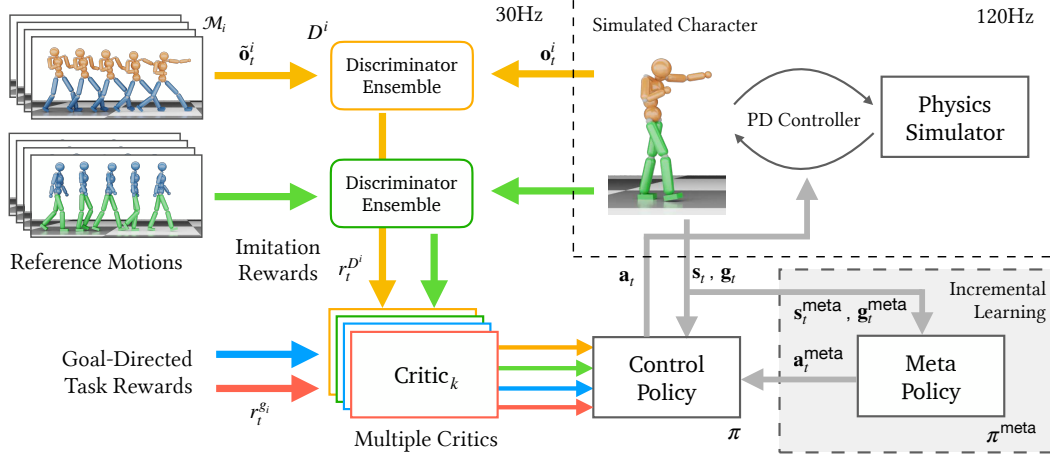


Fig. 2. Overview of the proposed system for composite motion learning with task control. Under the framework of reinforcement learning combined with a GAN-like structure for motion imitation, our approach employs a multi-critic architecture to train a physics-based controller involving multiple objectives. Based on this system, we further propose an optional incremental learning scheme that allows the control policy to fast learn new composite motions and tasks by reusing a pre-trained, meta policy.

weighting the rewards or priorities of multiple objectives. In addition, our approach provides a simple solution to adaptively balance the multiple objectives during policy updating without needing to find or estimate the Pareto front.

3 OVERVIEW

Our approach enables a physically simulated character to perform composite motions through imitating partial-body motions from multiple reference sources directly and simultaneously. This scheme turns the full-body motion imitation task into a multi-objective optimization problem, to which we can further introduce extra objectives for goal-directed control. We refer to Fig. 2 for an overview of our proposed system for composite motion learning with task control. We employ a GAN-like structure combined with reinforcement learning to train the control policy imitating the given reference motions. As such, we do not have to manually design a reward function for imitation learning or explicitly track a target pose from the reference motions. To learn composite motions, we decouple the full-body motion into several partial-body groups each of which imitates its own references. Based on this GAN-like structure, we propose a multi-objective learning framework that exploits multiple critics at the same time to help the control policy learn from multiple objectives, involving both composite motion imitation and goal-directed task control in a balanced way (Section 4). To accelerate training, we further consider an optional incremental learning scheme that reuses a pre-trained policy as the meta policy and allows a cooperative policy to adapt the meta one for new composite tasks (Section 5).

4 COMPOSITE MOTION LEARNING

Given a physically simulated character, we seek to train a control policy $\pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t)$ that simultaneously imitates motions from multiple reference ones, each focusing on specific body parts, while possibly completing specific goal tasks. At each time step t , the

control policy takes the character state $\mathbf{s}_t$ and a dynamic goal state variable $\mathbf{g}_t$ as the input and outputs the control signal (action) $\mathbf{a}_t$. We let $\mathbf{g}_t$ be an empty variable if no goal-directed control is involved. In the following, we detail our proposed approach for training π that decouples full-body motion allowing imitation performance to be evaluated and improved with respect to specific body parts, and converts the underlying composite motion learning problem into a multi-objective optimization problem.

4.1 Full-Body Motion Decoupling

At each time step t , we represent the character pose as $\mathcal{P}_t := \{(p_l, q_l, \dot{p}_l, \dot{q}_l) | t\}_{l=1}^{N_{\text{link}}}$, where $p_l \in \mathbb{R}^3$ and $q_l \in \mathbb{R}^4$ are the position and orientation (measured in the unit of quaternion) of each body link respectively, and $\dot{p}_l \in \mathbb{R}^3$ and $\dot{q}_l \in \mathbb{R}^3$ are the linear and angular velocities respectively. Given the geometry model and joint constraints of the simulated character, this representation can be converted into a joint space one defined by the skeletal joints' local position and velocity and the root's global position and orientation.

Let $\mathcal{M} \supset \{\tilde{\mathcal{P}}_t\}_t$ be the collection of reference motions which may contain multiple clips of pose trajectories $\{\tilde{\mathcal{P}}_t\}_t$ as the reference. To perform imitation learning, existing approaches either use a carefully designed reward function to compute the error between $\mathcal{P}_{t+1}$ and $\tilde{\mathcal{P}}_{t+1}$ [Bergamin et al. 2019; Chentanez et al. 2018; Park et al. 2019; Peng et al. 2018; Won et al. 2020], or employ an evaluator to assess the transfer $\mathcal{P}_t \rightarrow \mathcal{P}_{t+1}$ without explicitly comparing to any specific poses in the reference motions [Merel et al. 2017; Peng et al. 2021; Xu and Karamouzias 2021]. The former approaches usually need a motion tracking or generation mechanism to retrieve $\tilde{\mathcal{P}}_{t+1}$ from the reference motions. The latter typically build on the framework of adversarial generative networks (GANs) and rely on a discriminator to evaluate the transfer. Some approaches take poses from more than one frame during imitation performance evaluation in order to apply more constraints on the pose trajectory.

Nevertheless, all these approaches leverage the full-body character pose $\mathcal{P}_t$ and reference pose $\tilde{\mathcal{P}}_t \in \mathcal{M}$ to perform imitation learning, and thus intend to learn the full-body motions in $\mathcal{M}$.

To learn composite motions, ideally, we want the simulated character's partial body motions to come from different reference sources at a given time step t , i.e., the transfer of pose trajectory $\mathcal{P}_{t-n_i:t}^i \rightarrow \mathcal{P}_{t+1}^i$ should satisfy

$$\{\mathcal{P}_{t-n_i}^i, \dots, \mathcal{P}_t^i, \mathcal{P}_{t+1}^i\} \subset \mathcal{M}^i, \quad (1)$$

where $\mathcal{P}_t^i \subset \mathcal{P}_t$ is a partial-body pose from the simulated character, and $\mathcal{M}^i \supset \{\tilde{\mathcal{P}}_t^i\}_t$ is the reference motion collection containing only poses of the partial body group i . The full-body motion is constrained by using multiple $\mathcal{M}^i$ at the same time. Here, we follow Xu and Karamouzas [2021] and use a pose trajectory having $n_i + 2$ frames for imitation performance evaluation. The larger n_i is, the stricter the evaluation will be, as an error occurring at an earlier time step would negatively influence the evaluation of the following steps.

Typical partial body groups for a humanoid character would be the upper and lower body, arms, and torso. For example, we can let $\mathcal{M}^{\text{upper}}$ be a collection of greeting motions involving the upper body (arms, hands, torso and head), and $\mathcal{M}^{\text{lower}}$ be walking motions involving the lower body (pelvis, legs and feet). Then, the full body motion is expected to be the composite of $\mathcal{M}^{\text{upper}}$ (greeting) and $\mathcal{M}^{\text{lower}}$ (walking). To coordinate the motions from multiple body groups, we can let $\mathcal{P}_t^i$ and some other partial-body poses $\mathcal{P}_t^j$ share some common body link states. For example, let $\mathcal{P}_t^{\text{upper}}$ and $\mathcal{P}_t^{\text{lower}}$ share the state of one leg to avoid ipsilateral walking. Correspondingly, the leg state should be included in both $\mathcal{M}^{\text{upper}}$ and $\mathcal{M}^{\text{lower}}$ for the control policy to learn. We refer to Sections 6 and 7 for body splitting schemes used in our experiments, including typical upper and lower body decoupling schemes and more tailored ones for specific tasks such as juggling while walking. After decoupling the character's full-body motion into multiple sets of $\{\mathcal{P}_t^i\}_t$, we perform imitation learning with respect to each body group independently, where the control policy is expected to explore how to combine partial-body motions by itself without needing any full-body, composite motions to be provided as the reference.

4.2 Imitation Learning

To perform imitation learning, we build our approach off of GAN-like frameworks [Ho and Ermon 2016; Merel et al. 2017], which utilize a discriminator to evaluate imitation performance and generate reward signals for policy optimization using reinforcement learning algorithms. However, instead of using only one discriminator to perform full-body imitation performance evaluation, we employ multiple discriminators simultaneously, each of which deals with a body part group i associated with a collection of partial-body reference motions $\mathcal{M}^i$. Based on this framework, we can avoid designing reward functions to compute the imitation error for each specific body part group. Furthermore, each discriminator can take only its own interested body link states as input during training. Therefore, the provided $\mathcal{M}^i$ can still be a collection of full-body motions, but there is no need to explicitly generate any partial-body motions during preprocessing.

To stabilize the adversarial training process, we introduce a hinge loss [Lim and Ye 2017], gradient penalty term [Gulrajani et al. 2017], and an ensemble technique for training of discriminators as proposed in [Xu and Karamouzas 2021]. Following the literature, given $\mathbf{o}_t^i$ as the observation sampled from the simulated character and $\tilde{\mathbf{o}}_t^i$ as that sampled from the reference motions $\mathcal{M}^i$, the i -th ensemble of N discriminators, $D^i = \{D_n^i | n = 1, \dots, N\}$ is trained using the loss function:

$$\mathcal{L}_{D^i} = \frac{1}{N} \sum_{n=1}^N \left(\mathbb{E}_t [\max(0, 1 + D_n^i(\mathbf{o}_t^i))] + \mathbb{E}_t [\max(0, 1 - D_n^i(\tilde{\mathbf{o}}_t^i))] + \lambda^{\text{GP}} \mathbb{E}_t \left[\left(\|\nabla_{\tilde{\mathbf{o}}_t^i} D_n^i(\tilde{\mathbf{o}}_t^i)\|_2 - 1 \right)^2 \right] \right) \quad (2)$$

where $\tilde{\mathbf{o}}_t^i = \alpha \mathbf{o}_t^i + (1 - \alpha) \tilde{\mathbf{o}}_t^i$ with $\alpha \sim \text{UNIFORM}(0, 1)$ and λ^{GP} is gradient penalty coefficient.

According to Eq. 1, we define the observation space of a discriminator as

$$\mathbf{o}_t^i := \{\mathcal{P}_{t-n_i}^i, \dots, \mathcal{P}_t^i, \mathcal{P}_{t+1}^i\}. \quad (3)$$

In principle, the discriminator relies on $\mathbf{o}_t^i$ to evaluate the control policy's performance during the state-action-state transition $(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}_{t+1})$. The observation space theoretically should satisfy $\mathbf{o}_t^i \subseteq \{\mathbf{s}_t, \mathbf{s}_{t+1}\}$. Otherwise, the discriminator may rely on features unknown to the control policy, and thus it cannot effectively evaluate the policy's performance. Given that the control policy π in our formulation is still a full-body control policy, we simply define $\mathbf{s}_t$ as a full-body motion state:

$$\mathbf{s}_t := \{\mathcal{P}_{t-n}, \dots, \mathcal{P}_t\} \quad (4)$$

where $n \geq n_i$ for all i . We refer to the Appendix in the supplementary material for more details about the state and observation representation.

The hinge loss function provides a linear evaluation between $[-1, 1]$ to measure the similarity of a given pose trajectory sample $\mathbf{o}_t^i$ to any sample in the reference motions. Therefore, we define the reward term that evaluates the policy's imitation performance with respect to $\mathcal{M}^i$ for the body part group i at time t as:

$$r_t^{D^i}(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}_{t+1}) = \frac{1}{N} \sum_{n=1}^N \text{CLIP} \left(D_n^i(\mathbf{o}_t^i), -1, 1 \right). \quad (5)$$

It must be noted that even though $\mathbf{o}_t^i$ and $\tilde{\mathbf{o}}_t^i$ in Eq. 2 have the same subscript t , they are paired only for the gradient penalty computation (last term in Eq. 2). The discriminator ensemble here only evaluates the pose trajectory $\mathbf{o}_t^i$ independently, rather than comparing it against any specific target trajectory. Therefore, $\tilde{\mathbf{o}}_t^i$ can be randomly sampled from the reference motions by interpolation.

Overall, by employing multiple discriminator ensembles at each time step t , we will have a set of rewards, $\{r_t^{D^i}\}_{D^i}$, to evaluate the policy's performance of controlling the character to perform composite motions, i.e. simultaneously imitating different sets of reference motions corresponding to specific partial body parts. By doing so, we convert the task of composite motion learning to a multi-objective optimization problem under the framework of reinforcement learning.

4.3 Multi-Objective Learning

We consider policy optimization of a typical on-policy policy gradient algorithm by maximizing

$$\mathcal{L}_\pi = E_t [A_t \log \pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t)], \quad (6)$$

where $\mathbf{s}_t$ and $\mathbf{g}_t$ are the given character's and goals' state variables respectively, and A_t is the advantage which is typically estimated by $\{r_\tau\}_{\tau \geq t}$. In the common actor-critic architecture, a separate network (critic) is updated in tandem with the policy network (actor). The critic is employed to provide state-dependent value estimation, $V(\mathbf{s}_t) = E_\pi[\sum_{\tau \geq t} \gamma^{\tau-t} r_\tau] = E_\pi[r_t + \gamma V(\mathbf{s}_{t+1})]$, based on which A_t can be estimated with less variance, where γ is the discount factor regulating the importance of the contribution from future steps. To stabilize the training, standardization is often applied on A_t where the standardized advantage $\bar{A}_t$ is used in place of A_t for policy updating.

A typical solution for multi-objective tasks in reinforcement learning is to simply add together all objective-related reward terms, r_t^k , with some weights ω_k , i.e., $r_t = \sum_{k=1}^K \omega_k r_t^k$ for a K -objective problem. In such a way, we still have a scalar reward that can be used with Eq. 6 for policy updating. In practice, though, given that conflicts may exist among the different reward terms, manually tuning the values of ω_k to balance the composite objective of the character is not an intuitive task. For example, we may need the policy to put more effort into learning a difficult partial-body motion, instead of even with a trade-off in learning other motions, rather than only focusing on the easy ones to keep achieving a higher associated reward. In addition, our proposed approach performs reward estimation by employing multiple discriminators simultaneously, which are modeled by neural networks. This scheme brings a lot of uncertainty, as the reward distributions from different discriminators may differ a lot depending on the given reference motions, which could be unpredictable before training. Such a problem would deteriorate if we further introduce a set of goal-directed tasks, each having its own associated reward term which may compete against the imitation reward terms.

To balance the contributions of multiple objectives during policy updating, we propose to model the multi-objective learning problem as a multi-task one, where each objective is taken into account as an *independent task* and has a fixed importance during policy updating. To do so, instead of using $r_t = \sum_k \omega_k r_t^k$, we compute the advantage of A_t^k with respect to $\{r_\tau^k\}_{\tau \geq t}$ independently. Then, the optimization process becomes maximizing

$$\mathcal{L}_\pi = \sum_{k=1}^K E_t \left[\omega_k \bar{A}_t^k \log \pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t) \right], \quad (7)$$

where $\sum_k \omega_k = 1$ and $\bar{A}_t^k$ is the standardization of A_t^k , i.e.

$$\bar{A}_t^k = \frac{A_t^k - E_t[A_t^k]}{\sqrt{\text{Var}_t[A_t^k]}}. \quad (8)$$

This optimization process is equal to updating the policy with respect to each objective independently but always at the same scale proportional to ω_k . The introduction of ω_k gives us more flexibility to adjust the contributions toward each objective when conflicts

occur during policy updating. However, under our testing, a simple choice of $\omega_k = 1/K$, which means each objective is equally important, works well for most cases. We refer to the Appendix in the supplementary material for the choice of ω_k in our tested composite tasks.

During implementation, we can rewrite Eq. 7 as

$$\mathcal{L}_\pi = E_t \left[\left(\sum_k \omega_k \bar{A}_t^k \right) \log \pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t) \right] \quad (9)$$

such that the policy update can be done through backward propagation in one pass. From this equation, we can see that the nature of our approach is to introduce a dynamic coefficient constrained by the standard deviation of $\{A_t^k\}_t$ for each objective k . As such, the policy will be updated with respect to each objective adaptively. This separation of objectives leads to a single-policy multi-critic architecture. In Fig. 2, for example, we have two imitation related reward terms (yellow and green) for upper and lower body imitation respectively, and two goal-directed task reward terms (red and blue). Accordingly, we employ four critics denoted by CRITIC_k in the figure. Each CRITIC_k only participates in the estimation of A_t^k , and takes the reward associated with the objective k , i.e. $\{r_t^k\}_t$, for training.

Though the policy update is balanced through the proposed multi-critic architecture, the state values, which are decided by $\{r_t^k\}_t$, could differ still drastically with respect to each objective depending on the difficulty of given reference motions or the reward distributions of the goal-related tasks. To mitigate this issue and stabilize the training of critics, we introduce the value normalization scheme of *PopArt* [van Hasselt et al. 2016]. The value target under this scheme is normalized by the moving average and standard deviation for the critic network training. The output of a critic is unnormalized before joining the process of advantage estimation. Besides maintaining a normalizer for value targets, *PopArt* is designed to preserve the output precisely. Namely, with *PopArt*, the output of a critic is identical before and after the normalizer updates given the same input state $\mathbf{s}_t$ and $\mathbf{g}_t$. Such a design is to prevent the normalization from affecting the value state estimation, thereby stabilizing the policy training. In our implementation, each critic $\text{CRITIC}_k(\mathbf{s}_t, \mathbf{g}_t)$ has its own normalizer with a scalar scale and shift estimated independently with respect to its associated objective k . As we show in Section 6.6, the introduction of *PopArt* helps improve the policy performance as also demonstrated by previous works [van Hasselt et al. 2016; Yu et al. 2021].

5 INCREMENTAL LEARNING

Besides being able to perform a range of composite motions, humans typically learn such motions in an incremental manner. For example, if we know how to walk, we should be able to quickly learn how to hold our phone while walking. There is no need to relearn walking from scratch. Based on this intuition, we propose an incremental learning scheme for fast composite motion learning. Instead of training a policy completely from scratch, we reuse a pre-trained policy as a meta policy π^{meta} that allows the simulated character to perform a basic set of motions (walking in the previous example). Given π^{meta} , we train a new policy π to cooperate

ALGORITHM 1: Multi-Objective Incremental Learning

```

1 Prepare the meta policy  $\pi^{\text{meta}}$ ;
2 initialize the policy network  $\pi$ ;
3 initialize the critic network  $\text{CRITIC}_k$  where  $k = 1, \dots, K$  given  $K$ 
  objectives in the task;
4 initialize policy replay buffer  $\mathcal{T}$  and reward buffer  $\mathcal{R}$ ;
5 prepare reference motions  $\mathcal{M}^i$  for each discriminator ensemble  $D^i$ ;
6 while training does not converge do
7    $\mathcal{T} \leftarrow \emptyset, \mathcal{R} \leftarrow \emptyset$ ;
8   for each environment step  $t$  do
9      $\mathbf{a}_t^{\text{meta}} \sim \pi^{\text{meta}}(\cdot | \mathbf{s}_t^{\text{meta}}, \mathbf{g}_t^{\text{meta}})$ ;
10     $\mathbf{a}_t \sim \pi(\cdot | \mathbf{s}_t, \mathbf{g}_t, \mathbf{a}_t^{\text{meta}})$ ;
11     $\mathbf{s}_{t+1}, \mathbf{g}_{t+1}, \mathbf{r}_t^{\text{gt}} \leftarrow$  environment updates with character
      control signal of  $\mathbf{a}_t$ ;
12    extract observation  $\mathbf{o}_t^i$  from the state pair of  $\mathbf{s}_t$  and  $\mathbf{s}_{t+1}$  for
      each discriminator ensemble  $D^i$ ;
13     $\mathcal{T} \leftarrow \mathcal{T} \cup \{(\mathbf{s}_t, \mathbf{a}_t, \{\mathbf{o}_t^i\}_i)\}$ ;
14     $\mathcal{R} \leftarrow \mathcal{R} \cup \{r_t^k\}$  for each term  $k$  in  $\mathbf{r}_t^{\text{gt}}$ ;
15     $\mathbf{s}_t \leftarrow \mathbf{s}_{t+1}; \mathbf{g}_t \leftarrow \mathbf{g}_{t+1}$ ;
16    extract  $\mathbf{s}_t^{\text{meta}}$  and  $\mathbf{g}_t^{\text{meta}}$  from  $\mathbf{s}_t$  and  $\mathbf{g}_t$  respectively
17  end
18  for each discriminator ensemble  $D^i$  do
19    draw samples  $\tilde{\mathbf{o}}_t^{D^i}$  from  $\mathcal{M}^i$ ;
20    update  $D^i$  using  $\mathbf{o}_t^i$  from  $\mathcal{T}$  and  $\tilde{\mathbf{o}}_t^i$  based on Eq. 2;
21    for each  $\mathbf{o}_t^i$  in  $\mathcal{T}$  do
22      compute step-wise imitation reward  $r_t^{D^i}$  based on Eq. 5;
23       $\mathcal{R} \leftarrow \mathcal{R} \cup \{r_t^{D^i}\}$ 
24    end
25  end
26  for each reward term collection  $\{r_t^k\}_t$  in  $\mathcal{R}$  do
27    compute advantage  $A_t^k$  using  $\{r_\tau^k\}_{\tau \geq t}$  and state value
      estimation from  $\text{CRITIC}_k(\mathbf{s}_t, \mathbf{g}_t)$  unnormalized by PopArt;
28    compute value target  $V_t^k$  based on  $A_t^k$ ;
29    update the normalizer for  $\text{CRITIC}_k$  based on  $V_t^k$  using
      PopArt;
30    get normalized value target  $\bar{V}_t^k$  by PopArt;
31    get normalized advantage  $\bar{A}_t^k$  based on Eq. 8
32  end
33  for each policy update step do
34    update  $\pi$  using  $\{(\mathbf{s}_t, \mathbf{a}_t, \{\bar{A}_t^k\}_k)\}_t$  based on Eq. 9;
35    update each critic network  $\text{CRITIC}_k$  using  $\{\bar{V}_t^k\}_t$ 
36  end
37 end

```

with the meta policy, performing new composite motions by action addition (holding a phone + walking).

Formally, let $\pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t) := \mathcal{N}(\boldsymbol{\mu}_t, \boldsymbol{\sigma}_t^2)$ denote a Gaussian-based policy. By introducing a meta policy π^{meta} , we define the policy, which is trained to cooperate with π^{meta} for new composite motions as

$$\begin{aligned}
 \pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t, \mathbf{a}_t^{\text{meta}}) &:= \mathcal{N}(\boldsymbol{\mu}_t, \boldsymbol{\sigma}_t^2) + \mathbf{w}_t \text{STOP}(\mathbf{a}_t^{\text{meta}}) \\
 &= \mathcal{N}(\boldsymbol{\mu}_t + \mathbf{w}_t \text{STOP}(\mathbf{a}_t^{\text{meta}}), \boldsymbol{\sigma}_t^2),
 \end{aligned} \tag{10}$$

where the weight vector $\mathbf{w}_t$ has the same dimension with $\mathbf{a}_t^{\text{meta}}$, and $\mathbf{a}_t^{\text{meta}} \sim \pi^{\text{meta}}(\cdot | \mathbf{s}_t^{\text{meta}}, \mathbf{g}_t^{\text{meta}})$ is drawn from the meta policy. $\mathbf{w}_t$ are defined as a set of weights each of which is associated with a DoF in the action space of the meta policy. In our implementation, $\mathbf{w}_t$, $\boldsymbol{\mu}_t$ and $\boldsymbol{\sigma}_t$ are obtained by a neural network taking $\mathbf{s}_t$ and $\mathbf{g}_t$ as input, and thus are learnable. We put a "gradient stop" operator, $\text{STOP}(\cdot)$, on $\mathbf{a}_t^{\text{meta}}$, which means that the meta policy is fixed and will not be updated with π .

Using this incremental learning scheme, the new, cooperative policy adds its own action to the meta action $\mathbf{a}_t^{\text{meta}}$. The weight vector $\mathbf{w}_t$ decides the reliance of π on the meta policy π^{meta} with respect to each DoF in the action space. The bigger an element in $\mathbf{w}_t$ is, the more the cooperative policy relies on the meta policy to control the corresponding DoF. As such, π is trained incrementally to learn new composite motions by reusing the meta policy partially. This scheme does not require that $\mathbf{a}_t^{\text{meta}}$ and $\mathbf{a}_t$ must have exactly the same dimension, as we can assume zero values for the missing dimensions in $\mathbf{a}_t^{\text{meta}}$ or ignore the extra, uninteresting dimensions in $\mathbf{a}_t^{\text{meta}}$. Compared to a mixture-of-experts (MoE) model, where the action is obtained by a linear combination of the actions from multiple expert policies, our approach focuses on reusing partial-body motions from the meta policy. It would be very difficult for a MoE model to keep, for example, only the lower-body motion of one expert and replace the upper-body motion with that of another expert through a linear combination of the experts' full-body motions.

With the introduction of π^{meta} , we can replace $\pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t)$ in Eq. 7 with $\pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t, \mathbf{a}_t^{\text{meta}})$, and perform composite motion learning with goal-directed control under our proposed multi-objective learning framework. We refer to Algorithm 1 for the outline of the proposed multi-objective learning framework with incremental learning. To train a composite policy completely from scratch without using incremental learning, we can simply ignore π^{meta} and use $\pi(\mathbf{a}_t | \mathbf{s}_t, \mathbf{g}_t)$ solely in Algorithm 1.

6 EXPERIMENTS

In this section, we experimentally evaluate our approach on multiple challenging composite motion learning tasks. We show that our approach can effectively let motor control policies learn composite motions from multiple reference motions directly without manually generating any full-body motion as reference. Besides evaluating the imitation performance, we also apply our approach on several goal-directed control tasks combined with composite motion learning from unstructured reference data. The results demonstrate that our proposed approach can successfully tackle complex tasks balancing the learning of multiple objectives involving both partial-body motion imitation and goal-directed control. Finally, we perform ablation studies on our proposed multi-objective learning framework and incremental learning scheme.

6.1 Implementation Details

We run physics-based simulations using IsaacGym [Makoviychuk et al. 2021], which supports simulation with a large number of instances simultaneously by leveraging GPU. The simulated humanoid character has 15 body links and 28 DoFs, where the hands are fixed with the forearms and are uncontrollable. In the tasks involving a

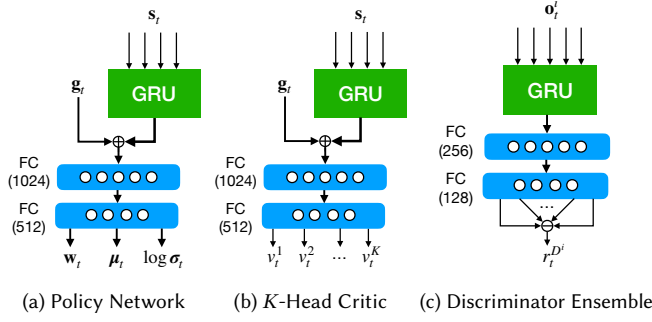


Fig. 3. Network structures. $\oplus$ denotes the concatenation operator and $\ominus$ denotes the average operator.

tennis player, we add 3 DoFs on the right wrist joint such that the character can control the racket more agilely, though the racket is fixed on the right hand. The simulation runs at 120Hz and the control policy at 30Hz. Differing from the previous works that employ a stable PD controller [Tan et al. 2011] for character control [Lee et al. 2022, 2021; Park et al. 2019; Peng et al. 2018, 2021; Won et al. 2020, 2022; Xu and Karamouzas 2021] we employ a normal, linear PD servo for faster simulation.

We use PPO [Schulman et al. 2017] as the base reinforcement learning algorithm for policy training and Adam optimizer [Kingma and Ba 2014] to perform policy optimization. To embed the character state s_t and the discriminator observation o_t^i sequentially, we employ a gated recurrent unit (GRU) [Chung et al. 2014] with a 256-dimension hidden state to process these temporal inputs. The embedded character state feature is concatenated with the dynamic goal state g_t if goal-directed control is involved, and then passed through a multilayer perceptron with two full-connected (FC) layers. The control policy is constructed as Gaussian distributions with independent components. The output of the policy network includes the mean μ_t and standard deviation σ_t parameters of the policy distribution as well as a weight vector w_t when incremental learning is exploited. The multiple critics in our multi-objective learning framework are modeled by a multi-head neural network. Similarly to the critic networks, we model a discriminator ensemble using a multi-head network. The outputs are averaged by Eq. 5 to produce the reward signal. All the network structures are shown in Fig. 3, in which we assume that there are K objectives in total. We refer to the Appendix in the supplementary material for the representation of g_t in our designed goal-directed tasks, and all hyperparameters used for policy training.

All the tested policies were trained on a machine equipped with an Nvidia V100 GPU. It typically takes about 1.5h to train a policy using a fixed budget of 20M samples (environment steps), for a pure composite motion imitation task. For complex tasks involving goal-directed control, it takes about 15 to 30 hours and requires about 2×10^8 to 4×10^8 samples to train a policy from scratch. By exploiting our incremental learning scheme to reuse a pre-trained meta policy, we can shorten the training time to about 30 minutes to 2 hours depending on the difficulty of the tasks.

6.2 Data Acquisition

All the motion data used for training are obtained from the LAFAN1 dataset [Harvey et al. 2020] and other commercial and publicly available motion capture datasets recorded at 30Hz. For single-clip imitation, we synthesize short reference motion clips of 1-3 seconds long (cf. Table 1). For tasks with goal-directed control, we extract several collections of motions (cf. Table 2), each of which contains multiple clips of reference motions with lengths varying from about 15 to 70 seconds. The juggling motion involves a single trial of a subject performing juggling while standing on a skate, while the collection of tennis swing motions contains four trials of forehand swings captured from different subjects. We retarget the local joint position from those motion data to our character model without extra manual reprocessing. We demonstrate that policies trained with our approach can perform motion synthesis from unstructured data for goal-directed control, and can explore how to perform composite motions by combining the partial-body motions from the reference motions without needing any manual processing for motion blending.

6.3 Imitation Performance

In Fig. 4, we highlight motion pose snapshots captured from some of our trained policies for composite motion learning. Each composite motion is learned based on two reference motion clips, one for the upper body and the other one for the lower body. From top to bottom, the names of corresponding motions are listed in Table 1. Overall, policies trained with our approach can perform very challenging composite motor skills by using the character's upper and lower body part groups at the same time. For example, in the motion combination of chest open and jumping jack (1st row), the control policy must keep the character's body balanced to perform the chest-open motion during jumping in the air, which is a pretty challenging task even for humans. Similar challenges arise when doing squats with the chest open (3rd row) and lunges with waist twisting (4th row). Besides simply following the two partial-body reference motions at the same time, the control policies must master how the partial motions could be combined such that the full-body motion is physically plausible. In the 4th row, for example, it is impossible for the character to keep twisting its waist while doing lunges at quite different frequencies. Similarly, in the motion combination of punch and walk (6th row) and that of punch and run (7th row), the character's foot has to contact the ground first in order to perform the punch action with the torso leaning forward. The control policy, thereby, must know when the punch action is doable and arrange the motion combination by itself, rather than strictly following the reference motions. Our approach does not require the given reference motions to be perfectly synchronized. The control policies take the character state as input and perform composite motions accordingly. Furthermore, the proposed dynamic sampling rate (see Appendix) allows the control policy to adjust the motion speed within an acceptable range for better motion combining.

To quantitatively evaluate the imitation performance, following previous literature [Harada et al. 2004; Peng et al. 2021; Tang et al. 2008; Xu and Karamouzas 2021], we leverage the technique of fast dynamic time warping (DTW) and measure the imitation error as

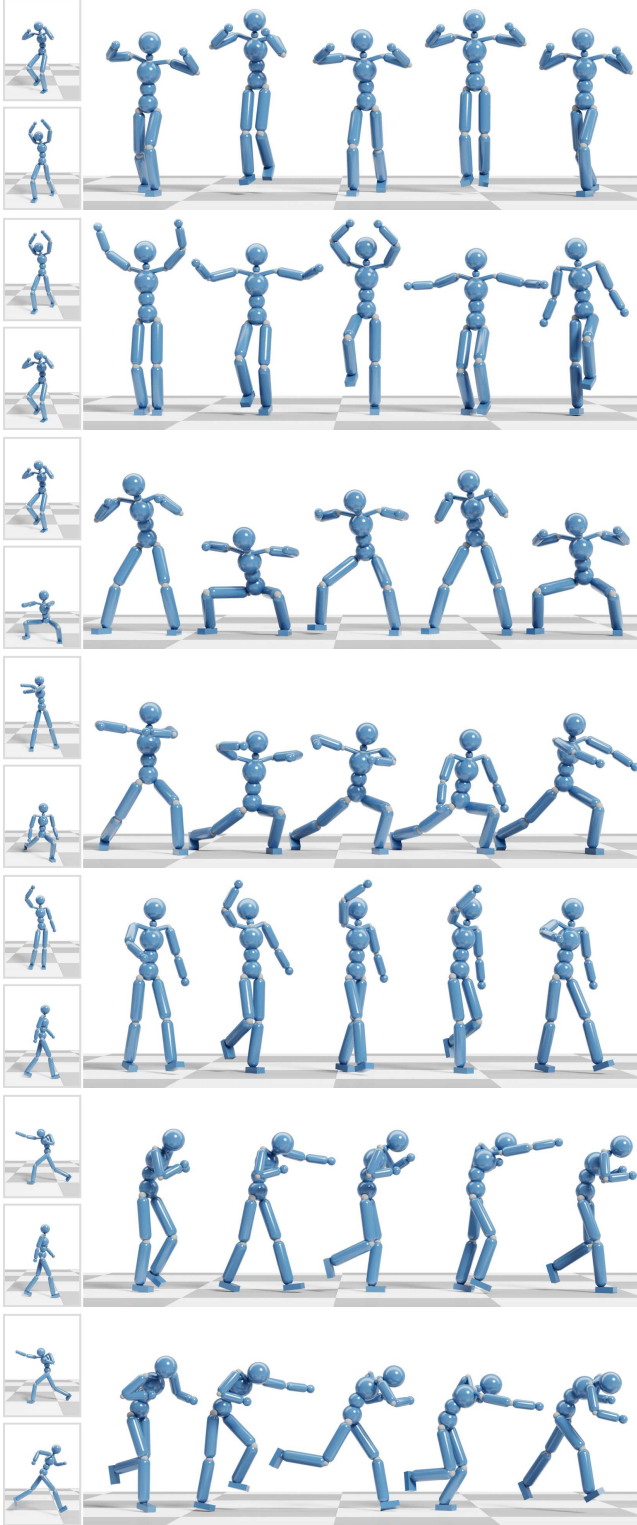


Fig. 4. Composite motions learned from multiple single-clip reference motions. The two snapshots shown on the left side of each row are the reference motions for the upper and lower body respectively.

Table 1. Imitation performance when learning composite motions from single clips of reference motions.

Composite Motion	Length [s]	Imitation Error [m]
Chest Open	2.10	0.11 ± 0.02
Front Jumping Jack (lower)	1.80	0.16 ± 0.03
Front Jumping Jack (upper)	1.80	0.30 ± 0.03
Walk In-place	2.10	0.29 ± 0.02
Chest Open	2.10	0.10 ± 0.01
Squat	1.67	0.09 ± 0.01
Waist Twist	3.37	0.15 ± 0.04
Leg Lunge	3.67	0.13 ± 0.02
Hand Waving	1.80	0.06 ± 0.03
Walk	1.10	0.09 ± 0.02
Punch	1.30	0.11 ± 0.02
Walk	1.10	0.10 ± 0.01
Punch	1.30	0.17 ± 0.03
Run	0.76	0.14 ± 0.01

follows:

$$e_t = \frac{1}{N_{\text{link}}^i} \sum_{l=1}^{N_{\text{link}}^i} \|p_l - \tilde{p}_l\|, \quad (11)$$

where $N_{\text{link}}^i = |\{\mathcal{P}_l^i\}|$ is the number of interesting body links in the i -th body part group, $p_l \in \mathbb{R}^3$ is the position of the body link l in the world space at the time step t , and $\tilde{p}_l$ is the body link's position in the reference motion. The evaluation results are shown in Table 1. Our approach can imitate the reference motions closely and balance the imitation of the two partial-body motions well. As can be seen, there is no big gap between the two imitation errors in a given composite motion combination, which means that policies trained with our approach do not just follow only one reference motion and ignore the other one. In contrast, without using our proposed multi-objective learning framework, the policy could prefer to track only one reference motion that is easy to follow. We refer to Section 6.6 for the related ablation study.

6.4 Goal-Directed Motion Synthesis

To test our approach with more complex tasks involving both composite motion learning and goal-directed control, we designed five goal-directed tasks, as shown in Figs. 5 and 6. In the *Target Heading* and *Target Location* tasks illustrated in Figs. 5a and 5b, the character is asked to respectively go along a target heading direction and toward a target location at a preferred speed. Besides the goal-directed objective, two motion imitation objectives are employed: one is for the lower-body and the other one is for the upper body. Differing from the examples shown in Fig. 4 where the walking and running motions are just single, short clips containing only one gait cycle, here we use a collection of unstructured walking and running motions as the reference for the lower body, as listed in Table 2. In the three examples shown in Fig. 5a, the upper body motions are learned from single reference motion clips, which are chest open, jumping jack, and punch respectively, as depicted by the small snapshots in the figure. In the examples shown in Fig. 5b, we use the motion collection of tennis footwork as the reference

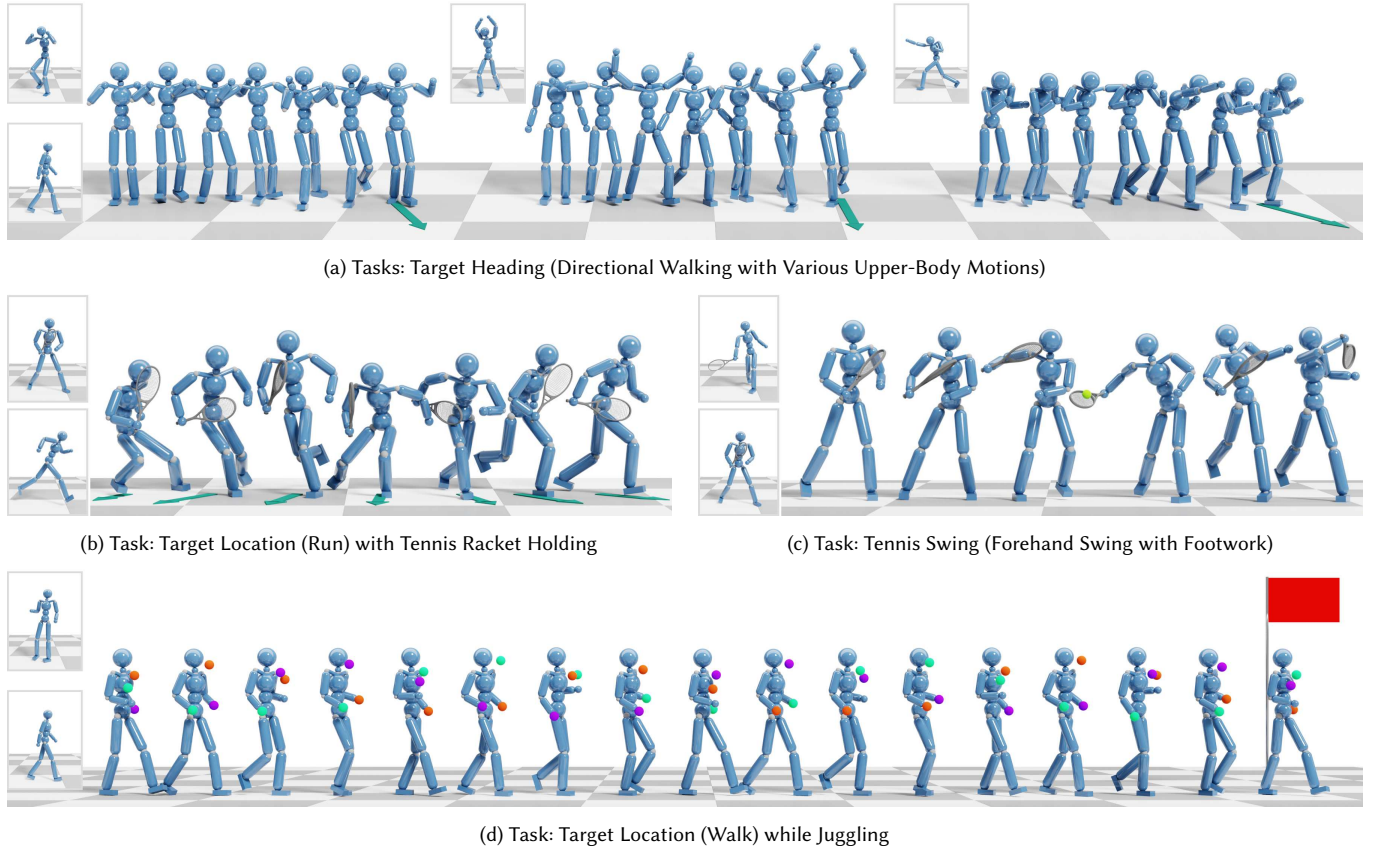


Fig. 5. Motion synthesis with composite motion learning and goal-directed control. Pose snapshots shown in the small windows are captured from the reference motions.

Table 2. Motion collections used for goal-directed control.

Motion Collection	# of Clips	Length [s]
Crouch	4	88.87
Walk	8	334.07
Run	4	282.87
Tennis Footwork	2	31.67
Tennis Swing	4	13.33
Aiming	2	48.77
Juggling	1	24.63

for the control policy to learn how to hold the racket. This task is relatively harder, as the reference motions for both the upper and lower body are unstructured. While following the reference motions closely, the control policies trained with our approach can effectively coordinate the character's upper and lower body poses to perform the composite motions during goal-steering navigation.

In the task of *Tennis Swing*, the character is expected to hit the ball successfully with a forehand. The provided collection of tennis swing motions contains four trials, where the subject performs forehand swings while standing still. The tennis ball in our implementation is generated randomly in a small region near the

character. As such, the control policy has to rely on the lower-body footwork motions to properly adjust the pose and position of the character relative to the tennis ball, while it relies on the upper body swing motions to swing effectively and on time. We note that the goal-directed reward in our design only evaluates the effectiveness of hitting based on the ball's outgoing speed and destination. The motion otherwise is decided completely by the control policy, which leverages two discriminator ensembles to perform imitation learning for the upper and lower body respectively.

The *Tennis Swing* task is challenging, as it is easy for the controlled character to solely hit the ball, but instead it is asked to do so by combining the motions from the reference collection (tennis swing for the upper body and tennis footwork for the lower body). The policy needs some exploration before finding a way to utilize poses from the reference motions to perform swings. In this process, imitation learning would fail if the policy simply tries to pursue a higher reward by simply hitting the ball. However, when the policy is trained using our proposed multi-objective learning framework, it can balance the imitation and goal-directed objectives, and perform forehand swings in the style of the reference motions. Additionally, while we provide only a small set of upper and lower body motions as the reference (cf. Table 2), the control policy successfully learns

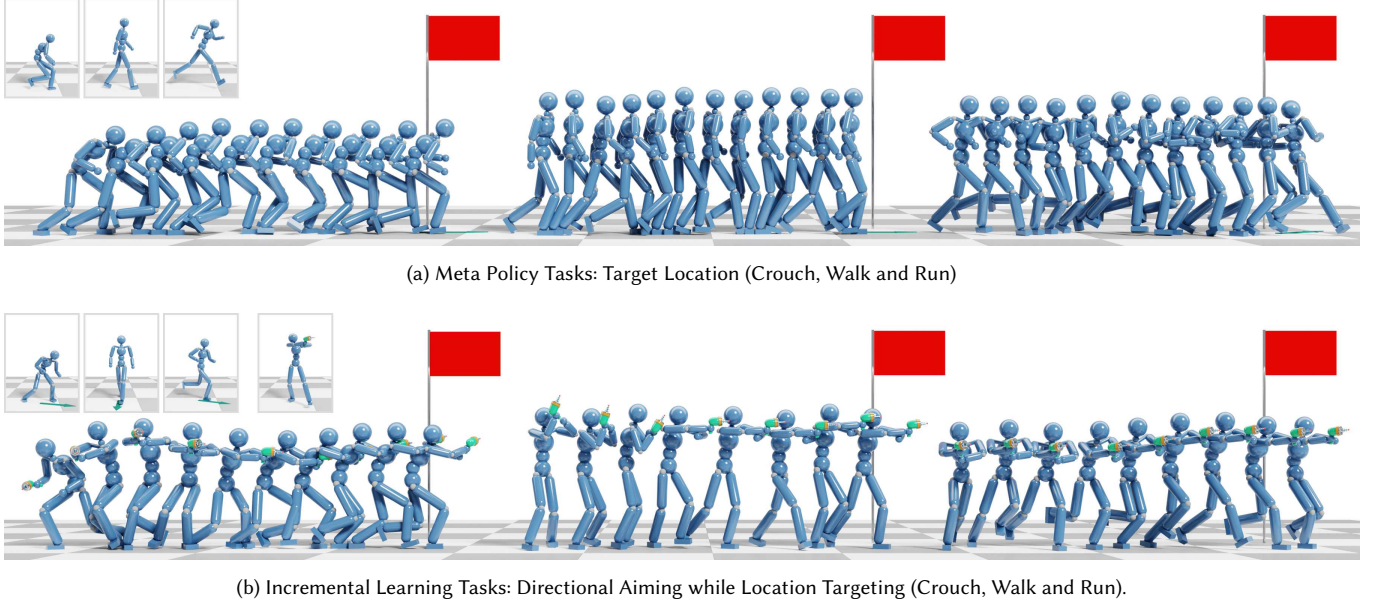


Fig. 6. Demonstration of incremental learning tasks, where goal-directed aiming motions are added to various locomotion behaviors from the meta policies.

how to combine the motions automatically to finish the task. In contrast, if we just leverage full-body reference motions, extra work is needed to generate various motions for the policy to learn. In addition, there are not enough demonstrations for the policy to perform tennis swings correctly in a human-like style by utilizing, for example, only standing swing motions without footwork.

Figure 5d shows another challenging composite task: *Target Location* while *Juggling*, where the character needs to juggle three balls while walking to the target location. This composite task involves four objectives: two imitation objectives and two goal-directed tasks of juggling and locomotion. In our experiment, when a ball is relatively close to a hand, it is assumed to be caught by and attached to that hand. The ball is automatically detached from hand at a fixed interval of 20 frames. In order to perform juggling successfully and successively, after a hand releases its ball, it must catch in time a flying target ball which was thrown by the other hand. This task is very challenging, as the control policy must explore how to perform ball throwing and catching in concert with the location-targeting task. Besides the difficulty of throwing and catching balls, the juggling reference motion involves a subject balancing on a skateboard with the body swaying from side to side¹. This increases the difficulty of composite motion learning to generate normal walking poses. Differing from the other examples that use a lower and upper-body split, here we decouple the body parts into two groups, where one group consists of the character's arms to imitate the juggling motion and the other group includes the rest of the body parts (torso, head, pelvis, and legs) taking the collection of walking motions as reference data. In such a way, our approach can effectively eliminate the body swings in the juggling reference motion, and generate

composite motions with the upper body moving naturally during goal-steering navigation.

The other goal-directed task explored in this study is *Aiming*, in which the character holds a toy weapon in its right hand and is expected to aim it toward a specific direction. In our experiments, that task is designed mainly to demonstrate the effectiveness of our proposed incremental learning scheme, which will be elaborated in the next section. We refer to the Appendix for the details of the setup of all of our goal-directed tasks, and the supplementary video for related animation results.

6.5 Incremental Learning

In Fig. 6, we show tasks used to test our proposed incremental learning scheme. The first row depicts three meta policies of locomotion, which are trained for the *Target Location* task completely from scratch using our proposed multi-objective learning framework. In contrast to previous examples, there is only one imitation objective about the full-body during training here, as shown by the snapshots on the top-left corner of the figure. In the 2nd row of the figure, we show the cooperative policies that are trained by incremental learning, while reusing the pre-trained, meta policies. In addition to the *Target Location* task, a new goal-directed task of *Aiming* is introduced during training the cooperative policies. The controlled character in this task needs to adjust its right forearm and let the toy pistol aim toward a goal direction specified dynamically.

The goal of this experiment is to demonstrate that the cooperative policies can properly exploit the meta policies to perform styled locomotion behaviors while quickly learning upper-body motions from the newly provided aiming reference motions, which also involve a new goal-directed task that is never seen by the meta policies. In Fig. 7, we visualize the weight vector $\mathbf{w}_t$ (cf. Eq. 10) for each DoF

¹FreeMoCap Project: <https://github.com/freemocap/freemocap>

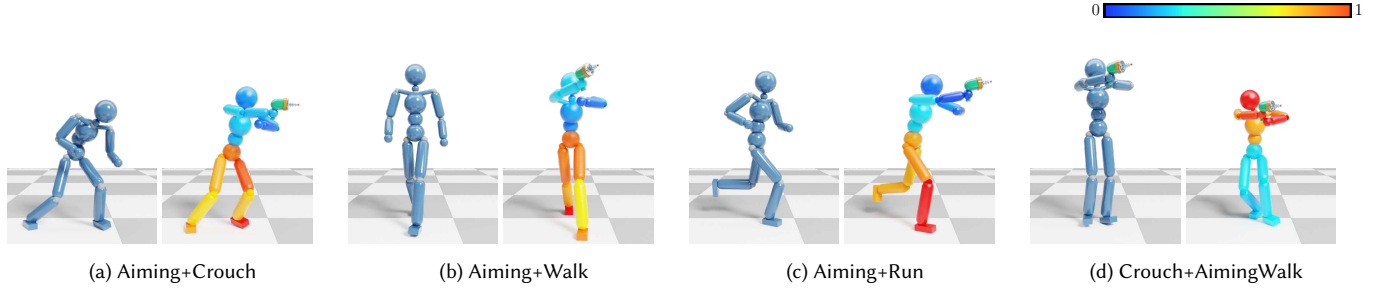


Fig. 7. Visualization of the incremental learning weight w_t (cf. Eq.10). The azure character shows the behavior from the meta policy. The colored character is controlled by the cooperative policy. The body link color identifies the weight for the associated DoF. The redder color represents higher weights, which means that the cooperative policy relies more on the meta policy to control the corresponding body parts of the character. The bluer color represents lower weights, which means that the cooperative policy mainly relies on itself to control the related body parts.

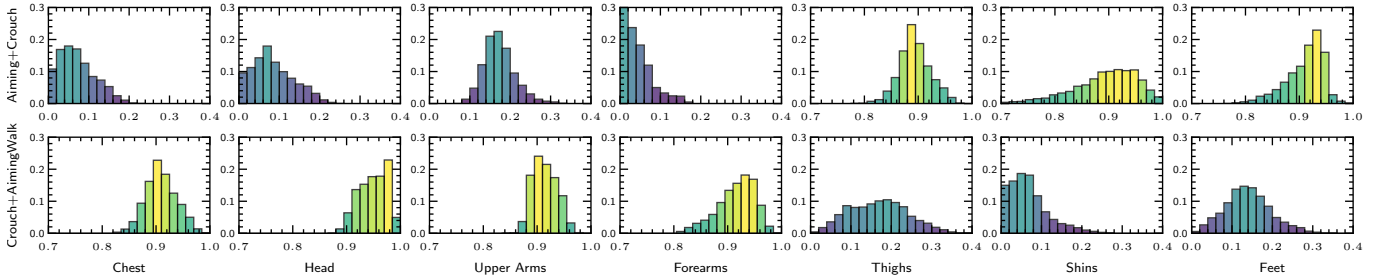


Fig. 8. Distributions of the incremental learning weights w_t for the tasks of Aiming+Crouch and Crouch+AimingWalk (cf. Fig. 7). The x-axis depicts the learned weights and the y-axis shows the corresponding distribution density, normalized by the total number of samples per body part grouping. The color saturation binds the weight range for higher distribution density, with brighter colors highlighting weights greater than 0.5. In the first task, the lower body is mainly controlled by the meta Crouch policy (high weights), while in the second task the AimingWalk meta policy mainly influences the upper body.

by coloring the associated body link. The first three examples show the results obtained when we add the aiming motions to the meta policies of locomotion. The fourth example shows the corresponding result of adding the crouch motion to the meta policy of aiming and walking. As opposed to the previous meta policies, this meta policy has four objectives: two imitation objectives for the upper (aiming) and lower (walking) body respectively, one *Target Location* task and one *Aiming* task.

As shown in the figure, in the three Aiming+Locomotion tasks where the meta policies are pre-trained for locomotion, the cooperative policies rely more on the meta policy for lower-body actions and control the upper-body parts for aiming primarily by themselves. In contrast, in Crouch+AimingWalk, we want the cooperative policy to replace the walking motions from the meta policy with crouching while keeping the upper-body motion of aiming. Here, as can be seen in the fourth case of the figure, the cooperative policy exploits the meta policy to perform aiming actions but performs crouching mainly on its own. In Fig. 8, we also plot the distribution of weights based on the collection of 5,000 consecutive frames from the Aiming+Crouch and Crouch+AimingWalk tasks. The statistical results are consistent with the above studied cases.

As an additional experiment, in Fig. 9, we show that control policies trained with our approach can support the interactive control scheme proposed by Xu and Karamouzas [2021]. In this experiment, we let the character perform a variety of locomotion styles

by switching the three trained Aiming+Locomotion policies interactively in response to external control signal provided by the user, and navigate to and aim at the target directions specified by the user dynamically.

6.6 Ablation Studies

We refer to the previous literature of ICCGAN [Xu and Karamouzas 2021] for ablation studies with respect to each component in the employed GAN-like structure for motion imitation, and to [Peng et al. 2021; Xu and Karamouzas 2021] for related analyses on the robustness of control policies trained using GAN-like structures combined with reinforcement learning. Here, we focus on the studies of the proposed multi-objective learning framework and incremental learning scheme.

In Fig. 10, we compare the performance of our proposed multi-objective (MO) learning framework to two baselines using three composite motion learning tasks from Section 4.1. The first baseline leverages our MO learning framework but does not make use of *PopArt* to normalize the value targets of each critic (w/o PopArt). The second baseline simply adds the rewards from the two discriminators together and models the composite motion learning task as a typical reinforcement learning problem (w/o MO). Both baselines are trained with our motion decoupling scheme described in Section 4.1 and simultaneously leverage two discriminators, one for the upper-body motion and one for the lower body. As can be seen from

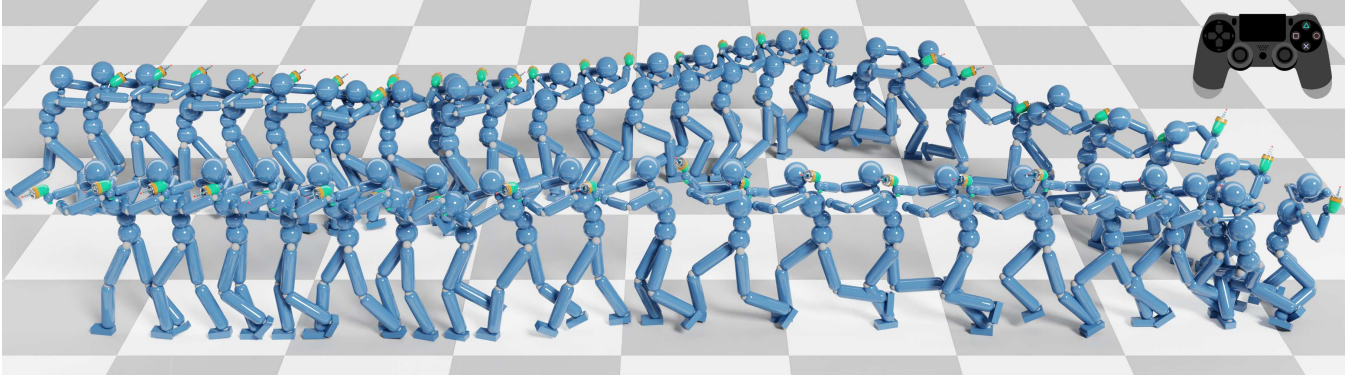


Fig. 9. Interactive control of switching between walking, crouching and running for location targeting while aiming.

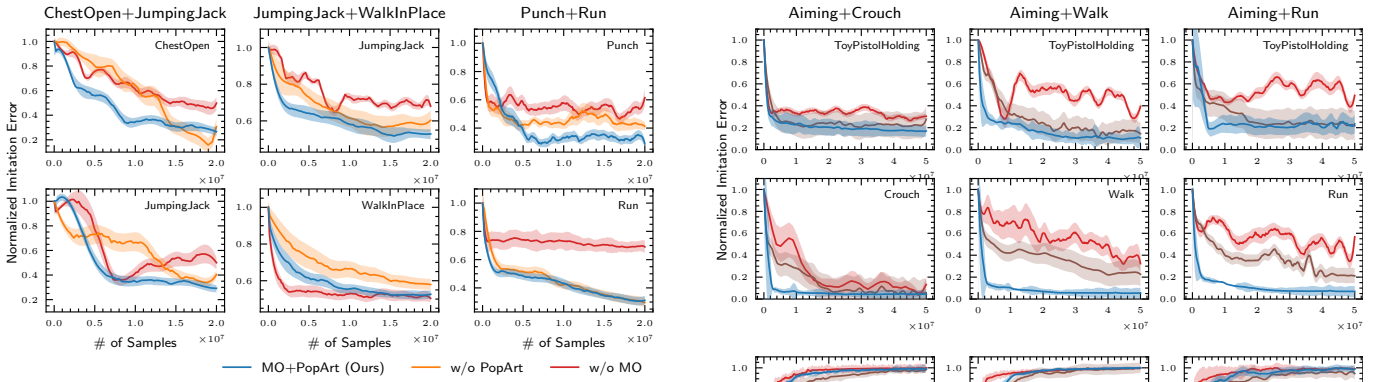


Fig. 10. Learning performance on tasks of composite motion learning from two single-clip reference motions, which are illustrated in Fig. 4. "MO" stands for the proposed multi-objective learning framework detailed in Section 4.3. Colored regions denote mean values $\pm$ a standard deviation based on 10 trials.

the figure, it is hard for "w/o MO" to balance the learning of the two reference motions. For example, in the ChestOpen+JumpingJack task, as the upper-body (ChestOpen) imitation error goes down, the lower-body (JumpingJack) error increases; in the Punch+Run task, the policy almost gives up on learning how to run, focusing on punching without too much success. In contrast, when leveraging our MO framework either with or without *PopArt*, the imitation errors of the upper and lower body show similar and stable trends, keep decreasing as the training goes on. Additionally, the introduction of *PopArt* typically facilitates better training, allowing for faster convergence speed, lower imitation error, and more robust training achieving similar performance across different trials.

Figure 11 shows the performance of our MO approach with and without exploiting the proposed incremental learning scheme. We also provide comparisons with the "w/o MO" baseline. The tested tasks have four objectives, as described in Section 6.5: two imitation objectives for the upper and lower body respectively, one *Target Location* task for the locomotion and one *Aiming* task. In the cases

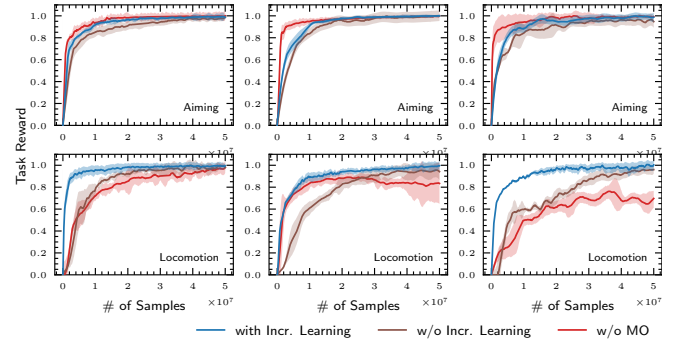


Fig. 11. Learning performance on three composite tasks where each task combines learning from two partial motions while accomplishing two goal objectives. Multi-objective learning in an incremental manner leads to sample-efficient training allowing for high-fidelity composite motion synthesis with goal-directed control. Colored regions denote mean values $\pm$ one standard deviation based on 10 trials.

using incremental learning, we employed a pre-trained, locomotion policy as the meta one. Consistent with the previous ablation study, we can see that the "w/o MO" baseline struggles to balance the different objective terms. Here, the character quickly achieves a high reward for the goal-directed *Aiming* task (3rd row) but fails to complete other objectives, and in particular to account for the motion style provided by the imitation reward terms. For example, the controlled character holds the toy pistol in an unnatural

way compared to the demonstrations in the provided reference motions as indicated by the high imitation error (1st row). While such issues are successfully resolved by our proposed MO framework, learning in a non-incremental way leads to sample inefficient training as compared to learning by leveraging a meta policy. Besides slow speed of convergence, non-incremental training can be time consuming for challenging multi-objective tasks. For example, in the Aiming+Run task, while the case with incremental learning only needs 1.5 hours to finish the training by using about 20 million samples, the non-incremental cases need about 20 more hours for training and will consume about 300 million more samples to achieve a similar performance.

7 LIMITATIONS AND FUTURE WORK

We present a technique for training composite-motion controllers using a multi-objective learning framework that is capable of combining multiple reference examples and task goals to control a physically-simulated character. We demonstrate that our approach can generalize to a large number of examples based on the availability of reference data. Likewise, we show its ability to accomplish simultaneous goal-driven tasks such as aiming at specific targets and moving to a target location with different locomotion styles. Furthermore, we can interactively control such character's actions, pushing the boundary of what is capable for physics-based characters to date.

Of course, there is still more to explore in this space. Our system is currently not well-equipped to handle behaviors which include multiple phases, as the imitation is not phase-locked in any fashion and our discriminators do not distinguish between different stages of an activity. Exploring the potential to add a state machine with state transitions could aid in this capacity [Starke et al. 2019]. Another shortcoming of the approach presently is that we do not account for variation across the humans that recorded the motion clips. This implies that we are introducing bias in the imitation process that may degrade the final quality of the animation. As is, the system is able to make adjustments automatically as needed based on the physical characteristics of the behavior but it cannot distinguish errors that are more stylistic.

In its current form, our system can not create new composite activities without performing additional training. A possible direction for future work is aimed at sidestepping this limitation to directly combine preexisting policies and greatly improve the scalability of trained controllers. That is, to train two (or more) policies independently and combine them at runtime to create a composite motion. Finally, in human motion, composite behaviors go beyond an anticipated split, e.g. the lower and upper body, which is one of the modest underlying assumptions in our current implementation. Instead, humans may enlist body parts and release them fluidly. For example, a well-trained martial artist changes the use of appendages quickly in fighting sequences. We wish to explore this direction in future investigations and believe that our proposed multi-objective learning framework can provide the foundation for such future endeavors.

Although we employed an upper and lower body split in most of our experiments, there is nothing tied to this body decoupling

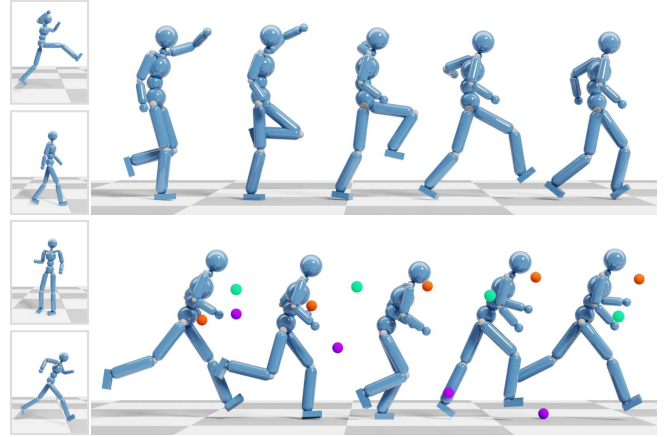


Fig. 12. Failure case study. Top: The character's body is bisected into a left and right group, imitating walking and jumping respectively. Bottom: Juggle while running.

scheme except that it is a practical general choice for deploying the limbs of the whole body. Currently, as long as the subtasks are compatible, our system is capable of combining motions along other body splits. For instance, in the *Juggling+TargetLocation* example discussed in Section 6.4, the trained policy controls the arms for juggling and the rest of the body for walking. Our approach may fail if, for example, the lower limbs are separated due to the requirements of physical balance. As an example, in Fig. 12, we show a failure case where the body is bisected into a left/right split and asked to imitate walking and jumping motions respectively. Such a composite motion is not well-defined, even for humans. We can see that though not falling down, the simulated character cannot imitate the two motions accurately, and instead performs an in-between motion where the character neither jumps up nor walks in an expected fashion.

In Fig. 12, we also show another failure case where running reference motions with an average speed of around $3.5m/s$ are provided for the *Juggling+TargetLocation* task. With the difficulty of juggling while moving at this higher speed, this example is significantly more challenging than the one shown in Fig. 5d. Even though we are able to synthesize the composite motions, the simulated character cannot juggle the balls successfully under these conditions. Currently, our approach cannot identify if a composite motion is compatible on its own, and instead, it relies on a human to combine behaviors with some domain knowledge about the affinity of the mixing and the feasibility of associated goal-directed tasks. Automating this would be a great direction for future work.

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²<https://www.rokoko.com>

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