

Supra-resonant wingbeats in insects

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Abstract

Powering small-scale flapping flight is challenging, yet insects sustain exceptionally fast wingbeats with ease. Since insects act as tiny biomechanical resonators, tuning their wingbeat frequency to the resonant frequency of their springy thorax and wings could make them more efficient fliers. But operating at resonance poses control problems and potentially constrains wingbeat frequencies within and across species. Resonance may be particularly limiting for the many orders of insects that power flight with specialized muscles that activate in response to mechanical stretch. Here, we test whether insects operate at their resonant frequency. First, we extensively characterize bumblebees and find that they surprisingly flap well above their resonant frequency via interactions between stretch-activation and mechanical resonance. Modeling and robophysical experiments then show that resonance is actually a lower bound for rapid wingbeats in most insects because muscles only pull, not push. Supra-resonance emerges as a general principle of high-frequency flight across five orders of insects from moths to flies.

Among the four evolutionary lineages of flying organisms, insects uniquely produce rapid, powerful wingbeats at the centimeter scale from the low whirl of a giant silkmoth to the near-kHz hum of a biting midge (Fig. 1a) (1, 2). Wingbeat frequency is a critical determinant of aerodynamic power production (3–6), but is only weakly predicted by body size at the species level. For example, bumblebees flap at 180 Hz (7), but bee-mimicking hawkmoths, *Hemaris diffinis* (8), flap at 60 Hz despite being nearly the same size. Resonance is a popular explanation for this many-to-one mapping between body size and wingbeat frequency. Most insects fly by deforming an elastic exoskeleton with ultrafast flight muscles (9–15). Flapping at their resonant

25 frequency theoretically allows for the costs of rapid wing acceleration to be offset by elastic
26 energy storage, but at the expense of frequency modulation capacity. While wing-clipping ex-
27 periments (3, 16) and models (9, 17) point to insects being resonant, it is an unresolved question
28 whether insects flap at resonance. Slow-flapping (<100 Hz), synchronous insects like moths
29 may not be overly restricted by resonance because their wingbeats are paced by time-periodic
30 neural signals, which can match or exceed the resonant frequency. However, resonance may be
31 particularly constraining for fast-flapping (typically >100 Hz) asynchronous insects that gen-
32 erate self-excited wingbeats with specialized muscles that activate in response to mechanical
33 stretch (18–20) (Fig. 1b). By combining new measurements of insect muscle and exoskeleton
34 with models of ‘spring-wing’ dynamics, we investigate whether insects flap at resonance across
35 taxa and flight mode, and if not, what timescales set their wingbeat frequencies.

36 **Bumblebees flap above their resonance frequency**

37 First, we focus our attention on the bumblebee, whose flight kinematics, morphology, and be-
38 havior have been characterized in detail. Using materials testing in the context of a ‘spring-
39 wing’ model of an insect’s elastic thorax, and the inertial and aerodynamic forces acting on the
40 wing (8, 10, 11, 20), we demonstrate that asynchronous bumblebees flap above their resonant
41 frequency (Fig. 1c-d). We estimated the resonance frequency of *Bombus impatiens*, by com-
42 bining measurements of bulk thoracic stiffness with estimates of wing inertia and wing-hinge
43 transmission ratio. The bumblebee’s undamped resonant frequency (f_n) is a function of the
44 measured thorax stiffness (k), the wing hinge transmission ratio (T , the ratio of angular wing
45 displacement to muscle displacement with units rad m^{-1}), and the inertia of the wings and
46 added mass of air around the wing (I , see SI for extended description of all parameters),

$$f_n = \frac{1}{2\pi} \sqrt{\frac{k}{T^2 I}} \quad (1)$$

47 The elastic thorax and main flight power muscles (Fig. 1c) are in a parallel configuration that
48 drive indirect actuation of the wing. We ignore series elasticity of the wing hinge, which is likely
49 small and would widen but not alter the location of the undamped resonant frequency peak (13)
50 (see Supplementary Discussion). We measured the isolated thorax stiffness of bumblebees using
51 vibrational testing and found it to be 4.1 kN/m (see SI section 2.1) Setting all parameters from
52 empirical measurements, we arrive at an undamped resonant frequency of $f_n = 94.9$ Hz, which
53 is 44% lower than average wingbeat frequencies (180 Hz) (7) (Fig. 1d). Our measured thorax
54 elasticity does not take into account active stiffness contributed by the flight muscles. Since the
55 upstroke and downstroke muscles are antagonistic, when one contracts the other is stretched
56 under near-tetanic activation. We estimate, conservatively, that active muscle stiffness is equal
57 to the summed stiffness of both pairs of flight muscles, increasing the total thoracic stiffness to
58 6.4 kN/m and the resonant frequency to 102 Hz (21) when considering stiffness contributions
59 from exoskeleton and active muscle. Propagating error in the three parameters k , T , and I , we
60 find that supra-resonant bumblebee wingbeats are robust to reasonable measurement error in

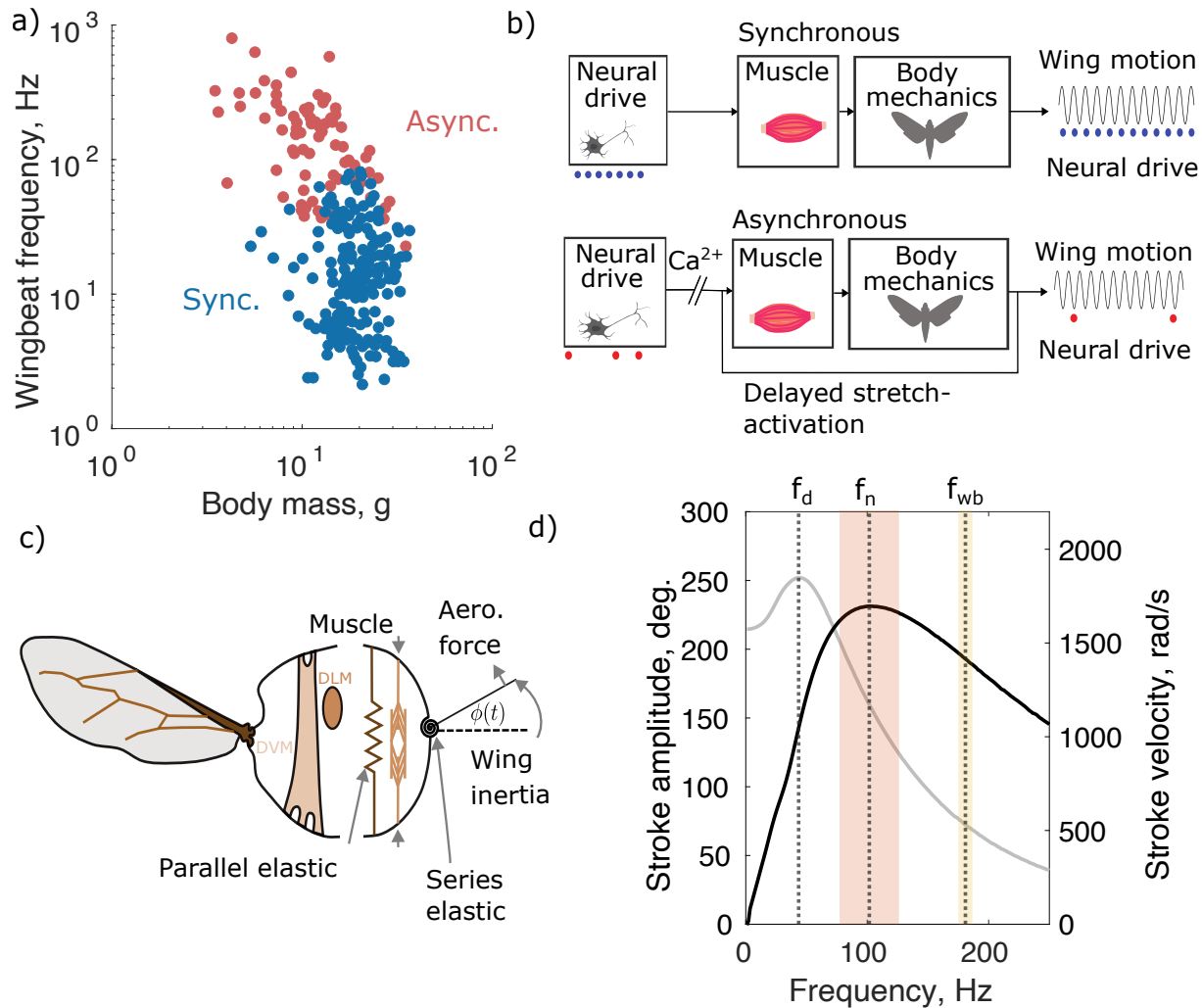


Figure 1: a). The division between synchronous and asynchronous insects helps explain the wide variation in insect wingbeat frequency. Data replotted from (1, 2). b) Insects with synchronous muscle produce wingbeats at a frequency set by the neural drive to the flight muscles (blue dots). Insects with asynchronous muscle produce faster wingbeats that are decoupled in frequency from the underlying neural drive (red dots). c) Schematic of a bumblebee showing flight muscle anatomy on the left, and a biomechanical model on the right. d) Simulated displacement resonance curve (grey) and velocity resonance curve (black) of a bumblebee, assuming a sinusoidal forcing. Displacement resonant frequency (f_d) and velocity resonant frequency (f_n) are both below wingbeat frequency (f_{wb}). Orange and yellow bars show 95% confidence intervals of the mean for velocity resonance and wingbeat frequencies respectively.

61 thorax or wing properties, resulting in resonant frequencies ranging from 76 to 124 Hz (Fig.
62 1d).

63 We can also reverse the analysis to ask what thorax stiffness is necessary for wingbeats to
64 be at the resonance frequency. This would require a stiffness of 21 kN/m, which is beyond
65 the largest stiffness that we measured and far exceeds any comparable stiffness measurements
66 (≈ 2 kN/m) (15, 22). Incorporating the effects of aerodynamic force production or internal
67 thoracic damping into the resonance calculation can only further depress the estimated reso-
68 nant frequency below wingbeat frequency (i.e. damped displacement resonance) (8, 11). More
69 complex resonant models could create nonlinear resonance at higher harmonics, but we are
70 interested here in the fundamental resonance from the exchange of inertial and elastic energy
71 during the wingstroke. Thus, in the absence of evidence that substantial elasticity is missing
72 from our measurements, we conclude that bumblebees are supra-resonant.

73 **Stretch-activated dynamics of asynchronous muscle**

74 The discrepancy between bumblebee resonant and wingbeat frequencies motivated us to con-
75 sider how the physiological process of stretch-activation in muscle can enable supra-resonant
76 flight in asynchronous insects. Asynchronous muscle generates active force in response to a
77 rapid stretch. This mechanical stretch-activation was measured previously by stretch-hold ex-
78 periments (18–20, 23) (Fig. 2a-b). The force response of isolated insect flight muscle to a step
79 length change under tetanic activation has a shape that is composed of four phases (24) (Fig.
80 2c). The first two phases are fast, associated with the viscoelastic response of the muscle tissue.
81 The slower third and fourth phases comprise the delayed stretch activation (dSA) force, which
82 can be described with a single characteristic timescale, t_o (the time taken to achieve peak dSA
83 force after the end of stretch (20)), and a constant, κ , the ratio of the rates of force decay (r_4)
84 to force rise (r_3) (Fig. 2d). An analogous process, delayed shortening de-activation (dSD) oc-
85 curs following rapid shortening (Fig. 2e, g) and is the inverse of dSA. We hypothesized that an
86 asynchronous insect can flap above resonance if its t_o is sufficiently fast with respect to its nat-
87 ural period, the reciprocal of natural frequency ($T_n = f_n^{-1}$). In this case the resulting wingbeat
88 frequency is set not just by the resonant mechanics, but by a combination of muscular (t_o) and
89 mechanical (T_n) timescales.

90 To measure a bumblebee's dSA timescale under typical flight conditions, we had to conduct
91 new stretch-hold experiments on isolated *B. impatiens* DLMs at the a realistic flight tempera-
92 ture of 40° C (25, 26) (Fig. 2a-e). While some measurements of bumblebee stretch-activation
93 exist, we are the first to make them in intact whole muscle at a realistic body temperature. We
94 measured the bumblebee stretch-activation timescale, t_o , to be 4.4 ± 1.0 ms, nearly the duration
95 of an entire wingbeat, which did not change depending on muscle length at the onset of stretch
96 (Fig. 2f-h). This value of t_o is somewhat faster than the only comparable characterizations in
97 bumblebees at lower temperatures (≈ 5 ms) (21, 27), which may be because dSA rate kinetics
98 are known to speed up with temperature (23). It is also substantially slower than the ≈ 2.5
99 ms necessary for dSA alone to drive 180 Hz wingbeats in response to stretch (the duration of

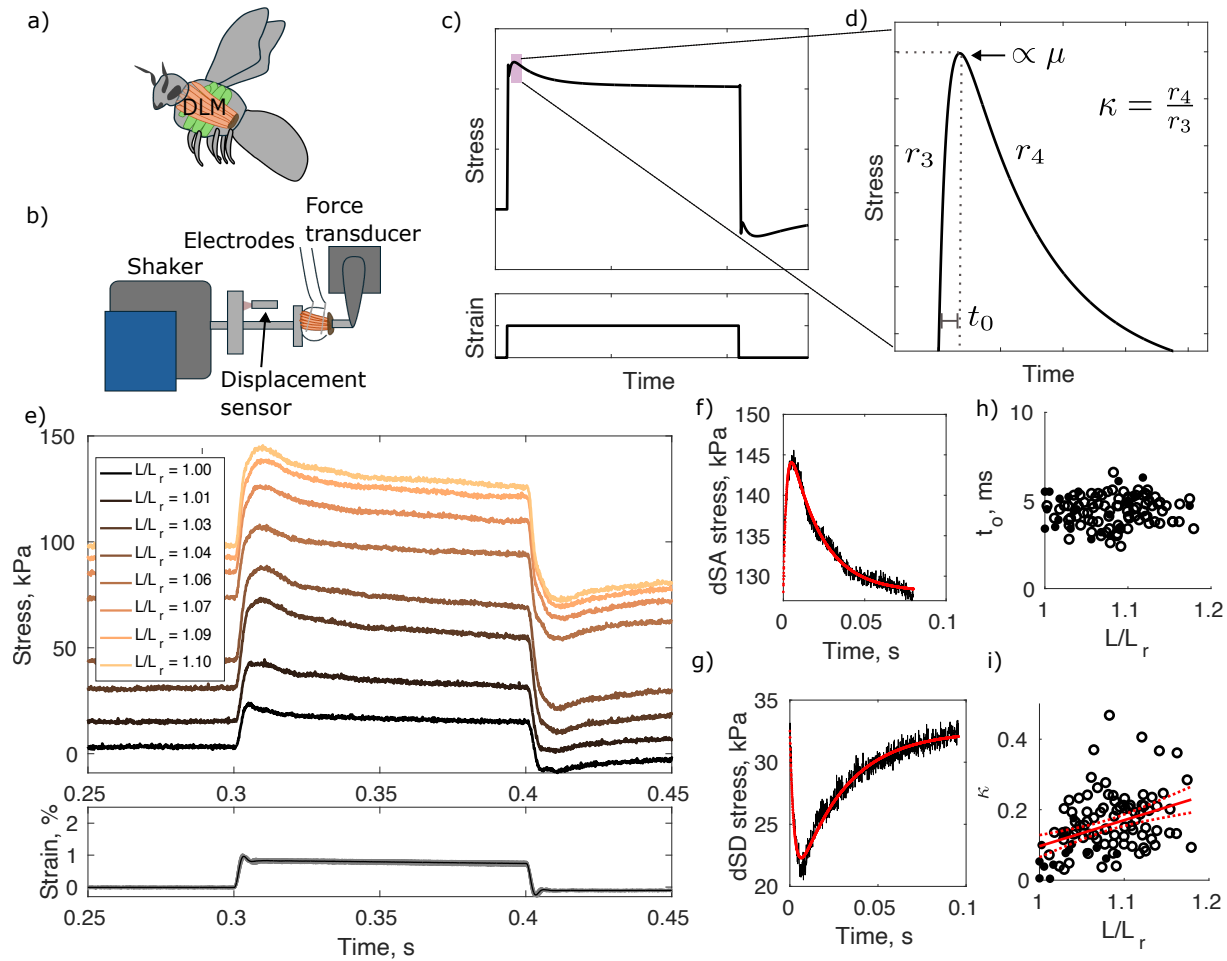


Figure 2: a). Location of the DLM (downstroke) muscles in a bumblebee. b). Schematic of muscle physiology apparatus used to apply step strains along the line-of-action of the DLM under tetanic stimulation. c). Zoomed out cartoon of a single stretch-hold-release-hold trial with purple bar blown up in panel d) Phases three and four of the dSA response, with corresponding rates of force rise (r_3) and force decay (r_4) notated. t_0 is the time until peak dSA force is reached, and κ is the ratio of r_4 to r_3 . μ is proportional to the height of the dSA response. e) dSA characterization experiments from a single individual. A 1% stretch was applied under tetanic stimulation at multiple starting lengths. f) dSA phases 3 and 4 from a single trial from a single individual. Red line denotes a double-exponential fit. g). dSD phases 3 and 4 from a single trial from a single individual. h) t_0 computed across all individuals at all starting lengths ($n=10$ individuals). i) κ computed across all individuals at all starting lengths. Closed and open circles correspond to dSA and dSD measurements respectively. Red line shows a linear regression with 95% confidence intervals.

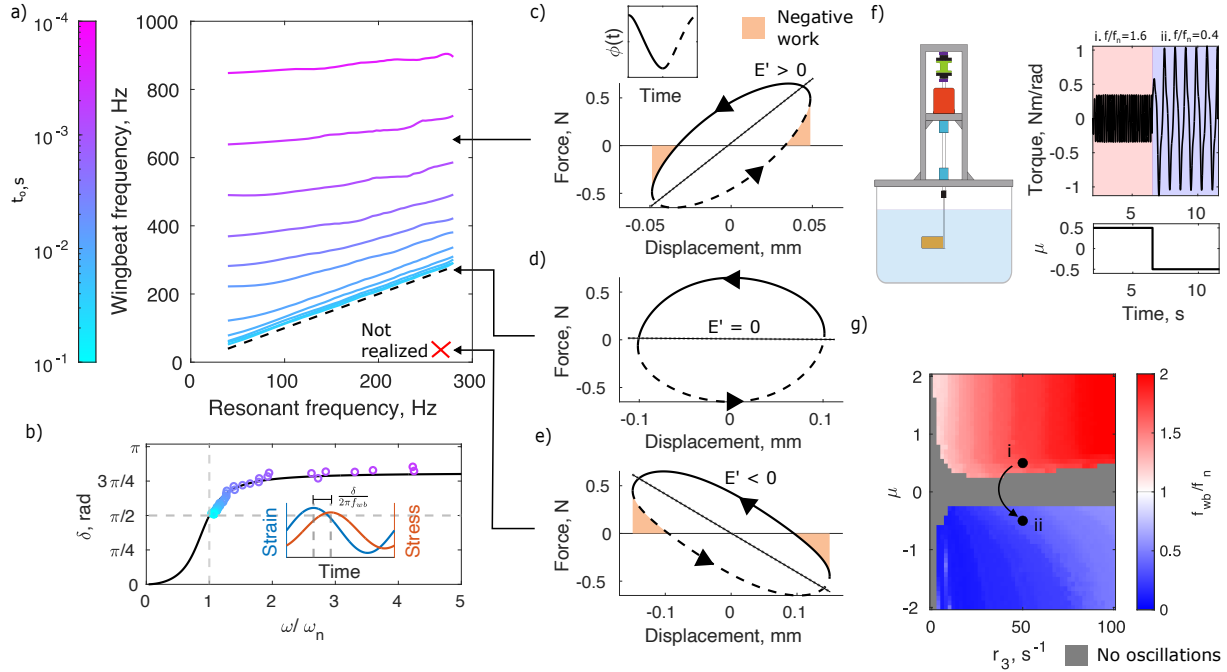


Figure 3: a). Parameter space of emergent wingbeats over a wide set of t_o and T_n that encompasses the physiological range for most insects. For any fixed value of t_o , there exists a linear relationship between resonant and emergent frequencies. At large t_o , this linear relationship collapses onto the equivalency line. As t_o decreases, wingbeat frequencies become supra-resonant, and increasingly independent of resonant frequency. Every point in simulation has been normalized such that steady-state peak-to-peak stroke amplitudes match bumblebee *in-vivo* conditions. b). Phase lag between stress and strain as a function of normalized frequency. Black line shows phase for a synchronous insect and colored dots show predictions from the asynchronous model for varying t_o , with the same color scale as in panel a). c-e). Work loop in force-displacement space for operation above (c), at (d), and below (e) resonance. Dotted lines correspond to upstroke and solid lines correspond to downstroke. At resonance, no negative work is required of the flight muscle. Above and below resonance, negative work is done in the second half and first half of each half-stroke, respectively. f). Robophysical experiment where the sign of the dSA force is changed from positive to negative, causing oscillations to transition from supra-resonant to sub-resonant. g). Space of asynchronous wingbeats in a robophysical flapper, demonstrating that transitions between sub- and supra-resonance occur only when the dSA force sign changes (i.e. across the $\mu = 0$ boundary). Parameter values corresponding to the transition in f). are shown by the arrow from i. to ii.

100 downstroke after being stretched during upstroke). The ratio of rates, κ , was weakly correlated
101 with resting muscle length and on average equal to 0.17 ± 0.03 (Fig. 2i). Thus, the muscular
102 stretch response is faster than the timescale of mechanical resonance.

103 **Asynchronous insects flap at or above resonance**

104 To test our hypothesis that a sufficiently fast stretch-activation timescale (i.e. t_o) can enable
105 supra-resonant wingbeats, we developed a biophysical model of asynchronous muscle-driven
106 resonant flight. We drive a 'spring-wing' model of the insect's thorax and wings (8, 10, 11) with
107 a simplified description of stretch-activated muscle, rooted in our stretch-hold experiments in
108 bumblebees (20, 30). Thus, we capture the essential dynamics of both stretch-activation and
109 resonant mechanics.

110 The model consists of two coupled, second-order differential equations. The oscillatory
111 dynamics of the wingstroke angle, $\phi(t)$ are parameterized by k_l , T , I , and an aerodynamic
112 damping coefficient Γ (Eq. 2). The stretch feedback-driven muscle forcing (Eq. 3) is parame-
113 terized by t_o and κ (see Supplementary Methods section 1.6.2). There is one free parameter, μ ,
114 which can be set by matching the amplitude of the output wingbeats to free-flight bumblebee
115 wingstroke amplitude. μ represents the strength of the dSA forcing and makes the dSA force
116 *in-vivo* proportional to the height of the two-phase response of the muscle to rapid stretch (Fig.
117 2c-d). Because the forcing is entirely state dependent and not prescribed exogenously (e.g. by
118 the nervous system) the system oscillates at an emergent frequency (See Supplementary Results
119 2.2).

$$I\ddot{\phi} + \Gamma|\dot{\phi}|\dot{\phi} + \frac{k_l}{T^2}\phi = \frac{\mu}{T}f_{dSA} \quad (2)$$

$$\ddot{f}_{dSA} + \alpha_2(t_o, \kappa)\dot{f}_{dSA} + \alpha_3(t_o, \kappa)f_{dSA} = -\alpha_3(t_o, \kappa)\dot{\phi} \quad (3)$$

121 Simulating Eqs. 2-3 and evaluating the resulting $\phi(t)$ wing stroke trajectories over a wide
122 range of muscular and mechanical timescales (t_o and T_n) reveal that resonance is a lower bound
123 on emergent wingbeat frequency (Fig. 3a). There exists a large region of parameter space in
124 which asynchronous insects can flap significantly above resonance. Consistent with observa-
125 tions from modifying the wing inertia of insects (3, 16, 31), the resonance frequency of the insect
126 increases as the emergent flapping frequency goes up, regardless of t_o (Fig. 3a). However, this
127 does not mean that the flapping frequency is at resonance. Fast stretch-activation, low t_o , results
128 in supra-resonant wingbeats, while slower t_o result in wingbeat frequencies that collapse onto
129 the wingbeat-resonant frequency equivalency line. Thus, stretch-activated resonant systems are
130 not constrained to resonance, and can oscillate supra-resonantly with the right combination of t_o
131 and T_n . Using our measured flight muscle stretch-activation timescale, we estimate a bumble-
132 bee wingbeat frequency which exceeds resonance by 33%, in agreement with our experimental
133 characterization of supra-resonance using thorax materials testing.

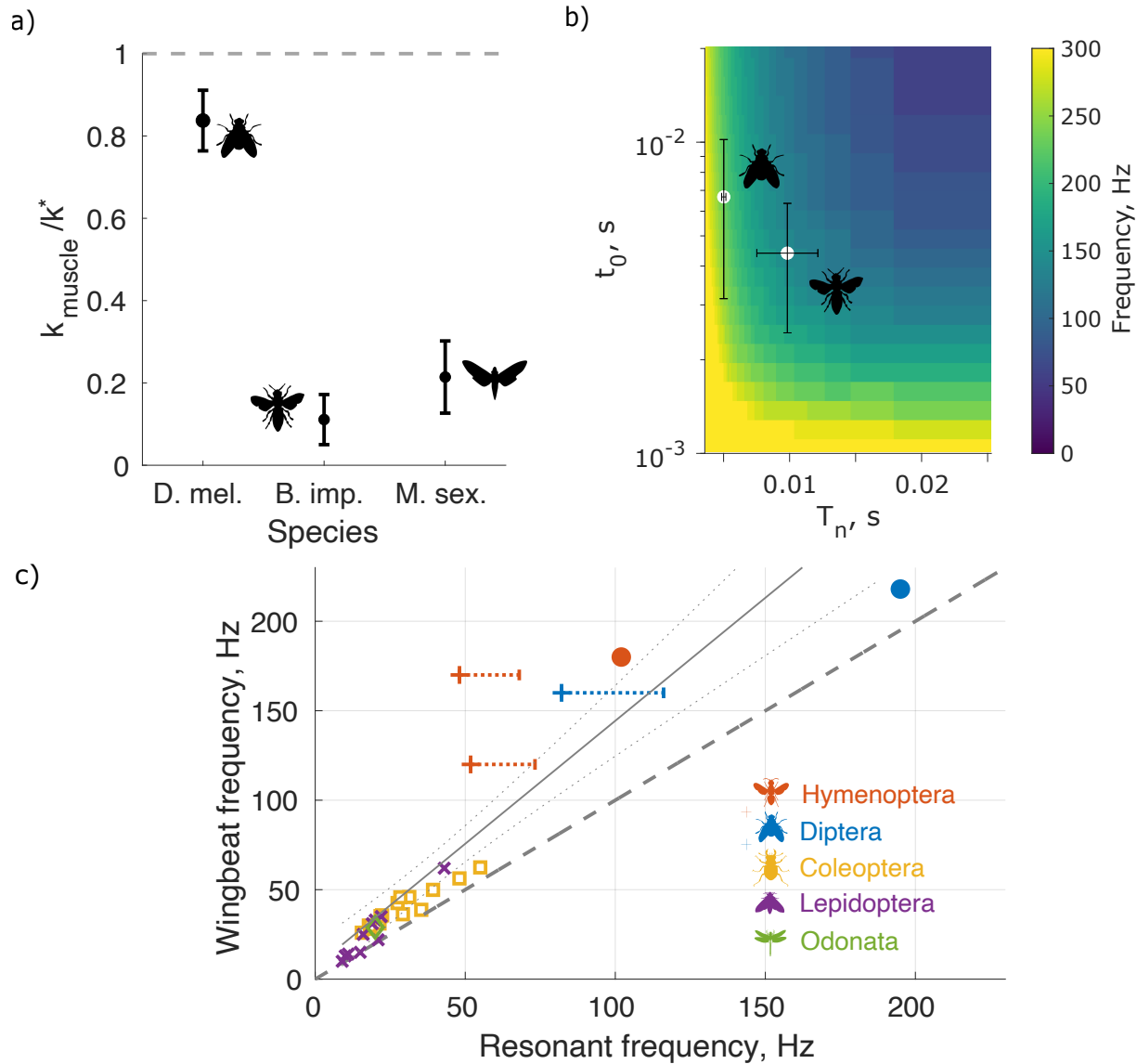


Figure 4: a). Fraction of perfectly resonant stiffness contributed by muscle alone for three insect species: fruitfly, bumblebee, and hawkmoth (21, 28, 29). b). Emergent asynchronous frequency space as a function of muscle time constant (t_o) and natural period (T_n). Both fruitfly and bumblebee achieve similar wingbeat frequencies with different combinations of t_o and T_n . c). Supra-resonant wingbeats across insects, compiling estimates from five insect orders. Markers - “x” (8), “+” (22), square (18), and diamond (17) - represent data from different studies. Dots show data from the current study. Dotted line shows equivalence of wingbeat and resonant frequencies. Orange bars show resonant frequency ranges assuming exoskeleton stiffness underestimates total thorax stiffness (exoskeleton + muscle) by up to a factor of two. Solid grey line shows a linear regression through all points, with dotted grey 95% CI.

134 **Muscle's asymmetry enforces supra-resonance**

135 Why are asynchronous flappers apparently only able to flap at or above resonance? This con-
136 straint emerges from muscle producing a positive force in response to stretch (i.e. always
137 'pulling' and never 'pushing'), such that increases in muscle stress will always lag positive
138 muscle strain (muscle extension) (Fig. 3b, inset). This phase lag is proportional to the stretch-
139 activation timescale (t_o), but can never be below a quarter cycle ($\pi/2$ radians) because increas-
140 ing t_o results in a frequency that asymptotes to resonance. As t_o increases, δ approaches $\pi/2$;
141 as t_o decreases, δ approaches a maximum. Thus, stretch-activated wingbeats can never be sub-
142 resonant, which would require $\delta < \pi/2$ (Fig. 3b, colored points). This contrasts with a syn-
143 chronous insect that has neurally activated muscle, which can theoretically achieve $0 < \delta < \pi$
144 by modulating the timing of neural signals to the flight muscles (Fig. 3b, black line). This
145 would be equivalent to activating the muscle such that it produces significant force in the half
146 cycle prior to lengthening (32–36).

147 The necessity of asynchronous insects to be supra-resonant can be visualized in the work-
148 loop representation of muscle function, which visualizes muscle work output as the area en-
149 closed in active force vs. displacement space (37–40). In this space, the effective storage mod-
150 ulus, E' , of the workloop represents the elastic component of the total muscle force necessary
151 to supply all energy requirements for flight (see Supplementary Results 2.3). $E' = 0$ represents
152 perfect exchange between wing kinetic energy and thoracic elastic energy (i.e. $f_{wb} = f_n$) (Fig.
153 3d). $E' \neq 0$ represents non-resonant conditions where the thorax is either too stiff or not stiff
154 enough with respect to the wingbeat frequency (Fig. 3c,e). The hysteresis of the loop is propor-
155 tional to the phase lag δ between force and displacement. The resulting area within the loop is
156 the effective loss modulus, E'' , representing the mechanical energy generated by the muscle.

157 At steady-state, the muscle forcing $f_{dSA}(t)$ will always follow a counter-clockwise ellipse
158 (negative loss modulus or positive net work) with a nonnegative storage modulus. This enforces
159 a phase lag, δ , of $\pi/2 < \delta < \pi$ in stress with respect to strain. If the insect is supra-resonant, its
160 muscle will produce negative work, dissipating energy, during the second half of each halfstroke
161 while the wing is decelerating (Fig. 3c, shaded area). Muscle assisting in the slowing of the
162 wing on each half cycle is only possible in a supra-resonant system, since the thoracic spring
163 will not be stiff enough to absorb all of the wing's kinetic energy before it reaches its extremal
164 positions. At resonance, the storage modulus of the muscle is identically zero and no negative
165 work is required at any point in the wingbeat (Fig. 3d). Below resonance, an overly stiff
166 thoracic spring would cause rapid wing acceleration that is counteracted by muscle dissipating
167 energy in the acceleration phase of each half-stroke (Fig. 3e, shaded area). Thus, a sub-resonant
168 asynchronous insect would have to generate negative work directly following stretch, which is
169 incompatible with the polarity of muscular dSA force response. Muscles only pull, they do not
170 push.

171 **Supra- and sub-resonance realized through a robophysical model**

172 While the physiological limitations of biological muscle limit oscillations to at or above reso-
173 nance, engineered actuators are not necessarily limited to this regime. In contrast, they can push
174 and pull. Following from the sub-resonant work loop (Fig. 3e), we predict that an engineered
175 system with muscle dSA-like actuators that pushed instead of pulled should be able to realize
176 sub-resonant asynchronous wingbeats. We demonstrate asynchronous sub-resonant oscillations
177 in a dynamically scaled robophysical flapping wing by controlling a brushless DC motor with a
178 velocity feedback-driven forcing analogous to dSA (Eqs. 2-3) (30). This system is also unable
179 to oscillate below its resonant frequency, when controlled with a muscle-like dSA forcing (Fig.
180 3f, i.). However, by changing the sign of the dSA force such that a negative (i.e. pushing)
181 force follows stretch, stable sub-resonant oscillations emerge that are bounded above by the
182 resonance frequency (Fig. 3f, ii.). By systematically changing μ in the model that controls our
183 roboflapper motor, we see the boundary of switching between supra- and sub-resonant behavior
184 is at $\mu = 0$, where the sign of the dSA force flips (Fig. 3g). Thus, we demonstrate that the
185 physiology and arrangement of antagonistic stretch-activated muscles in asynchronous insect
186 thoraces constrain them to supra-resonant wingbeats.

187 Sub-resonance is realizable in some biological muscle-driven systems as well. For instance,
188 unlike asynchronous insects, synchronous insects can, in theory, be sub-resonant. They could
189 neurally activate their muscles at timings that would enable negative work production in the first
190 part of each half-stroke. Practically, this would require the downstroke muscle (or a combination
191 of muscles) to produce significant force during the beginning of upstroke, and vice versa. This
192 would require either multiple downstroke or upstroke muscles or a large degree of coactivation
193 which would likely reduce the production of useful work from the muscles. While we do not see
194 such activation patterns in insects, they are common in terrestrial locomotion especially where
195 multiple muscles operate in synergy at a joint or in a limb (33–36, 41). Indeed, some terrestrial
196 animals like kangaroos are sub-resonant (42), but do not have to contend with the asynchronous
197 muscle dynamics present in bumblebees or our robophysical flapper.

198 Supra- and sub-resonant systems also exhibit a key difference in how they modulate power
199 output outside of the steady state. In a supra-resonant system, acceleration is muscle-driven
200 and spring-assisted, with negative muscle work (dissipation) coinciding with the deceleration
201 phase of the wingstroke (Fig. 3c). The muscle assists the spring. This enables supra-resonant
202 systems to inject additional accelerative power via transient increases in agonist muscle force.
203 However, in sub-resonant systems, acceleration is driven by the spring and braked by the agonist
204 muscle (Fig. 3e). Positive power production is limited by the spring's capacity to return elastic
205 energy and additional agonist muscle force would only decelerate the wing faster. Thus, an
206 important benefit of supra-resonance for asynchronous insects may be to maintain the capacity
207 to transiently boost wing acceleration via positive muscle power production in the first part of
208 each half-stroke (Fig. 3c).

209 Two timescales pace asynchronous wingbeats

210 Having validated our model in bumblebees, we used recent characterizations of *Drosophila*
211 *melanogaster* muscle stiffness and flight mechanics to show that this widely-studied fruitfly is
212 also supra-resonant, although to a lesser degree than *B. impatiens*. *D. melanogaster* has more
213 than three orders of magnitude less mass than a bumblebee, but paradoxically has a wingbeat
214 frequency of around 200 Hz, which is very close to that of *B. impatiens* (43). Measurements
215 of fruitfly delayed stretch activation timescale, t_o , range from 5-8 ms which is slower than
216 our measured t_o for bumblebees (Fig. 2h) (44). We hypothesize that fruitflies have evolved a
217 similar wingbeat frequency to bees despite being much smaller in part by having relatively slow
218 stretch-activation in comparison to their natural period. Indeed, fruitfly wing inertia is roughly
219 four orders of magnitude smaller than that of a bumblebee, which in isolation would suggest a
220 resonant frequency far greater than ≈ 100 Hz we measured in bees.

221 To test this hypothesis, we first need an estimate of the bulk stiffness of the fruitfly thorax.
222 While exoskeletal stiffness values for fruitflies have not been measured, functional stiffness
223 in the fly thorax is thought to be dominated by active muscular elasticity, rather than parallel
224 thoracic stiffness. This is due to fruitflies' combination of small wing inertia compared to bees,
225 and asynchronous muscle which has much higher resting stiffness than synchronous muscle (19,
226 21, 28, 45). We quantify whether existing estimates of muscle elasticity alone are sufficient to
227 estimate resonance frequency, by deriving a new metric describing the contribution of muscular
228 elasticity to bulk thorax stiffness: the ratio of the active muscle stiffness k_{muscle} to the stiffness
229 that would be required to drive perfectly resonant wingbeats, $k^* = (2\pi f_{wb})^2 T^2 I$ (Fig. 4a).
230 This expression depends on nonlinear interactions between morphological (wing inertia, I),
231 kinematic (wingbeat frequency, f_{wb}), and biomechanical (transmission ratio, T) parameters.
232 It is not a simple function of body size. Bumblebees and moth thoraces are dominated by
233 exoskeletal stiffness, which is in excess of muscular stiffness by at least three-fold yet their
234 free flight frequencies are still above their undamped resonance. In contrast, *Drosophila* muscle
235 does supply nearly all the elasticity needed to drive wingbeats close to resonance (Fig. 4a).

236 Armed with a stiffness estimate for *Drosophila* we can then apply the same approach we
237 took with bumblebees to test if they operate at their resonant frequency. When we estimate
238 *Drosophila* resonant and wingbeat frequencies using Eqs. 1-3, we find a predicted emergent
239 wingbeat frequency (221 Hz) that is supra-resonant at 18% in excess of resonance (187 Hz)
240 (Fig. 4b). Supra-resonance arises from a combination of a much larger transmission ratio
241 (ratio of wingbeat angle change to muscle displacement) by virtue of small body size as well
242 as slower stretch-activation (longer t_o). These frequencies are within the range of measured
243 free-flight wingbeat frequencies. While series-elastic effects in moths and bees are not large
244 enough to significantly impact our results (see Supplementary Discussion), high series-elastic
245 compliance in *Drosophila*-scale flies may widen their resonance curves to the point where they
246 can still achieve near-maximal resonant energy return while being supra-resonant (13). Thus,
247 our modeling demonstrates how dSA causes a single frequency that exceeds f_n to emerge from
248 a band of potentially equally efficient frequencies in insects with significant series compliance.

249 We find that bees and flies realize similar asynchronous wingbeat frequencies through different
250 combinations of t_o and T_n while remaining slightly (flies) to significantly (bees) supra-resonant
251 (Fig. 4b).

252 **Supra-resonance as a general principle of insect flight**

253 Our experimental and theoretical characterizations of resonance in bees and flies point to supra-
254 resonance as a general principle of insect flight, but how broadly does it apply? Collating our
255 results with the only other comparable characterizations of resonance (17, 18, 22), we show that
256 supra-resonance applies to asynchronous bees, flies, and beetles, and synchronous moths. Even
257 the dragonfly, a synchronous insect with a direct flight muscle architecture appears to operate
258 above its resonance peak. This suggests that supra-resonance is not limited to insects with indi-
259 rect flight muscles so long as there is some degree of elasticity in the muscles or wing hinge (17).
260 Thus, our results demonstrate a general pattern of supra-resonant wingbeats in insects, with all
261 insects included flapping at or above their resonant frequency. Insects generally fall on a line
262 with slope > 1 (slope = 1.32, $p < 0.001$, $r^2 = 0.77$) but an intercept statistically indistinguish-
263 able from 0. Thus across taxa, insects maintain a roughly constant ratio of wingbeat to resonant
264 frequency, with slower-flapping insects flapping extremely close to, but not below, resonance.

265 Interestingly, *Drosophila* lies closer to resonance than predicted by a line of best fit through
266 all other species (slope = 1.84, $p < 0.001$, $r^2 = 0.80$), suggestive that higher frequency insects
267 may not continue to experience a divergence between resonant and wingbeat frequencies. This
268 makes sense in the context of its larger t_o compared to that of a bumblebee (44), despite being
269 orders of magnitude less massive. In addition, smaller insects achieve roughly the same am-
270 plitude wingbeats with much smaller muscle displacements, resulting in a sharply increasing
271 transmission ratio (driving a decrease in T_n) with size. Adaptations in wing hinge musculature
272 and gearing (2, 46) may tune the transmission ratio and enable modulation of wingstroke param-
273 eters without changing wingbeat frequency. Thus, a combination of effects on t_o and T_n likely
274 pushes millimeter-scale fliers closer to resonance than bees, making way for extreme kinematic
275 and morphological adaptation to facilitate maneuverability (47).

276 Our results demonstrate that the physiology of asynchronous muscle activation under cyclic
277 strain constrains many insects to operation at or above resonance, suggestive of a widespread
278 advantage to supra-resonant flight. The apparent ubiquity of supra-resonant flight also demon-
279 strates that resonance tuning is not necessary for insect flight systems. While smaller insects
280 generally beat their wings faster and have higher resonant frequencies, competing biomechan-
281 ical and physiological pressures from muscle, wing, and exoskeleton make perfectly resonant
282 wingbeats a precarious target for selection. The capacity for supra-resonance widens the phe-
283 notypic space for successful flight, opening up the possibility of evolutionary tuning of insect
284 resonant properties for control, efficiency, or speed (8, 12, 48, 49).

285 Operation above resonance may enable increased frequency-modulation capacity in asyn-
286 chronous insects via modulation of resonant properties, such as during different buzzing modes
287 in bees, or during sensory feedback driven maneuvers in flies (31, 50). For example, decreas-

288 ing the transmission ratio by keeping the wings retracted (such as during bumblebee defense
289 buzzing) would drastically decrease the resonant period, and could easily result in a doubling
290 of wingbeat frequency without any modification of muscle properties (Fig. 4b) (51). Such a
291 mode of frequency modulation would not be possible if bumblebees had much faster muscle
292 stretch activation kinetics (t_o), because the low- t_o region of the parameter space has a flat rela-
293 tionship between emergent and natural frequency (Fig. 3a, 4b). Similar modulation capacity in
294 synchronous insects is possible by transient neurogenic frequency changes during perturbation
295 recovery (8, 12, 48).

296 Temperature-dependent modulation of wingbeat frequency via changing stretch-activation
297 time constants may be important in thermogenesis buzzing, or for insects that fly in cold condi-
298 tions such as alpine honeybees (52). One unique challenge faced by insects at the size of a fruit-
299 fly and smaller is that they cannot maintain flight muscle temperatures significantly above ambi-
300 ent temperature. This temperature constraint may cause faster-flapping insects to have a slower
301 t_o since stretch-activation timescales are known to be highly temperature-sensitive (23, 53).
302 Modulation of wingbeat frequency by calcium-dependent potentiation of asynchronous muscle
303 force may also be more effective above resonance (54). In general, our results suggest that
304 the timescale of asynchronous muscle's stretch activated dynamics (t_o) and the timescale of
305 the mechanics of resonant spring-wing thorax (T_n) are independent axes by which the emer-
306 gent wingbeat frequency can change over long timescales by selection, or short timescales by
307 phenotypic plasticity (Fig. 4b).

308 Asynchronous flight was a key evolutionary innovation that opened the possibility for su-
309 perfast wingbeat frequencies, enabling insects to miniaturize and diversify. Contrary to the
310 longstanding hypothesis of resonance tuning, our materials testing, muscle physiology, dynam-
311 ical and robophysical modeling demonstrate that many asynchronous insects flap significantly
312 above their resonant frequency. We highlight a mechanism for asynchronous supra-resonance:
313 a tug-of-war between intrinsic physiological timescale of asynchronous muscle and the resonant
314 mechanics of the thorax and wings. Supra-resonance also generalizes to multiple synchronous
315 orders, despite their wingbeat frequency being determined neurally. Thus, supra-resonance is
316 an underappreciated and widespread property of insect flight, that underscores the importance
317 of balancing efficiency and agility across Earth's smallest aerial locomotors.

318 References

- 319 1. Dudley R. 2002 *The biomechanics of insect flight: form, function, evolution*. Princeton
320 University Press.
- 321 2. Deora T, Gundiah N, Sane SP. 2017 Mechanics of the thorax in flies. *Journal of Experi-*
322 *mental Biology* **220**, 1382–1395.
- 323 3. Greenewalt CH. 1960 The Wings of Insects and Birds as Mechanical Oscillators. *Proceed-*
324 *ings of the American Philosophical Society* **104**, 605–611.

- 325 4. Dickinson MH, Lehmann FO, Chan WP. 1998 The control of mechanical power in insect
326 flight. *American Zoologist* **38**, 718–728.
- 327 5. Aiello BR, Tan M, Bin Sikandar U, Alvey AJ, Bhinderwala B, Kimball KC, Barber JR,
328 Hamilton CA, Kawahara AY, Sponberg S. 2021 Adaptive shifts underlie the divergence
329 in wing morphology in bombycoid moths. *Proceedings of the Royal Society B: Biological
330 Sciences* **288**.
- 331 6. Darveau CA. 2024 Insect Flight Energetics And the Evolution of Size, Form, And Function.
332 *Integrative And Comparative Biology* **64**, 586–597.
- 333 7. Buchwald R, Dudley R. 2010 Limits to vertical force and power production in bumblebees
334 (Hymenoptera: *Bombus impatiens*). *Journal of Experimental Biology* **213**, 426–432.
- 335 8. Wold ES, Aiello BR, Harris M, bin Sikandar U, Lynch J, Gravish N, Sponberg SN. 2024
336 Moth resonant mechanics are tuned to wingbeat frequency and energetic demands. *Pro-
337 ceedings of the Royal Society B: Biological Sciences* **291**.
- 338 9. Weis-Fogh T. 1973 Quick estimates of flight fitness in hovering animals, including novel
339 mechanisms for lift production. *Journal of experimental Biology* **59**, 169–230.
- 340 10. Lynch J, Gau J, Sponberg S, Gravish N. 2021 Dimensional analysis of spring-wing systems
341 reveals performance metrics for resonant flapping-wing flight. *Journal of the Royal Society
342 Interface* **18**.
- 343 11. Gau J, Wold ES, Lynch J, Gravish N, Sponberg S, Sponberg S. 2022 The hawkmoth wing-
344 beat is not at resonance. pp. 1–5.
- 345 12. Gau J, Gemilere R, Lds-Vip, Lynch J, Gravish N, Sponberg S. 2021 Rapid frequency mod-
346 ulation in a resonant system: Aerial perturbation recovery in hawkmoths. *Proceedings of
347 the Royal Society B: Biological Sciences* **288**.
- 348 13. Pons A, Beatus T. 2022 Distinct forms of resonant optimality within insect indirect flight
349 motors. *Journal of The Royal Society Interface* **19**.
- 350 14. Pons A. 2023 The self-oscillation paradox in the flight motor of *D. melanogaster*. *Arxiv*.
- 351 15. Jankauski MA. 2020 Measuring the frequency response of the honeybee thorax. *Bioinspi-
352 ration and Biomimetics* **15**.
- 353 16. Sotavalta O. 1952 Flight-tone and wing-stroke frequency of insects and the dynamics of
354 insect flight. *Nature* **170**, 1057–1058.
- 355 17. Weis-Fogh T. 1972 Energetics of Hovering Flight in Hummingbirds and in *Drosophila*.
356 *Journal of Experimental Biology* **56**, 79–104.

- 357 18. Machin KE, Pringle JWS. 1959 The physiology of insect fibrillar muscle - II Mechanical
358 properties of a beetle flight muscle. *Proceedings of the Royal Society of London. Series B.*
359 *Biological Sciences* **151**, 204–225.
- 360 19. Josephson RK, Malamud JG, Stokes DR. 2000 Asynchronous muscle: A primer. *Journal*
361 *of Experimental Biology* **203**, 2713–2722.
- 362 20. Gau J, Lynch J, Aiello B, Wold E, Gravish N, Sponberg S. 2023 Bridging two insect flight
363 modes in evolution, physiology and robophysics. *Nature* **622**.
- 364 21. Josephson RK. 1997 Power output from a flight muscle of the bumblebee *Bombus terrestris*.
365 III. Power during simulated flight. *Journal of Experimental Biology* **200**, 1241–1246.
- 366 22. Casey C, Heveran C, Jankauski M. 2023 Experimental studies suggest differences in the
367 distribution of thorax elasticity between insects with synchronous and asynchronous mus-
368 culature. *Journal of the Royal Society Interface* **20**.
- 369 23. Molloy JE, Kyrtatas V, Sparrow JC, White DC. 1988 Kinetics of flight muscles from insects
370 with different wingbeat frequencies. *Nature* **328**, 449–451.
- 371 24. Swank DM. 2012 Mechanical analysis of *Drosophila* indirect flight and jump muscles.
372 *Methods* **56**, 69–77.
- 373 25. Joos B, Young PA, Casey TM. 1991 Wingstroke frequency of foraging and hovering bum-
374 blebees in relation to morphology and temperature. *Physiological Entomology* **16**, 191–200.
- 375 26. Heinrich B. 1993 *The hot-blooded insects: strategies and mechanisms of thermoregulation*.
376 Harvard University Press.
- 377 27. Gilmour KM, Ellington CP. 1993 in vivo Muscle Length Changes in Bumblebees and the
378 in vitro Effects on Work and Power . *Journal of Experimental Biology* **183**, 101–113.
- 379 28. Pons A, Perl I, Ben-Dov O, Maya R, Beatus T. 2023 Solving the thoracic inverse problem
380 in the fruit fly. *Bioinspiration and Biomimetics* **18**.
- 381 29. Tu MS, Daniel TL. 2004 Submaximal power output from the dorsolongitudinal flight mus-
382 cles of the hawkmoth *Manduca sexta*. *Journal of Experimental Biology* **207**, 4651–4662.
- 383 30. Lynch J, Gau J, Sponberg S, Gravish N. 2022 Autonomous Actuation of Flapping Wing
384 Robots Inspired by Asynchronous Insect Muscle. .
- 385 31. Salem W, Cellini B, Jaworski E, Mongeau JM. 2023 Flies adaptively control flight to com-
386 pensate for added inertia. *Proceedings of the Royal Society B: Biological Sciences* **290**.

- 387 32. Harrison SM, Whitton RC, King M, Haussler KK, Kawcak CE, Stover SM, Pandy MG.
388 2012 Forelimb muscle activity during equine locomotion. *Journal of Experimental Biology*
389 **215**, 2980–2991.
- 390 33. Westerga J, Gramsbergen A. 1993 Changes in the electromyogram of two major hindlimb
391 muscles during locomotor development in the rat. *Experimental Brain Research* **92**, 479–
392 488.
- 393 34. Dallmann CJ, Dürr V, Schmitz J. 2019 Motor control of an insect leg during level and
394 incline walking. *Journal of Experimental Biology* **222**.
- 395 35. Gillis GB, Flynn JP, McGuigan P, Biewener AA. 2005 Patterns of strain and activation in
396 the thigh muscles of goats across gaits during level locomotion. *Journal of Experimental*
397 *Biology* **208**, 4599–4611.
- 398 36. Engberg I, Lundberg A. 1969 An Electromyographic Analysis of Muscular Activity in the
399 Hindlimb of the Cat during Unrestrained Locomotion. *Acta Physiologica Scandinavica* **75**,
400 614–630.
- 401 37. Dickinson MH, Farley CT, Full RJ, Koehl MA, Kram R, Lehman S. 2000 How animals
402 move: An integrative view. *Science* **288**, 100–106.
- 403 38. Josephson RK. 1985 Mechanical Power Output From Striated Muscle During Cyclic Con-
404 traction. *Journal of Experimental Biology* **114**, 493–512.
- 405 39. Anh A. 2012 How muscle function - the work loop technique. *Journal of Experimental*
406 *Biology* **215**, 1051–1052.
- 407 40. Sponberg S, Abbott E, Sawicki GS. 2023 Perturbing the muscle work loop paradigm to
408 unravel the neuromechanics of unsteady locomotion. *Journal of Experimental Biology* **226**.
- 409 41. Labonte D, Holt NC. 2022 Elastic energy storage and the efficiency of movement. *Current*
410 *Biology* **32**, R661–R666.
- 411 42. Cavagna GA, Legramandi MA. 2015 Running, hopping and trotting: Tuning step frequency
412 to the resonant frequency of the bouncing system favors larger animals. *Journal of Experi-*
413 *mental Biology* **218**, 3276–3283.
- 414 43. Lehmann FO, Dickinson MH. 1997 The changes in power requirements and muscle effi-
415 ciency during elevated force production in the fruit fly *Drosophila melanogaster*. *Journal*
416 *of Experimental Biology* **200**, 1133–1143.
- 417 44. Loya AK, Van Houten SK, Glasheen BM, Swank DM. 2022 Shortening deactivation: quan-
418 tifying a critical component of cyclical muscle contraction. *American Journal of Physiology*
419 *- Cell Physiology* **322**, C653–C665.

- 420 45. Josephson RK, Malamud JG, Stokes DR. 2000 Power output by an asynchronous flight
421 muscle from a beetle. *Journal of Experimental Biology* **203**, 2667–2689.
- 422 46. Melis JM, Siwanowicz I, Dickinson MH. 2023 Machine learning reveals the control me-
423 chanics of the insect wing hinge. *bioRxiv*.
- 424 47. Farisenkov SE, Kolomenskiy D, Petrov PN, Engels T, Lapina NA, Lehmann FO, Onishi R,
425 Liu H, Polilov AA. 2022 Novel flight style and light wings boost flight performance of tiny
426 beetles. *Nature* **602**, 96–100.
- 427 48. Wold ES, Liu E, Lynch J, Gravish N, Sponberg S. 2024 The Weis-Fogh Number Describes
428 Resonant Performance Tradeoffs in Flapping Insects. *Integrative And Comparative Biology*
429 **64**, 632–643.
- 430 49. Lynch J, Wold ES, Gau J, Sponberg SN, Gravish N. 2024 Energetic and control tradeoffs
431 in spring-wing systems. *arXiv*.
- 432 50. Salem W, Cellini B, Kabutz H, Prasad HKH, Cheng B, Jayaram K, Mongeau JM. 2022 Flies
433 trade off stability and performance via adaptive compensation to wing damage. *Science*
434 *Advances* **8**, 1–12.
- 435 51. Pritchard DJ, Vallejo-Marín M. 2020 Floral vibrations by buzz-pollinating bees achieve
436 higher frequency, velocity and acceleration than flight and defence vibrations. *Journal of*
437 *Experimental Biology* **223**.
- 438 52. Dillon ME, Dudley R. 2014 Surpassing Mt. Everest: Extreme flight performance of alpine
439 bumble-bees. *Biology Letters* **10**, 2–5.
- 440 53. Gilmour KM, Ellington CP. 1993 Power Output of Glycerinated Bumblebee Flight Muscle.
441 *Journal of Experimental Biology* **183**, 77–100.
- 442 54. Lehmann FO, Skandalis DA, Berthé R. 2013 Calcium signalling indicates bilateral power
443 balancing in the *Drosophila* flight muscle during manoeuvring flight. *Journal of the Royal*
444 *Society Interface* **10**.
- 445 55. Wold ES, Lynch J, Gravish N, Sponberg S. 2023 Structural damping renders the hawkmoth
446 exoskeleton mechanically insensitive to non-sinusoidal deformations. *Journal of the Royal*
447 *Society Interface* **20**.
- 448 56. Gau J, Gravish N, Sponberg S. 2019 Indirect actuation reduces flight power requirements
449 in *Manduca sexta* via elastic energy exchange. *Journal of the Royal Society Interface* **16**.
- 450 57. Dudek DM, Full RJ. 2006 Passive mechanical properties of legs from running insects.
451 *Journal of Experimental Biology* **209**, 1502–1515.

- 452 58. Dickinson MH, Lehmann FO, Sane SP. 1999 Wing rotation and the aerodynamic basis of
453 insect flight. *Science* **284**, 1954–1960.
- 454 59. Han JS, Kim JK, Chang JW, Han JH. 2015 An improved quasi-steady aerodynamic model
455 for insect wings that considers movement of the center of pressure. *Bioinspiration and*
456 *Biomimetics* **10**.
- 457 60. Ellington CP. 1984 The aerodynamics of hovering insect flight. II. Morphological param-
458 eters. *Philosophical Transactions of the Royal Society of London. B, Biological Sciences*
459 **305**, 17–40.
- 460 61. Whitney JP, Wood RJ. 2012 Conceptual design of flapping-wing micro air vehicles. *Bioin-*
461 *spiration and Biomimetics* **7**.
- 462 62. Josephson RK. 1997 Power output from a flight muscle of the bumblebee *Bombus terrestris*.
463 III. Power during simulated flight. *Journal of Experimental Biology* **200**, 1241–1246.
- 464 63. Elliott SJ, Tehrani MG, Langley RS. 2015 Nonlinear damping and quasi-linear modelling.
465 *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineer-*
466 *ing Sciences* **373**.
- 467 64. Peckham M, Molloy JE, Sparrow JC, White DC. 1990 Physiological properties of the dorsal
468 longitudinal flight muscle and the tergal depressor of the trochanter muscle of *Drosophila*
469 *melanogaster*. *Journal of Muscle Research and Cell Motility* **11**, 203–215.
- 470 65. Chan WP, Dickinson MH. 1996 In vivo length oscillations of indirect flight muscles in the
471 fruit fly *Drosophila virilis*. *Journal of Experimental Biology* **199**, 2767–2774.
- 472 66. King MJ, Buchmann SL, Spangler H. 1996 Activity of asynchronous flight muscle from
473 two bee families during sonication (buzzing). *Journal of Experimental Biology* **199**, 2317–
474 2321.
- 475 67. Dudley R, Ellington CP. 1990 Mechanics of Forward Flight in Bumblebees: I. Kinematics
476 and Morphology. *Journal of Experimental Biology* **148**, 19–52.
- 477 68. Siomava N, Wimmer EA, Posnien N. 2016 Size relationships of different body parts in the
478 three dipteran species *Drosophila melanogaster*, *Ceratitis capitata* and *Musca domestica*.
479 *Development Genes and Evolution* **226**, 245–256.
- 480 69. Bullock SH. 1999 Relationships among Body Size , Wing Size and Mass in Bees from a
481 Tropical Dry Forest in México Author (s): Stephen H . Bullock Source : Journal of the
482 Kansas Entomological Society , Vol . 72 , No . 4 (Oct . , 1999), pp . 426-439 Published by
483 : Allen P. *Journal of the Kansas Entomological Society* **72**, 426–439.

- 484 70. Pons A. 2024 Modelling rate-independent damping in insect exoskeleta via singular integral
485 operators. *bioRxiv* pp. 1–31.
- 486 71. Weaver Jr W, Timoshenko SP, Young DH. 1991 *Vibration problems in engineering*. John
487 Wiley & Sons.
- 488 72. Dickinson M, Farman G, Frye M, Bekyarova T, Gore D, Maughan D, Irving T. 2005 Molec-
489 ular dynamics of cyclically contracting insect flight muscle in vivo. *Nature* **433**, 330–333.
- 490 73. Walker SM, Schwyn DA, Mokso R, Wicklein M, Müller T, Doube M, Stampanoni M,
491 Krapp HG, Taylor GK. 2014 In Vivo Time-Resolved Microtomography Reveals the Me-
492 chanics of the Blowfly Flight Motor. *PLoS Biology* **12**.
- 493 74. Glasheen BM, Eldred CC, Sullivan LC, Zhao C, Reedy MK, Edwards RJ, Swank DM. 2017
494 Stretch activation properties of *Drosophila* and *Lethocerus* indirect flight muscle suggest
495 similar calcium-dependent mechanisms. *American Journal of Physiology - Cell Physiology*
496 **313**, C621–C631.
- 497 75. Fry SN, Sayaman R, Dickinson MH. 2005 The aerodynamics of hovering flight in
498 *Drosophila*. *Journal of Experimental Biology* **208**, 2303–2318.